## **CMPT 280**

Tutorial: Heaps

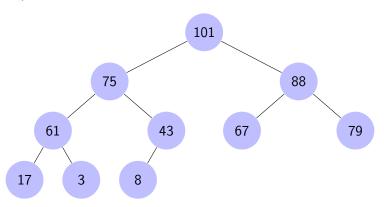
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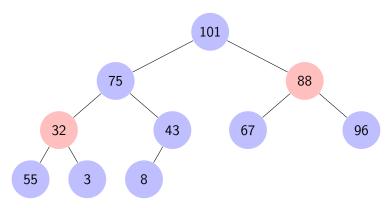
#### Heaps

- A heap is a special kind of array-based binary tree.
- Recall arrayed binary trees:
  - Every level is full except possibly the last level
  - All elements on the last level are as far to the left as possible.
- Heaps have an additional property, called the *heap property*: Every node is at least as large as both it's children.
- Thus, a heap is a "pile" of "stuff" where the largest things are on top.

#### A heap:



Not a heap (heap property is violated at red nodes):



#### Heap Insertion

Remember: heaps are usually implemented with arrayed trees.

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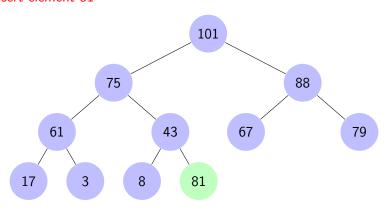
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```
Algoirthm insert(H, e)
Inserts the element e into the heap H.

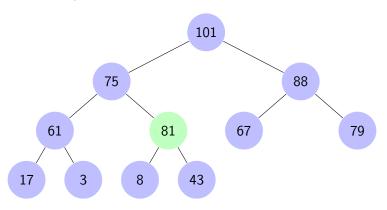
Insert e into H normally, as in ArrayedBinaryTreeWithCursors280<I>
// (put it in the left-most open position at the bottom level of the tree)

while e is larger than its parent and is not at the root:
    swap e with its parent
```

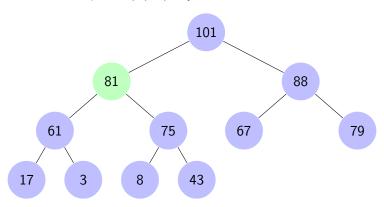
#### Insert element 81



#### After first swap.



After second swap. Heap property now satisfied.



## Heap Deletion

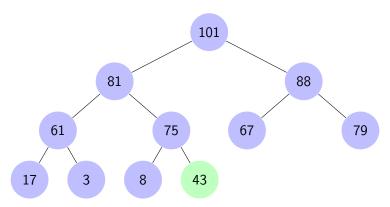
Heaps are dispensers. The current item is always the root. Thus when we remove from the heap, we always remove the top item.

```
Algorithm deleteItem(H)
Removes the largest element from the heap H.

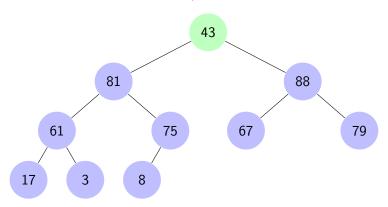
// Since the largest element in a heap is always at the root...
Remove the root from H normally, as in ArrayedBinaryTreeWithCursors280<I>
// (copy the right-most element in the bottom level, e, into the root,
// remove the original copy of e.)

while e is smaller than its largest child
swap e with its largest child
```

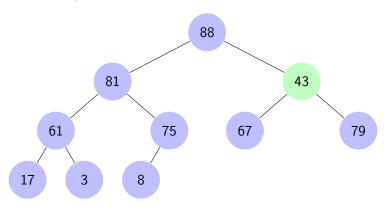
To remove the current element (always the root), move 43 to the root, overwriting 101.



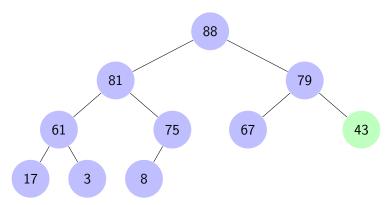
#### After move. Now we have to swap...



#### After first swap...



After second swap. Heap property restored.



#### **Exercises**

- Starting with the heap on the previous slide, insert 3 items of your choice, then remove three items of your choice.
- For at least one of the resulting heaps, draw its array representation.

#### Data Structures Humour

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