

Modeling *Science*

David M. Blei

Department of Computer Science
Princeton University

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Joint work with John Lafferty (CMU)

Modeling *Science*

Poisoning by ice-cream.

No chemist certainly would suppose that the same poison exists in all samples of ice-cream which have produced untoward symptoms in man. Mineral poisons, copper, lead, arsenic, and mercury, have all been used in ice-cream. In some instances, however, they have been used with criminal intent. In other cases their presence has been accidental. Likewise, that vanilla is sometimes the bearer, at least, of the poison, is well known to all chemists. Dr. Bartley's idea that the poisonous properties of the cream which he examined were due to gelatine is certainly of interest from a theoretical view. The dissonance principle, however, in this case arises from the decomposition of the gelatine; or with the gelatine there may be introduced into the milk a ferment, by the growth of which a poison is produced.

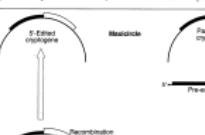
But in the cream which I examined, none of the above sources of the poisoning existed. There were no mineral salts present. No gelatin of any kind had been added in making the cream. The oil used was shown to be not poisonous. This showing was made not by a chemical analysis, which might not have been conclusive, but Mr. Novis and I drank the vanilla extract which was used, and no ill results followed. Still, from this cream we isolated the same poison which I had before found in poison cheese (*Zeitschrift für physiologische chemie*, x,

RNA Editing and the Evolution of Parasites

Larry Simpson and Dmitri A. Marley

The bacteriophage lambda, together with some other groups of eukaryotes, appears to contain DNA molecules containing repressor proteins. Within the bacteriophage, there are two types of structural genes: those for the capsid, which consist of both late and early genes, and the temperate bacteriophages, which also contain structural genes.

For example, the antigenicity of the lambda virus is determined by several unique genetic features (see accompanying figure). One of these is the presence of which a DNA site of alkali-labile thymine nucleotides. This RNA-DNA hybrid molecule can open up, forming a loop (so-called "recognition element") or (in the case of certain deletion mutants) a few nucleotides of the coding region of mRNA (5'-capping) or at multiple specific sites in the coding region of mRNA (pre-ohring). The



edges have been using the presented model of May et al. (1973). (1) they study the population dynamics of animals and plants by exemplifying ecosystems. This complex arises from two sources: The tangled web interactions that constitute natural communities provide a myriad of different pathways for species to interact, both directly and indirectly. (2) They study the population dynamics, the nonlinear feedback processes present in all natural populations can lead to complex dynamical behavior. Natural populations can show persistent oscillatory behavior between abundance and decline, the latter characterized by extinctions. If such chaotic dynamics were common in nature, then this would have important ramifications for the management and conservation of natural resources. On page 389 of this issue, Costantino et al. (2) provide the next

The authors are in the Department of Biology, Imperial College London, Silwood Park, Ascot, Berks, SL5 7PY, UK. E-mail: m.sassier@biol.ac.uk

Charles Godfray and Michael Hasen

Charles Godfray and Michael Hassell

move over the surface of the attractor, sets of adjacent trajectories are pulled apart, then stretched and folded, so that it becomes increasingly difficult to predict where they will be the future. The strength of the stretching that goes rise to the extreme sensitivity to initial conditions can be measured mathematically estimating the Lyapunov exponent, which measures the rate of separation of nearby trajectories, and sometimes otherwise. There have been many attempts to estimate attractor dimension, and Lyapunov exponents from time series data, and some candidate chaotic populations have been identified [some insects, bacteria, and even human children] decreased, and the statistical distribution (5).



Cannibalism and chaos
The four beetles, *Tribolium castaneum*, exhibit chaotic population dynamics when the amount of cannibalism is altered in a mathematical model.

- On-line archives of document collections require better organization. Manual organization is not practical.
- Our goal: To discover the hidden thematic structure with hierarchical probabilistic models called *topic models*.
- Use this structure for browsing, search, and similarity.

Modeling *Science*

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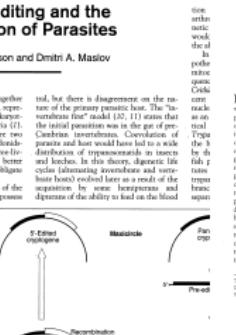
But in the cream which I examined, none of the above sources of the poisoning existed. There were no mineral poisons present. No gelatine of any kind had been used in making the cream. The vanilla was not present in the cream. This showed that was not, not by a chemical analysis, and I did not have been conclusive, but Mr. Novis, and I drank the vanilla extract which was used, and no ill results followed. Still, from this cream we isolated the same poison which I have before found in poisonous cheese (*Zeitschrift für physiologische chemie*, x,

RNA Editing and the Evolution of Parasites

Larry Simpson and Dmitri A. Maslov

The transplanted segment, together with some of its own cytoplasm, separates the anterior portion of each of the two blastomeres. In the blastomeres, there are two rows of large, polygonal, nucleated, epidermal cells, each row having two basal layers and several rows of more superficial, non-nucleated, epidermal cells.

Perhaps because of the intimacy of the contact between the two blastomeres, several unique genetic features are associated with each of them. One of which is a RNA striking of mitochondrial transcripts. This RNA, which is present in both blastomeres, can readily hybridize with a complementary strand of either mRNA (λ mismatch) or at multiple specific sites with a complementary rRNA (poly-chime). The poly-chime RNA is composed of



Chaotic Beetles

Charles Godfray and Michael Hassell

Ecologists have known since the pioneering work of Odum and the 1970s (11) that the underlying dynamics of natural systems can be exceedingly complex. This complexity of interactions that constitute our natural community provide a source of different pressures or species to interact both at a local and global scale. The interactions and processes involving the nonlinear feedback processes present in all natural populations can result in complex dynamic behavior. Natural populations can show persistent oscillatory behavior, which may be induced by extreme sensitivity to initial conditions. If such chaotic dynamics were common in nature, then this would have important ramifications for the management and conservation of natural resources. On page 369 of this issue, Costello et al. (12) provide the most

contrary evidence to date of complex dynamics and chaos in a biological population—of the flour beetle, *Tribolium confusum* (see figure).

It is very difficult to demonstrate complex dynamics in populations in the field. In its various forms, a chronically fluctuating population will superficially resemble a stable or cyclic population, but finally by the normal random perturbations experienced by all species. Often a long enough time series diagnostic tools can be used to identify the true signatures of chaos. In this space, chaotic trajectories come, i.e., in "strange attractors,"

now over the surface of the attractor, so adjacent trajectories will be pulled apart, then stretched and folded, so that it becomes increasingly difficult to predict the future behavior of the system. The strength of the stretching that gives rise to the extreme sensitivity to initial conditions can be measured mathematically estimating the Lyapunov exponent, which is a measure of how much two nearby trajectories diverge or converge over time. There have been many attempts to estimate attractor dimension and Lyapunov exponents from experimental data, and various candidate chaotic populations have been identified [some insects, nematodes, and yeast] called "strange attractors" (but not all of them display the characteristic fractal-like scaling properties of a true strange attractor), but the identification of strange attractors precludes any broad generalization (5).

Gambelism and chaos
The four beetles, *Tribolium castaneum*, exhibit chaotic population dynamics when the amount of sterilization is altered. A mathematical model

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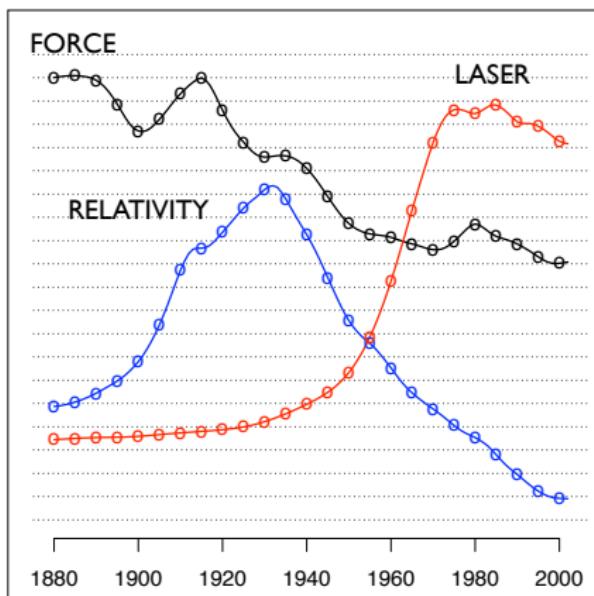
- Our data are the pages *Science* from 1880-2002 (from JSTOR)
 - No reliable punctuation, meta-data, or references.
 - Note: this is just a subset of JSTOR's archive.

Discover topics from a corpus

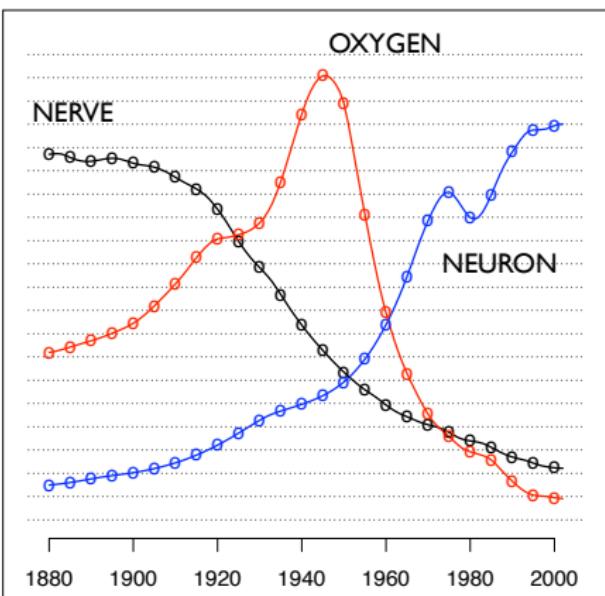
human	evolution	disease	computer
genome	evolutionary	host	models
dna	species	bacteria	information
genetic	organisms	diseases	data
genes	life	resistance	computers
sequence	origin	bacterial	system
gene	biology	new	network
molecular	groups	strains	systems
sequencing	phylogenetic	control	model
map	living	infectious	parallel
information	diversity	malaria	methods
genetics	group	parasite	networks
mapping	new	parasites	software
project	two	united	new
sequences	common	tuberculosis	simulations

Model the evolution of topics over time

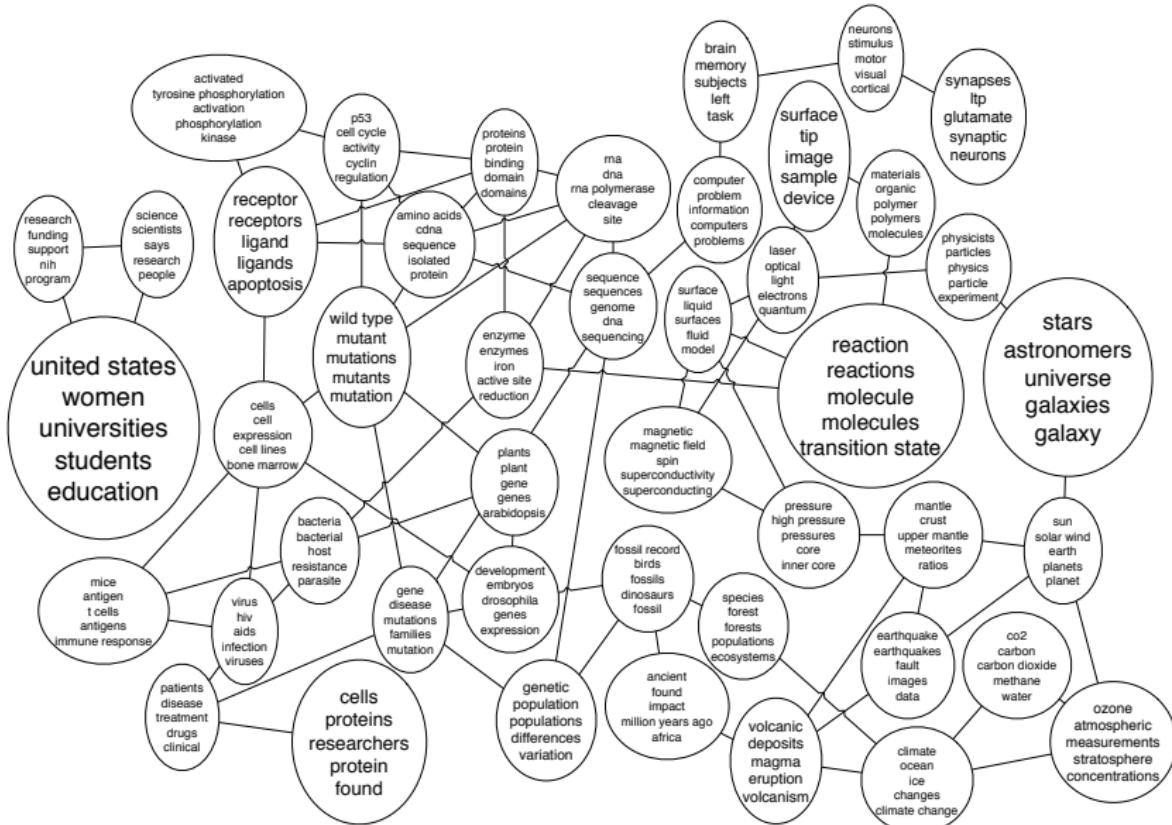
"Theoretical Physics"



"Neuroscience"



Model connections between topics



Outline

- 1 Introduction
- 2 Latent Dirichlet allocation
- 3 Dynamic topic models
- 4 Correlated topic models

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- 1 Introduction
- 2 Latent Dirichlet allocation
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Probabilistic modeling

- ① Treat data as observations that arise from a generative probabilistic process that includes hidden variables
 - For documents, the hidden variables reflect the thematic structure of the collection.
- ② Infer the hidden structure using *posterior inference*
 - What are the topics that describe this collection?
- ③ Situate new data into the estimated model.
 - How does this query or new document fit into the estimated topic structure?

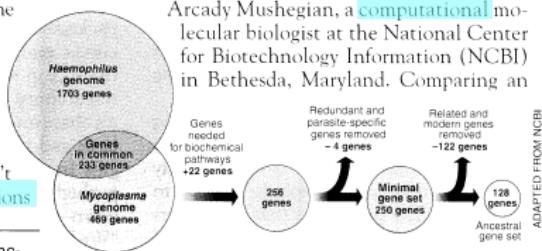
Intuition behind LDA

Seeking Life's Bare (Genetic) Necessities

COLD SPRING HARBOR, NEW YORK—How many genes does an organism need to survive? Last week at the genome meeting here,* two genome researchers with radically different approaches presented complementary views of the basic genes needed for life. One research team, using computer analyses to compare known genomes, concluded that today's organisms can be sustained with just 250 genes, and that the earliest life forms required a mere 128 genes. The other researcher mapped genes in a simple parasite and estimated that for this organism, 800 genes are plenty to do the job—but that anything short of 100 wouldn't be enough.

Although the numbers don't match precisely, those predictions

"are not all that far apart," especially in comparison to the 75,000 genes in the human genome, notes Siv Andersson of Uppsala University in Sweden, who arrived at the 800 number. But coming up with a consensus answer may be more than just a genetic numbers game, particularly as more and more genomes are completely mapped and sequenced. "It may be a way of organizing any newly sequenced genome," explains Arcady Mushegian, a computational molecular biologist at the National Center for Biotechnology Information (NCBI) in Bethesda, Maryland. Comparing an



* Genome Mapping and Sequencing, Cold Spring Harbor, New York, May 8 to 12.

Stripping down. Computer analysis yields an estimate of the minimum modern and ancient genomes.

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Simple intuition: Documents exhibit multiple topics.

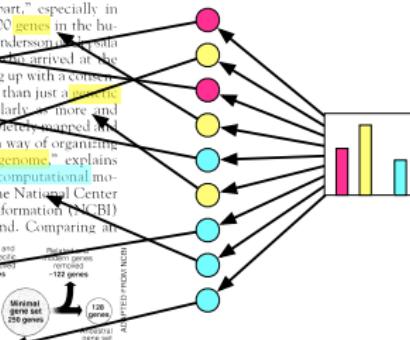
Generative process

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- Cast these intuitions into a generative probabilistic process
- Each document is a random mixture of corpus-wide topics
- Each word is drawn from one of those topics

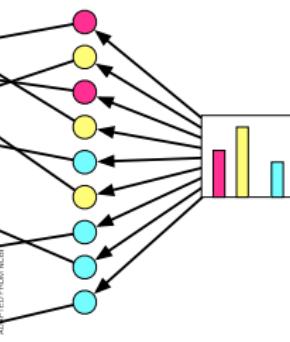
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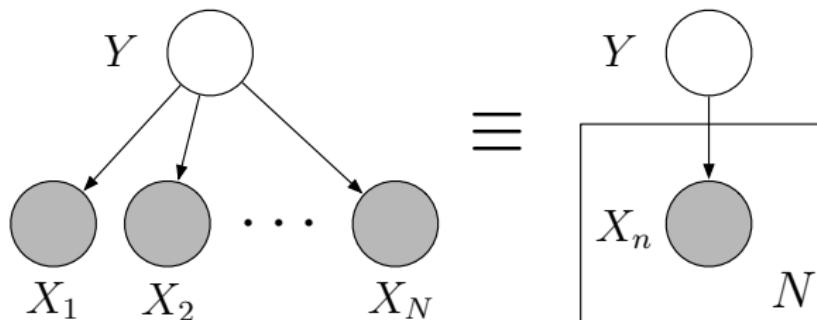


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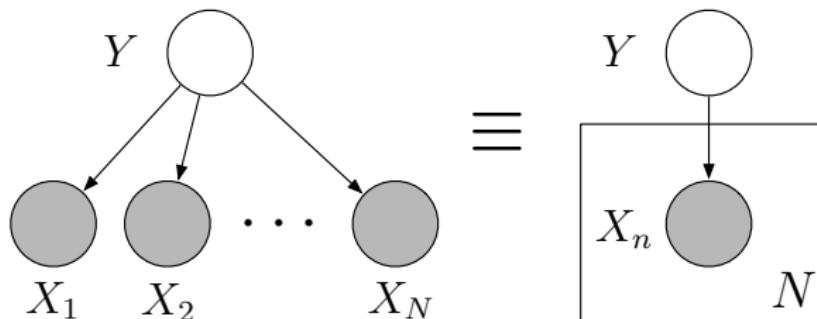
- In reality, we only observe the documents
- Our goal is to infer the underlying topic structure
 - What are the topics?
 - How are the documents divided according to those topics?

Graphical models (Aside)



- Nodes are random variables
- Edges denote possible dependence
- Observed variables are shaded
- Plates denote replicated structure

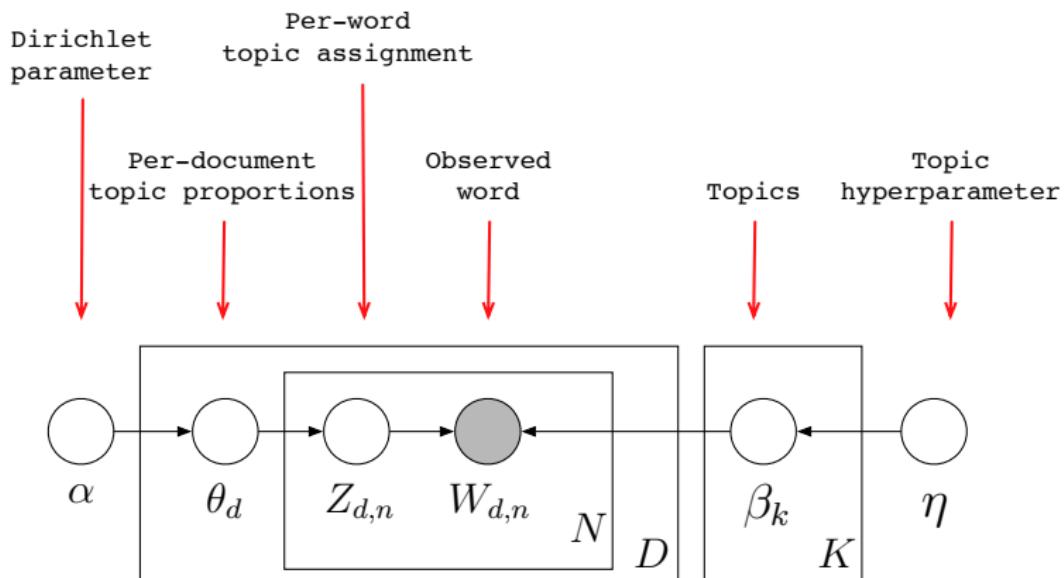
Graphical models (Aside)



- Structure of the graph defines the pattern of conditional dependence between the ensemble of random variables
- E.g., this graph corresponds to

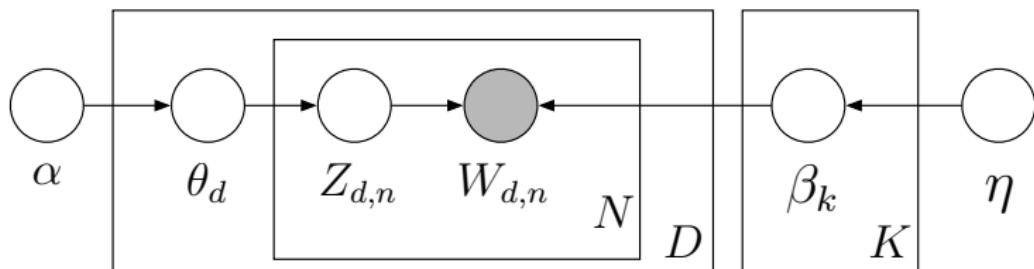
$$p(y, x_1, \dots, x_N) = p(y) \prod_{n=1}^N p(x_n | y)$$

Latent Dirichlet allocation



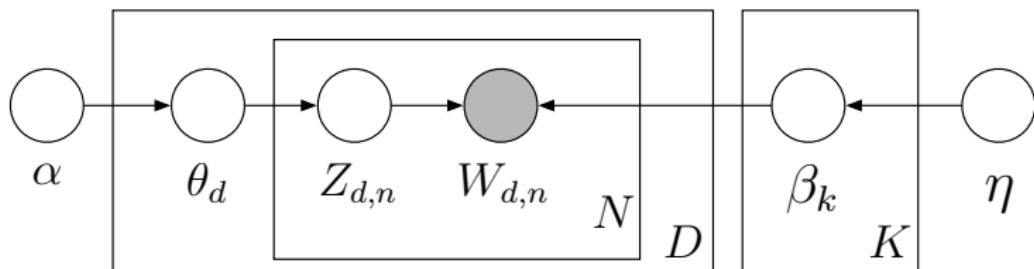
Each piece of the structure is a random variable.

Latent Dirichlet allocation



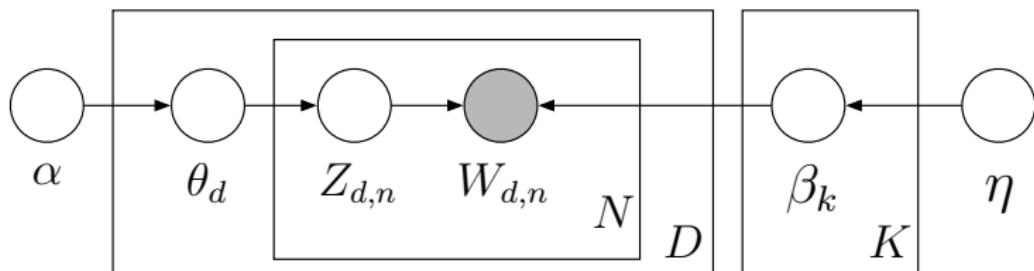
- ① Draw each topic $\beta_i \sim \text{Dir}(\eta)$, for $i \in \{1, \dots, K\}$.
- ② For each document:
 - ① Draw topic proportions $\theta_d \sim \text{Dir}(\alpha)$.
 - ② For each word:
 - ① Draw $Z_{d,n} \sim \text{Mult}(\theta_d)$.
 - ② Draw $W_{d,n} \sim \text{Mult}(\beta_{z_{d,n}})$.

Latent Dirichlet allocation



- From a collection of documents, infer
 - Per-word topic assignment $z_{d,n}$
 - Per-document topic proportions θ_d
 - Per-corpus topic distributions β_k
- Use posterior expectations to perform the task at hand, e.g., information retrieval, document similarity, etc.

Latent Dirichlet allocation

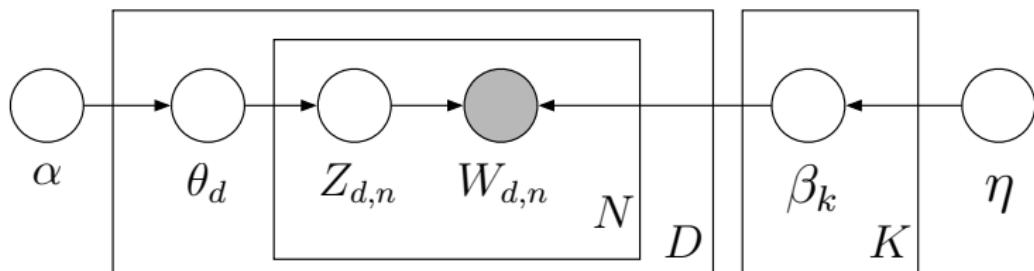


- Computing the posterior is intractable:

$$\frac{p(\theta | \alpha) \prod_{n=1}^N p(z_n | \theta) p(w_n | z_n, \beta_{1:\kappa})}{\int_{\theta} p(\theta | \alpha) \prod_{n=1}^N \sum_{z=1}^K p(z_n | \theta) p(w_n | z_n, \beta_{1:\kappa})}$$

- Several approximation techniques have been developed.

Latent Dirichlet allocation



- Mean field variational methods (Blei et al., 2001, 2003)
- Expectation propagation (Minka and Lafferty, 2002)
- Collapsed Gibbs sampling (Griffiths and Steyvers, 2002)
- Collapsed variational inference (Teh et al., 2006)

Example inference

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COLD SPRING HARBOR, NEW YORK—How many genes does an organism need to survive? Last week at the genome meeting here,* two genome researchers with radically different approaches presented complementary views of the basic gene needed for life. One research team, using computer analysis to compare known genomes, concluded that the minimum set of genes contained with just 250 genes, and that the earliest life forms required a mere 128 genes. The other researcher mapped genes in a simple parasite and estimated that for this organism, 800 genes are plenty to do the job—but that anything short of 100 wouldn't be enough.

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- **Data:** The OCR'ed collection of *Science* from 1990–2000
 - 17K documents
 - 11M words
 - 20K unique terms (stop words and rare words removed)
- **Model:** 100-topic LDA model using variational inference.

Example inference

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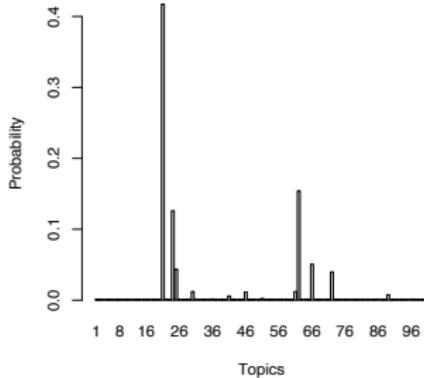
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Example topics

human	evolution	disease	computer
genome	evolutionary	host	models
dna	species	bacteria	information
genetic	organisms	diseases	data
genes	life	resistance	computers
sequence	origin	bacterial	system
gene	biology	new	network
molecular	groups	strains	systems
sequencing	phylogenetic	control	model
map	living	infectious	parallel
information	diversity	malaria	methods
genetics	group	parasite	networks
mapping	new	parasites	software
project	two	united	new
sequences	common	tuberculosis	simulations

LDA summary

- LDA is a powerful model for
 - Visualizing the hidden thematic structure in large corpora
 - Generalizing new data to fit into that structure
- LDA is a mixed membership model (Erosheva, 2004) that builds on the work of Deerwester et al. (1990) and Hofmann (1999).
- For document collections and other grouped data, this might be more appropriate than a simple finite mixture

LDA summary

- *Modular*: It can be embedded in more complicated models.
 - E.g., syntax and semantics; authorship; word sense
 - *General*: The data generating distribution can be changed.
 - E.g., images; social networks; population genetics data
 - Variational inference is fast; lets us to analyze large data sets.
-
- See Blei et al., 2003 for details and a quantitative comparison.
 - Code to play with LDA is freely available on my web-site,
<http://www.cs.princeton.edu/~blei>.

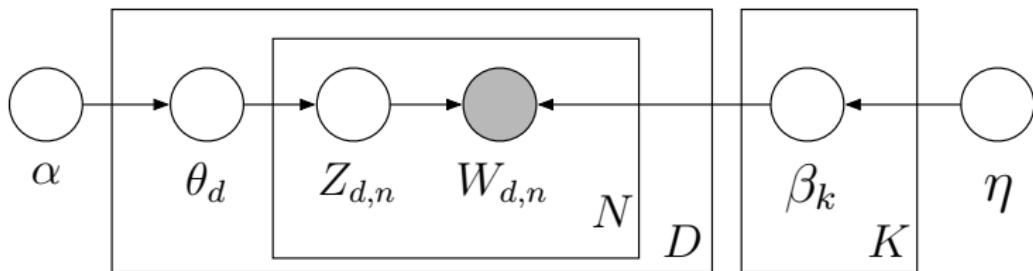
LDA summary

- But, LDA makes certain assumptions about the data.
- When are they appropriate?

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LDA and exchangeability

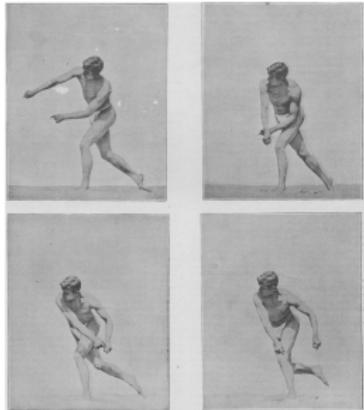


- LDA assumes that documents are exchangeable.
- I.e., their joint probability is invariant to permutation.
- This is too restrictive.

Documents are not exchangeable

"Instantaneous Photography" (1890)

Photo, who has taken thousands of pictures of flying birds, racing horses, jumping deer, etc., all selected for their speed, and for the fact that they are the most difficult to catch. In this series he has taken, for instance, the hurdle-jump of a racing horse, which requires a shutter speed of one-thousandth of a second; and he has once made twenty-four pictures of the different positions in



INSTANTANEOUS PHOTOGRAPHY OF AN ATHLETE IN MOTION - EADWEARD MUYBRIDGE

likely measured, because the eye has never been able to observe time.

Thus comes a document rich and important material for the study of motion, for the study of the laws of mechanics, and for the purposes more valuable by showing whole series of pictures giving a definite record of the successive positions of a body during a period of time, for the purpose of getting a clear idea of a

given interval. A short picture showing the different phases of a motion, & a long picture showing the different phases of a motion caused by the action in throwing a pebble, reproduced from instantaneous photographic ideas by Mr. Muybridge, are given in the following pages.

Mr. Alexander Bell constructed an apparatus which he called the "Kinetograph," which was used to take pictures of the human figure. In this instrument the series o-

"Infrared Reflectance in Leaf-Sitting Neotropical Frogs" (1977)

North American frogs we examined (Bufo debilis, R. borealis D.L.) conform to the general pattern of infrared reflectance observed in other frogs (R. catesbeiana, M. amphibia, H. sphenocephalus, M. cinereum) and H. cyanostictus, which sit on leaves and are not sharply aposematic (Fig. 1).

Cole and McDiarmid (1977) found this frog to have the Australian tree frog (*Dendropsophus leucophyllatus*) and the green tree frog (*A. moreletii*) and light (*A. cinnamomea*) dorsal coloration, while the ventral surface was covered red pigment is unusual

metabolism (H. H. Shultz and C. M. Schmid, personal communication). Infrared reflectance was also observed in the tree frog (*Hyla arborea*), which sits on leaves, but the eyes of birds and the pit organs of frogs do not appear to be infrared receptors.

In pigeons and chickens, the sensitivity of the retina to infrared rays is about 10 times greater than that of humans (7), and the tawny owl (*Strix aluco*) can see infrared rays (8). Visual sensitivity extending just into the infrared region is also known in some green frogs (green tree frogs), although cerebrals and photoreceptors are not yet well understood. Red and cereal pit organs are usually interpreted as infrared receptors, but no mechanism for infrared production on vertebrate blood is yet known (9). In thermal insulation, however, frogs may be unique. We observed frogs that sit on infrared sinks among leaves, and we observed frogs that sit on infrared emitters. Predators by birds and snakes are often attracted to infrared and crypsis coloration in tropical leaf-sitting frogs.

PATRICK H. STARKEY*

Department of Biology, University of
Alfred Harvey Foundation,
University of Southern California,
Los Angeles 90089. RAY W. McDIARMID
Department of Biology, University of
South Florida, Tampa 33606

Received and Note

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4. J. D. Johnson, W. J. Wertheim, and R. W. McDiarmid. 1978. *Journal of Herpetology* 12: 109-111.
5. J. D. Johnson and R. W. McDiarmid. 1978. *Journal of Herpetology* 12: 109-111.
6. Johnson, J. D. and McDiarmid, R. W. 1978. Infrared reflectance in leaf-sitting neotropical frogs. *Science* 195: 125-127.
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8. J. D. Johnson and R. W. McDiarmid. 1978. *Journal of Herpetology* 12: 109-111.
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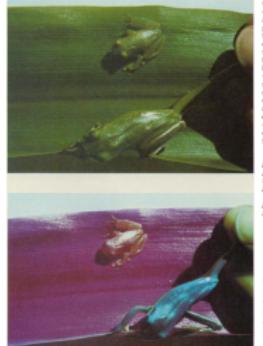


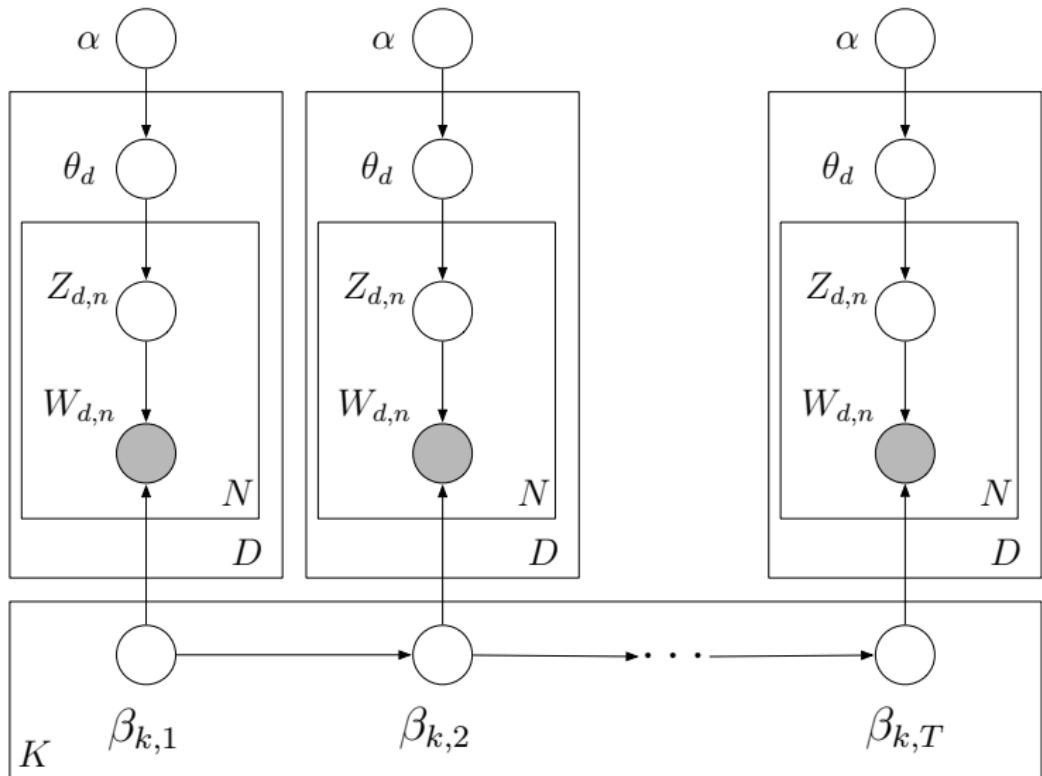
Fig. 1. A comparison of the color characteristics of a bright and a dark-colored frog in a contrasted environment. The bright frog (*Hyla arborea*) is shown sitting on a dark leaf, and the dark frog (*Hyla arborea*) is shown sitting on a bright leaf. The bright frog reflects more infrared energy than the dark frog, and the dark frog reflects more infrared energy than the bright frog. The bright frog is visible to birds and snakes, while the dark frog is not.

- Documents about the same topic are not exchangeable.
- Topics evolve over time.

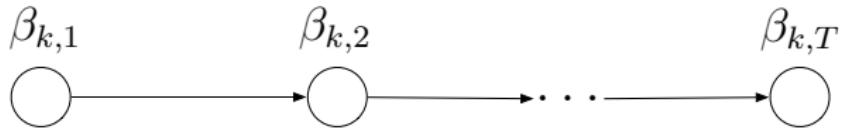
Dynamic topic model

- Divide corpus into sequential slices (e.g., by year).
- Assume each slice's documents exchangeable.
 - Drawn from an LDA model.
- Allow topic distributions evolve from slice to slice.

Dynamic topic models



Modeling evolving topics



- Use a logistic normal distribution to model evolving topics (Aitchison, 1980)
- A state-space model on the natural parameter of the topic multinomial (West and Harrison, 1997)

$$\beta_{t,k} | \beta_{t-1,k} \sim \mathcal{N}(\beta_{t-1,k}, I\sigma^2)$$

$$p(w | \beta_{t,k}) = \exp \left\{ \beta_{t,k} - \log(1 + \sum_{v=1}^{V-1} \exp\{\beta_{t,k,v}\}) \right\}$$

Posterior inference

- Our goal is to compute the posterior distribution,

$$p(\beta_{1:T,1:K}, \theta_{1:T,1:D}, \mathbf{z}_{1:T,1:D} \mid \mathbf{w}_{1:T,1:D}).$$

- Exact inference is impossible
 - Per-document mixed-membership model
 - Non-conjugacy between $p(w \mid \beta_{t,k})$ and $p(\beta_{t,k})$
- MCMC is not practical for the amount of data.
- Solution: Variational inference

Science data



TECHVIEW: DNA S E Q U E N C I N G

Sequencing the Genome, Fast

James C. Mullikin and Amanda A. McMurray



Genome sequencing projects reveal the genetic makeup of an organism by reading off the sequence of the DNA bases, which encodes all of the information necessary for the life of the organism. The base sequence contains four nucleotides—adenine, thymidine, guanosine, and cytosine—which are linked together into long double-helical chains. Over the last two decades, automated DNA sequencers have made the process of obtaining the base-by-base sequence of DNA...

- Analyze JSTOR's entire collection from *Science* (1880-2002)
- Restrict to 30K terms that occur more than ten times
- The data are 76M words in 130K documents

Analyzing a document

Original article

Topic proportions



TECHVIEW: DNA SEQUENCING

Sequencing the Genome, Fast

James C. McHale and Amanda A. McHenry

Genome sequencing projects reveal the genetic makeup of an organism by reading off the sequence of its DNA base pairs. One of the major reasons necessary for the life of the sequence is the cost of the reagents—dye, salts, solvents—adenine, thymidine, guanine, cytosine, uracil, and so forth, among many other bases. Over the last two decades, automated DNA sequencing has become faster and more accurate, allowing the base-by-base sequence of DNA to be determined. In addition, as more and more genes are sequenced across a genome, these sequencers require more and more labeled DNA molecules to be used. As the DNA molecules move past a given point in the gel, they are detected by a sensor that is specific to the base in the end of the molecule. This allows the signal to be automatically recorded.

The latest sequencer to be launched is Parkersburg, West Virginia's ABI Prism 3700 DNA Analyzer, which, like the ABI 3730, can sequence up to 96 samples at a time. The ABI 3700 is a high-throughput sequencer that can sequence up to 1,000 samples per day. Early interest in the ABI 3700 has been generated by ABI's parent company, PerkinElmer Applied Biosystems Corporation, anticipating that >200 of these machines will be sold to academic and pharmaceutical companies to produce new sequences for the extensive 3-gigabase (Gb) of the human genome project. The ABI 3700 is a high-throughput sequencer that can sequence up to 1,000 samples per day. Assuming the read length of each sequence is 1000 bp, the number of sequencing data (in read length) and any section from the original sequence is 1000 bp, the average of 10 overlapping independent reads (100 bp overlap) would mean that each process will require 110,000 ABI 3700 machine days. With ~250 machines, this would take 440 days, or about 434 days, which affords some margin of error for the sequencing process.

At the Sanger Center, we have finished 140 Mb of genomic sequence. With a rate

of genomes, including 81 Mb of sequence from the human genome, the ABI 3700 is a high-throughput sequencer that can sequence up to 1,000 samples per day. The ABI 3700 is a high-throughput sequencer that can sequence up to 1,000 samples per day. Two sequencing runs, each consisting of 48 samples, are required to sequence a genome. The ABI 3700 is a high-throughput sequencer that can sequence up to 1,000 samples per day. Two sequencing runs, each consisting of 48 samples, are required to sequence a genome.

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The authors are at The Sanger Centre, Wellcome Trust Genome Campus, Cambridge, UK. E-mail: jmc@east.sanger.ac.uk

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are available. In fact, a system that could sequence 100 Mb of sequence in a single pass is preferable, if both systems cost the same. This is because the quality of the sequence obtained from a single pass is higher than that obtained from multiple passes. This is an important parameter when evaluating new sequencing technologies.

We have directly compared the ABI 3700 sequencer to the ABI 373XL slab gel sequencer. Both systems were run with human genomic DNA. The ABI 3700 sequencing gel was obtained from both machines with human genomic DNA. The ABI 373XL sequencing gel was obtained from the ABI 3700 sequencing gel and prepared and sequenced with our standard sequencing kit, Big Dye Terminator chemistry.

Analyzing a document

Original article

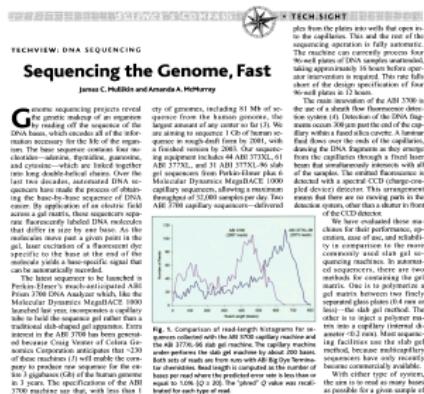


Fig. 1. Comparison of read-length histograms for samples collected with the ABI 3700 capillary machine and the ABI 377 capillary machine.

Genome sequencing projects reveal the precise makeup of an organism by reading the sequence of the whole DNA genome. In addition, the human genome project requires the life of the sequencer to be extended to include sequencing of chlorophyll—adenine, thymidine, guanosine, and cytosine—and an additional 100,000 sequencing double-stranded clones. Over the last two decades, automated DNA sequencing has become the dominant method for obtaining the base-pair sequence of DNA molecules. In the first decade, as each sequencer scans a gel matrix, these sequencers separate fluorescently labeled DNA molecules that fluoresce at different wavelengths. These molecules move past a given point in the gel at different times, depending on their specificity to the base in the end of the sequence. The sequence of the signal can be unambiguously recorded.

The latest sequencer to be launched is PerkinElmer's ABI 3700 capillary machine. All previous 3700 DNA Analyzers, while like the ABI 377, have a throughput of 100 samples per hour, have required a 24-hour run time, incompletely a capillary system to hold the sequenced gel rather than a sequencing gel. Early interest in the ABI 3700 has been generated by the announcement of Applied Biosystems Corporation anticipates that >200 million dollars will be invested by its company to produce new sequencers for the use of 3-gigabases (Gb) of the human genome in 2003. This is a significant increase over the ABI 3700 machine, which, with less than 1 hour of sequencing time, can sequence 768 samples per day. Assuming the next sequencer to be developed will have a similar rate of sample sequencing (in read length) and any savings from the use of a longer sequencing gel, the average of 10 overlapping independent read lengths of 1000 bp per sample, the new machine process will require >100,000 ABI 3700 machine days. With 200 machines, this would require 500 days or about 434 days, which affords some margin of error, but still represents a significant cost.

At the Sanger Center, we have finished 140 Gb of genomic sequence. From a rate-

The authors are at The Sanger Centre, Wellcome Trust Genome Campus, Hinxton, Cambridge CB10 1Sa, UK. E-mail: jmc@east.sanger.ac.uk

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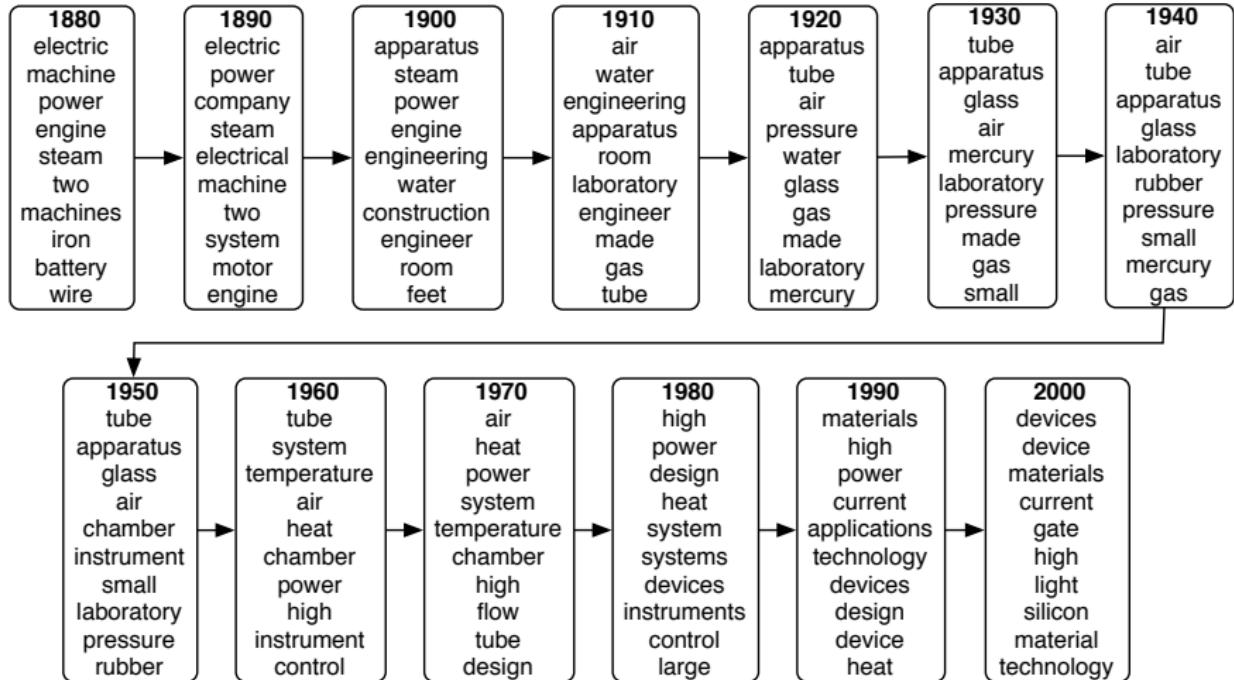
Most likely words from top topics

sequence
genome
genes
sequences
human
gene
dna
sequencing
chromosome
regions
analysis
data
genomic
number

devices
device
materials
current
high
gate
light
silicon
material
technology
electrical
fiber
power
based

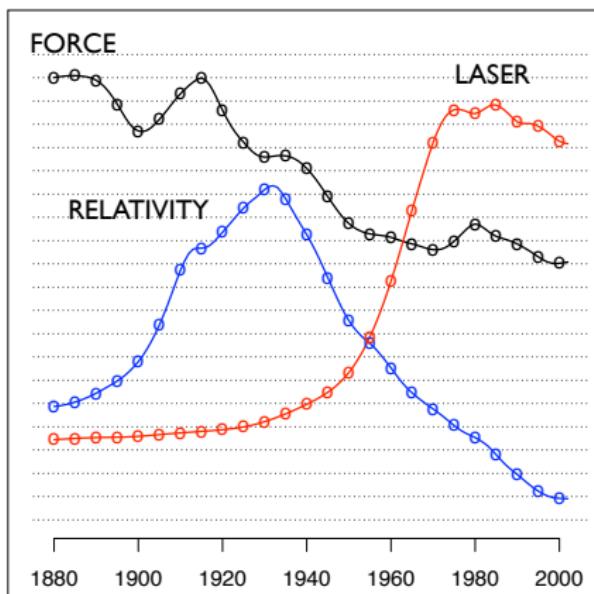
data
information
network
web
computer
language
networks
time
software
system
words
algorithm
number
internet

Analyzing a topic

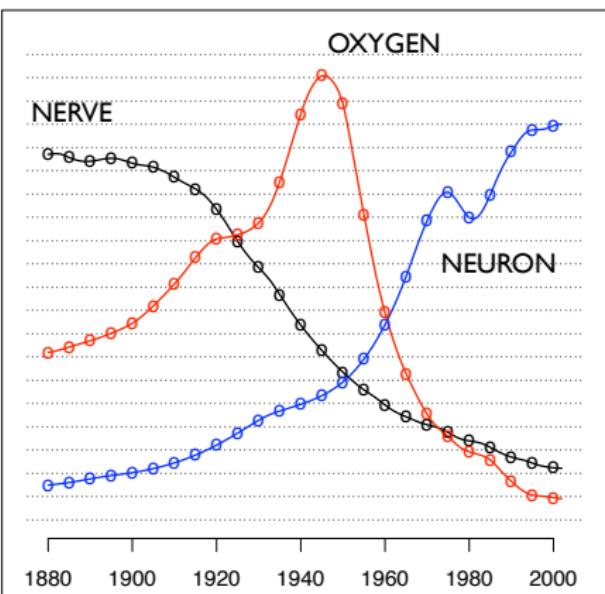


Visualizing trends within a topic

"Theoretical Physics"



"Neuroscience"



Time-corrected document similarity

- Consider the expected Hellinger distance between the topic proportions of two documents,

$$d_{ij} = E \left[\sum_{k=1}^K (\sqrt{\theta_{i,k}} - \sqrt{\theta_{j,k}})^2 \mid \mathbf{w}_i, \mathbf{w}_j \right]$$

- Uses the latent structure to define similarity
- Time has been factored out because the topics associated to the components are different from year to year.
- Similarity based only on topic proportions

Time-corrected document similarity

The Brain of the Orang (1880)

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SCIENCE.

Problems in these cases, which were submitted to the author on the 2d of December last for correction or re-publication, were referred to the author by the editor-in-chief, Mr. S. C. Hall, and were accepted without any express name. After publication Professor Agassiz sent me a copy of his article, and I am sending him a copy of this paper. We therefore request our readers to consider this paper as published by the author.

The author has been informed that Dr. G. H. V. Sharpe and Professor J. E. Bickart are preparing more elaborate reports on the orang brain, and promises them to send it early day.

THE BRAIN OF THE ORANG.*

BY MAYER C. HARRISON, M.D.

The brain of the orang has been figured by Tiedemann, Gmelin, Homann, etc. On account, however, of the rather confused nature of the illustrations of the subject, I send a copy of my own figures of the several parts of my Orang's brain (Figs. 1 to 5), which may assist in the identification of the parts described. The membranes were in a high state of complete decay, and the brain was in a very bad condition, having been disengaged from the skull, when the author received it. In his description of the brain he says that "the brain was perfectly dried." This is a gross error, as is also the statement that "the brain was perfectly dried before its deposition in all time." The brain was, however, perfectly dried when it was sent to me, and was perfectly dried when only a slightly thickened skin of the anterior part of the brain remained.

The brain was perfectly dried when it was sent to me,

as in the Orang the postero-cerebral fissure does not reach the rachis, being separated from it by the transverse fissure, which is situated in front of the postero-cerebral fissure. According to Homann, this disposition obtains in the orang, gibbon, orangutan, and chimpanzee, but in the orang it is the reverse. According to Tiedemann, the postero-cerebral fissure passes into the calcarine fissure, and according to Gmelin it passes into the calcarine fissure, and according to Homann it is situated in front of the parietal lobe. The brain of the orang is, however, wider, and more elevated than is the brain of the chimpanzee, and the postero-cerebral fissure is, therefore, more posterior, and the parietal lobe is, therefore, more anterior, than in the chimpanzee. The postero-cerebral fissure is, therefore, more anterior in the orang than in the chimpanzee, and the parietal lobe is, therefore, more anterior in the orang than in the chimpanzee.

In the orang, the postero-cerebral fissure is, therefore, more anterior than in the chimpanzee, and the parietal lobe is, therefore, more anterior in the orang than in the chimpanzee. The postero-cerebral fissure is, therefore, more anterior than in the chimpanzee, and the parietal lobe is, therefore, more anterior in the orang than in the chimpanzee. The postero-cerebral fissure is, therefore, more anterior than in the chimpanzee, and the parietal lobe is, therefore, more anterior in the orang than in the chimpanzee. The postero-cerebral fissure is, therefore, more anterior than in the chimpanzee, and the parietal lobe is, therefore, more anterior in the orang than in the chimpanzee. The postero-cerebral fissure is, therefore, more anterior than in the chimpanzee, and the parietal lobe is, therefore, more anterior in the orang than in the chimpanzee.

The greatest diameter of the brain is, however, in the

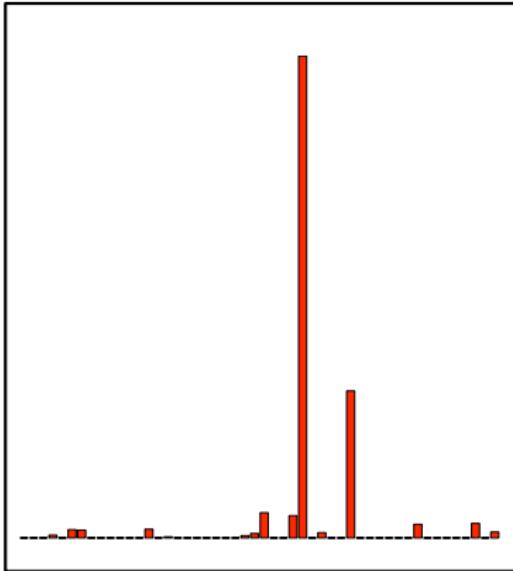


Fig. 1.

The brain of the Orang. The parietal, and nose are the most prominent features. The brain is, however, in the orang, the postero-cerebral fissure is, therefore, more anterior than in the chimpanzee, and the parietal lobe is, therefore, more anterior in the orang than in the chimpanzee. The postero-cerebral fissure is, therefore, more anterior than in the chimpanzee, and the parietal lobe is, therefore, more anterior in the orang than in the chimpanzee. The postero-cerebral fissure is, therefore, more anterior than in the chimpanzee, and the parietal lobe is, therefore, more anterior in the orang than in the chimpanzee.

* From the Proceedings of the Academy of Natural Sciences, Phila., etc.

The postero-cerebral fissure is, therefore, more anterior than in the chimpanzee, and the parietal lobe is, therefore, more anterior in the orang than in the chimpanzee. The postero-cerebral fissure is, therefore, more anterior than in the chimpanzee, and the parietal lobe is, therefore, more anterior in the orang than in the chimpanzee.



Time-corrected document similarity

Representation of the Visual Field on the Medial Wall of Occipital-Parietal Cortex in the Owl Monkey (1976)

project, the systematic exploration of the medial occipital-parietal cortex was explored with microelectrode-guided recording methods. The owl monkeys were anaesthetized with sodium pentobarbital and placed in a stereotaxic frame. Plastic-coated microelectrodes were used to record from small clusters of neurons in the visual field. The microelectrode penetrations parallel to the medial wall of the occipital-parietal cortex. Recording fields were placed by moving circular spots or rectangular slits and bars onto the medial wall of the brain. A translucent plastic sheet was placed onto the plastic brain slides to prevent damage to the brain. The painted eye clearly was

covered with an opaque shield. Electrode tracks and recording sites were recorded on the original plastic slides. The monkeys were anaesthetized with sodium pentobarbital and placed in a stereotaxic frame. Plastic-coated microelectrodes were used to record from small clusters of neurons in the visual field. The microelectrode penetrations parallel to the medial wall of the occipital-parietal cortex. Recording fields were placed by moving circular spots or rectangular slits and bars onto the medial wall of the brain. A translucent plastic sheet was placed onto the plastic brain slides to prevent damage to the brain. The painted eye clearly was

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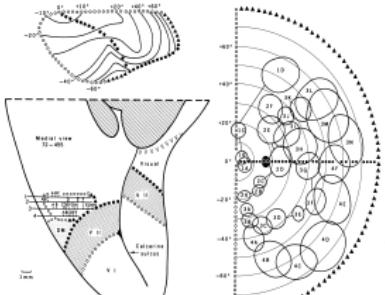
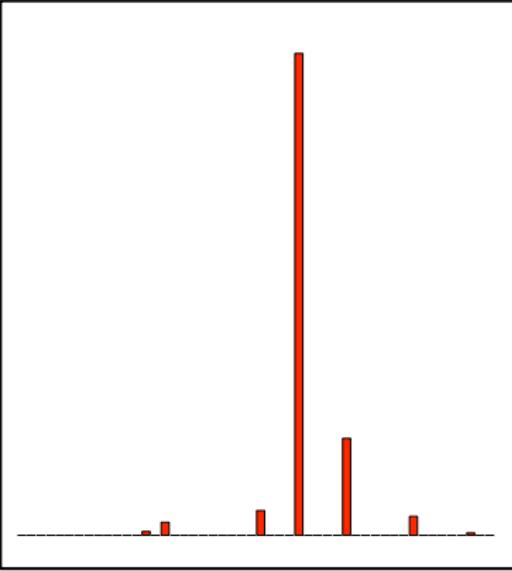


Fig. 1. Medial view of the owl monkey's brain showing receptive field data for the medial visual area in owl monkey 72-455. The diagram on the left is a lateral view of the brain with the medial wall of the occipital-parietal cortex indicated. Anatomical up and down directions are indicated. The diagram on the right is a medial view of the brain with the medial wall of the occipital-parietal cortex indicated. The numbers indicate the representation of the vertical meridians (indicated by the squares) on the medial wall of the brain. The numbers indicate the representation of the horizontal meridians (indicated by the circles) on the medial wall of the brain. The numbers indicate the representation of the peripheral regions (indicated by the triangles) on the medial wall of the brain. DM is the dorsomedial visual area. OM indicates the position of the optic disc or blind spot.

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Browser of Science

Automatic Analysis, Theme Generation, and Summarization of Machine-Readable Texts

Gerard Salton, James Allan, Chris Buckley.

Vast amounts of text material are now available in machine-readable processing. Here, approaches are outlined for manipulating and subject areas in accordance with user needs. In particular, method mining text themes, traversing texts selectively, and extracting subject reflect text content.

Many kinds of texts are currently available in machine-readable form and are amenable to automatic processing. Because the available databases are large and cover many different subject areas, automatic aids must be provided to users interested in accessing the data. It has been suggested that links be placed between related pieces of text, connecting, for example, particular text paragraphs to other paragraphs covering related subject matter. Such a linked text structure, often called hypertext, makes it possible for the reader to start with particular text passages and use the linked structure to related text elements (1). Unfortunately, a major problem in building hypertext systems for automatically building large hypertext structures and for using such structures in a sophisticated way have not been available. Here we give methods for constructing text relation maps and for using text relations to access and use text databases. In particular, we outline procedures for determining text themes, traversing texts selectively, and extracting summary statements that reflect text content.

Text Analysis and Retrieval: The Smart System

The Smart system is a sophisticated text retrieval tool, developed over the past 30 years, that is based on the vector space

The authors are in the Department of Computer Science, Cornell University, Ithaca, NY 14853-7501, USA

model of retrieval model, all information as well as information sent by sets, or words typically a word, associated with the document. In principle chosen from a context a thesaurus, but before constructing such for unrestricted top to derive the terms under consideration terms assigned to a text content.

Because the term frequency-weighted introduced a term weight signs high weights to and lower weights to A powerful term-weight kind is the well-known term frequency (f_t) frequency (f_t) in t with a low frequency (f_t). Such terms distinguish which they occur frequently.

When all texts are sent by weighted $D_i = (d_{i1}, d_{i2}, \dots)$ weight assigned to a similarity measure between pairs of vectors. Thus, a



"Automatic Analysis, Theme Generation, and Summarization of Machine-Readable Texts" (1994)

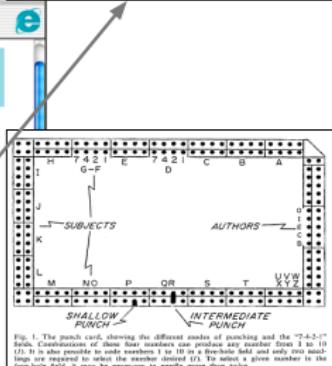
TOPIC	PROB
data computer system information network	0.30
information library text index libraries	0.19
two three four different single	0.16

DOCUMENT	SCORE
"Global Text Matching for Information Retrieval" (1991)	0.2570
"Automatic Text Analysis" (1970)	0.3110
"Gauging Similarity with n-Grams: Language-Independent Categorization of Text" (1995)	0.3210
"Developments in Automatic Text Retrieval" (1991)	0.3480
"Simple and Rapid Method for the Coding of Punched Cards" (1962)	0.3610
"Data Processing by Optical Coincidence" (1961)	0.4290
"Pattern-Analyzing Memory" (1976)	0.4320
"The Storing of Pamphlets" (1899)	0.4440
"A Punched-Card Technique for Computing Means, Standard Deviations, and the Product-Moment Correlation Coefficient and for Listing Scattergrams" (1946)	0.4550

Global Text Matching for Information Retrieval

GERARD SALTON* AND CHRIS BUCKLEY

An approach is outlined for the retrieval of natural language texts in response to available search requests and for the recognition of content similarities between text excerpts. The proposed retrieval process is based on flexible text matching procedures carried out in a number of different text environments and is applicable to large text collections covering unrestricted subject matter. For unrestricted text environments this system appears to outperform other currently available methods.



THE STORING OF PAMPHLETS.

On reading Professor Minot's explanation of his method of storing pamphlets as given in the issue of December 30th I feel inclined to add a word in commendation of the method. I began using these boxes six or seven years ago and now have 152 upon my shelves. About one-half are devoted to Experiment Station bulletins, the boxes being labeled by States and arranged alphabetically. The other half is used for miscellaneous pamphlets on subjects pertaining to my line of work. The boxes have proved perfectly satisfactory in every way, and as a simple time-saving device they are worth many times the cost. My system of pamphlets arrangement differs in some ways from that adopted by Professor Minot and has been adopted only after trial of several other methods.

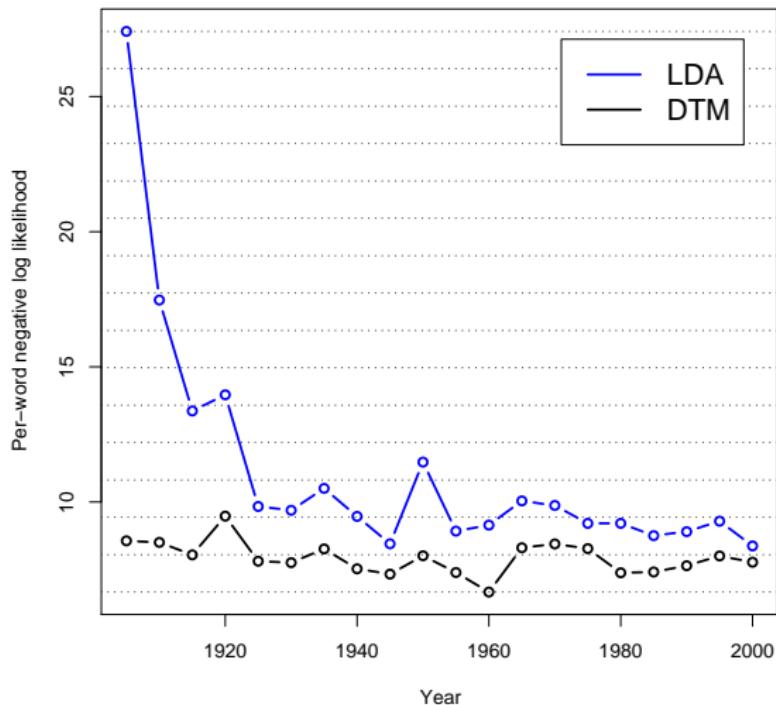
Quantitative comparison

- Compute the probability of each year's documents conditional on all the previous year's documents,

$$p(\mathbf{w}_t | \mathbf{w}_1, \dots, \mathbf{w}_{t-1})$$

- Compare exchangeable and dynamic topic models

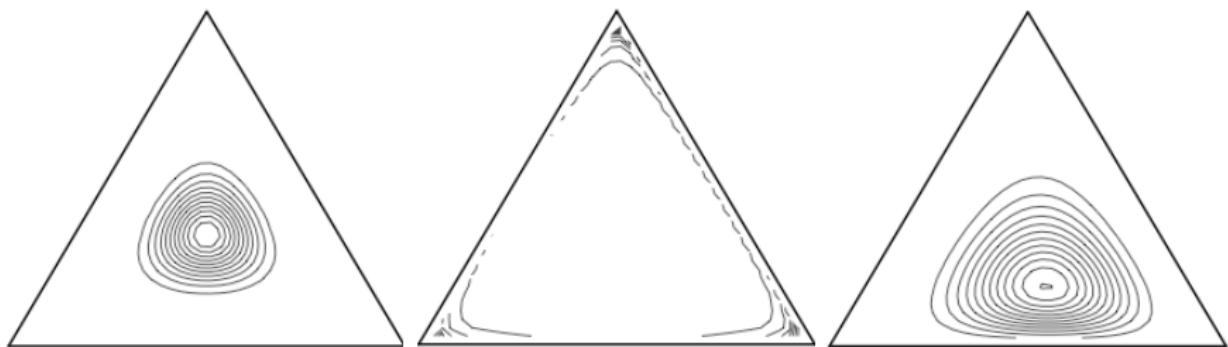
Quantitative comparison



Outline

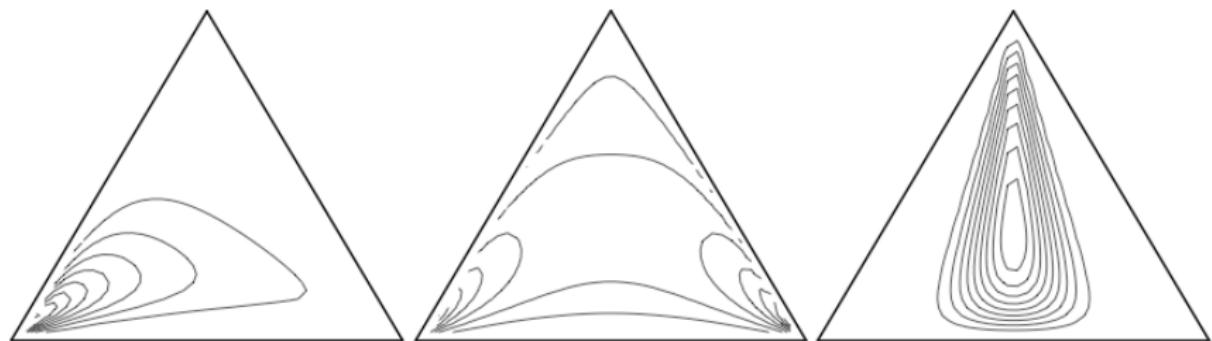
- 1 Introduction
- 2 Latent Dirichlet allocation
- 3 Dynamic topic models
- 4 Correlated topic models

The hidden assumptions of the Dirichlet distribution



- The Dirichlet is an exponential family distribution on the *simplex*, positive vectors that sum to one.
- However, the near independence of components makes it a poor choice for modeling topic proportions.
- An article about *fossil fuels* is more likely to also be about *geology* than about *genetics*.

The logistic normal distribution

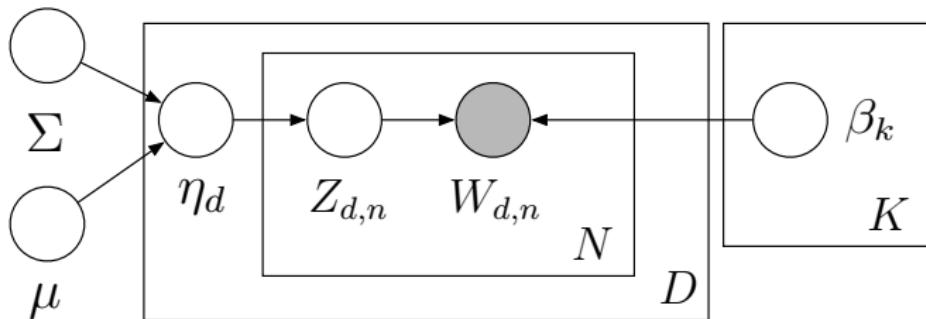


- The logistic normal is a distribution on the simplex that can model dependence between components.
- The natural parameters of the multinomial are drawn from a multivariate Gaussian distribution.

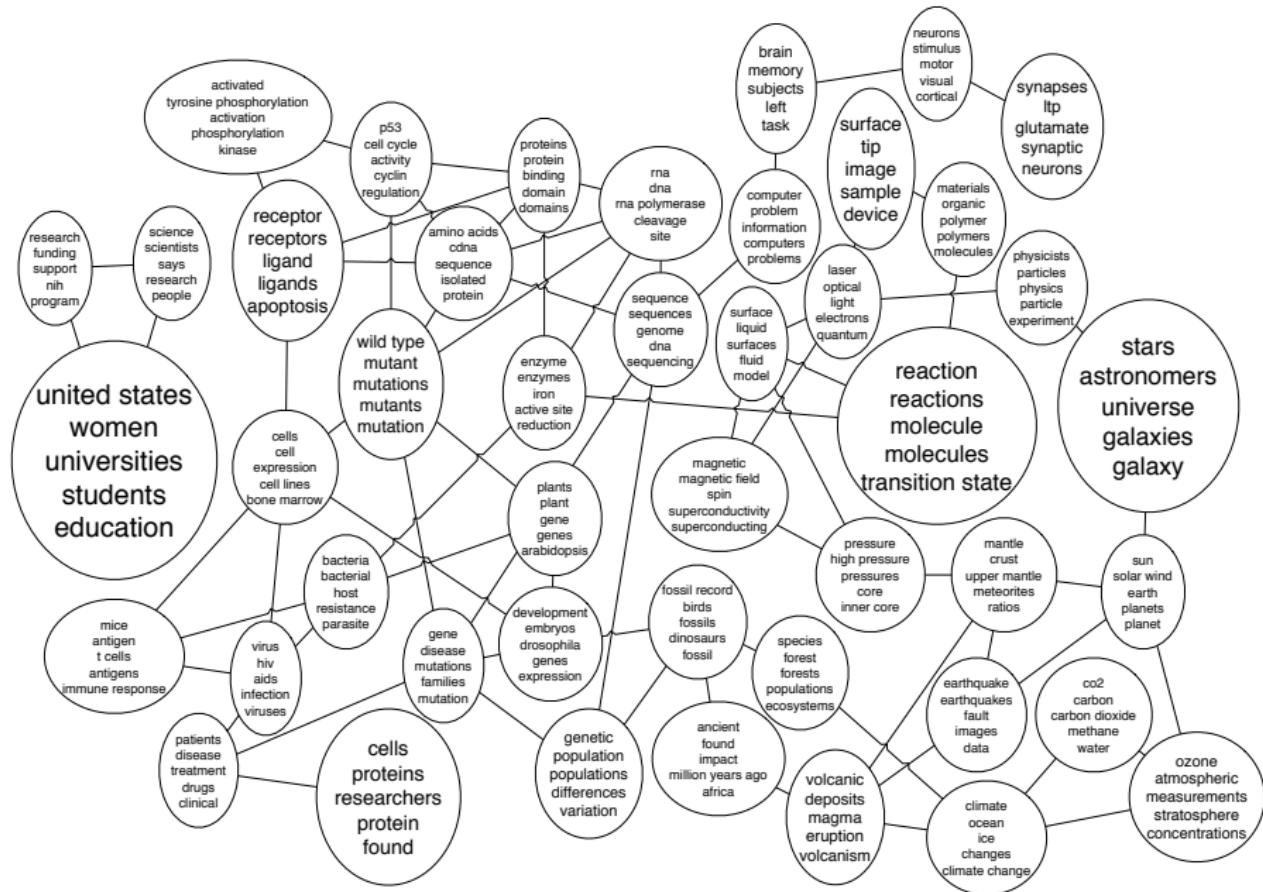
$$X \sim \mathcal{N}_{K-1}(\mu, \Sigma)$$

$$\theta_i = \exp\{x_i - \log(1 + \sum_{j=1}^{K-1} \exp\{x_j\})\}$$

Correlated topic model (CTM)



- Draw topic proportions from a logistic normal, where topic occurrences can exhibit correlation.
- Use for:
 - Providing a “map” of topics and how they are related
 - Better prediction via correlated topics



Summary

- Topic models provide useful descriptive statistics for analyzing and understanding the latent structure of large text collections.
- Probabilistic graphical models are a useful way to express assumptions about the hidden structure of complicated data.
- Variational methods allow us to perform posterior inference to automatically infer that structure from large data sets.
- Current research
 - Choosing the number of topics
 - Continuous time dynamic topic models
 - Topic models for prediction
 - Inferring the impact of a document

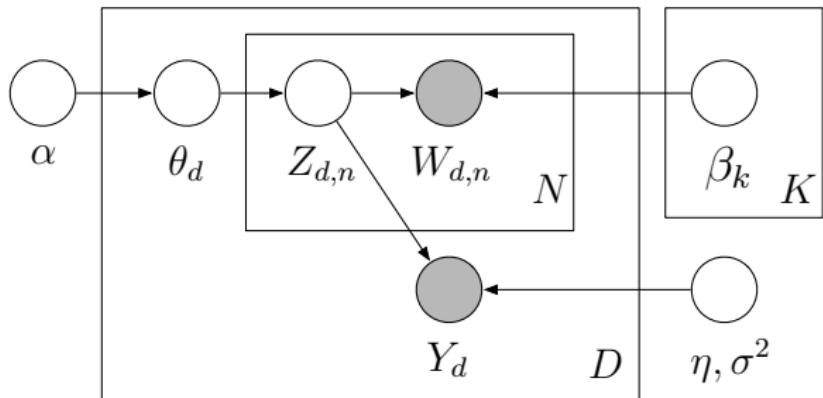
“We should seek out unfamiliar summaries of observational material, and establish their useful properties... And still more novelty can come from finding, and evading, still deeper lying constraints.”

(John Tukey, *The Future of Data Analysis*, 1962)

Supervised topic models (with Jon McAuliffe)

- Most topic models are *unsupervised*. They are fit by maximizing the likelihood of a collection of documents.
- Consider documents paired with response variables.
For example:
 - Movie reviews paired with a number of stars
 - Web pages paired with a number of “diggs”
- We develop *supervised topic models*, models of documents and responses that are fit to find topics predictive of the response.

Supervised LDA



- ① Draw topic proportions $\theta | \alpha \sim \text{Dir}(\alpha)$.
- ② For each word
 - ① Draw topic assignment $z_n | \theta \sim \text{Mult}(\theta)$.
 - ② Draw word $w_n | z_n, \beta_{1:N} \sim \text{Mult}(\beta_{z_n})$.
- ③ Draw response variable $y | z_{1:N}, \eta, \sigma^2 \sim \mathcal{N}(\eta^\top \bar{z}, \sigma^2)$, where

$$\bar{z} = (1/N) \sum_{n=1}^N z_n.$$

Comments

- SLDA is used as follows.
 - Fit coefficients and topics from a collection of document-response pairs.
 - Use the fitted model to predict the responses of previously unseen documents,

$$E[Y | w_{1:N}, \alpha, \beta_{1:K}, \eta, \sigma^2] = \eta^\top E[\bar{Z} | w_{1:N}, \alpha, \beta_{1:K}].$$

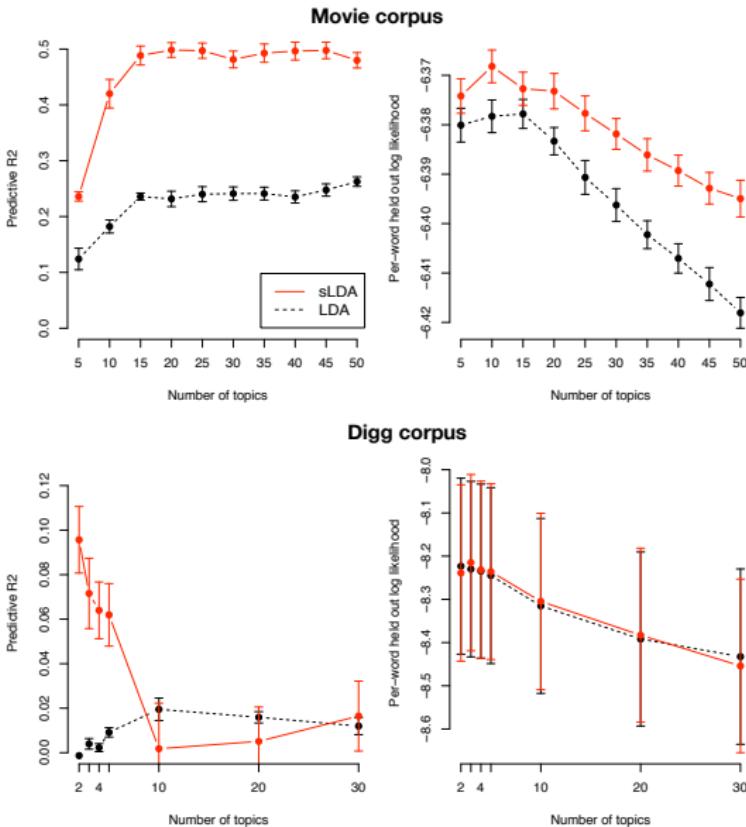
- The process enforces that the document is generated first, followed by the response. The response is generated from the particular topics that were realized in generating the document.

Example: Movie reviews



- We fit a 10-topic sLDA model to movie review data (Pang and Lee, 2005).
 - The documents are the words of the reviews.
 - The responses are the number of stars associated with each review (modeled as continuous).
- Each component of coefficient vector η is associated with a topic.

Simulations



Diversion: Variational inference

- Let $x_{1:N}$ be observations and $z_{1:M}$ be latent variables
- Our goal is to compute the posterior distribution

$$p(z_{1:M} | x_{1:N}) = \frac{p(z_{1:M}, x_{1:N})}{\int p(z_{1:M}, x_{1:N}) dz_{1:M}}$$

- For many interesting distributions, the marginal likelihood of the observations is difficult to efficiently compute

Variational inference

- Use Jensen's inequality to bound the log prob of the observations:

$$\log p(x_{1:N}) \geq \mathbb{E}_{q_\nu} [\log p(z_{1:M}, x_{1:N})] - \mathbb{E}_{q_\nu} [\log q_\nu(z_{1:M})].$$

- We have introduced a distribution of the latent variables with free *variational parameters* ν .
- We optimize those parameters to tighten this bound.
- This is the same as finding the member of the family q_ν that is closest in KL divergence to $p(z_{1:M} | x_{1:N})$.

Mean-field variational inference

- Complexity of optimization is determined by factorization of q_ν
- In *mean field variational inference* q_ν is fully factored

$$q_\nu(z_{1:M}) = \prod_{m=1}^M q_{\nu_m}(z_m).$$

- The latent variables are independent.
 - Each is governed by its own variational parameter ν_m .
- In the true posterior they can exhibit dependence (often, this is what makes exact inference difficult).

MFVI and conditional exponential families

- Suppose the distribution of each latent variable conditional on the observations and other latent variables is in the exponential family:

$$p(z_m | \mathbf{z}_{-m}, \mathbf{x}) = h_m(z_m) \exp\{g_m(\mathbf{z}_{-m}, \mathbf{x})^T z_m - a_m(g_i(\mathbf{z}_{-m}, \mathbf{x}))\}$$

- Assume q_v is fully factorized and each factor is in the same exponential family:

$$q_{v_m}(z_m) = h_m(z_m) \exp\{\nu_m^T z_m - a_m(\nu_m)\}$$

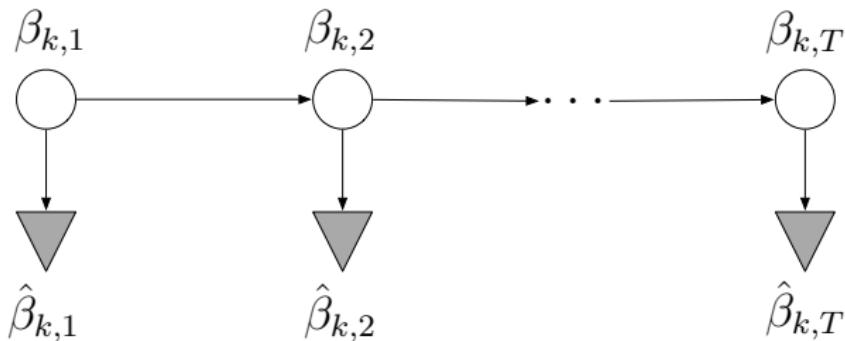
MFVI and conditional exponential families

- Variational inference is the following coordinate ascent algorithm

$$v_m = \mathbb{E}_{q_v}[g_m(\mathbf{z}_{-m}, \mathbf{x})]$$

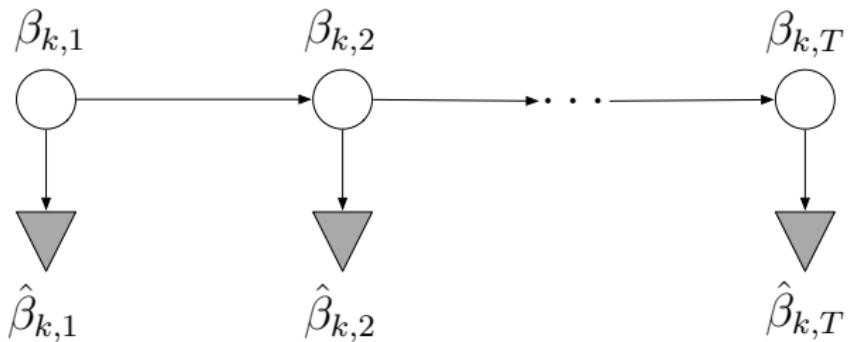
- Notice the relationship to Gibbs sampling

Variational family for the DTM



- Distribution of θ and z is fully-factorized (Blei et al., 2003)
- Distribution of $\{\beta_{1,k}, \dots, \beta_{T,k}\}$ is a *variational Kalman filter*
- Gaussian state-space model with free *observations* $\hat{\beta}_{k,t}$.
- Fit observations such that the corresponding posterior over the chain is close to the true posterior.

Variational family for the DTM



- Given a document collection, use coordinate ascent on all the variational parameters until the KL converges.
- Yields a distribution close to the true posterior of interest
- Take expectations w/r/t the simpler variational distribution