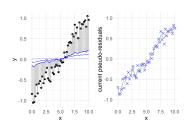
Introduction to Machine Learning

Gradient Boosting - Illustration



Learning goals

- See simple visualizations of boosting in regression
- Understand impact of different losses and base learners

GRADIENT BOOSTING ILLUSTRATION - GAM

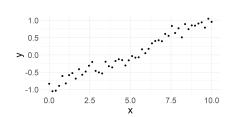
GAM / Splines as BL and compare L2 vs. L1 loss.

- L2: Init = optimal constant = mean(y); for L1 it's median(y)
- BLs are cubic *B*-splines with 40 knots.
- PRs *L*2: $\tilde{r}(f) = r(f) = y f(\mathbf{x})$
- PRs L1: $\tilde{r}(f) = sign(y f(\mathbf{x}))$
- Constant learning rate 0.2

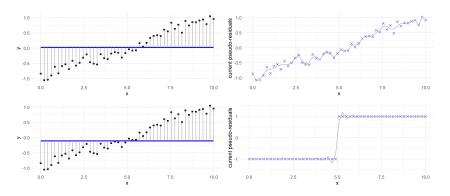
Univariate toy data:

$$y^{(i)} = -1 + 0.2 \cdot x^{(i)} + 0.1 \cdot sin(x^{(i)}) + \epsilon^{(i)}$$

$$n = 50 \ ; \epsilon^{(i)} \sim \mathcal{N}(0, 0.1)$$

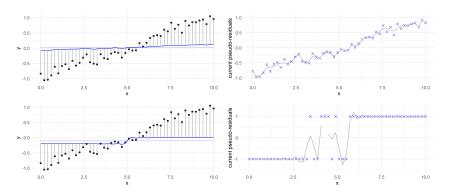


Top: L2 loss, bottom: L1 loss



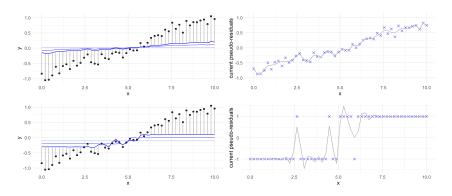
Iteration 1

Top: L2 loss, bottom: L1 loss



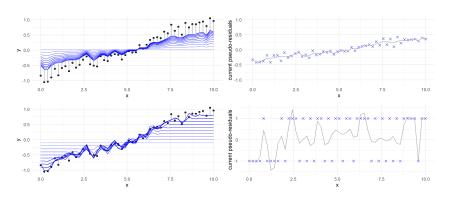
Iteration 2

Top: L2 loss, bottom: L1 loss



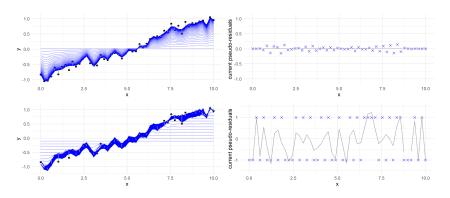
Iteration 3

Top: L2 loss, bottom: L1 loss



Iteration 10

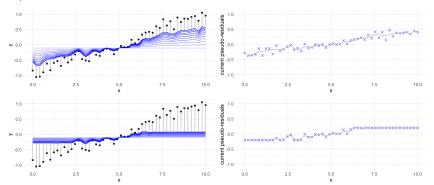
Top: L2 loss, bottom: L1 loss



Iteration 100

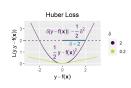
GAM WITH HUBER LOSS

Top: δ = 2, bottom: δ = 0.2.



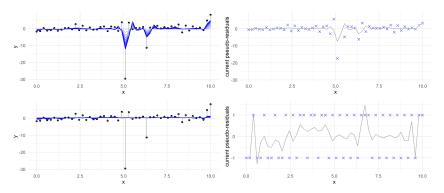
Iteration 10

For small δ , PRs are often bounded, resulting in L1-like behavior, while the upper plot more closely resembles L2 loss.



GAM WITH OUTLIERS

Instead of Gaussian noise, let's use t-distrib, that leads to outliers in y. Top: L2, bottom: L1.

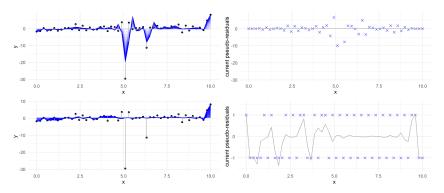


Iteration 10

L2 loss is affected by outliers rather strongly, whereas L1 solely considers residuals' sign and not their magnitude, resulting in a more robust model.

GAM WITH OUTLIERS

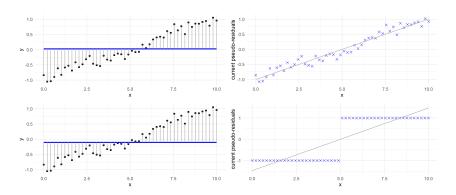
Instead of Gaussian noise, let's use t-distrib, that leads to outliers in y. Top: L2, bottom: L1.



Iteration 100

L2 loss is affected by outliers rather strongly, whereas L1 solely considers residuals' sign and not their magnitude, resulting in a more robust model.

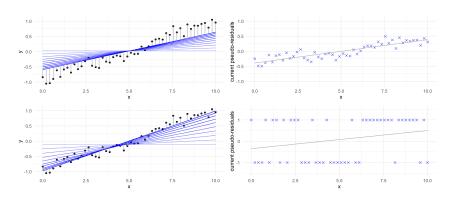
Top: L2, bottom: L1.



Iteration 1

L2: as $\tilde{r}(f) = r(f)$, BL of 1st iter already optimal; but learn rate slows us down.

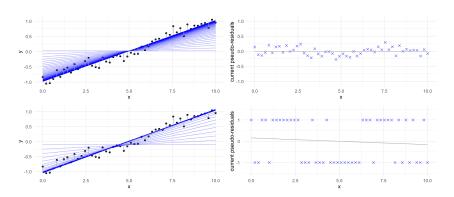
Top: L2, bottom: L1.



Iteration 10

L2: as $\tilde{r}(f) = r(f)$, BL of 1st iter already optimal; but learn rate slows us down.

Top: L2, bottom: L1.



Iteration 100

L2: as $\tilde{r}(f) = r(f)$, BL of 1st iter already optimal; but learn rate slows us down.