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អត្តមនសខ្ទេម

Simultaneous Localization and Mapping (SLAM) គឺជារបៀបមួយដែលត្រូវបានប្រើ
ប្រាស់យ៉ាងទូលំទូលាយសម្រាប់ការកំណត់ទីតាំងរបស់រូប៉ូតនិងបង្កើតជាផែនទីនៅក្នុង
បរិស្ថានជំវិញដូចជាលំនៅដ្វាន អាគារ សាលារៀន រោងចក្រ ជាដើម។ បើទោះបីជារបៀប
មួយនេះត្រូវបានប្រើប្រាស់និងអភិវឌ្ឈន៍យ៉ាងក៏ដោយក៏ទិន័យដែលទទូលបានមានភាព
ល្អៀងដោយសារតែភាពមិនសុក្រិត (Noise) នៃឧបករណ៍និងបរិស្ថាន។ ដូចនេះហើយទើប
ឧបករណ៍ (Sensor) ផ្សេងៗត្រូវបានជ្រើសរើសមកប្រើប្រាស់បញ្ចូលគ្នា (Fusion) ដើម្បីធ្វើអោ
យទិន័យដែលទទូលបានមានភាពប្រសើរដែលអាចទទូលយកបាន។ទិន័យដែលទទូល
បានអាចអនុញ្ញាតឱ្យយើងប្រើប្រាស់និងអនុវត្តជាមួយប្រាជ្ញាសិប្បនិម្មិត (AI) ដូចជា ការ
គ្រង់នៃគន្លងដំណើរ (Path Planning), ការធ្វើដំណើរក្នុងបរិស្ថានដែលមានភាពមិនបិតថេរ
(Dynamic Environment Navigation), ការចតយានយន្តស្វ័យប្រវិត្ត(Autonomous Parking),
ល។ សារណាមួយនេះនិយាយអំពីការអនុវត្ត Simultaneous Localization and Mapping
(SLAM) ដោយប្រើប្រាស់ Light Detection and Ranging Sensor (Lidar)។ MATLAB, Robotic
Operation System (ROS), GAZEBO Simulation គ្រូវបានប្រើសំរាប់ច្រីគំរូ និង Simulate។

RESUME

Simultanés Localisation et Mapping (SLAM) est une méthode qui a été utilisé par tout le monde pour localiser la location de robot et en même temp créer the plan de l'environnement au round de robot comme la maison, le bâtiment, l'université ou l'usine. Malgré le fait que cette méthode a été utilisé est développé de temp a temp, le data qui est obtient par cette méthode n'est pas précis cause par bruit d'appareil de senseur et l'environnement. De cette manière de plus en plus appareils de senseur sont choisi pour faire la fusion de senseur à la suite d'obtenir le data qui est optimise et plus acceptable. Le data qui nous obtenons par le SLAM méthode permet-nous d'utiliser and exécuter l'artificiel intelligent comme Trajectoires Planification (Path Planning), Navigation de Dynamique Environnement (Dynamic Environment Navigation), Autonome Parking (Autonomous Parking), etc. Ce mémoire présente l'application de Simultanés Localisation et Mapping (SLAM) par utilise Light Detection and Ranging Senseur (Lidar). MATLAB, Robotic Operation System (ROS), GAZEBO Simulation sont utilisé pour modéliser et simuler.

ABSTRACT

Simultaneous Localization and Mapping (SLAM) is a method that widely used for localizing the location of the robot and at the same time, create Occupancy Map of the environment such as residence, building, university/school, and factory. Despite the fact that this method is used and developed from time to time, the data acquired is not accurate that cause by noise produced by sensor and the environment surrounding. Thus, multiple sensors were chosen for sensor fusion in pursuit of obtaining the synthesized data that is optimized and acceptable. The data acquired from SLAM method allow us to use and implement the Artificial intelligent (AI) such as Robot Path Planning, Dynamic Environment Navigation, Autonomous Parking, etc. This thesis presents the Implementation of Simultaneous Localization and Mapping (SLAM) using Light Detection and Ranging Sensor (LIDAR). MATLAB, Robotic Operation System (ROS), Gazebo Simulation is used for modeling and simulation.

ABBREVIATION AND SYMBOLS

SLAM Simultaneous Localization and Mapping

IMU Inertial Measurement UnitROS Robotic Operation System

WMR Wheeled Mobile Robot

ICR Instantaneous center of rotation

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1. INTRODUCTION

1.1. Background

Simultaneous Localization and Mapping (SLAM) has been known to be one of the methods that has been used to localize the position of Robot in Global Frame at the same time creating the map out of that environment to further and enhance its autonomous functionality. To obtain the most accurate map data, multiple devices have been used in sensor fusion method to produce the best possible result. SLAM method has been widely used with Wheeled Mobile Robot (WMR) in order to acquire the map of the environment that the robot or vehicle currently in. The map of the environment that acquired from this method could be further in used of Path Planning and Autonomous Navigation.

1.2. Objectives

In this project, we present SLAM algorithm to build Occupancy Grid Map of surrounding environment using Lidar by the implementation of Hector SLAM ROS package, Gmapping SLAM ROS package and MATLAB SLAM. Gazebo 3D Simulation Software will be used to simulate the model of WMR that equipped with simulate sensor (Lidar, IMU, Odometry) and the surrounding environment. RVIZ will be used as the visualization tool for Occupancy Map, WMR model, robot trajectories and sensor data.

1.3. Scope

The Occupancy Grid Map is represented in two dimensional (2D) as (x,y). The Two Wheels Differential drive WMR is designed in two dimensional (2D) planar motion (x,y) and the orientation of the robot is represented by the rotation angle ϕ from the global map frame. All the work has been done inside the Gazebo 3D Simulation. The environment is considered to be Indoor. We are using the sensor data that is obtained from the simulation 2D Lidar, IMU, Odometry.

2. LITERATURE REVIEWS

Navigating of robots around the unknown environment has been a challenging problem for the robotic community for the past years. The majority of mobile robot require map of the environment so that it can move inside that place. Building the map from the bottom up is very essential because it reduces the amount of work that involves the installation of mobile robots. In addition, it enables the mobile robot to easily adapt to change without human intervention. As the matter of fact, mapping is one of the core competencies of a truly autonomous robot.(Thrun, 2002)

SLAM is a method that is used for building and updating the map of the environment while the robot is moving inside the unknown environment and localizing itself in the map. SLAM takes all the available sensors that are equipped on the robot to estimate its position and collects scans from any ranging sensor, builds up the occupancy map and determines the location of itself in that map. The trajectory of the mobile robot and landmark are all being estimated from the input data of the sensor online without pre-knowledge of location.

In SLAM, we use a probabilistic approach in order to solve the SLAM problem. We called it Probabilistic SLAM. In this approach the probabilistic distribution is required to be computed during the process. There are two main forms of the SLAM problem: Online SLAM and Full SLAM.

Online SLAM is the process of estimating the posterior map from a recently collected data from sensors at time t

$$p(x_t, m | z_{1:t}, u_{1:t})$$
 (Eq 2.1.)

Where x_t is the position at time t

m is the map

 $z_{1:t}$ is the measurement

 $u_{1:t}$ is the control vector

Full SLAM is the process of calculating the posterior map from the full trajectories of the mobile robot.

$$p(x_{1:t}, m|z_{1:t}, u_{1:t})$$
 (Eq 2.2.)

Where $x_{1:t}$ is the position from the initial time to time t

m is the map

 $z_{1:t}$ is the measurement

 $u_{1:t}$ is the control vector

3. SIMULTANEOUS LOCALIZATION AND MAPPING USING LIDAR

3.1. Occupancy Grid

3.1.1. Introduction / Properties

Occupancy grid map is one of many pieces of information that are required for the mobile robot for navigation tasks such as path planning, driving a round, mapping the environment, and localizing. It is a 2D representation of the environment.

Occupancy grid map consists of many occupancy grids cells. Each of grid cells is represented as an occupied cell or a free cell according to the calculation of binary probability value. In short, a 2D occupancy map is a large set that contains a probability value in every cell.

$$m_{x,y} = \{free, occupied\} = \{0,1\}$$
 (Eq 3.1.)

The occupied cell is represented by a probability value of (1) with black color and the free cell is represented by a probability value of (0) with white color. On the Assumption of that the cell is either occupied or free, each probability value contain in each cell are independent, and the surrounding environment is static.

Occupancy grid maps are fine-grained grids defined over the continuous space of locations and often used after solving the SLAM problem by some other means, and taking the resulting path estimates for granted.

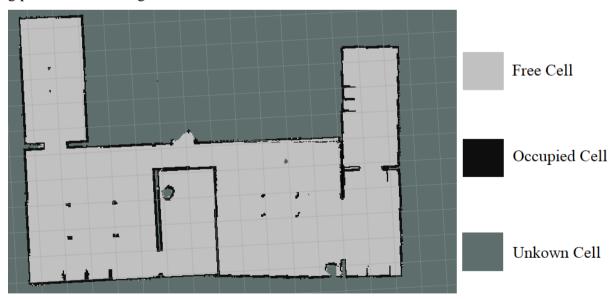


Figure 3.1. Occupancy Grid Map

3.1.2. Occupancy Grid Mapping Algorithm

In Occupancy Grid Mapping Algorithm also known as mapping with known pose the control $u_{1:t}$ is omitted. The main goal of any occupancy grid mapping algorithm is to calculate the posterior over maps given the data represented in probability value

$$p(m|z_{1:t},x_{1:t})$$
 (Eq 3.2.)

Where m is the map

 $z_{1:t}$ the set of all measurements up to time t

 $x_{1:t}$ is the path of the robot, that is, the sequence of all its poses.

In the occupancy grid, each grid cells address is represented with index. The size of grid cell is expressed with map resolution m_r [m/cell].

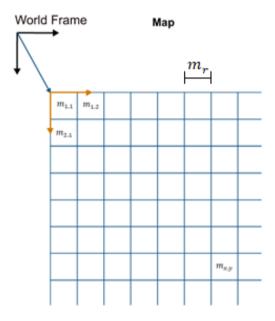


Figure 3.2. Occupancy Grid Map Cell

Let m_i denote the grid cell with index i. An occupancy grid map partitions the space into finitely many grid cells

$$m = \sum_{i} m_i \tag{Eq 3.3.}$$

The notation $p(m_i = 1)$ or $p(m_i)$ will refer to a probability that a grid cell is occupied.

The standard occupancy grid approach breaks down the problem of estimating the map into a collection of separate problems, namely that of estimating

$$p(m_i | z_{1:t}, x_{1:t})$$
 (Eq 3.4.)

for all grid cell m_i . Each of these estimation problems is now a binary problem with static state.

This decomposition is convenient but not without problems. In particular, it does enable us to represent dependencies among neighboring cells; instead, the posterior over maps is approximated as the product of its marginals:

$$p(m | z_{1:t}, x_{1:t}) = \prod_{i} p(m_i | z_{1:t}, x_{1:t})$$
 (Eq 3.5.)

As the estimation of Occupancy Grid cell has become a static state binary problem, we are using Static State Binary Bayes Filters.

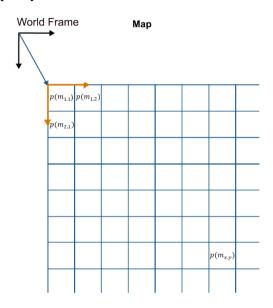


Figure 3.3. Occupancy Grid Map Probability Cell

When using occupancy grids with probability values, the goal is to estimate the probability of obstacle locations for use in real-time robotics applications. The Occupancy Map uses a *log-odds* representation of the probability values for each cell. Each probability value is converted to a corresponding *log-odds* value for internal storage. The value is converted back to probability when accessed. This representation efficiently updates probability values with the fewest operations. Thus, integrate sensor data into the map can be calculate quickly.

(The MathWorks, 2019)

Log-odd Notation

$$odd(x \ event) = \frac{probability \ of \ x \ event \ happen}{probability \ of \ x \ event \ not \ happen} = \frac{p(x)}{p(-x)} = \frac{p(x)}{1 - p(x)}$$
 (Eq 3.6.)

The Log-odd is the logarithm of above equation

$$l(x) := \log \frac{p(x)}{1 - p(x)}$$
 (Eq 3.7.)

$$p(x) = 1 - \frac{1}{1 + expl(x)}$$
 (Eq 3.8.)

Substitute in $p(m_i | z_{1:t}, x_{1:t})$ with p(x), We get

$$l_{t,i} = log \frac{p(m_i | z_{1:t}, x_{1:t})}{1 - p(m_i | z_{1:t}, x_{1:t})}$$
(II) (Eq 3.9.)

On (I) Using Bayes rule, we get

$$p(m_i | z_{1:t}, x_{1:t}) = \frac{p(z_t | m_i, z_{1:t-1}, x_{1:t}) p(m_i | z_{1:t-1}, x_{1:t})}{p(z_t | z_{1:t-1}, x_{1:t})}$$
(Eq 3.10.)

Using Markov Assumption on Eq 3.10., we get

$$p(m_i | z_{1:t}, x_{1:t}) = \frac{p(z_t | m_i, x_t) p(m_i | z_{1:t-1}, x_{1:t-1})}{p(z_t | z_{1:t-1}, x_{1:t})}$$
(Eq 3.11.)

We have

$$p(z_t|m_i, x_t) = \frac{p(m_i|z_t, x_t)p(z_t|x_t)}{p(m_i|x_t)}$$
 (Eq 3.12.)

Substitute Eq 3.12. to Eq 3.11., we get

$$p(m_i | z_{1:t}, x_{1:t}) = \frac{p(m_i | z_t, x_t) p(z_t | x_t) p(m_i | z_{1:t-1}, x_{1:t-1})}{p(m_i | x_t) p(z_t | z_{1:t-1}, x_{1:t})}$$
(Eq 3.13.)

Using Markov Assumption on Eq 3.13., We get

$$p(m_i | z_{1:t}, x_{1:t}) = \frac{p(m_i | z_t, x_t) p(z_t | x_t) p(m_i | z_{1:t-1}, x_{1:t-1})}{p(m_i) p(z_t | z_{1:t-1}, x_{1:t})}$$
(Eq 3.14.)

On (II) We have

$$1 - p(m_i | z_{1:t}, x_{1:t}) = p(-m_i | z_{1:t}, x_{1:t})$$
 (Eq 3.15.)

The same calculation above, we obtain

$$p(-m_i | z_{1:t}, x_{1:t}) = \frac{p(-m_i | z_t, x_t) p(z_t | x_t) p(-m_i | z_{1:t-1}, x_{1:t-1})}{p(-m_i) p(z_t | z_{1:t-1}, x_{1:t})}$$
(Eq 3.16.)

Divide **Eq 3.14.** with **Eq 3.16.**

$$\frac{p(m_i \mid z_{1:t}, x_{1:t})}{1 - p(m_i \mid z_{1:t}, x_{1:t})} = \frac{\frac{p(m_i \mid z_t, x_t) p(z_t \mid x_t) p(m_i \mid z_{1:t-1}, x_{1:t-1})}{p(m_i) p(z_t \mid z_{1:t-1}, x_{1:t})}}{\frac{p(-m_i \mid z_t, x_t) p(z_t \mid x_t) p(-m_i \mid z_{1:t-1}, x_{1:t-1})}{p(-m_i) p(z_t \mid z_{1:t-1}, x_{1:t})}}$$

$$\frac{p(m_i \mid z_{1:t}, x_{1:t})}{1 - p(m_i \mid z_{1:t}, x_{1:t})} = \frac{\frac{p(m_i \mid z_t, x_t) \ p(m_i \mid z_{1:t-1}, x_{1:t-1})}{p(m_i)}}{\frac{p(-m_i \mid z_t, x_t) \ p(-m_i \mid z_{1:t-1}, x_{1:t-1})}{p(-m_i)}}$$

$$\frac{p(m_i \mid z_{1:t}, x_{1:t})}{1 - p(m_i \mid z_{1:t}, x_{1:t})} = \frac{p(m_i \mid z_t, x_t) p(m_i \mid z_{1:t-1}, x_{1:t-1}) p(-m_i)}{p(-m_i \mid z_t, x_t) p(-m_i \mid z_{1:t-1}, x_{1:t-1}) p(m_i)}$$

$$\frac{p(m_i \mid z_{1:t}, x_{1:t})}{1 - p(m_i \mid z_{1:t}, x_{1:t})} = \frac{p(m_i \mid z_t, x_t)}{p(-m_i \mid z_t, x_t)} \frac{p(m_i \mid z_{1:t-1}, x_{1:t-1})}{p(-m_i \mid z_{1:t-1}, x_{1:t-1})} \frac{p(-m_i)}{p(m_i)}$$
(Eq 3.17.)

Apply *Log* on **Eq 3.17.**

$$\log \frac{p(m_i | z_{1:t}, x_{1:t})}{1 - p(m_i | z_{1:t}, x_{1:t})} = \log \left(\frac{p(m_i | z_t, x_t)}{p(-m_i | z_t, x_t)} \frac{p(m_i | z_{1:t-1}, x_{1:t-1})}{p(-m_i | z_{1:t-1}, x_{1:t-1})} \frac{p(-m_i)}{p(m_i)} \right)$$

We get

$$log \frac{p(m_i | z_{1:t}, x_{1:t})}{1 - p(m_i | z_{1:t}, x_{1:t})} = log \frac{p(m_i | z_t, x_t)}{p(-m_i | z_t, x_t)} + log \frac{p(m_i | z_{1:t-1}, x_{1:t-1})}{p(-m_i | z_{1:t-1}, x_{1:t-1})} + log \frac{p(-m_i)}{p(m_i)}$$

$$l_{t,i} = l(m_i | z_{1:t}, x_{1:t}) = l(m_i | z_t, x_t) + l(m_i | z_{1:t-1}, x_{1:t-1}) - l(m_i)$$

$$l_{t,i} = inverse_sensor_model(m_i, x_t, z_t) + l_{t-1,i} - l_0$$
(Eq 3.20.)

Where

$$l(m_i|z_t, x_t) = inverse_sensor_model(m_i, x_t, z_t)$$
 $l(m_i|z_{1:t-1}, x_{1:t-1}) = l_{t-1,i}$
 $l(m_i) = l_0$

Table 3.1. The Occupancy Grid Algorithm, with Binary Bayes Filter (Thrun, 2002)

Occupancy Grid Mapping Algorithm	Line
Algorithm occupancy_grid_mapping($\{l_{t-1,i}\}, x_t, z_t$):	1
For all cell m_i do	2
If m_i in perceptual field of z_t then	3
$l_{t,i} = l_{t-1,i} + inverse_sensor_model(m_i, x_t, z_t) - l_0$	4
else	5
$l_{t,i} = l_{t-1,i}$	6
endif	7
Endfor	8
return $\{l_{t,i}\}$	9

Eq 3.20. is used to update the occupancy grid cell. In **Table 3.1.**Line4, if the grid cell falls inside the scan area of lidar, the algorithm will return a new grid cell that its probability value change according to the scan if it is occupied or free. In **Table 3.1.**Line 6, if the grid cell does not fall inside the scan area of lidar, its probability value remains unchanged.

3.1.3. Inverse Sensor Model for Lidar

In Eq 3.20., to update the occupancy grid, we incorporate a new the measurement from the lidar and update the existing probability value inside each grid with new calculation from lidar. Given the current WMR position on a cell grid and the measurement from a lidar scan region, we assign the probability value to the cell that lidar beam past through. If the detection happens in cells grid, the probability value of that cells grid will be calculated with a new assign probability value from lidar output represented with l_{occ} , and the cells which shorter from occupied cell will be assign as free cells lidar output represented with l_{free} . If there is not any occupied detection from lidar outside the lidar max scan range, the cells will be considered to be unknown represented with l_0 prior cells.

In this thesis, we assign
$$l_{occ}$$
 =0.9 l_{free} =0.4 l_0 =0.5

Table 3.2. Inverse 2D Lidar Sensor Model Algorithm (Steven Waslander, n.d.)

Inverse Lidar Sensor Model Algorithm	Line
Algorithm inverse_lidar_sensor_model(i, x_t, z_t):	1
Let x_i , y_i be the center of mass of m_i	2
$r^{i} = \sqrt{\left(m_{x}^{i} - x_{1,t}\right)^{2} + \left(m_{y}^{i} - x_{2,t}\right)^{2}}$	3
$\phi^{i} = \tan^{-1} \frac{(m_{x}^{i} - x_{1,t})}{(m_{y}^{i} - x_{2,t})} - x_{3,t}$	4
$k = argmin_j \phi^i - \phi^s_j $	5
If $r > \min(r_{\max}^s)$	6
return l_0	7
If $r_k^s < r_{\max}^s$	8
return l_{occ}	9
If $r^i \leq r_k^s$	10
return l_{free}	11
endif	12

Where r is the range from lidar to grid cell

 m_x , m_y is the center of cell

 x_1, x_2 is sensor location

3.2. Simultaneous Localization and Mapping (SLAM) Algorithm

There is numerous SLAM algorithm that has been develop over the year. One of them is Scan Matching. Scan matching is the process of aligning laser scans with each other (Scan to Scan Matching) or with an existing map (Scan to Map Matching). Using Scan Matching algorithm, the main idea is to find the rigid transformation in robot pose from two different scans. Scan Matching algorithm can be corporate with many different kinds of range finder sensors. Thus, in this thesis we use lidar as our range finder sensor. As the lidar scans data being subscribe with ROS and publish to the algorithm, scans get aligned with the existing map, or another scan and the matching is implicitly performed with all preceding scans.(Kohlbrecher et al., 2011)

To find the rigid transformation of robot pose that make the best lidar scan alignment, we have to find transformation $\xi = (p_x, p_y, \phi)^T$ that minimizes

$$\xi^* = argmin_{\xi} \sum_{i=1}^{n} [1 - M(S_i(\xi))]^2$$
 (Eq 3.21.)

Where

 $S_i(\xi)$ are the world coordinates of scan endpoint $S_i = \begin{pmatrix} S_{i,x} \\ S_{i,y} \end{pmatrix}$

 $S_i(\xi)$ is the function of ξ , the pose of the robot in the world coordinate.

$$S_{i}(\xi) = \begin{pmatrix} \cos\phi & -\sin\phi \\ \sin\phi & \cos\phi \end{pmatrix} \begin{pmatrix} s_{i,x} \\ s_{i,x} \end{pmatrix} + \begin{pmatrix} p_{x} \\ p_{y} \end{pmatrix}$$
 (Eq 3.22.)

The function $M(S_i(\xi))$ return the map value at the coordinate given by $S_i(\xi)$. Given some starting estimate of ξ , we want to estimate $\Delta \xi$ which optimize the error measure according to

$$\sum_{i=1}^{n} \left[1 - M(S_i(\xi)) \right]^2 \to 0$$
 (Eq 3.23.)

Using the first order of Taylor expansion of $M(S_i(\xi + \Delta \xi))$ we get

$$\sum_{i=1}^{n} \left[1 - M(S_i(\xi)) - \nabla M(S_i(\xi)) \frac{\partial S_i(\xi)}{\partial \xi} \Delta \xi) \right]^2 \to 0$$
 (Eq 3.24.)

This equation in minimized by setting the partial derivative with respect to $\nabla \xi$ to zero

$$2\sum_{i=1}^{n} \left[\nabla M \left(S_{i}(\xi) \right) \frac{\partial S_{i}(\xi)}{\partial \xi} \right]^{T} \left[1 - M \left(S_{i}(\xi) \right) - \nabla M \left(S_{i}(\xi) \right) \frac{\partial S_{i}(\xi)}{\partial \xi} \Delta \xi) \right] = 0 \qquad \text{(Eq 3.25.)}$$

Solving for $\Delta \xi$ yields the Gauss-Newton equation for the minimization problem

$$\Delta \xi = H^{-1} \sum_{i=1}^{n} \left[\nabla M \left(S_i(\xi) \right) \frac{\partial S_i(\xi)}{\partial \xi} \right]^T \left[1 - M(S_i(\xi)) \right]$$
 (Eq 3.26.)

Where

$$H = \left[\nabla M \left(S_i(\xi) \right) \frac{\partial S_i(\xi)}{\partial \xi} \right]^T \left[\nabla M \left(S_i(\xi) \right) \frac{\partial S_i(\xi)}{\partial \xi} \right]$$

An approximation for the map gradient $\nabla M(S_i(\xi))$ is provided is section IV-A in Hector SLAM (Kohlbrecher et al., 2011)

With Eq 3.22., we get

$$\frac{\partial S_i(\xi)}{\partial \xi} = \begin{pmatrix} 1 & 0 & -\sin\phi s_{i,x} - \cos\phi s_{i,y} \\ 0 & 1 & \cos\phi s_{i,x} - \sin\phi s_{i,y} \end{pmatrix}$$
 (Eq 3.27.)

3.3. Robotic Operating System (ROS)

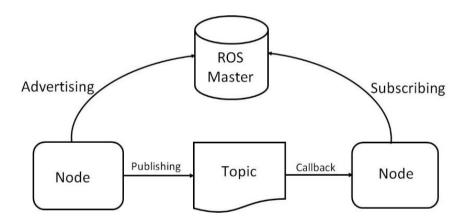


Figure 3.4. ROS Framework

Robotic operating system (ROS) is an open source framework develop for robotic purpose. It contains libraries and package that are already build and ready to use for robot. ROS is a peer-to-peer network of process that could run on multiple devices that connected via network.

ROS center of communication is ROS Master. ROS master act as a keeper of topics and services registration and information of ROS node. ROS nodes are the process of performing the computation. It publishes or subscribes ROS messages with other nodes via ROS topics. ROS message is data that have been simplified into a structure.

3.3.1. Gazebo Simulation

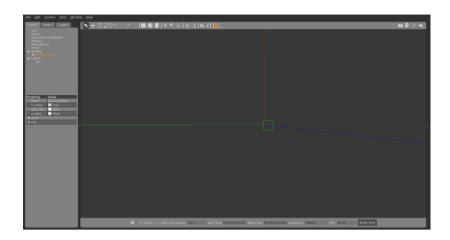


Figure 3.5. Gazebo Simulation Window

Gazebo is an open source physic 3D simulator that allow user to simulate and design the robot and the environment. Gazebo has the ability to simulate a highly accurate robot and sensor with the noise from the environment similarly to a game engine. In this thesis, we use Gazebo simulator a main software for our robot, sensor, and the environment simulation.

3.3.1.1 Gazebo Environment

In Gazebo environment, user can create their own robot accordingly to their design as well as the scenario of the surrounding environment for the experiment. In this thesis, we use Turtlebot3 Burger as a main simulate WMR that are equipped with Lidar, IMU, Odometry sensor. In addition to that, multiple scenarios will be used for SLAM implementation.

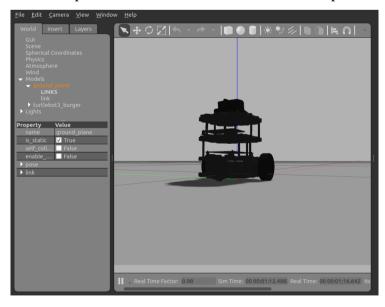


Figure 3.6. Turtlebot3 Burger Simulation Window

3.3.1.2 Subscribed / Published Topic

In Gazebo 3D Simulator, the WMR (Turtlebot3 Burger) subscribed to a controller keyboard teleoperation topic in order to move via the command from the user. Gazebo publish multiple ROS massage data such as robot state, link state, lidar, IMU and Odometry sensor, to the ROS topic from the simulator onto ROS master. By using the ROS message from the simulation, we can use it as a simulate data source for SLAM.

```
File Edit View Search Terminal Help
royuth@yuth-Inspiron-5459:~$ rostopic list
/clock
/cmd vel
/gazebo/link_states
/gazebo/model_states
/gazebo/parameter_descriptions
/gazebo/parameter updates
/gazebo/set_link_state
/gazebo/set model state
imu
'joint_states
/odom
/rosout
rosout_agg
scan
```

Figure 3.7. Gazebo Simulation ROS Topic **Table 3.3.** Publish and Subscribe Simulation Topic

Topic	Message type	Frame ID	Description	Function
/joint_states	/sensor_msgs /JointState		Status of joint in robot	Publish
/cmd_vel	/geometry_msgs /Twist		Command WMR	Subscribe
/imu	/sensor_msgs /Imu	/base_imu	Data from IMU	Publish
/odom	/nav_msgs /Odometry	/odom	Data from Odometry	Publish
/scan	/sensor_msgs /Laserscan	/base_laser	Data from lidar	Publish
/tf	/tf/tfMessage		Transform package	Publish

3.3.2. Coordinate Frame

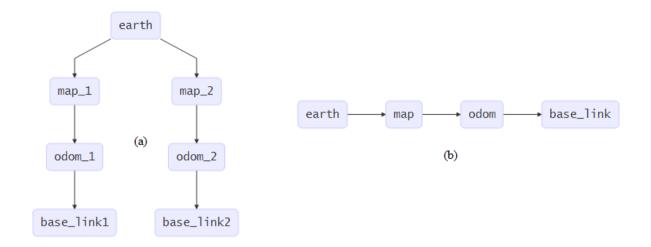


Figure 3.8. Coordinate Frame Relationship (a) Multiple Map; (b) Single Map

In SLAM, there are multiple coordinate frames that we need to utilize. Thus, we must define the base reference of those coordinates. According to ROS community guideline REP[105] (Wim Meeuseen, 2010) Coordinate Frames for Mobile Platform, we define

- Base_link or Base_frame as the coordinate that attached to mobile robot base. We define it as the point of reference of the WMR. Base_link is main link that WMR sensor is attached to.
- **Odom** as the world-fixed frame that is continuous without discrete jumps. This frame is drift over time that can accumulate the error in long term or in a large-scale map.
- **Map** as the world-fixed frame that is not continuous. In this frame the pose of WMR can be change with discrete jump.
- **Earth** as the coordinate the allow interaction between multiple maps.
- Laser_frame as the coordinate that assign to Lidar.

In the Gazebo Simulation, Lidar sensor is attached on top of the WMR. Thus, the when the WMR move, the coordinate of the Lidar move along with it. Map frame and Odom frame, is the static coordinate, while Base frame and Lidar coordinate move it Map frame and Odom frame.

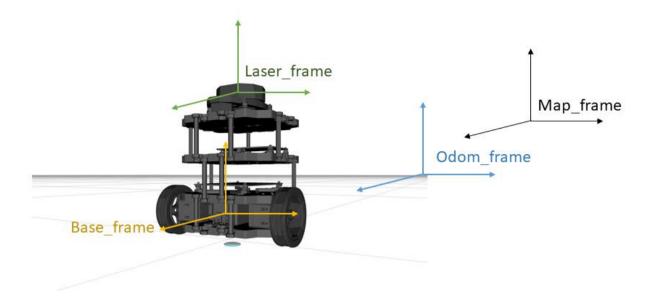


Figure 3.9. Simulation Coordinate Frame

3.3.3. *tf Tree*

In any physical system there tend to be more than one coordinate frame. Thus, keeping track of all the coordinate frame is very important in our work.

tf the one of the most important ROS packages that enable user to track all coordinate frame as well as maintaining the relationship between each frame and publish it during the operation time, we can compute and transform one frame to another frame with this simple tf package. tf defined the robot with position and orientation. Position is expressed as vector (x, y, z) and the orientation is expressed as quaternion vector form with (x, y, z, w).

In this thesis, tf package for static transform publisher has been used for transform coordinate system. In order to using this package, the following syntax has been used static_transform_publisher x y z yaw pitch roll frame_id child_frame_id period_in_ms where

static_transform_publisher is the name of tf package

x/y/z is offset [m]

yaw/pitch/roll is rotation about x, y, z in [rad]

frame_id is the name of main frame

childframe_id is the name of the frame that will be transform to

period is how often to send a transform [ms]

3.3.4. RVIZ

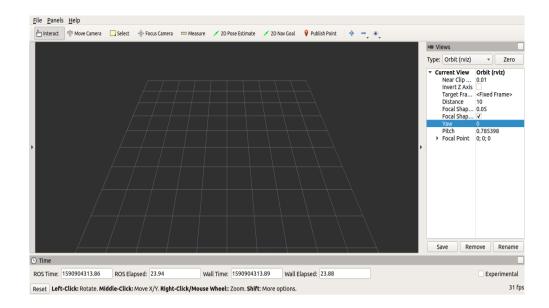


Figure 3.10. RVIZ Window

RVIZ is one of the 3D visualizations tools in ROS. RVIZ allow us to visualize and verify the incoming data from the ROS messages. In this thesis, RVIZ is used to visualize the Occupancy Grid Map, Robot Model, Sensor Data.

3.4. SLAM Packages

There are numerous Open source SLAM packages that developed by many robotic communities over the year. Most notable are Hector SLAM, Gmapping SLAM, and MATLAB SLAM which are used in this thesis for the implementation of SLAM.

3.4.1. Hector SLAM Package (ROS)

Hector SLAM Package is one of many SLAM packages in ROS develop by Team Hector. Hector SLAM use hector_mapping ROS node for SLAM algorithm, provide the map of the environment. Scan Matching SLAM approach has been implemented in order to determine the displacement of WMR in 2D from previous and current consecutive scan. Hector SLAM can be use with or without the odometry data.(Stefan Kohlbrecher, 2012)

Table 3.4. Publish and Subscribe Hector SLAM Topic

Topic	Message Type	Description	Function	
/scan	/sensor_msgs	Data from Lidar	Subscribe	
/sean	/LaserScan	Data Holli Lidai		
/syscommand	/std_msgs	User command Reset map	Subscribe	
/syscommand	/String	Osci command Reset map	Buosciide	
/map_metadata	/nav_msgs	Map Data	Publish	
/map_metadata	/MapMetaData	Map Data	i uolisii	
/man	/nav_msgs	Map Data	Publish	
/map	/OccupancyGrid	Wap Data	r ublisii	
/slam out nosa	/geometry_msgs	Robot pose estimated	Publish	
/slam_out_pose	/PoseStamped	without covariance	i uonsn	
/poseupdata	/gaomatry maga	Robot pose estimated with		
	/geometry_msgs	Gaussian estimation of	Publish	
	/PoseWithCovarianceStamped	uncertainty		

 Table 3.5. Hector SLAM Parameters

Parameters Name	Description
base_frame	Main frame attached to robot for localization
map_frame	Frame of the map
odom_frame	Frame attached to Odometry
map_resolution	Size of grid cell in [m]
map_size	Number of cells per axis
map_start_x	Map origin on x axis
map_start_y	Map origin on y axis
map_update_distance_tresh	Threshold for performing map update in [m]
map_update_angle_tresh	Threshold for performing map update in [m]
map_pub_period	The map publish period in [s]
map_multi_res_levels	The number of map multi-resolution grid levels
updata_factor_free	The map update modifier for free cell l_{free}
update_factor_occupied	The map update modifier for occupied cell l_{occ}

laser_min_dist	The minimum distance for laser scan endpoint to be used	
rasci_mm_dist	in system in [m]	
locar may dist	The maximum distance for laser scan endpoint to be	
laser_max_dist	used in system in [m]	
laser_z_min_value	The minimum height relative to the laser_frame	
laser_z_max_value	The maximum height relative to the laser_frame	
pub_map_odom_transform	Publish map_frame to odom_frame	
output timing	Output timing information for processing of every laser	
output_timing	scan	
scan_subscriber_queue_size	The queue size of the scan subscriber	
pub_map_scanmatch_transform	Publish map_frame to scanmatcher_frame	
tf_map_scanmatch_transform_	Commetchen from a name	
frame_name	Scanmatcher_frame name	

Hector SLAM Package Provide tf Transform /map_frame to /odom_frame that estimate the current robot's pose in /map_frame. We have to provide our own tf transform from robot link (/base_link) to lidar link (/laser_frame) using tf static_transform_publisher ROS package.

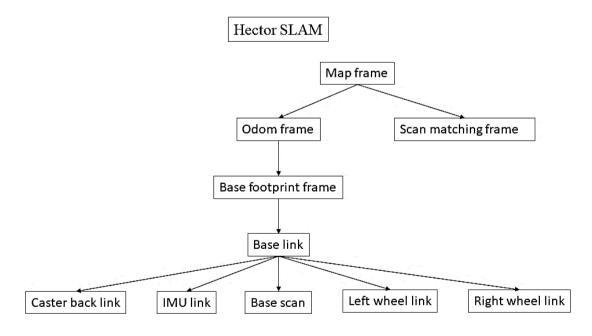


Figure 3.11. Hector SLAM tf frame

3.4.2. Gmapping SLAM Package (ROS)

Gmapping SLAM is another SLAM ROS package which is developed by OpenSlam. Gmapping SLAM provide a laser-based SLAM by using slam_gmapping ROS node. Gmapping SLAM use Scan Matching algorithm for matching the income scans just like Hector SLAM. Using Gmapping SLAM required an odometry information in order to localize the robot pose. (Brian Gerkey, 2019)

Table 3.6. Publish and Subscribe Gmapping SLAM Topic

Topic	Message Type	Description	Function
/scan	/sensor_msgs	Data from Lidar	Subscribe
/scan	/LaserScan	Data Hom Eldar	Subscribe
/tf	/tf/tfMessage	Frame transformation	Subscribe
/ 1	/nav_msgs	Man Data	ta Publish
/map_metadata	/MapMetaData	Map Data	ruonsn
/map	/nav_msgs	Map Data	Publish
	/OccupancyGrid		Publish
		Entropy of the distribution estimation	
/entropy	/std_msgs/Float64	over robot's pose (higher is more	Publish
		uncertain)	

Table 3.7. Gmapping SLAM Parameters

Parameters Name	Description
inverted_laser	Laser CCW or CW
throttle_scans	Process 1 out of this many scan (Skip scan)
base_frame	Main frame attached to robot for localization
map_frame	Frame of the map
odom_frame	Frame attached to Odometry
map_update_interval	Duration between map update [s]
maxurange	Maximum usable range of the laser
sigma	The greedy endpoint matching
kernelsize	Look for a correspondence
lstep	The optimization step in translation

astep The optimization step in rotation

interation The number of iterations of the scan matcher

lsigma The sigma of beam used for likelihood computation

Gain used while evaluating the likelihood for smoothing

ogain resampling effects

Number of beams to skip

Minimum score for considerating the outcome of the scan

minimumscore matching good

odom error in translation as a function of translation (ρ/ρ)

odom error in translation as a function of rotation (ρ/θ)

str Odom error in rotation as a function of translation (θ/ρ)

stt Odom error in rotation as a function of rotation (θ/θ)

linearupdate Process a scan each time robot translates

angularupdate Process a scan each time robot rotates

Process a scan if the last scan processed is older that update

temporalupdate

lskip

time [s]

resamplethreshold The Neff based resampling threshold

particles Number of Particle in the filter

xmin Initial map size in x axis [m]

xmax Initial map size in x axis [m]

ymin Initial map size in y axis [m]

ymax Initial map size in y axis [m]

delta Size of grid cell in [m]

llsamplerange Translational sampling range for the likelihood

llsamplestep Translational sampling step for the likelihood

lasamplerange Angular sampling range for the likelihood

lasamplestep Angular sampling step for the likelihood

occ_thresh Threshold on gmapping's occupancy value.

maxrange Lidar maximum range

Gmapping SLAM Package Provide tf Transform /map_frame to /odom_frame that estimate the current robot's pose in /map_frame. We have to provide our own tf transform from lidar link (laser_frame) to robot link (base_link) and robot link (base_link) to odometry link (odom) using tf static_transform_publisher.

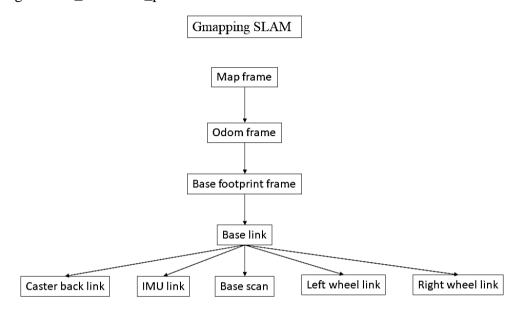


Figure 3.12. Gmapping SLAM tf frame

3.4.3. MATLAB SLAM Package

Using MATLAB SLAM in Navigation Toolbox, we create an object that waiting for the series of incoming scan data from ROS Lidar subscribe function. We use **scansAndPoses** function to retrieve the collected scan and the estimated poses from the class the stored the scans information, then build the occupancy map using **buildMap** function.

Table 3.8. MATLAB SLAM Function

Function	Parameters		Description	
Function	Input	Description Output		
lidarSLAM	mapResolution	Lidar Slam	Create on chicatta standidaman	
	maxLidarRange	Create an object to store lida Class		
lidarScan	Ranges	Lidar data	Create lidarscan object from lidar	
	Angles	Liuai uata		
addScan	lidarSLAM	C 11 1	Add scan to lidarSLAM object	
		Collected scans		
	lidarScan			

scansAndPoses	lidarSLAM	scans	Extract scans and poses from	
		optimizedPoses	lidarSLAM object	
buildMap	Scans		Create an acquirency man	
	OptimizedPoses	OccupancyMap		
	mapResolution	Оссирансумар	Create an occupancy map	
	maxLidarRange			

3.5. Wheel Mobile Robot

Wheel Mobile Robot is one of the ground robots that move via the wheel that attached to robot's body frame. There are different types of WMR that can be named after the number of wheels, drive mode, etc. WMR usually has been used as moving platform to move another object. In Robotic Community, WMR are equipped with sensors for further its functionality.

In this thesis, we use the Turtlebot3 Burger two wheels differential drive robot as a moving platform for our simulation.



Figure 3.13. Turtlebot3 Burger

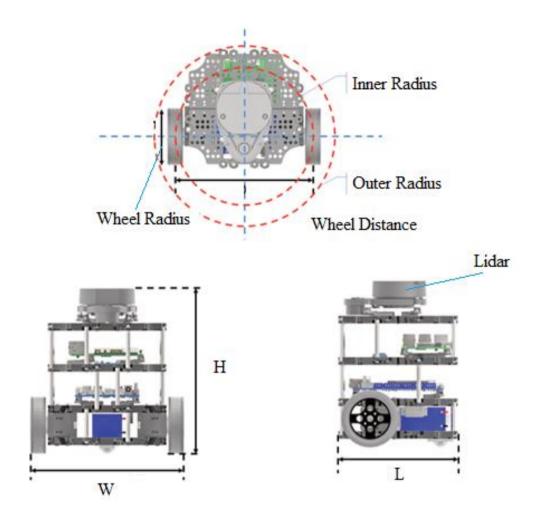


Figure 3.14. Turtlebot3 Burger Specification

Table 3.9. Hardware Specification

Parameters	Value	Unit
Wheel Radius	66	mm
Robot Width (W)	178	mm
Robot Length (L)	138	mm
Robot Height (H)	192	mm
Distance between wheel	160	mm
Robot Outer Radius	105	mm
Robot Inner Radius	80	mm
Maximum Translational velocity	0.22	mm/s
Maximum Rotational velocity	2.84	rad/s

Table 3.10. WMR Sensor

Sensor	Description	
Lidar	360 degrees scanner	
	Gyroscope 3 Axis	
IMU	Accelerometer 3 Axis	
	Magnetometer 3 Axis	
Odometer	2 Wheels Odometer	

3.5.1. Differential Drive WMR Kinematic Model

The WMR pose in 2D plane is defined in state vector as

$$\xi(t) = \begin{bmatrix} p_{x(t)} \\ p_{y(t)} \\ \phi(t) \end{bmatrix}$$
 (Eq 3.28.)

The Global coordinate frame is represented as (X_g, Y_g) , and Robot frame is represented as (X_m, Y_m) . Using ROS coordinate system representation as Global Frame is /map_frame and WMR frame is /base_link. The relation between the global frame and robot frame is defined by a translation vector $[x, y]^T$ and rotation matrix about z axis

$$R_z(\phi) = \begin{bmatrix} \cos\phi & \sin\phi & 0\\ -\sin\phi & \cos\phi & 0\\ 0 & 0 & 1 \end{bmatrix}$$
 (Eq 3.29.)

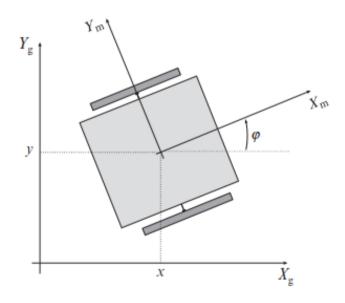


Figure 3.15. 2D Coordinate of Robot

For Two Wheels Differential drive WMR, its movement is depending on the rotation velocity of each wheel. These two wheels is independent to each other, meaning one can rotate faster or slower than the other. To make the rotation, each wheel could rotate in the same or different direction of each other at the different rotation rate. During the rotation of WMR in circular motion, there exist a common point that is intersect of 2-wheel axes called Instantaneous center of rotation (ICR).(Klančar et al., 2017)

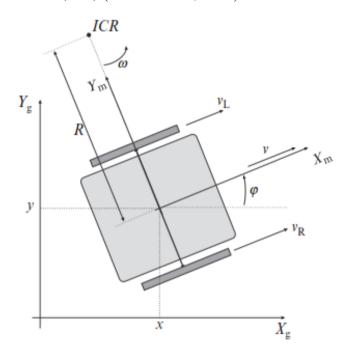


Figure 3.16. Differential Drive Kinematics

Let $v_R(t)$ is the velocity of the right wheel

 $v_L(t)$ is the velocity of the left wheel

r is the wheel radius

L is the distance between wheel

R(t) is the ICR

 $\omega(t)$ is the angular velocity in which both wheel rotate in the instance of time

v(t) is the WMR tangential velocity

 $\omega(t)$ is expressed as

$$\omega(t) = \frac{v_L(t)}{R(t) - L/2}$$
 (Eq 3.30.)

$$\omega(t) = \frac{v_{R(t)}}{R(t) - L/2}$$
 (Eq 3.31.)

From **Eq 3.30.** and **Eq 3.31.**

$$\omega(t) = \frac{v_R(t) - v_L(t)}{L}$$
 (Eq 3.32.)

$$R(t) = \frac{L}{2} \frac{v_R(t) + v_L(t)}{v_R(t) - v_L(t)}$$
 (Eq 3.33.)

v(t) is expressed as

$$v(t) = \omega(t)R(t) = \frac{v_R(t) + v_L(t)}{2}$$
 (Eq 3.34.)

Each wheel tangential velocities are expressed as

$$v_L(t) = r\omega_L(t) \tag{Eq 3.35.}$$

$$v_R(t) = r\omega_R(t)$$
 (Eq 3.36.)

In Local coordinate frame, WMR kinematic

$$\begin{bmatrix} p_{x_m(t)} \\ p_{y_m(t)} \\ \dot{\phi}(t) \end{bmatrix} = \begin{bmatrix} v_{x_m}(t) \\ v_{y_m}(t) \\ \omega(t) \end{bmatrix} = \begin{bmatrix} \frac{r}{2} & \frac{r}{2} \\ -\frac{r}{L} & \frac{r}{L} \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \omega_L(t) \\ \omega_R(t) \end{bmatrix}$$
(Eq 3.37.)

In Global coordinate frame, WMR kinematic

$$\begin{bmatrix} p_{x(t)} \\ p_{y(t)} \\ \dot{\phi}(t) \end{bmatrix} = \begin{bmatrix} \cos(\phi(t)) & 0 \\ \sin(\phi(t)) & 0 \\ 0 & 1 \end{bmatrix} v(t)$$

$$(Eq 3.38.)$$

Eq 3.38. can be written in discrete Euler integration form with discrete time instant $t = kT_s$ where T_s is the sampling interval and k = 0,1,2,...

$$p_{x(k+1)} = p_{x(k)} + v(k)T_{s}\cos(\phi(k))$$

$$p_{y(k+1)} = p_{y(k)} + v(k)T_{s}\sin(\phi(k))$$

$$\phi(k+1) = \phi(k) + \omega(k)T_{s}$$
(Eq 3.39.)

Forward Kinematics

Odometry of the robot is the pose of the robot at time t that is obtained by integration of kinematic model. Odometry is explored more in 3.6.2.

$$p_{x(t)} = \int_0^t v(t) \cos(\phi(t)) dt$$

$$p_{y(t)} = \int_0^t v(t) \sin(\phi(t)) dt$$

$$\phi(t) = \int_0^t \omega(t) dt$$
(Eq 3.40.)

Case 1: If v and ω is assumed to be constant during sample time x(k+1), y(k+1), $\phi(k+1)$ is expressed in Eq 3.39.

Case 2: If trapezoidal numerical integration is used, a better approximation is:

$$p_{x(k+1)} = p_{x(k)} + v(k)T_s\cos\left(\phi(k) + \frac{\omega(k)T_s}{2}\right)$$

$$p_{y(k+1)} = p_{y(k)} + v(k)T_s\sin\left(\phi(k) + \frac{\omega(k)T_s}{2}\right)$$

$$\phi(k+1) = \phi(k) + \omega(k)T_s$$
(Eq 3.41.)

Case 3: If exact integration is applied

$$p_{x(k+1)} = p_{x(k)} + \frac{v(k)}{\omega(k)} (\sin(\phi(k) + \omega(k)T_s) - \sin(\phi(k)))$$

$$p_{y(k+1)} = p_{y(k)} - \frac{v(k)}{\omega(k)} (\cos(\phi(k) + \omega(k)T_s) - \cos(\phi(k)))$$

$$\phi(k+1) = \phi(k) + \omega(k)T_s$$
(Eq 3.42.)

3.6. Sensor

3.6.1. Light Detection and Ranging Sensor (LIDAR)

Lidar is a remote sensing device that use light pulses laser to detect the distance from an object and has been widely used for multi-purposes including navigation and mapping. Lidar usually contain of laser scanner and DC motor. DC motor rotates the laser scanner in 360 degrees circle in order to obtain a full 360 degrees of the environment. In this thesis, we use the simulation from 2D lidar that scan a 2D slice of a surrounding 3D environment.

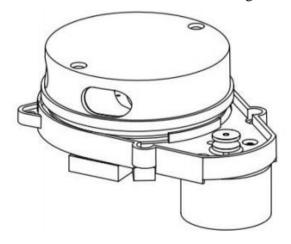


Figure 3.17. Lidar

3.6.1.1 Coordinate Frame

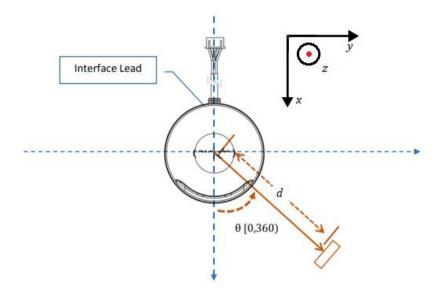


Figure 3.18. Lidar Coordinate System

Lidar Coordinate in 3D Cartesian coordinate system is (x, y, z) where z is pointing upward. But we only use the 2D Lidar simulation data, thus the Lidar Coordinate will be represented in 2D Cartesian coordinate system (x, y) and the rotation angle of θ . The distance from the center of the laser scan to the object is d. When the DC motor rotate, different angle θ and distance d will be recorded, each θ and d are correspond to each other.

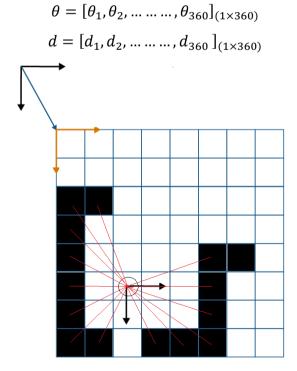


Figure 3.19. Lidar Laser Beam

3.6.1.2 Published ROS Topic

In ROS, Lidar node launch and publish on /scan topic with ROS message type sensor_msg/LaserScan.msg. The Lidar coordinate frame is /laser_frame.

Table 3.11. Lidar Properties

ROS message	Definition	Unit
header	Timestamp and frame_id	
angle_min	Started angle of scan	rad
angle_max	End angle of scan	rad
angle_increment	Angular distance between scan to scan	rad
time_increment	Time between one full scan to one full scan	S
scan_time	Time between scan to scan	S
range_min	Minimum range	m
range_max	Maximum range	m
ranges	Range data in one full scan	m
intensities	Intensity data	_

3.6.2. Odometry

Odometry is the estimation of robot position and velocity within the environment using the calculation from the sensor data. Odometry can be computed from odometry source such as wheel odometry, visual odometry (camera), or an IMU.

In Odometry 3D coordinate system the robot position is represented as (P_x, P_y, P_z) and the orientation of the robot is represented as ϕ . As our robot is in 2D planar motion, thus we only interested in $\begin{pmatrix} p_x \\ p_y \\ \phi \end{pmatrix}$ as written in state space form.

When using ROS message, the odometry directly publish with the position and the orientation of the robot from the simulated environment. The position is expressed as (x, y, z) and the orientation in quaternion form (x, y, z, w).

3.6.2.1 Published ROS Topic

In ROS, Odometry node launch and publish on /odom topic with ROS message type nav_msgs/Odometry.msg. The Odometry coordinate frame is /odom_frame.

 Table 3.12. Odometry Properties

ROS message	Definition	
Header	Timestamp and frame_id	
Child_frame_id		
Geometry_msgs/PoseWithCovariance	Estimation of WMR Position in free space with	
Geometry_msgs/rose withCovariance	uncertainty	
Coometer, maga/Paga	Contain the information of the position (x, y, z)	
Geometry_msgs/Pose	and orientation in quaternion form (x, y, z, w)	
Geometry_msgs/TwistWithCovariance	Estimation of WMR Velocity in free space with	
Geometry_msgs/1 wist with Covariance	uncertainty	
Coometer, maga/Twist	Contain the information of velocity in linear and	
Geometry_msgs/Twist	angular	

4. SIMULATION AND DISCUSSION

4.1. Simulation

In this thesis, we use Gazebo Simulation as our data source. Three of SLAM package, Hector SLAM, Gmapping SLAM and MATLAB SLAM, are carrying out. Using keyboard command to control robot movement in Gazebo simulation. During the operation time, the simulation output the sensor data and we subscribe to the data to use in each of SLAM packages. In ROS the Occupancy Grid will be viewed in RVIZ while in MATLAB it will be view in MATLAB Figure.

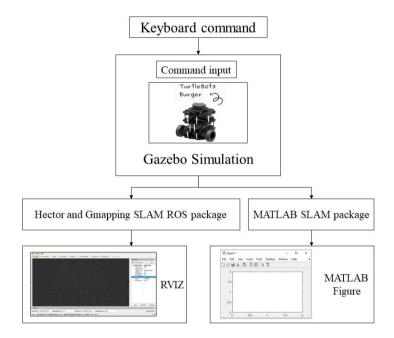


Figure 4.1. Simulation Flow

4.2. Preparation Simulation

Before the simulation start, we have to configure the parameters of each package as well as our WMR parameters to meet our desire and as close as possible to the real-world condition. The file that required to modify are:

For Hector SLAM Package configuration main SLAM file Mapping_default.launch, we set odom_frame to /odom, base_frame to /base_footprint, scan_topic to /scan, map_frame to /map. For Gmapping SLAM Package configuration main SLAM file gmapping_default.launch, we set odom_frame to /odom, base_frame to /base_footprint, map_frame to /map.

For MATLAB SLAM Package configuration script, we initiate MATLAB and ROS communication with rosinit function and set subscriber to ROS scan topic /scan.

4.3. Data Collection and Analysis

MATLAB SLAM

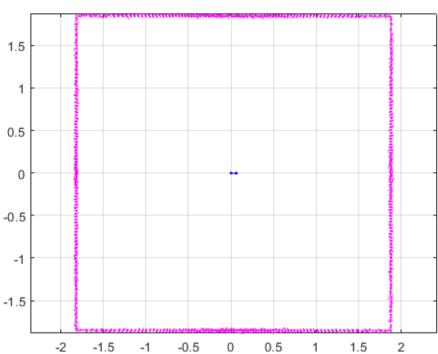


Figure 4.2. MATLAB Pose Graph SLAM gazebo_stage_1

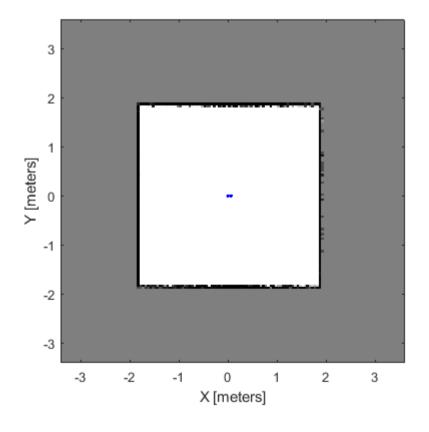


Figure 4.3. MATLAB Occupancy Map gazebo_stage_1

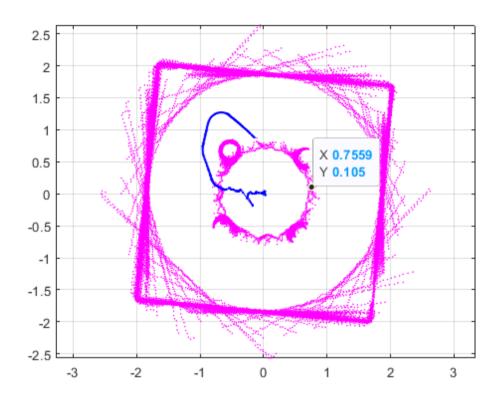


Figure 4.4. MATLAB Pose Graph SLAM gazebo_stage_2

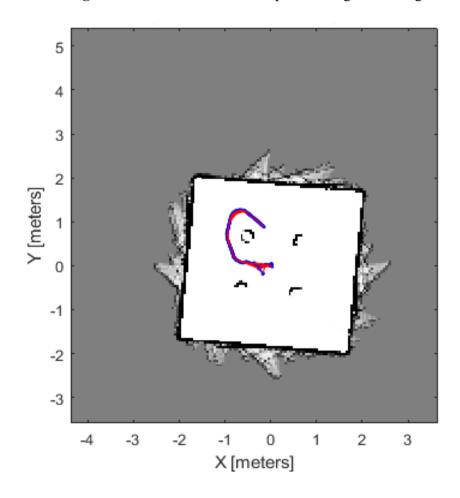


Figure 4.5. MATLAB Occupancy Map gazebo_stage_2

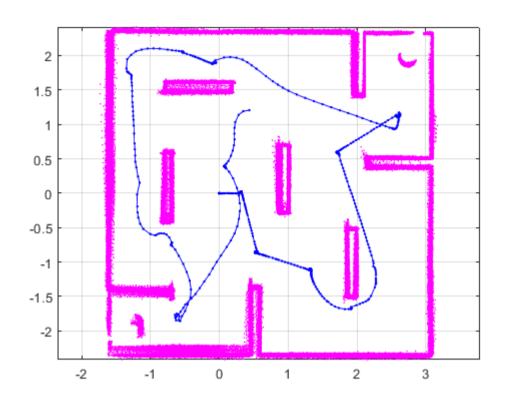


Figure 4.6. MATLAB Pose Graph SLAM gazebo_stage_3

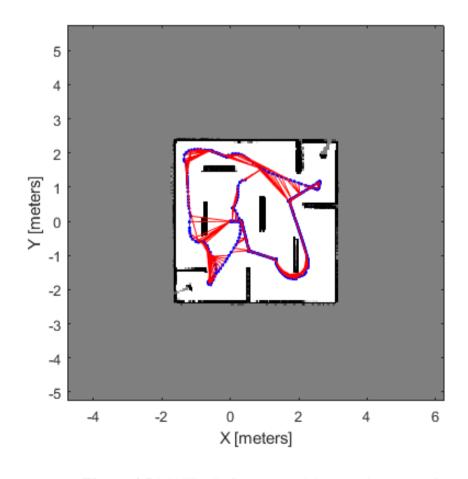


Figure 4.7 MATLAB Occupancy Map gazebo_stage_3

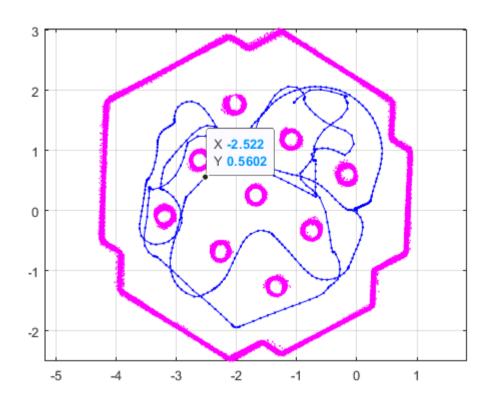


Figure 4.8. MATLAB Pose Graph SLAM gazebo_world

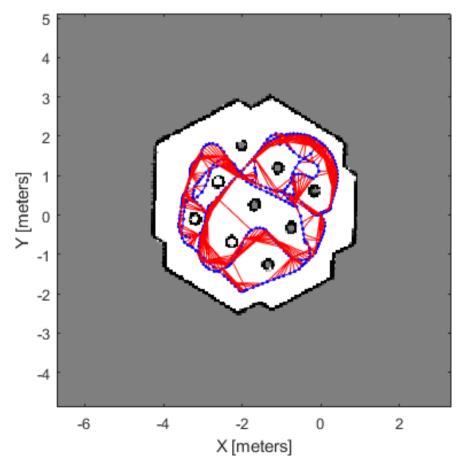


Figure 4.9. MATLAB Occupancy Map gazebo_world

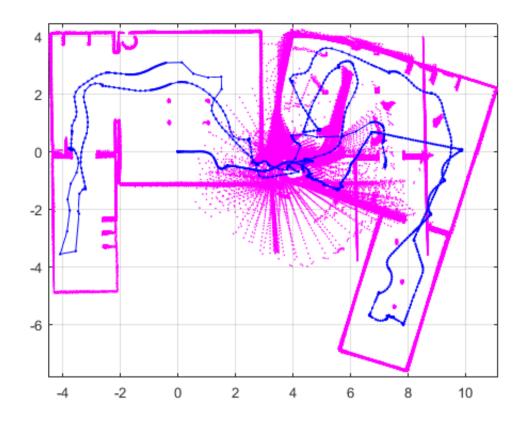


Figure 4.10. MATLAB Pose Graph SLAM gazebo_house

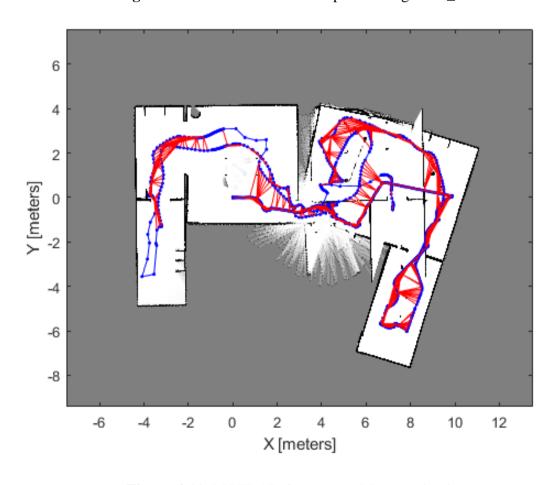


Figure 4.11. MATLAB Occupancy Map gazebo_house

Hector SLAM and Gmapping SLAM Packages

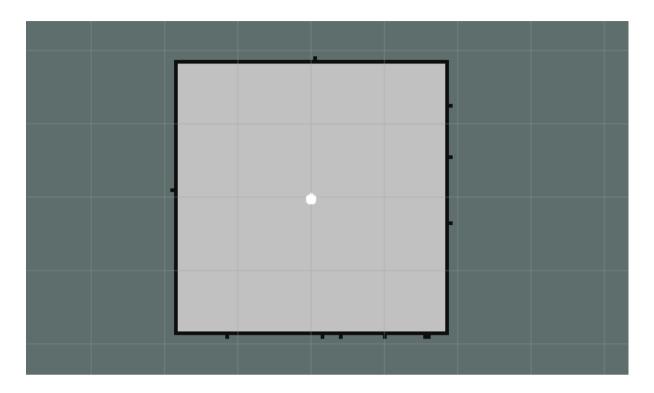


Figure 4.12. Gmapping SLAM Occupancy Map gazebo_stage_1

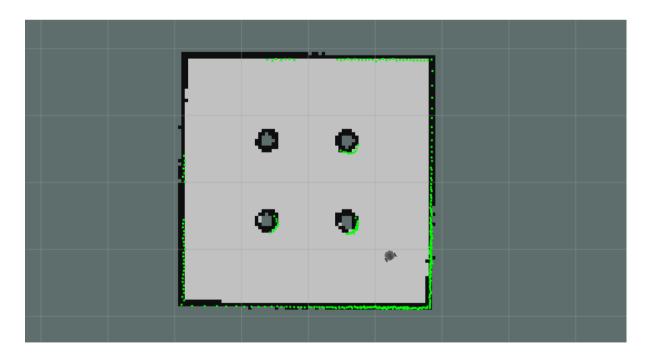


Figure 4.13. Gmapping SLAM Occupancy Map gazebo_stage_2

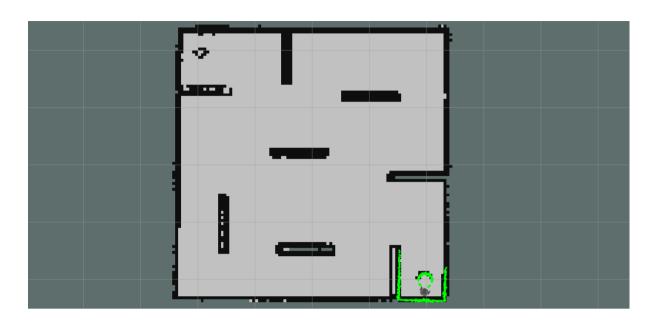


Figure 4.14. Gmapping SLAM Occupancy Map gazebo_stage_3

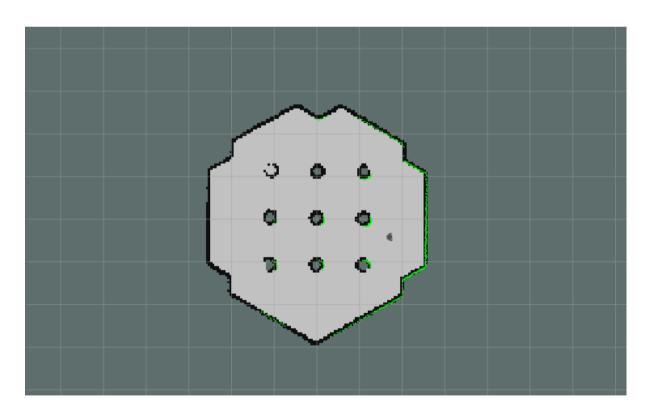


Figure 4.15. Gmapping SLAM Occupancy Map gazebo_world

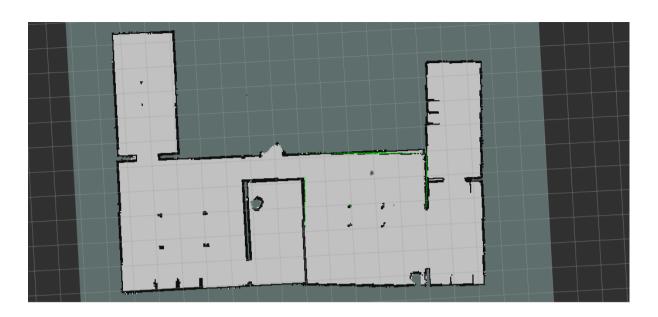


Figure 4.16. Gmapping SLAM Occupancy Map gazebo_house

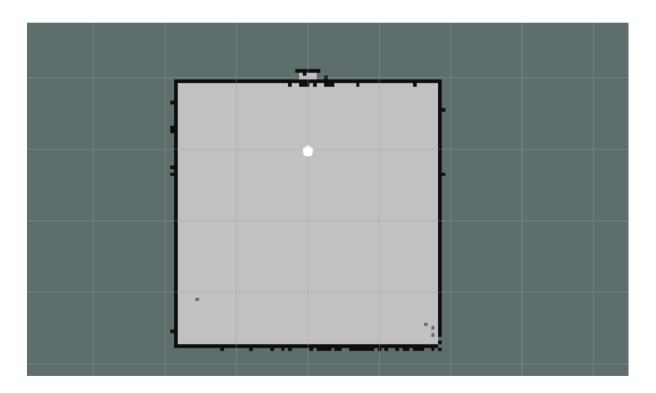


Figure 4.17. Hector SLAM Occupancy Map gazebo_stage_1

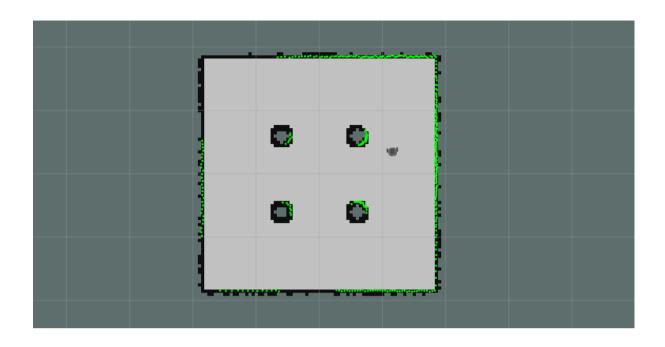


Figure 4.18. Hector SLAM Occupancy Map gazebo_stage_2

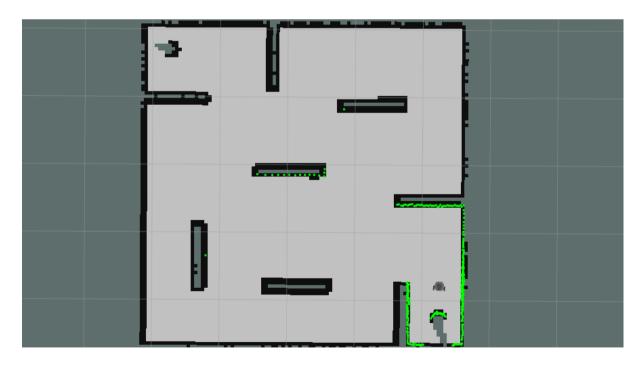


Figure 4.19. Hector SLAM Occupancy Map gazebo_stage_3

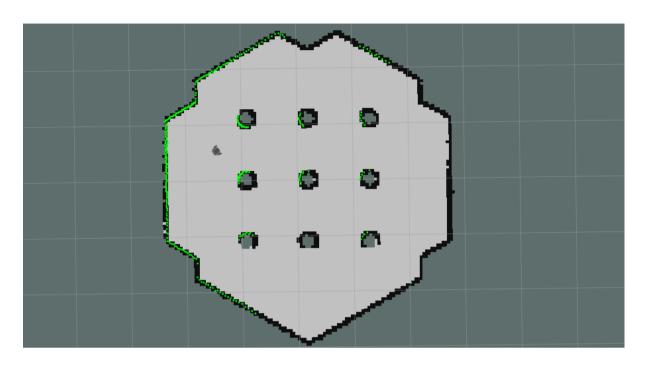


Figure 4.20. Hector SLAM Occupancy Map gazebo_world



Figure 4.21. Hector SLAM Occupancy Map gazebo_house

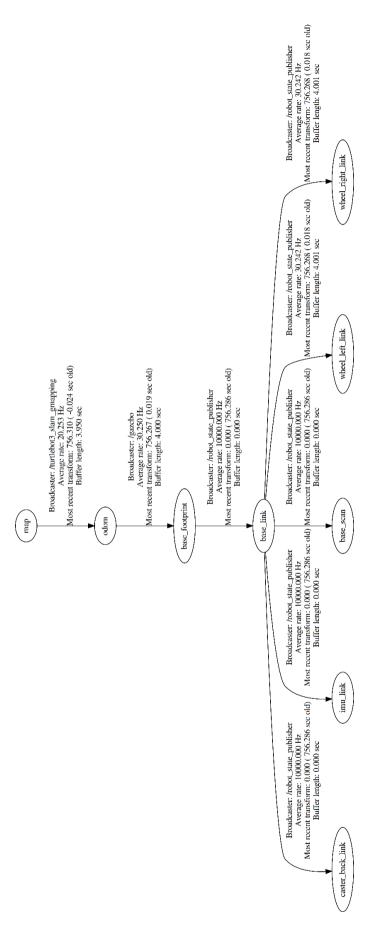


Figure 4.22. Gmapping SLAM tf Tree

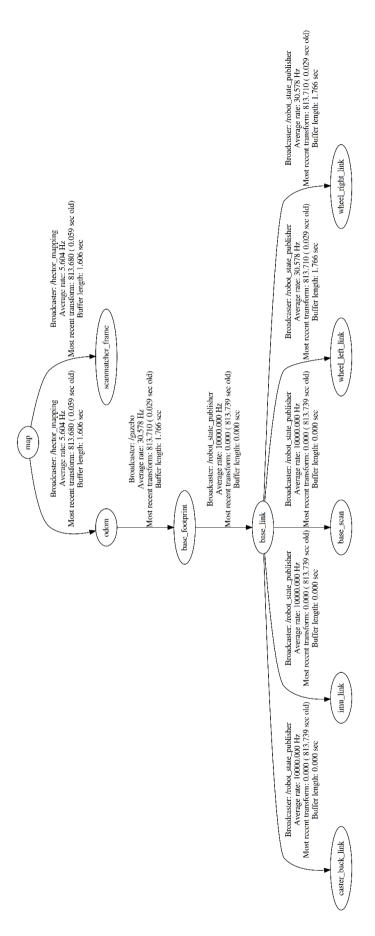


Figure 4.23. Hector SLAM tf Tree

5. CONCLUSION AND RECOMMENDATION

5.1. Conclusion

To conclude in this thesis, SLAM algorithm is presented. By using the simulation software, we are able to simulate the two-wheel differential drive WMR equipped with Lidar sensor and Odometry that publish data to implement SLAM. ROS is used as the main operation system to carry out the SLAM packages such as Hector SLAM, Gmapping SLAM, and MATLAB SLAM to create the Occupancy Grid Map of the simulated environment. While RVIZ and MATLAB are used for displaying the Occupancy Grid Map and sensor data. Comparing the obtained map from SLAM to the simulation environment, we can see the map represents the environment well in small scale map but induces error for a bigger scale one because of the accumulated error from odometry data. As the matter of fact, these maps can be used for robot navigation field.

5.2. Recommendation Future Work

Using this SLAM approach with the data from the simulation give an acceptably good result. For the future work, this approach will be using in real world condition with the real data from the WMR and sensor. As we know, the incoming data from the real sensor will be corrupted by noise that effect on the obtained occupancy grid map. Thus, the sensor data filter can be used to correctly create an acceptable map for real use purpose such as path planning, autonomous driving and dynamic environment navigation with the help from other type of sensors.

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 2) Module 2: Mapping for Planning / Coursera. Retrieved June 28, 2020, from
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APPENDIX A

MATLAB SLAM

MATLAB SLAM script

```
%clear
close all
clc
응응
laser = rossubscriber('/scan'); %subscribe to /scan topic
maxLidarRange = 3.4;
mapResolution = 20;
slamAlg = lidarSLAM(mapResolution, maxLidarRange);
slamAlg.LoopClosureThreshold = 210;
slamAlg.LoopClosureSearchRadius = 8;
for i = 1:1500
    laserdata = receive(laser,1);
    Angles = double([0:0.0175:6.2832]');
    Ranges = double(laserdata.Ranges);
    lidarScanNew=lidarScan(Ranges, Angles);
    [isScanAccepted, loopClosureInfo, optimizationInfo] =
addScan(slamAlg, lidarScanNew);
    if isScanAccepted
        fprintf('Added scan %d \n', i);
    end
end
응응
figure
show(slamAlg);
title({'Map of the Environment Pose Graph'});
%% occupancy grid map built
[scans, optimizedPoses] = scansAndPoses(slamAlg);
map = buildMap(scans, optimizedPoses, mapResolution,
maxLidarRange);
```

```
figure;
show(map);
hold on
show(slamAlg.PoseGraph, 'IDs', 'off');
hold off
title('Occupancy Grid Map Built Using Lidar SLAM');
```

APPENDIX B

Hector SLAM

```
Hector SLAM configuration file:
```

```
hector_ws/src/hector_slam/hector_mapping/launch/mapping_default.launch
```

```
<?xml version="1.0"?>
<launch>
  <arg name="tf map scanmatch transform frame name"</pre>
default="scanmatcher frame"/>
  <arg name="base frame" default="base footprint"/>
  <arg name="odom frame" default="odom"/>
  <arg name="pub map odom transform" default="true"/>
  <arg name="scan subscriber queue size" default="5"/>
  <arg name="scan topic" default="scan"/>
  <arg name="map size" default="2048"/>
  <node pkg="hector mapping" type="hector mapping"</pre>
name="hector mapping" output="screen">
    <!-- Frame names -->
    <param name="map frame" value="map" />
    <param name="base frame" value="$(arg base frame)" />
    <param name="odom frame" value="$(arg odom frame)" />
    <!-- Tf use -->
    <param name="use tf scan transformation" value="true"/>
    <param name="use tf pose start estimate" value="false"/>
    <param name="pub map odom transform" value="$(arg</pre>
pub map odom transform)"/>
    <!-- Map size / start point -->
    <param name="map resolution" value="0.050"/>
```

```
<param name="map size" value="$(arg map size)"/>
    <param name="map start x" value="0.5"/>
    <param name="map_start y" value="0.5" />
    <param name="map multi res levels" value="2" />
    <!-- Map update parameters -->
    <param name="update factor free" value="0.4"/>
    <param name="update_factor occupied" value="0.9" />
    <param name="map update distance thresh" value="0.4"/>
    <param name="map update angle thresh" value="0.06" />
    <param name="laser z min value" value = "-1.0" />
    <param name="laser z max value" value = "1.0" />
    <!-- Advertising config -->
    <param name="advertise map service" value="true"/>
    <param name="scan subscriber queue size" value="$(arg</pre>
scan subscriber queue size)"/>
    <param name="scan topic" value="$(arg scan topic)"/>
    <!-- Debug parameters -->
    <!--
      <param name="output_timing" value="false"/>
      <param name="pub drawings" value="true"/>
      <param name="pub debug output" value="true"/>
    -->
    <param name="tf map scanmatch transform frame name"</pre>
value="$(arg tf map scanmatch transform frame name)" />
  </node>
  <node pkg="tf" type="static transform publisher"</pre>
name="map_nav_broadcaster" args="0 0 0 0 0 map odom 100"/>
</launch>
```

Hector SLAM launch file:

```
hector_ws/src/hector_slam/hector_slam_launch/launch/tutorial.launch
```

```
<?xml version="1.0"?>
<launch>
  <arg name="geotiff map file path" default="$(find</pre>
hector geotiff)/maps"/>
  <param name="/use sim time" value="true"/>
  <node pkg="rviz" type="rviz" name="rviz"</pre>
    args="-d $(find
hector slam launch)/rviz cfg/mapping demo.rviz"/>
  <include file="$(find</pre>
hector mapping)/launch/mapping default.launch"/>
  <include file="$(find</pre>
hector geotiff)/launch/geotiff mapper.launch">
    <arg name="trajectory source frame name"</pre>
value="scanmatcher frame"/>
    <arg name="map_file_path" value="$(arg</pre>
geotiff map file path)"/>
  </include>
</launch>
```

APPENDIX C

Gmapping SLAM

Gmapping SLAM configuration file:

<launch>

 $gmapping_ws/gmapping/launch/slam_gmapping_pr2.launch$

```
<!-- Arguments -->
  <arg name="set base frame" default="base footprint"/>
  <arg name="set odom frame" default="odom"/>
  <arg name="set map frame" default="map"/>
  <!-- Gmapping -->
  <node pkg="gmapping" type="slam gmapping"</pre>
name="turtlebot3_slam gmapping" output="screen">
    <param name="base frame" value="$(arg set base frame)"/>
    <param name="odom frame" value="$(arg set odom frame)"/>
    <param name="map frame" value="$(arg set map frame)"/>
    <param name="map update interval" value="2.0"/>
    <param name="maxUrange" value="3.0"/>
    <param name="sigma" value="0.05"/>
    <param name="kernelSize" value="1"/>
    <param name="lstep" value="0.05"/>
    <param name="astep" value="0.05"/>
    <param name="iterations" value="5"/>
    <param name="lsigma" value="0.075"/>
    <param name="ogain" value="3.0"/>
    <param name="lskip" value="0"/>
    <param name="minimumScore" value="50"/>
    <param name="srr" value="0.1"/>
    <param name="srt" value="0.2"/>
    <param name="str" value="0.1"/>
    <param name="stt" value="0.2"/>
    <param name="linearUpdate" value="1.0"/>
```

```
<param name="angularUpdate" value="0.2"/>
    <param name="temporalUpdate" value="0.5"/>
    <param name="resampleThreshold" value="0.5"/>
    <param name="particles" value="100"/>
    <param name="xmin" value="-10.0"/>
    <param name="ymin" value="-10.0"/>
    <param name="xmax" value="10.0"/>
    <param name="ymax" value="10.0"/>
    <param name="delta" value="0.05"/>
    <param name="llsamplerange" value="0.01"/>
    <param name="llsamplestep" value="0.01"/>
    <param name="lasamplerange" value="0.005"/>
    <param name="lasamplestep" value="0.005"/>
  </node>
</launch>
Gmapping SLAM launch file: gmapping_ws/src/tutorial.launch
<?xml version="1.0"?>
<launch>
  <param name="use sim time" value="true" />
  <node pkg="rviz" type="rviz" name="rviz"</pre>
    args="-d $(find
gmapping_launch)/rviz cfg/mapping test.rviz"/>
<node pkg="gmapping" type="slam_gmapping"</pre>
```

name="gmapping thing" output="screen" >

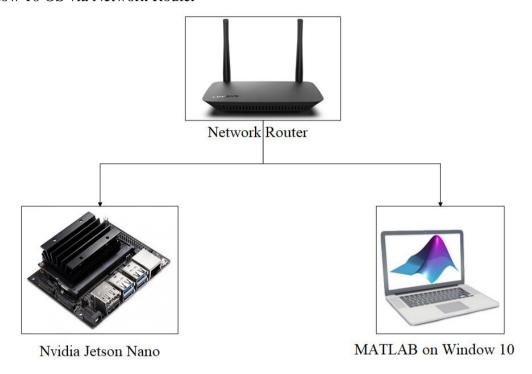
```
<param name="scan" value="scan" />
    <param name="odom_frame" value="odom" />
        <param name="base_frame" value="base_footprint" />
        <param name="map_frame" value="map" />
        </node>

</launch>
```

APPENDIX D

Interfacing ROS with MATLAB

We are using ROS melodic on Nvidia Jetson Nano running Ubuntu 18.04 LTS (Bionic Beaver) with MATLAB 2019b running on Window10 OS. Nvidia Jetson Nano connect to Window 10 OS via Network Router



To establish connection between ROS on Ubuntu and ROS on MATLAB, we have to find IP address of both devices.

• For Window 10, open cmd window and enter 'ipconfig'

• For Ubuntu, open terminal and enter 'ip addr'

```
😑 🗊 yuth@yuth-VirtualBox: ~
vuth@yuth-VirtualBox:~$ ip addr
1: lo: <LOOPBACK,UP,LOWER UP> mtu 65536 qdisc noqueue state UNKNOWN group defaul
t qlen 1000
     link/loopback 00:00:00:00:00:00 brd 00:00:00:00:00:00
     inet 127.0.0.1/8 scope host lo
  valid_lft forever preferred_lft forever
inet6 ::1/128 scope host
  valid_lft forever preferred_lft forever
2: enp0s3: <BROADCAST,MULTICAST,UP,LOWER_UP> mtu 1500 qdisc pfifo_fast state UP
group default qlen 1000
     inet 192.168.56.101/24 brd 192.168.56.255 scope global dynamic enp0s3
  valid_lft 555sec preferred_lft 555sec
     inet6 fe80::9f35:338e:2b86:ce59/64 scope link
         valid_lft forever preferred_lft forever
3: enp0s8: <BROADCAST,MULTICAST,UP,LOWER_UP> mtu 1500 qdisc pfifo_fast state UP
group default glen 1000
     link/ether 08:00:27:51:bf:ee brd ff:ff:ff:ff:ff:ff
inet 10.0.3.15/24 brd 10.0.3.255 scope global dynamic enp0s8
valid_lft 86355sec preferred_lft 86355sec
inet6 fe80::1579:a938:a30e:9bd0/64 scope link
         valid_lft forever_preferred_lft forever
yuth@yuth-VirtualBox:~$
```

Testing Connection between device via pinging

• For Window 10, in cmd window, enter 'ping <ubuntu ip address>'

• For Ubuntu, in terminal, enter 'ping <window ip address>'

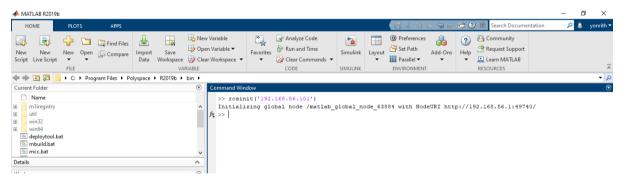
```
yuth@yuth-VirtualBox: ~
yuth@yuth-VirtualBox: ~$ ping 192.168.56.1
PING 192.168.56.1 (192.168.56.1) 56(84) bytes of data.
^C
--- 192.168.56.1 ping statistics ---
7 packets transmitted, 0 received, 100% packet loss, time 6147ms

yuth@yuth-VirtualBox: ~$ ping 192.168.56.101
PING 192.168.56.101 (192.168.56.101) 56(84) bytes of data.
64 bytes from 192.168.56.101: icmp_seq=1 ttl=64 time=0.020 ms
64 bytes from 192.168.56.101: icmp_seq=2 ttl=64 time=0.061 ms
64 bytes from 192.168.56.101: icmp_seq=3 ttl=64 time=0.060 ms
64 bytes from 192.168.56.101: icmp_seq=4 ttl=64 time=0.043 ms
^C
--- 192.168.56.101 ping statistics ---
4 packets transmitted, 4 received, 0% packet loss, time 3067ms
rtt min/avg/max/mdev = 0.020/0.046/0.061/0.016 ms
```

On Jetson Nano, Initiate command 'roscore' in ubuntu terminal to begin ROS Master

```
yuth@yuth-VirtualBox:~$ roscore
... logging to /home/yuth/.ros/log/a8f791d0-b9fc-11ea-9da2-0800272f780e/roslaunc
h-yuth-VirtualBox-1910.log
Checking log directory for disk usage. This may take awhile.
Press Ctrl-C to interrupt
Done checking log file disk usage. Usage is <1GB.
started roslaunch server http://yuth-VirtualBox:36905/
ros comm version 1.12.14
SUMMARY
======
PARAMETERS
* /rosdistro: kinetic
  /rosversion: 1.12.14
NODES
auto-starting new master
process[master]: started with pid [1921]
ROS_MASTER_URI=http://yuth-VirtualBox:11311/
setting /run_id to a8f791d0-b9fc-11ea-9da2-0800272f780e
process[rosout-1]: started with pid [1934]
started core service [/rosout]
```

Establish connection from MATLAB to ROS machine via command 'rosinit <ubuntu ip address>'



Testing the ROS connection by calling ROS topic in MATLAB via 'rostopic list'

