Cooperative Gating and Spatial Organization of Membrane Proteins through Elastic Interactions

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Biological membranes are elastic media in which the presence of a transmembrane protein leads to local bilayer deformation. The energetics of deformation allow two membrane proteins in close proximity to influence each other's equilibrium conformation via their local deformations, and spatially organize the proteins based on their geometry. We use the mechanosensitive channel of large conductance (MscL) as a case study to examine the implications of bilayer-mediated elastic interactions on protein conformational statistics and clustering. The deformations around MscL cost energy on the order of 10 k_BT and extend \sim 3 nm from the protein edge, as such elastic forces induce cooperative gating, and we propose experiments to measure these effects. Additionally, since elastic interactions are coupled to protein conformation, we find that conformational changes can severely alter the average separation between two proteins. This has important implications for how conformational changes organize membrane proteins into functional groups within membranes.

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Introduction

Biological membranes are active participants in the function and spatial organization of membrane proteins [1–3]. At the simplest level, the membrane positions proteins into a two-dimensional space, where they are often laterally organized into groups. These groups can serve specific purposes on the cell surface and within organelles, such as sensing, adhesion, and transport [4–9]. Electrostatic and van der Waals forces help drive lateral organization [10]; however, there is an additional class of purely bilayer-mediated elastic forces that can facilitate the formation of complexes of membrane proteins.

Conformational changes of membrane proteins result from a wide range of environmental factors including temperature, pH, ligand and small molecule binding, membrane voltage, and membrane tension. Likewise, conformational state is often tightly coupled with function (e.g., for ion channels) [11–13]. In this work, we demonstrate how elastic interactions can communicate information about protein conformation from one neighboring protein to another, coupling their conformational state. Additionally, we find that these interactions lead to spatial organization within the bilayer that is strongly dependent on protein conformation.

We suggest that elastic forces play a role in the function and spatial organization of many membrane proteins across many cell types, given the generically high areal density of membrane proteins [14] and the strength of these interactions. We use the mechanosensitive channel of large conductance (MscL) from *Escherichia coli* as the model protein for this study. MscL is a transmembrane homopentamer found in the plasma membrane of *E. coli* (and many other bacteria) serving as an emergency relief valve under hypoosmotic shock [11,15,16]. As membrane tension increases, this nonselective ion channel changes conformation from a closed state to an open state, releasing water and osmolytes [17,18].

Though several substates have been identified in this gating transition, the relatively short dwell-times in these substates as compared with the fully open or fully closed states allows us to approximate the protein as a simple two-state system [17,19]. Crystal and electron-paramagnetic-resonance structures suggest the bilayer-spanning region is nearly cylindrical in both the open and closed conformations [15,20,21], making MscL particularly amenable to mechanical modeling. Electrophysiology of reconstituted channels allows measurement of the state of one or more of these proteins with excellent temporal and number resolution. Therefore, theoretical predictions for how elastic interactions change the gating behavior of a MscL protein can be readily tested using electrophysiology and other experimental techniques.

Following earlier work, we use continuum mechanics to break down the deformation caused by a cylindrical transmembrane protein into a term penalizing changes in bilayer thickness and a term penalizing bending of a bilayer leaflet [22–26], and we introduce a third term that preserves bilayer volume under deformation [27]. Due to its structural symmetry, MscL can be characterized by its radius and bilayer-spanning thickness in its two conformations (i.e., open and closed), neglecting any specific molecular detail (see Figure 1). As these geometric parameters change with conformation, the bilayer-mediated interaction between two channels is altered. Using the interaction potentials in

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Abbreviations: MscL, mechanosensitive channel of large conductance

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Author Summary

Membranes form flexible boundaries between the interior of a cell and its surrounding environment. Proteins that reside in the membrane are responsible for transporting materials and transmitting signals across these membranes to regulate processes crucial for cellular survival. These proteins respond to stimuli by altering their shape to perform specific tasks, such as channel proteins, which allow the flow of ions in only one conformation. However, the membrane is not just a substrate for these proteins, rather it is an elastic medium that bends and changes thickness to accommodate the proteins embedded in it. Thus, the membrane plays a role in the function of many proteins by affecting which conformation is energetically favorable. Using a physical model that combines membrane elastic properties with the structure of a typical membrane protein, we show that the membrane can communicate structural and hence conformational information between membrane proteins in close proximity. Hence, proteins can "talk" and "respond" to each other using the membrane as a generic "voice." We show that these membrane-mediated elastic forces can ultimately drive proteins of the same shape to cluster together, leading to spatial organization of proteins within the membrane.

each combination of conformations, we explore how both the single-channel and interacting energetics affect the spatial and conformational behavior of two channels.

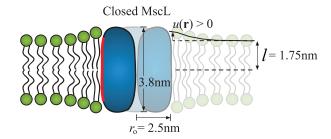
In the first section we cover the physical principles behind bilayer deformation due to the presence of membrane proteins. In the second section we explore the differences in gating behavior of two MscL proteins when held at a fixed separation. In the third section we explore the conformational and spatial behavior of diffusing MscL proteins as a function of areal density. Finally, in the fourth section we discuss the relevance of these forces as compared with other classes of bilayer-mediated forces and support our hypotheses with results from previous experiments.

Results

Elastic Deformation Induced by Membrane Proteins

The bilayer is composed of discrete lipid molecules whose lateral diffusion ($D \sim 10 \,\mu\text{m}^2$ /s) [28] is faster than the diffusion of transmembrane proteins ($D \sim 0.1-1 \, \mu \text{m}^2 / \text{s}$) [29–31]. In the time it takes a transmembrane protein to diffuse one lipid diameter, many lipids will have exchanged places near the protein to average out the discreteness of the lipid molecules. Additionally, the transition time for protein conformational change (~5 μs) [32] is slow compared with lipid diffusion. Hence, we argue the bilayer can be approximated as a continuous material in equilibrium with well-defined elastic properties [33]. Further, we choose to formulate our analysis in the language of continuum mechanics, rather than lateral pressure profiles [34]. In particular, each leaflet of the bilayer resists changes in the angle between adjacent lipid molecules, leading to bending stiffness of the bilayer [22,35]. Likewise, the bilayer has a preferred spacing of the lipid molecules in-plane and will resist any changes in this spacing due to external tension [36]. Finally, experiments suggest that the volume per lipid is conserved [37,38] such that changes in bilayer thickness are accompanied by changes in lipid spacing [2,33].

Transmembrane proteins can compress and bend a bilayer leaflet via at least two mechanisms. The protein can force the



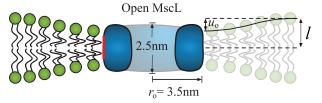


Figure 1. Schematic of Bilayer Deformations due to MscL

Mismatch between the hydrophobic regions of the lipid bilayer and an integral membrane protein gives rise to bending and compression deformations in each leaflet of the bilayer. The largest deformations occur at the protein–lipid interface, and over the scale of a few nanometers the bilayer returns to its unperturbed state. MscL is shown schematically at zero tension in its closed and open states with relevant dimensions. The red region of the protein indicates the hydrophobic zone. The hydrophobic mismatch at the protein–lipid interface is denoted by $u_{\rm o}$. The deformation profile, denoted by $u({\bf r})$, is measured with reference to the unperturbed leaflet thickness (/) from the protein center at ${\bf r}=0$.

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bilayer to adopt a new thickness, matching the hydrophobic region of the protein to the hydrophobic core of the bilayer. Additionally, a noncylindrical protein can induce a slope in the leaflet at the protein-lipid interface [25,39].

For transmembrane proteins such as MscL that can be approximated as cylindrical, symmetry dictates that the deformation energy of the bilayer is twice the deformation energy of one leaflet. Presuming the protein does not deform the bilayer too severely, we can write the bending and compression (thickness change) energies in a form analogous to Hooke's law, and account for external tension with a term analogous to PV work. We denote the deformation of the leaflet by the function $u(\mathbf{r})$, which measures the deviation of the lipid head-group from its unperturbed height as a function of the position \mathbf{r} (see Figure 1). In all the calculations that follow, the physical parameters chosen are representative of a typical phosphocholine (PC) lipid bilayer, and the number of lipids in this model bilayer is fixed. The energy penalizing compression of the bilayer is

$$G_{\text{comp}} = \frac{K_A}{2} \int \left(\frac{u(\mathbf{r})}{l}\right)^2 d^2 \mathbf{r} \tag{1}$$

where K_A is the bilayer area stretch modulus ($\sim 58~k_BT/\mathrm{nm}^2$, k_BT is the thermal energy unit) and l is the unperturbed leaflet thickness ($\sim 1.75~\mathrm{nm}$) [36]. The bending energy of a leaflet is

$$G_{\text{bend}} = \frac{\kappa_b}{4} \int \left(\nabla^2 u(\mathbf{r}) - c_o \right)^2 d^2 \mathbf{r}$$
 (2)

where κ_b ($\sim 14~k_BT$) is the bilayer bending modulus, c_o is the spontaneous curvature of the leaflet [33,36,40], and $\nabla^2 = \partial^2 l \partial x^2 + \partial^2 l \partial y^2$ is the Laplacian operator.

Coupling external tension to bilayer deformations is more subtle than the previous two energetic contributions. We note that the bilayer is roughly forty times more resistant to volume change than area change [37,38]; hence if a transmembrane protein locally thins the bilayer, lipids will expand in the area near the protein to conserve volume. Likewise, if the protein locally thickens the bilayer, lipids near the protein will condense (see Figure 1). Therefore, the area change near the protein is proportional to the compression $u(\mathbf{r})$, and the work done on the bilayer is the integrated area change multiplied by tension

$$G_{\text{ten}} = \tau \int \frac{u(\mathbf{r})}{l} d^2 \mathbf{r}$$
 (3)

where τ is the externally applied bilayer tension [24,27]. Slightly below bilayer rupture, and near the expected regime of MscL gating, $\tau \approx 2.6 k_B T / \text{nm}^2$ [17,36]. In total, the bilayer deformation energy is

$$G = \frac{1}{2} \int \left(K_A \left(\frac{u}{l} + \frac{\tau}{K_A} \right)^2 + \kappa_b (\nabla^2 u - c_o)^2 \right) d^2 \mathbf{r}$$
 (4)

where we have made use of the constant bilayer area to elucidate the interplay between tension and compression. Specifically, we added a constant proportional to membrane area and τ^2 , which is identically zero when calculating differences in free energy.

To obtain the length and energy scales of these deformations, we nondimensionalize the bilayer deformation energy, G. We scale both the position **r** and displacement $u(\mathbf{r})$ by $\lambda =$ $(\kappa_b l^2 / K_A)^{1/4} \approx 1$ nm, the natural length scale of deformation, to give the new variables ρ and $\eta(\rho)$, respectively, where $\rho = r/\lambda$ and $\eta(\boldsymbol{\rho}) = u(\mathbf{r})/\lambda$. Then G can be written as

$$G = \frac{\kappa_b}{9} \int ((\eta + \chi)^2 + (\nabla^2 \eta - \nu_o)^2) d^2 \rho$$
 (5)

where $v_o = \lambda c_o$ is the dimensionless spontaneous curvature and $\chi = \tau l/K_A \lambda$ is the dimensionless tension, which is ≈ 0.09 in the regime of MscL gating. The energy scale is set by the bending modulus, κ_b .

Using the standard Euler-Lagrange equation from the calculus of variations [41], the functional for the deformation energy can be translated into the partial differential equation

$$\nabla^4 \eta + \eta + \chi = 0. \tag{6}$$

The deformation profile $u(\mathbf{r})$ that solves this partial differential equation depends on four boundary conditions. In the far-field, we expect the bilayer to be flat and slightly thinner in accordance with the applied tension, i.e., $|\nabla u(\infty)| = 0$ and $\mathbf{u}(\infty) = -\tau l/K_A$, respectively. At the protein-lipid interface ($\mathbf{r} =$ r_o) the hydrophobic regions of the protein and the bilayer must be matched, i.e., $u(r_0) = u_0$ (see Figure 1), where u_0 is onehalf the mismatch between the hydrophobic region of the protein and the hydrophobic core of the bilayer. Finally, the slope of the bilayer at the protein-lipid interface is set to zero (i.e., $|\nabla u(r_0)| = 0$). The motivation for this last boundary condition is subtle and will be examined in more detail in the Discussion.

To understand how the deformation energy scales with hydrophobic mismatch (u_0) , protein size (r_0) , and tension (τ) , we solve Equation 6 analytically for a single cylindrical protein. The deformation energy is

$$G_{\text{single}} = \pi \kappa_b \int_{\rho_o}^{\infty} \left((\eta + \chi)^2 + (\nabla^2 \eta - \nu_o)^2 \right) \rho d\rho \tag{7}$$

where $\rho_o = \mathbf{r}_o / \lambda$ is the dimensionless radius of the protein. The leaflet deformation around a single protein is a linear combination of zeroth-order modified Bessel functions of the second kind (K_0) [25,26]. For proteins such as MscL with a radius larger than λ (i.e., 1 nm), the deformation energy is well-approximated by

$$G_{\text{single}} = \pi \kappa_b \left(\frac{u_o}{\lambda} + \frac{\tau}{K_A} \frac{l}{\lambda} \right)^2 \left(1 + \sqrt{2} \frac{r_o}{\lambda} \right).$$
 (8)

The deformation energy scales linearly with protein radius and depends quadratically on the combination of hydrophobic mismatch (u_0) and tension (τ) . This makes the overall deformation energy particularly sensitive to the hydrophobic mismatch, and hence leaflet thickness l. The deformation energy is fairly insensitive to changes in K_A (i.e., most terms in the energy are sublinear), and generally insensitive to changes in the bending modulus since $G \propto \kappa_b^{1/4}$.

Using our standard elastic bilayer parameters and the dimensions of a MscL channel (see Figure 1), the change in deformation energy between the closed and open states is $\Delta G_{\text{single}} \approx 50 \text{ k}_B T$. The measured value for the free energy change of gating a MscL protein, including internal changes of the protein and deformation of surrounding lipids is ≈ 51 k_BT [19]. This close correspondence does not indicate that bilayer deformation accounts for all of the free energy change of gating [42], but does suggest that it is a major contributor.

The gating energy of two channels in close proximity is a complex function of their conformations and the distance between them. As two proteins come within a few nanometers of each other (i.e., a few λ), the deformations that extend from their respective protein-lipid interfaces begin to overlap and interact. The bilayer adopts a new shape (i.e., a new $u(\mathbf{r})$), distinct from the deformation around two independent proteins, and hence the total deformation energy changes as well. This is the physical origin of the elastic interaction between two bilayer-deforming proteins [23,24].

Each protein imposes its own local boundary conditions on the bilayer, which vary with conformation; hence, the deformation around a pair of proteins is a function of their individual conformation and the distance between them. A MscL protein has two distinct conformations, hence there can be pairwise interactions between two closed channels, an open and a closed channel, or two open channels (see Figure 2). Tension also affects the deformations. The hydrophobic mismatch can be either positive or negative (i.e., the protein can be thicker or thinner than the bilayer), thus tension will strengthen the interaction of proteins that are thicker than the bilayer (e.g., the closed-closed interaction of two MscL proteins) and weaken the interaction of proteins that are thinner than the bilayer (e.g., the open-open interaction). This effect is demonstrated in Figure 2. The interactions due to leaflet deformations have been explored before [23,24], but our model elucidates the role that these interactions can play in communicating conformational information between proteins. Additionally, in our model, tension can play an important role in determining the overall deformation energy around a protein.

In a one-dimensional model, the interaction potentials can

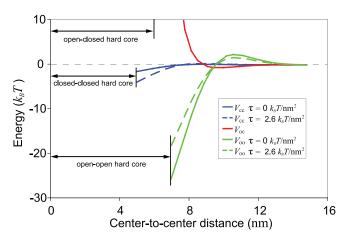


Figure 2. Elastic Potentials between two MscL Proteins

To minimize deformation energy, two transmembrane proteins exert elastic forces on each other. MscL has three distinct interaction potentials between its two distinct conformations. External tension weakens the interaction between two open channels $(V_{\rm co})$ and strengthens the interaction between two closed channels $(V_{\rm cc})$, but has almost no effect on the interaction between an open and closed channel $(V_{\rm cc})$. The openopen and closed–closed interactions are both more strongly attracting than the open–closed interaction, indicating that elastic potentials favor interactions between channels in the same state. The "hard core" distance is where the proteins' edges are in contact. doi:10.1371/journal.pcbi.0030081.g002

be solved for analytically. For two identical proteins in close proximity (e.g., closed-closed and open-open interactions), the approximate shape of the potential is linearly attractive $\kappa_b (u_0/\lambda)^2 (d/2\lambda - \sqrt{2})$. Between two dissimilar proteins in close proximity (e.g., open-closed interaction), the potential is approximately $\kappa_b (u_o/\lambda)^2 \pi^4 / 4(d/\lambda)^3$, where in both cases d is measured from the edges of the proteins. This illustrates the general principle that two similar proteins attractively interact, while two dissimilar proteins tend to repel each other. This one-dimensional model helps build intuition for what governs the strength of elastic interactions. Whether the interaction is attractive or repulsive, the strength of the interaction is dominated by its quadratic dependence on the combination of hydrophobic mismatch and tension-induced thinning. Hence, interactions between proteins that deform the membrane more severely are simultaneously more sensitive to tension. These effects are demonstrated in Figure 2, where the closed-closed interaction, which has less hydrophobic mismatch, is both weaker and less sensitive to tension than the open-open interaction. In a two-dimensional bilayer, the geometry of the two proteins makes it difficult to solve for the interaction analytically, thus numerical techniques were used (see Materials and Methods).

This theoretical framework provides a strong foundation for understanding how protein geometries and lipid properties give rise to elastic interactions. With this, we can investigate how elastic forces change the conformational statistics of a two-state protein population.

Gating Behavior of Two Interacting Channels

To probe the range of separations over which elastic interactions affect the gating of two MscL proteins, we need to account for the noninteracting energetics of gating a single channel in addition to the interactions between two channels. The noninteracting energy is the sum of three effects. First,

there is some energetic cost to deform the surrounding membrane, which we already calculated as $\Delta G_{\rm single}$. Second, there is some cost to change the protein's increase first two effects are the gating energy $\Delta G_{\rm gate} \approx 51~k_BT$ for MscL [19]. Finally, there is an energetic mechanism that overcomes these costs and opens the channel as tension increases. This mechanism is provided by the bilayer tension working in concert with the conformational area change of the protein ($\Delta A \approx 20~{\rm nm}^2$ for MscL [19]). Given the experimentally determined values for $\Delta G_{\rm gate}$ and the area change during gating, the critical tension, defined by $\Delta G_{\rm gate} = \tau \Delta A$, is $\tau_c = 2.6~k_B T/{\rm nm}^2$.

In our thermodynamic treatment, we need to keep track of the conformations of each protein in a population in a way that allows us to tabulate the noninteracting and interacting contributions to the free energy. To this end, we assign a state variable, s_i , to each channel, indicating the conformational state of a protein, where $s_i = 0$ indicates that the ith channel is closed and $s_i = 1$ indicates that the ith channel is open. The noninteracting energy for two channels is then

$$H_{\text{non}}(s_1, s_2; \tau) = (G_{\text{gate}} - \tau \Delta A)(s_1 + s_2).$$
 (9)

If both channels are closed ($s_1 = s_2 = 0$), the free energy is defined to be zero. If one channel is open and the other closed ($s_1 = 1$, $s_2 = 0$, or, $s_1 = 0$, $s_2 = 1$), this counts as the cost to gate one channel working against the benefit at a particular tension to opening the channel. Likewise, this counts twice if both channels are open ($s_1 = s_2 = 1$). We will measure all energies that follow in units of k_BT ($\approx 4.14 \times 10^{-21}$).

As we alluded to earlier, the interacting component of the free energy between two channels is a function of their states $(s_1 \text{ and } s_2)$, their edge separation (d), and the tension. Using a numerical relaxation technique to minimize the functional in Equation 5 (see Materials and Methods), we calculated the interaction potentials $H_{\text{int}}(s_1, s_2, d; \tau)$ for a range of tensions and separation distances (see Figure 2). The total energy, $H_{\text{non}} + H_{\text{int}}$, is used to derive the Boltzmann weight for the three possible configurations of the two-channel system,

$$z(s_1, s_2) = e^{-(H_{\text{non}}(s_1, s_2; \tau) + H_{\text{int}}(s_1, s_2, d; \tau))}.$$
 (10)

The probability that the system has two closed channels is

$$P_0 = \frac{z(0,0)}{Z} \tag{11}$$

where the partition function *Z* is the sum of the Boltzmann weights for all possible two-channel configurations,

$$Z = \sum_{s_1, s_2 = 0}^{1} z(s_1, s_2) = z(0, 0) + 2z(0, 1) + z(1, 1).$$
 (12)

Likewise, the probabilities for the system to have exactly one or two open channels are

$$P_1 = \frac{2z(0,1)}{Z}$$
 and $P_2 = \frac{z(1,1)}{Z}$, (13)

respectively. Finally, the probability for any one channel in this two channel system to be open is

$$P_{\text{open}}(\tau, d) = \frac{z(0, 1) + z(0, 1)}{Z}.$$
 (14)

If the distance between two channels is much greater than λ , they will behave independently. As the channels get closer (d

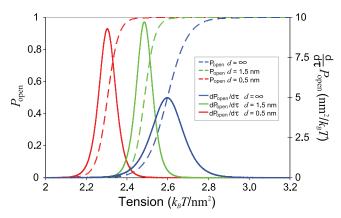


Figure 3. Conformational Statistics of Interacting MscL Proteins Interactions between neighboring channels lead to shifts in the probability that a channel will be in the open state (dashed lines). The sensitivity and range of response to tension, $dP_{\rm open}/d\tau$, are also affected by bilayer deformations (solid lines). $P_{\rm open}$ and $dP_{\rm open}/d\tau$ are shown for separations of 0.5 nm (red) and 1.5 nm (green) with reference to noninteracting channels at $d=\infty$ (blue). Interactions shift the critical gating tension for the closest separation by $\sim 12\%$. Additionally, the peak sensitivity is increased by $\sim 90\%$ from ~ 5 nm²/ k_BT to ~ 9.5 nm²/ k_BT , indicating a Hill coefficient of ~ 2 . doi:10.1371/journal.pcbi.0030081.g003

 $\leq 5\lambda$) they begin to interact and their conformational statistics are altered. $P_{\rm open}$ as a function of tension for certain fixed separations is shown in Figure 3. The openopen interaction is the most energetically favorable for most separations, hence the transition to the open state generally shifts to lower tensions as the distance between the two proteins is decreased. Though the edge spacing can be small, even fractions of the width of a lipid molecule, the two-dimensional nature of the interaction means that the majority of the interaction is mediated by lipids in the intervening region between the two proteins. Thus, a continuum model is still applicable, albeit less accurate, for very small protein separations.

Interactions also affect channel "sensitivity," defined as the derivative of $P_{\rm open}$ with respect to tension, which quantifies how responsive the channel is to changes in tension. The full-width at half maximum of this peaked function is a measure of the range of tension over which the channel has an appreciable response. The area under the sensitivity curve is equal to 1, hence increases in sensitivity are always accompanied by decreases in range of response, as demonstrated by the effects of the beneficial open–open interaction on channel statistics (see Figure 3).

In summary, we find that elastic interactions between two proteins have significant effects when the protein edges are closer than ~ 5 nm. At these separations the elastic interactions alter the critical gating tension and change the tension sensitivity of the channel (see Figure 3). The critical gating tension and sensitivity are the key properties that define the transition to the open state, and are analogs to the properties that define the transition of *any* two-state membrane protein. Hence, we have shown that elastic interactions can affect protein function at a fundamental level.

Interactions between Diffusing Proteins

With an understanding of how two proteins will interact at a fixed distance, we now study the conformational statistics of two freely diffusing MscL proteins allowed to interact via their elastic potentials. In biological membranes, transmembrane proteins that are not rigidly attached to any cytoskeletal elements are often free to diffuse throughout the membrane and interact with various lipid species as well as other membrane proteins. On average, the biological areal density of such proteins is high enough ($\sim 10^3 - 10^4 \ \mu m^{-2}$ [14]) that elastic interactions should alter the conformational statistics and average protein separations.

We expect that if two MscL proteins are diffusing and interacting, the open probability will be a function of their areal density as well as the tension. It then follows that for a given areal density, elastic interactions will couple conformational changes to the average separation between the proteins. To calculate the open probability of two diffusing MscL proteins, the Boltzmann weight for these proteins to be in the conformations s_1 and s_2 must be summed at every possible position, giving

$$\langle z(s_1, s_2) \rangle = e^{-H_{\text{non}}} \iint e^{-H_{\text{int}}} d^2 \mathbf{r}_1 d^2 \mathbf{r}_2$$
 (15)

where $\langle ... \rangle$ indicates a sum over all positions. The distance between the proteins is measured center-to-center as $|\mathbf{r}_1 - \mathbf{r}_2|$ and only the absolute distance between the two proteins determines their interaction, hence we can rewrite the integrand as a function of $r = |\mathbf{r}_1 - \mathbf{r}_2|$. We then change the form of the integrand to

$$e^{-H_{\rm int}(s_1, s_2, r; \tau)} = 1 + f_{12}(r) \tag{16}$$

which allows us to separate the interacting effects from the noninteracting effects (the function f_{12} is often called the Mayer-f function). Thus, the position-averaged Boltzmann weights are

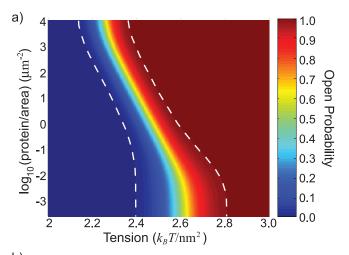
$$\langle z(s_1, s_2) \rangle = e^{-H_{\text{non}}} \left(1 + \frac{2\pi}{A} \int_0^\infty f_{12}(r) r \mathrm{d}r \right)$$
 (17)

where A is the total area occupied by the two proteins. Following our previous calculations, the probability that any one channel is open in this two-channel system is

$$P_{\text{open}}(\tau, \alpha) = \frac{\langle z(0,1) \rangle + \langle z(0,1) \rangle}{\langle Z \rangle}$$
 (18)

where α is the protein areal density (i.e., $\alpha = 2/A$) and $\langle Z \rangle = \sum_{s_1, s_2} \langle z(s_1, s_2) \rangle$.

In Figure 4A, we plot $P_{\text{open}}(\tau, \alpha)$ over a wide range of areal density, from the area of ~100 lipids up to areas on the whole-cell scale. The more beneficial open-open interaction tends to shift the transition to the open state to lower tensions, with the most pronounced effect being when the two proteins are most tightly confined. For the estimated biological membrane protein density of $\sim 10^3$ - $10^4 \ \mu m^{-2}$ (or \sim 10-30 nm spacing) [14], the gating tension is decreased by \sim 13%, the sensitivity is increased by \sim 85%, and the range of response is decreased by \sim 55%. For the in vivo expression of MscL of $\sim 1-10 \ \mu m^{-2}$ [43], the gating tension is reduced by \sim 7%, the sensitivity is increased by \sim 70%, and the range of response is decreased by ~40%. These changes in gating behavior are accessible to electrophysiological experiments where MscL proteins can be reconstituted at a known areal density ($\sim 0.1-10 \ \mu m^{-2}$), and the open probability can be measured as a function of tension.



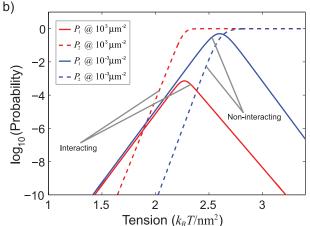


Figure 4. Elastic Interactions Lower Open Probability Transition and Couple Conformation Changes

Two MscL proteins in a square box of area A diffuse and interact via their elastic potentials.

(A) At low areal density, the response to tension is the same as an independent channel. As the areal density increases, the more beneficial open-open interaction (see Figure 2) shifts the open probability to lower tensions and decreases the range of response (dashed lines) while increasing the peak sensitivity, indicating that areal density can alter functional characteristics of a transmembrane protein.

(B) The probability for exactly one channel to be open $(P_1, \text{ solid lines})$ is shown at a low (blue) and high (red) areal density. For tensions past the critical tension, interacting channels are ~1,000 times less likely to gate individually. The probability for both channels to be open simultaneously $(P_2, dashed lines)$ is shown for low (blue) and high (red) areal density. The tension at which two simultaneously open channels are favored is significantly lower for interacting channels. Together these facts signify a tight coupling of the conformational changes for two interacting channels. doi:10.1371/journal.pcbi.0030081.g004

In addition to lowering the critical tension and augmenting channel sensitivity, the conformational states of channels are tightly coupled by their interaction. The probability that exactly one channel is open (P_1) decreases dramatically as areal density increases. For tensions above the critical tension, interacting channels ($\sim 10^3 \ \mu m^{-2}$) are nearly three orders of magnitude less likely to gate as single channels than their noninteracting counterparts ($\sim 10^{-3} \, \mu m^{-2}$), as shown in Figure 4B. Additionally, the tension at which it is more likely to have both channels open, rather than a single channel, is significantly lower for interacting channels, signaling that gating is a tightly coupled process. In addition to altering the

open probability of two channels, the favorable open-open interaction provides an energetic barrier to leaving the open-open state. Based on a simple Arrhenius argument, the average open lifetime of two channels that are both open and interacting will be orders of magnitude longer than two open but noninteracting channels.

Having shown conformational coupling over a range of areal densities, it is reasonable to expect that elastic interactions will affect the separation between two proteins. We ask, how do interactions affect the average separation between proteins? How often will we find the two proteins separated by a distance small enough that we can consider them "dimerized"?

From Equations 15 and 16, it follows that the Boltzmann weight for the two proteins to be separated by a distance r is

$$z(s_1, s_2, r) = e^{-H_{\text{non}}} \frac{2\pi}{A} (1 + f_{12})r.$$
 (19)

The probability that the proteins are separated by a distance r, regardless of their conformation, is

$$P(r) = \frac{Z(r)}{\langle Z \rangle} = \frac{\sum_{s_1, s_2} z(s_1, s_2, r)}{\langle Z \rangle}$$
 (20)

from which we calculate the average separation

$$\langle r \rangle = \frac{1}{\langle Z \rangle} \int Z(r) r dr$$

$$= \frac{1}{\langle Z \rangle} \sum_{s_1, s_2} e^{-H_{\text{non}}} \left(\delta \frac{\pi}{6} \sqrt{A} + \frac{2\pi}{A} \int_{0}^{\infty} f_{12} r^2 dr \right)$$
(21)

This equation is valid as long as the area does not confine the proteins so severely that they are sterically forced to interact. The constant δ is an order-one quantity that is defined by the entropic component of average separation on a surface S, given by

$$\iint\limits_{S(A)} |\mathbf{r}_1 - \mathbf{r}_2| \frac{\mathrm{d}^2 \mathbf{r}_1}{A} \frac{\mathrm{d}^2 \mathbf{r}_2}{A} = \delta \frac{\pi}{6} \sqrt{A}$$
 (22)

and depends on the actual shape of the surface. For a square box, $\delta \approx 1$, and for a circle, $\delta \approx \sqrt{2}$. The average separation of two MscL proteins as a function of tension is plotted for various areal densities in Figure 5. For certain densities, elastic interactions couple the conformational change from the closed to open state with a decrease in the average separation by more than two orders of magnitude. Our estimates of biological membranes yield fairly high membrane-protein densities ($\sim 10^3$ - $10^4 \, \mu m^{-2}$) [14], which corresponds to the more highly confined conditions on Figures 4-6. In the native E. coli plasma membrane, MscL, with a copy number of ~ 5 [43], is present at a density of $\sim 1-10 \ \mu m^$ which means that even membrane proteins expressed at a low level are subject to the effects of elastic interactions.

To quantify the effects of interaction on the spatial organization of two channels, we define a "dimerized" state by the maximum separation below which two channels will favorably interact with an energy greater than k_BT (i.e., $H_{int}(s_1,$ s_2 , τ , r) < -1). This defines a critical separation, $r_c(s_1, s_2, \tau)$, which depends on the conformations of each protein and the tension. The probability that the two proteins are found with a separation less than or equal to r_c is

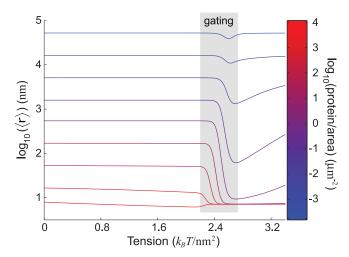


Figure 5. Average Separation between Proteins Drops Significantly due to Elastic Interactions

The average separation between two diffusing MscL proteins in a box of area A is plotted as a function of tension for a range of areal densities, each shown as a different line color. The grey region roughly indicates when gating is occurring. At low areal density (mostly blue), the conformational change does not draw the proteins significantly closer together. As the areal density increases, the conformational change is able to draw the proteins up to \sim 100 times closer than they would otherwise be. At the highest areal density (mostly red), the steric constraint of available area intrinsically positions the proteins close to one another regardless of their conformation. The average separation begins to increase again as higher tension weakens the open–open interaction. doi:10.1371/journal.pcbi.0030081.g005

$$P_{\text{dimer}}(\tau, \alpha) = \frac{1}{\langle Z \rangle} \sum_{s_1, s_2} e^{-H_{\text{non}}} \left(\frac{\pi r_c^2}{A} + \frac{2\pi}{A} \int_0^{r_c} f_{12} r dr \right)$$
(23)

This "dimerization probability" is plotted as a function of tension and areal density in Figure 6.

At low tension and high areal density, the channels are closed and near enough that the closed-closed interaction can dimerize them a fraction of the time. Keeping the areal density high, increasing tension strengthens the closed-closed interaction, and the dimerization probability increases until tension switches the channels to the open state, where the significantly stronger open-open interaction dimerizes them essentially 100% of the time. When the areal density decreases to moderate levels, as denoted by the white dashed lines in Figure 6, the dimerization is strongly correlated with the conformational change to the open state. The zero tension separation between the two proteins for this one-to-one correlation is ~ 40 nm to ~ 2 µm. Finally, when the areal density is very low, entropy dominates, and neither the closedclosed, nor the open-open interaction is strong enough to dimerize the channels. Understanding the onset and stability of dimers is an important first step in understanding the formation of larger oligomers of membrane proteins. As the areal density of membrane proteins increases, clusters of more than two proteins become favorable and are energetically stabilized by their multibody interactions. For a rigorous theoretical treatment of these multibody interactions, we refer the interested reader to [44-46].

In summary, we have shown that over a broad range, areal density plays a nontrivial role in allowing two channels to communicate conformational information. This communica-

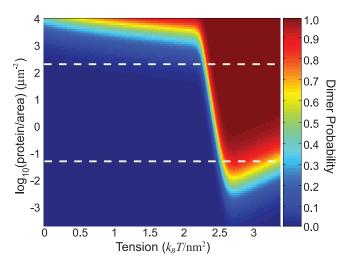


Figure 6. Elastic Interactions Tightly Couple Conformational Change with Protein Dimerization

Diffusing MscL proteins are considered dimerized when they are close enough that they attract with an energy greater than k_BT . At high areal density, the net attractive closed–closed interaction is sufficient to dimerize the two channels part of the time. As the areal density decreases, the closed–closed interaction is not strong enough to dimerize the two channels—now dimerization only happens at higher tensions after both channels have switched to the open conformation. As the areal density decreases further, the open–open interaction is no longer strong enough to overcome entropy. This loss of dimerization is amplified by the fact that the open–open interaction is weaker at higher tensions (see Figure 2). The white dashed lines roughly indicate the range of areal densities for which dimerization probability and open channel probability are equal to each other (see Figure 4). doi:10.1371/journal.pcbi.0030081.g006

tion can lead to large changes in the average separation between two proteins and the probability that they will be found together in a dimerized state. This may have implications for how conformational changes of transmembrane proteins in biological membranes are able to facilitate the formation of functional groups of specific proteins.

Discussion

In this section, we will perform a brief survey of other bilayer-mediated forces between proteins and make a comparison of their relative length and energy scales. We will also address some of the finer details of our model and how boundary conditions can affect deformation energy around a protein. Finally, we will suggest experiments using MscL to observe the predicted changes in conformational statistics, as well as provide evidence from previous experiments that leaflet interactions lead to significant changes in conformational statistics.

There are at least two other classes of purely bilayer mediated forces between membrane proteins. The first is a different type of bilayer deformation that bends the midplane of the bilayer. This arises from transmembrane proteins with a conical shape that impose a bilayer slope at the protein-lipid interface [39,47]. If the protein does not deform the bilayer too severely, the mid-plane deformation energy of a bilayer is

$$G_{\text{mid}} = \frac{1}{2} \int \left(\tau(\nabla h(\mathbf{r}))^2 + \kappa_b (\nabla^2 h(\mathbf{r}))^2 \right) d^2 \mathbf{r}$$
 (24)

where $h(\mathbf{r})$ is the deviation of the height of the mid-plane from a flat configuration [26,35]. These kinds of interactions have been calculated for a variety of bilayer curvature environments and protein shapes at zero tension [47,48]. Using a bilayer bending modulus of $\sim 100 k_B T$, attractive interactions of order $\sim 1-5$ k_BT were found when the proteins were separated by one to two protein radii (which we estimate to be 5-10 nm measured center-to-center for a typical transmembrane protein). If we adjust the energy scale to be consistent with a PC bilayer bending modulus of $\sim 14 k_B T$, this lowers the interaction energetics to $\sim 0.4-2$ k_BT . Hence, although the length scale of appreciable interaction for midplane deformation is longer than for leaflet deformation, the interaction energies from leaflet deformation can be ten times greater depending on protein geometry. The deformation fields $h(\mathbf{r})$ and $u(\mathbf{r})$ exert their effects independent of one another [26], suggesting that while energetically weaker than leaflet deformation, mid-plane deformation probably also contributes to the spatial organization and conformational communication between transmembrane proteins. However, for the resting tension of many biological membranes [49], the interaction due to midplane deformation has a length scale $(\sqrt{\kappa_b/\tau} \approx 50 \text{ nm})$ longer than the nominal spacing of proteins ($\sim 10-30$ nm [14]). Thus, one protein can shield other proteins from feeling the deformation of a neighboring protein, and hence interactions are not (in general) pairwise additive. In fact, this is a general feature for both leaflet and midplane elastic interactions—they can be shielded by the presence of other proteins, and nonspecific protein interactions can couple to conformation and position within the membrane in the same manner as the specific interactions we have explored in the previous sections.

The second class of bilayer-mediated forces is a product of the thermal fluctuations of the bilayer. There is a small thermal force due to the excluded volume between two proteins, calculated via Monte Carlo methods to have a favorable $\sim 2 k_B T$ interaction [50]. This force only exists when the proteins are separated by a fraction of the width of a lipid molecule. There is also a long-range thermal force, due to the surface fluctuations of the bilayer, which tends to drive two rigid proteins closer together [10,51]. This force is proportional to $1/r^4$ and is generally attractive. Estimates using this power law indicate that the interaction is $\sim 1 k_B T$ when the center-to-center separation is roughly two protein radii. Though elegant, the derivation of this force is only valid in the far-field, thus how this force might contribute to conformational communication between proteins in close proximity is not entirely clear.

To gauge the overall importance of leaflet interactions, the virial coefficient used in Equation 17,

$$C_V = 2\pi \int_0^\infty f_{12}(r)r dr, \qquad (25)$$

quantifies how the combination of length and energy scales leads to a deviation from noninteracting behavior; it is *exponentially* sensitive to the energy but only *quadratically* sensitive to the length scale. One can interpret the virial coefficient as the area per particle that makes the competing effects of entropy and interaction equivalent. Using this measure, we estimated the virial coefficients for all of these bilayer-mediated forces and found that leaflet deformations,

while having a short length scale, actually lead to the most significant deviation from noninteracting behavior, due to their high energy scale. We estimate the virial coefficients from leaflet interactions to be $\sim 10^4$ – 10^6 nm², while midplane bending interactions are $\sim 10^3$ nm², and the thermal forces $\sim 10^2$ nm².

Examining our elastic model in greater detail, we have assumed that the slope of the leaflet at the protein-lipid interface is zero, which eliminates any dependence on the spontaneous and Gaussian curvatures of the leaflet. In a more general continuum-mechanical theory, the slope would be left as a free parameter with respect to which the energy could be minimized [25]. We examined this possibility and found that, at most, the energy was reduced by a factor of two. Spontaneous curvature couples to the slope of the leaflet at the protein-lipid interface; however, the spontaneous curvature of bilayer forming lipids, such as phosphocholines, is small [52]. In addition, for proteins whose radius is larger than λ , if we assume the modulus associated with Gaussian curvature is of the same magnitude as the mean curvature modulus (κ_b) [53], the Gaussian contribution to the deformation energy is a second-order effect. We also examined the possibility of a term proportional to $(\nabla u)^2$; using the interfacial tension ($\sim 5 k_B T / \text{nm}^2$) as a modulus for this term, these effects were also second-order. Finally, we imposed the "strong hydrophobic matching" condition at the proteinlipid interface, assuming that the interaction of lipids with the hydrophobic zone of the protein is very favorable. Relaxing this condition would result in a decrease in the magnitude of the hydrophobic matching condition, u_o , and hence an overall decrease of interaction energetics [26].

There are experimental and mechanical reasons to believe the boundary slope on a cylindrical protein is small. The membrane protein gramicidin was used to comment on this so-called "contact angle" problem of lipid-protein boundary conditions [22,54]. It was found that indeed the slope was nearly zero. From a mechanical standpoint, if the lipids are incompressible, a positive boundary slope that deviates significantly from zero would correspond to the creation of an energetically costly void at the protein-lipid interface when the protein is shorter than the bilayer. Conversely, lipids would have to penetrate the core of the protein to produce a negative slope when the protein is taller than the bilayer, again a very costly proposition.

We examined a roughly cylindrical protein and demonstrated the interesting effects elastic interactions would have in such cases. However, the scope of possible effects increases when noncylindrical proteins are considered. Most notably, noncylindrical cross-sections allow for orientational degrees of freedom in the interaction, hence such proteins do not just attract or repel each other, but would have preferred orientations in the membrane with respect to each other.

Measuring the changes in conformational statistics of two MscL proteins held at a fixed separation would allow for quantitative verification of our predictions. Electrophysiology is a common tool used to probe the conformation of ion channels, and is routinely used to measure the open probability of a single MscL protein in vitro [17,19,55]. Cysteine point mutations on the outer edges of two MscL proteins [20] could be covalently linked [56–59] by a polymer with a specific length (\sim 0.5–10 nm) to control the separation distance [60,61].

Linking stoichiometry could be controlled genetically [62] to ensure one channel interacts with only one other channel.

Similar experiments have been performed using gramicidin A channels [63]. The conducting form of gramicidin A is a cylindrical transmembrane protein which, like MscL, tends to compress the surrounding bilayer [22,33,64] and hence have a beneficial interaction. Electrophysiology of polypeptidelinked gramicidin channels [63] qualitatively supports our hypothesis that the beneficial interaction of the deformed lipids around two gramicidin channels significantly increases the lifetime of the conducting state [65]. As another example, recent FRET studies showed that oligomerization of rhodopsin is driven by precisely these kinds of elastic interactions, and exhibits a marked dependence on the severity of the deformation as modulated by bilayer thickness [66]. Additionally, recent experimental work has shown that the bacterial potassium channel KscA exhibits coupled gating and spatial clustering in artificial membranes [67].

In summary, we have demonstrated that leaflet deformations are one of the key mechanisms of bilayer-mediated protein-protein interactions. We provided support for our choice of boundary conditions at the protein-lipid interface, and suggested that extensions of our model have exciting possibilities for the specificity of elastic interaction. Finally, we suggested how one might measure the predicted changes in conformational statistics and drew an analogy to previous gramicidin channel experiments.

Conclusion

We have described the important role of an elastic bilayer in the function of, and communication between, membrane proteins. The interplay between the length scale of interaction (a few nanometers) and the energetics of interaction (on the order of $10 k_B T$) mean elastic interactions are relevant over a wide range of areal densities, from protein separations on the order of nanometers up to a micron or more. Transmembrane proteins can communicate information about their conformational state via the deformations they cause in the surrounding bilayer. We demonstrated with a model protein, the tension-sensitive channel MscL, how deformations lead to elastic forces and result in cooperative channel gating. Additionally, we found that elastic interactions strongly correlate conformational changes to changes in spatial organization, aggregating two channels even at low areal densities, and hence bringing them together over very large distances relative to their size.

The elastic theory presented here can be easily expanded to include more complex deformation effects (such as spontaneous curvature) and protein shapes, and is applicable to any protein that causes thickness deformation in the membrane. Our calculations for the conformational statistics, average separation, and dimerization are insensitive to the actual stimulus triggering the conformational change. Hence, we suggest that elastic interactions are likely to play a role in the function and organization of many membrane proteins that respond to environmental stimuli by forming functional

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groups of multiple membrane proteins. Recent work suggests chemotactic receptors in *E. coli* function by precisely this kind of spatially clustered and conformationally coupled modality [68].

Materials and Methods

To compute the pairwise elastic potentials in Figure 2, we discretize the bilayer height, $\eta(\rho)$, and minimize the deformation energy in Equation 5 using a preconditioned conjugate gradient approach. A separate minimization with the aforementioned boundary conditions, including the zero-slope boundary condition, was computed for each combination of channel configurations, protein–protein separation, and bilayer tension. Except in the regions of the bilayer nearby a protein at position (x_o, y_o) , we use a Cartesian grid with spacing $dx = dy = 0.1\lambda = 0.093$ nm. However, since deformations in the bilayer are largest at the circular membrane–protein interface, we interpolate between a polar grid at the interface at $\mathbf{r} = r_o$ and a Cartesian grid along the square S defined by $|x - x_o| < \Delta$, $|y - y_o| < \Delta$, where Δ is chosen to be an integral multiple of dx. This interpolation ensures an accurate estimate of the elastic deformation energy of a single protein and preserves the symmetry of the protein in its immediate vicinity.

The lines connecting the grid points along S define n_{θ} angular grid points θ_i $(i=1,\ldots,n_{\theta})$, and n_r+1 grid points within the interpolation region are defined by the polar coordinates $(r_{ij},\theta_i)=(r_o+\delta r_ij/n_r,\theta_i)$, where r_o is the radius of the protein and the distance from the center of the protein to S along θ_i is $r_o+\delta r_i$ (e.g., for $\theta_i=0,\delta r_i=\Delta-r_o$; for $\theta_i=\pi/4,\delta r_i=\Delta\sqrt{2}-r_o$). For a protein in the open or closed configuration, Δ was chosen such that $n_\theta=320$ or 224, respectively.

The deformation energy determined using this numerical relaxation method is converged with respect to dx, Δ , and the overall dimensions of the bilayer (18.5 nm \times 37.1 nm), and reproduces the analytic results for a single protein given by Equation 8. The elastic potentials were determined over the relevant range of channel separations from 0 to \sim 8 nm (measured from protein edge to protein edge), and for a range of bilayer tensions from 0 to $3.4~k_BT$ nm².

Supporting Information

Accession Numbers

The primary accession numbers (in parentheses) from the Protein Data Bank (http://www.pdb.org) are: MscL (2OAR; formerly 1MSL), gramicidin A ion channel (1GRM), bacterial potassium ion channel KscA (1F6G), and bovine rhodopsin (1GZM).

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Author contributions. TU conceived and designed the experiments. TU, KCH, and EP performed the experiments. TU, KCH, EP, and RP analyzed the data and contributed to writing the paper.

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