Reduced amino acid alphabets can improve the sensitivity and selectivity of pairwise sequence alignments

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Many proteins with widely diverged sequences are found to share a common fold, as evidenced in the wealth of structures now available in the Protein Data Bank (PDB). One idea that has found utility in various applications including protein folding is the concept of a reduced amino acid alphabet, wherein similar amino acids are clustered together. We tested many of the amino acid clustering schemes proposed in the literature with an all-versus-all pairwise search of sequences in the DALI database of structurally aligned proteins to determine what advantages might be gained from reducing the alphabet in identifying structurally similar proteins. In order to evaluate the results of the study we combined several metrics popular in the literature and in information retrieval: mean precision, area under the Receiver Operating Characteristic curve and recall at a fixed error rate. This extensive study encompassed more than 150 different amino acid "alphabets" representing the full range of possible reductions with alphabet sizes ranging from 2 to 19 letters. In contrast to some previous work which found only loss of performance with reduced alphabets, we find that in mean precision, recall versus errors per query and area under the Receiver Operating Characteristic curve, reduced alphabets in many cases *outperform* full alphabets. We find that reduced alphabets can perform at a level comparable to full alphabets in correct pairwise alignment of sequences and can show increased sensitivity to pairs of sequences with structural similarity but low sequence identity. The statistical significance of these findings was also evaluated based on the results of a Bayesian bootstrap method introduced by Price *et al.* [1]. Based on these results we hypothesize that reduced alphabets may also show performance gains with more sophisticated methods such as profile and pattern searches.

I. INTRODUCTION

Naturally occurring protein structures are observed to adopt "folds" i.e. a common group of secondary structures with the same orientation and topology. Current estimates of the number of protein folds in Nature is estimated to be between one thousand and ten thousand in total [2], an astonishingly low number compared with the huge space of possible amino acid sequences. From the wealth of structures and their associated sequences now available in the Protein Data Bank (PDB) it is clear that the same protein fold may be generated by different amino acid sequences. In some cases the sequences underlying similar structures show almost zero sequence identity (see e.g. [3]). This large degeneracy invites us to look for a coarse-grained sequence description that will reveal the underlying structural similarities between these apparently dissimilar sequences. Fig. 1 highlights an example of three proteins with extensive structural but scant sequence similarity, in this case between ParM, which is encoded on a transferable plasmid found in bacteria such as *E. coli*; actin, which is found in eukaryotes, and Ta0583, a recently crystallized protein found in the archaeon *T. acidophilum*.

We take the inspiration for our coarse-grained, reduced alphabet study from the hydrophobic-polar (HP) model for protein folding, introduced by Dill [9] to study the folding of globular proteins. This model derives from the observation that hydrophobicity will tend to dictate a minimum free energy protein conformation with hydrophobic residues buried in the interior and the hydrophilic residues exposed at the surface of a folded protein, suggesting that these gross features are dominant in dictating the fold. The HP model has been used fruitfully with lattice folding methods to generate structures with motifs analogous to those in natural proteins [10] as well as to design *de novo* small globular proteins by patterning of polar and non-polar residues [11].

Furthermore, previous experimental work with reduced amino acid alphabets in protein folding studies has shown that, in many cases, a reduced alphabet is sufficient to produce native-like proteins. The four-helix bundle protein Rop was studied by Munson *et al.* who showed that 32 amino acids in the hydrophobic core comprising eight different residues (ACEFILQT) could be replaced by patterning with just two amino acids (AL) to produce native-like proteins that showed activity *in vitro* [12], though only one mutant showed activity *in vivo* [13]. Schafmeister *et al.* designed *de novo* a 108 residue four-helix bundle with a seven letter alphabet (AEGKLQS) and validated their results with a crystal structure [14]. Riddle *et al.* were able to produce functional variants of the 57 residue Src SH3 β-sheet domain in which 38 of 40 targeted residues comprising 15 distinct amino acids were successfully mutated to a reduced alphabet of just 5 amino acids (AEGIK) [15].
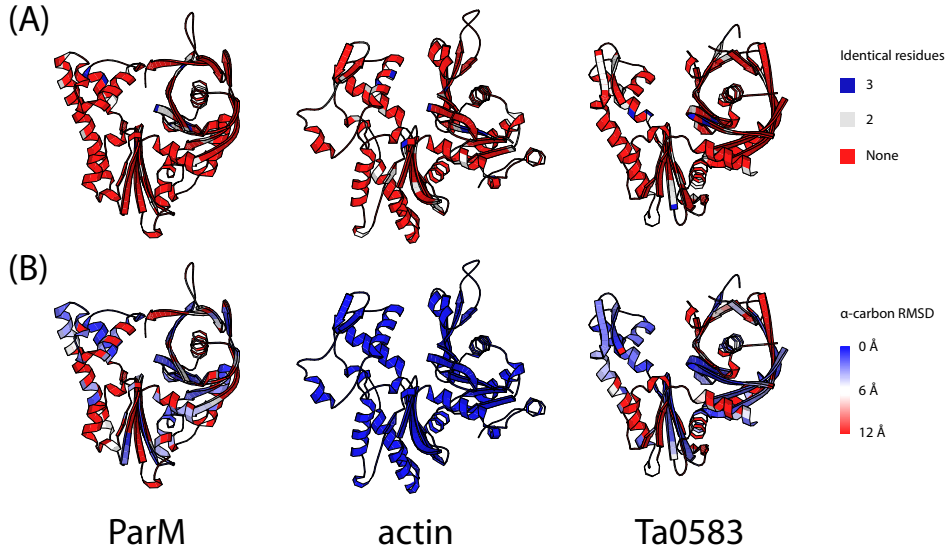
FIG. 1: **Comparison of sequence versus structural similarity.** This schematic shows eukaryotic actin from humans and two actin homologs, prokaryotic ParM from *E. coli* and archaeal Ta0583 from *T. acidophilum.* These three proteins share a common fold but have very low sequence identity, illustrated here by comparing sequence versus structural agreement following superposition of the three structures. In both panels A and B red indicates low, white moderate and blue high agreement. In panel A we see that sequence conservation is poor between the three proteins overall, with only a few residues conserved identically in all three (blue) or in two of three (white). In panel B we observe that the structures themselves show much higher similarity; the structures of ParM and Ta0583 are colored by the RMSD of their α-carbon backbones from actin with red indicating $\approx 12\,\text{Å}$ deviation, white $\approx 6\,\text{Å}$ deviation and blue indicating near overlap. There are numerous examples of proteins in this "twilight zone"[4] of low sequence identity ($\lesssim 25\%$) that have a common fold. The proteins shown here were aligned using STAMP [5], included in the MultiSeq [6] extension of VMD [7] and the figure was made with MolScript v2.1.2 [8]. The PDB accession codes are 1yag for actin, 1mwm for ParM and 2fsj for Ta0583.

Given the success of the HP and other reduced alphabet models in reproducing important features of protein structure and folding together with the experimental success in designing native-like proteins from reduced alphabets, we surmise that these simple folding ideas might also be reflected in pairwise alignments of the sequences of structurally similar proteins. Searches by BLAST and other alignment tools have at their heart a 20 by 20 symmetric scoring matrix (comprising 210 parameters) that effectively measure Nature's propensity to substitute one amino acid for another as evolution proceeds. We hypothesize that by properly grouping the 20 naturally occurring amino acids into classes and thereby coarse-graining the scoring matrices, similarities in protein sequence that are not readily seen in the full 20 letter alphabet would be revealed. By all of the measures we used, reduced alphabets showed increased effectiveness at identifying structurally similar proteins

as defined by the DALI database by a modest though statistically significant amount. Based on these gains in pairwise alignments and other past successes in the literature, we believe that the reduced alphabet approach applied to more sensitive methods, e.g. PSI-BLAST profile searches, holds promise for detecting structurally related proteins with weak sequence similarity.

The remainder of the paper is organized as follows. In Section II we describe our procedure for coarse-graining substitution matrices, outline the reduced alphabet schemes tested and reference databases used in this study as well as describe the principal metrics for this work: area under the Receiver Operating Characteristic curve, mean pooled precision and recall at 0.01 errors per query. In Section III we present the results of all-versus-all sequence alignments using each of the reduced alphabets, showing the performance of reduced alphabets in comparison with various common full 20 letter substitution matrices. The results of a study comparing structural alignments with sequence alignments are also shown for the full and reduced alphabets. Finally in Section IV we compare the results of this study with other similar work and speculate on promising avenues for further development with the reduced alphabet concept.

II.   METHODS

Substitution matrices.   There are many amino acid substitution matrices that have been formulated for pairwise sequence database searches; one of the most commonly used matrices and the default choice for BLAST searches is BLOSUM62. The BLOSUM family of substitution matrices is based on a log-odds ratio of the observed and expected frequencies of amino acids in a reference set of alignments where a sequence identity cutoff has been applied (62% in the case of BLOSUM62). This method, originally proposed by Henikoff and Henikoff [16], is described briefly here. Let us label the naturally occurring amino acids with indices 1-20; we may then derive a matrix c_{ij} with each entry of the matrix being the tally of the observed pairings of amino acid i with amino acid j in the reference alignments. Pairwise alignments do not distinguish between aligning e.g. AD and DA, so if the total count of ij and ji pairs is C (with $i \neq j$) we assign $c_{ij} = c_{ji} = C/2$ to reflect this symmetry. The underlying reason for this symmetry is that we assume no *a priori* knowledge of the order in which the sequences arose; without such knowledge, the likelihood of a substitution from e.g. A to G and G to A are equal. The observed probability matrix o_{ij} is the normalized c_{ij} matrix:

$$o_{ij} = \frac{c_{ij}}{\sum_{i=1}^{20} \sum_{j=1}^{20} c_{ij}}. \tag{1}$$

The frequencies of each of the amino acids p_i is now easily calculated from o_{ij}:

$$p_i = \sum_{j=1}^{20} o_{ij}, \tag{2}$$

and the expected (random) probability of aligning amino acid i with j is:

$$e_{ij} = p_i \, p_j. \tag{3}$$

The substitution matrix score m_{ij} is calculated from the observed and expected probabilities as a log-odds ratio:

$$m_{ij} = m_{ji} = \log_b \left(\frac{o_{ij}}{e_{ij}} \right). \tag{4}$$

where the base of the logarithm is usually chosen as $b = 2$ so that m_{ij} has units of bits of information (though substitution matrix values are sometimes measured in half-bits or other fractional bit units). For convenience of notation, the BLOSUM series of matrices will be referred to hereafter as BL followed by the level of sequence identity used in building the matrix e.g. BL62 for the BLOSUM matrix with 62% identity cutoff.

We follow this log-odds method in formulating matrices based on a reduced alphabet. Each reduced alphabet scheme clusters amino acids together into groups where all amino acids within a group are considered identical. Given N groups of amino acids defining a reduced alphabet, the new frequency of group I is calculated as:

$$p_I = \sum_{k \in I} p_k, \tag{5}$$

where k runs over each amino acid in group I. The new expected and observed probabilities to align group I with group J are:

$$e_{IJ} = p_I \, p_J, \tag{6}$$

$$o_{IJ} = \sum_{i \in I} \sum_{j \in J} o_{ij}. \tag{7}$$

Finally, the new matrix entries in the reduced $N \times N$ matrix are:

$$M_{IJ} = \log_b \left(\frac{o_{IJ}}{e_{IJ}} \right) \tag{8}$$

$$= \log_b \left[\frac{\sum_{i \in I} \sum_{j \in J} o_{ij}}{\sum_{i \in I} p_i \sum_{j \in J} p_j} \right]. \tag{9}$$

This method differs from that used in some previous reduced alphabet studies [17, 18] which used the arithmetic mean of the subsitution matrix entries; using the mean of the subsitution matrix scores is inconsistent with the log-odds probability scheme upon which the substitution matrices are based.

Reduced alphabet schemes. A reduced alphabet is any clustering of amino acids based on some measure of their relative similarity. Many such schemes have been proposed; the ones used in this study are briefly reviewed here together with the abbreviations used to refer to them. If a name for the scheme is given by the authors (e.g. SDM and DSSP) it has also been used here, otherwise abbreviations are formed by using the first letters of the names of the first and last authors. Thomas and Dill [19] created a hierarchy of amino acid groupings based on intuitive physicochemical considerations (TD). Mirny and Shakhnovich [20] constructed a six letter alphabet based mostly upon intuition as well as a study of the effects of disulfide bonds on protein folding which suggested separating aliphatic hydrophobic and aromatic hydrophobic residues [21] (MS). Solis and Rackovsky [22] posited clusters based on maximum preservation of structural information (DSSP and GBMR). Andersen and Brunak [23] searched for clusters of amino acids based on the ability of standard methods to correctly predict secondary structure from the simplified sequences (AB). Cieplak *et al.* [24] used the Miyazawa-Jernigan interaction matrix [25] together with a distance-based clustering scheme to partition the naturally occurring amino acids into 2- and 5-letter groups (CB). Prlić *et al.* [26] derived new substitution matrices based on structural alignments of proteins with low sequence identity and then clustered the amino acids based on those matrices (SDM and HSDM). On the basis of a comparison of early substitution matrices, Landès and Risler [27] proposed a 10-letter alphabet that showed promise for increasing the sensitivity of protein alignment searches (LR). Li *et al.* [18] proposed grouping schemes based on preservation of information in global sequence alignments between a sequence and its reduced-alphabet version. They produced two groupings, one allowing amino acids to change their order or "interlace" (LW-I) and one where they were not allowed to change order (LW-NI). The LW schemes were identical at the levels of 2, 3 and 15 through 19 letters. We also note that the CB and LW schemes were identical at the 2 letter level. Melo and Marti-Renom [28] created a 5 letter clustering of amino acids based on the Johnson-Overington matrix (JO20) [29], which they found performed well in aligning homologous sequences and fold assessment (MM). Murphy, Wallqvist and Levy [17], inspired by experimental successes in designing proteins with reduced alphabets, proposed clusters of amino acids based on the BL50 substitution matrix (ML). Liu *et al.* [30] studied the pair frequency counts in the Miyazawa-Jernigan and BL50 matrices to find deviations from a random background and based thereon proposed a clustering of amino acids (LZ-MJ and LZ-BL). Finally, Wang and Wang [31] derived clusters from the Miyazawa-Jernigan matrix by preserving maximal similarity between a reduced-alphabet version of the matrix and the full 20 by 20 matrix (WW). They found a five letter alphabet (IKEAG) that matched with what Baker *et al.* [15] had found in their experimental study producing SH3 domains from reduced alphabets. Each of these schemes produced a hierarchy of

2	LIVFMYWC									DNTSKEQRAGPH												
3	LIVFMYW		C							DNTSKEQRAGPH												
4	LIVFMYW		C							DNTSKEQRAGP								H				
5	LIVFMY		W	C						DNTSKEQRAGP								H				
6	LIVFMY		W	C						DNTSKEQRAG						P		H				
7	LIVFMY		W	C						DNTSKEQRA					G		P	H				
8	LIVFM	Y	W	C						DNTSKEQRA					G		P	H				
9	LIVFM	Y	W	C						DNTSKEQR			A		G		P	H				
10	LIVFM		Y	W	C	DN				TSKEQR			A		G		P	H				
12	LIVF	M	Y	W	C	DN				TSKEQ		R	A		G		P	H				
14	LIV	F	M	Y	W	C	DN		TS	KEQ		R	A		G		P	H				
15	LIV	F	M	Y	W	C	D N		TS	KEQ		R	A		G		P	H				
16	LIV	F	M	Y	W	C	D N		TS	KE	Q	R	A		G		P	H				
17	LIV	F	M	Y	W	C	D N	T S		KE	Q	R	A		G		P	H				
20	L I V	F	M	Y	W	C	D N	T S	K	E	Q	R	A		G		P	H				

TABLE I: The hierarchy of amino acid classes in the HSDM reduced alphabet scheme [26]. The first column gives the number of groups or "letters" in the reduced alphabet; the amino acid groupings at each level are shown on the right.

amino acid classes, as typified by the dendrogram of the HSDM scheme [26] in Table I. At each level in the hierarchy the number of classes or "letters" in the alphabet is increased. We tested each of the reduced alphabet schemes in the papers just cited; Table II shows the abbreviations for each scheme, the various levels of clusterings comprising the scheme and the frequency matrix and gap penalties used. In this work, reduced alphabet matrices will be referred to by the alphabet scheme (TD, SDM, HSDM etc.) followed by the number of letters in the alphabet e.g. HSDM17.

Protein database. We chose the DALI (<u>D</u>istance m<u>A</u>trix a<u>LI</u>gnment) database [32] which uses fully automated methods to cluster protein domains based on their structural similarity as our "gold standard" for determining the structural relatedness of proteins. DALI partitions each protein structure in the PDB into domains by maximizing criteria of compactness and recurrence of those domains [33]. After determining the domains, all-versus-all structural alignments of the domains are executed and a z-score estimated to indicate the statistical significance of those alignments [33]. Finally, the domains are clustered into families based on z-score cutoffs; a cut-off z-score greater than 2, indicating statistically significant structural similarity at the 2σ level, is used to define proteins with roughly the same "fold" [33].

The sequence library for this study was drawn from the DALI *pdb90* database using each of the representative sequences in the domain fold classes defined by the DALI Domain Dictionary [33, 34], both available for download at the DALI website [35]. All pairs of sequences within the same domain fold class are considered to be structurally related "hits" (true positives) in our database searches.

Scheme	Alphabet sizes	Substitution matrix	Gap penalties Open	Extend
AB* [23]	2-19	BL62	11	1
CB* [24]	2,5	BL62	11	1
DSSP* [22]	2-14	BL62	11	1
GBMR* [22]	2-14	BL62	11	1
HSDM [26]	2-10,12,14-17	HSDM	19	1
LR* [27]	10	BL62	11	1
LW-I* / LW-NI* [18]	2-19	BL62	11	1
LZ-MJ* / LZ-BL [30]	2-16	BL50	11	1
MM [28]	5	JO20	140	0
ML [17]	2,4,8,10,15	BL50	12	2
MS [20]	6	BL62	11	1
SDM [26]	2-4,6-8,10-14	SDM	7	1
TD* [24]	2-10,14	BL62	11	1
WW* [31]	5	BL62	11	1

TABLE II: Reduced alphabet schemes investigated in this work. Abbreviations and references are listed in the first column; alphabet sizes, matrix used and gap penalties are also shown. Wherever possible we used the matrices and gaps given in the original articles referenced, though we note that the starred schemes were proposed independently of any particular substitution matrix. In those cases, the BL62 frequency counts were used to derive the coarse-grained matrices with 11/1 gaps. In addition to the reduced alphabet schemes tested above we also tested the following full 20 by 20 matrices: BL50 11/1, BL50 12/2, BL62 7/1, BL62 11/1, JO20 140/0, SDM 7/1 and HSDM 19/1.

In total 13,351 sequences were drawn from the *pdb90* database, representing 2780 fold classes. One domain fold class, number 1636, was not represented in the database because its representative sequence, *1mwxA_1*, was not found in the latest version of *pdb90* available for download. We also note that there were 1264 sequences which were singletons i.e. they were the only members of their DALI fold class; these sequences are in some sense undetectable since they have no true positive relationship to any other protein in the database.

Alignment program. All-versus-all Smith-Waterman alignments were executed using SSEARCH version 3.4 from the FASTA sequence alignment suite [36, 37]; the alignments were ranked by E-value as calculated by the default SSEARCH statistics option (specified by the "-z 1" switch on the command line).

Generation of search results. We executed all-versus-all alignments, using each sequence in the DALI *pdb90* database in turn as a query against the remaining sequences. The results of all these searches were then pooled into a single list of results ranked by the E-value assigned by SSEARCH; when true and false positives shared an E-value, the false positive alignments were ranked ahead of the true positives to obtain a conservative estimate of discriminating power.

Reference sequence alignments. Structural alignment of protein domains with the DALI method produces a reference list of structurally equivalent pairs of residues [32]. We compared these structure-based alignments with the alignments produced by SSEARCH and tallied the fraction of structurally equivalent residues found by SSEARCH local alignments. The database of structurally equivalent residues, *dali_fragments*, was obtained from the DALI downloads website [35].

III. RESULTS

A scoring matrix should ideally be able to both detect related pairs of proteins (true positives) and reject non-related pairs (false positives); these properties are termed sensitivity and selectivity, respectively, and in many instances they compete with one another in the sense that as a matrix is tuned to be more sensitive it often loses selectivity and vice versa. After pooling the results of querying the database with each sequence, we choose a particular E-value and consider all results at this E-value or lower to be "hits". The recall, fall-out, precision and errors per query (EPQ) are calculated from the list of hits as follows:

$$\mathrm{recall} \;=\; \frac{\mathrm{tp}}{\mathrm{N_{tp}}}, \tag{10}$$

$$\mathrm{fall\text{-}out} \;=\; \frac{\mathrm{fp}}{\mathrm{N_{fp}}}, \tag{11}$$

$$\mathrm{precision} \;=\; \frac{\mathrm{tp}}{\mathrm{tp} + \mathrm{fp}}, \tag{12}$$

$$\mathrm{EPQ} \;=\; \frac{\mathrm{fp}}{\mathrm{N_{seq}}}, \tag{13}$$

where tp is the number of true positive hits, fp is the number of false positive hits and $\mathrm{N_{seq}}$ is the total number of sequences; $\mathrm{N_{tp}}$ and $\mathrm{N_{fp}}$ are the total number of true and false positive relationships in the database, respectively. Moving down the pooled list of search results we generate successively larger groups of hits at increasing E-values with associated values for recall, fall-out, precision and EPQ. The three curves analyzed in this work are precision versus recall, recall versus fall-out (also called the Receiver Operating Characteristic or ROC curve) and recall versus EPQ (also called the coverage versus errors per query or CVE plot), all parametrized by increasing E-value. We define the mean pooled precision to be the integral of the precision versus recall curve for the combined list of search results; this number gives the average precision achieved over the entire range of recall and HSDM17 achieves the best result by this metric. The area under the ROC curve measures the ability of a matrix to identify related pairs by assigning them lower E-values than pairs of proteins that are not related over the entire list of pooled results; SDM12 is the top performer here. Finally the

recall at 0.01 EPQ gives the number of true positives returned at a fixed, low error rate. Recall may be normalized in several ways, as defined by Green and Brenner [38]. Recall without normalization gives equal weight to each true positive relationship; quadratic normalization weights true positive hits so that each fold represented in the database has equal weight. Linear normalization is a compromise between these two, giving each sequence in the database equal weight and is meant to take into account the fact that folds are not equally represented in Nature [2]. We find that the top performer in recall at 0.01 EPQ with linear normalization to be GBMR4; this matrix also ranked in the top ten in recall without normalization and under quadratic normalization (see Table IV).

We wish to also note that many reduced alphabets beyond the three we mentioned above outperform the BLAST-default matrix, BL62 with 11/1 gaps. Among the 151 scoring matrices tested in this work, BL62 ranked 38th overall in area under the ROC curve, 18th in mean pooled precision, and 111th, 102nd and 104th in recall at 0.01 EPQ with no, linear and quadratic normalization, respectively. In the remaining plots we will compare the top performers in mean pooled precision (HSDM17), area under the ROC curve (SDM12) and recall at 0.01 EPQ (GBMR4) with one another, using BL62 11/1 as the baseline.

Mean pooled precision. Precision versus recall curves are shown in panel A of Fig. 2 for GBMR4, HSDM17 and SDM12; the mean pooled precision is the area under this curve. A perfect method would have a mean pooled precision value of unity, maintaining 100% precision until all true positives have been identified. The mean pooled precision for all of the HSDM, SDM, and GBMR alphabets is plotted in panel B of Fig. 2. Section (A) of Table III shows that mean pooled precision tends to favor larger alphabets, and the HSDM family of alphabets consistently achieves good results in this area.

Note that even the strongest performers in mean pooled precision cannot maintain a high level of precision beyond a recall value of about 0.4. This means that only about 40% of the total number of true positives can be reliably identified before additional true positives in the list of hits become buried in a flood of false positives in a sort of "needle-in-a-haystack" situation. The steep dropoff in mean precision in Fig. 2(A) indicates the limits of what can be achieved with pairwise sequence alignment.

Area under the ROC curve. The area under the ROC curve has a very specific interpretation: it is equal to the probability of assigning a lower expect value to a true positive than to a false positive [39]. Therefore it gives a measure of the sensitivity of a scoring matrix to related sequences over the entire pooled list of results. The top 10 finishers according to this metric are shown in the section B of Table III. The top overall performer in detecting structurally related proteins by pairwise search is the SDM12 matrix; another notable high performer is LZ-MJ6 which finished in
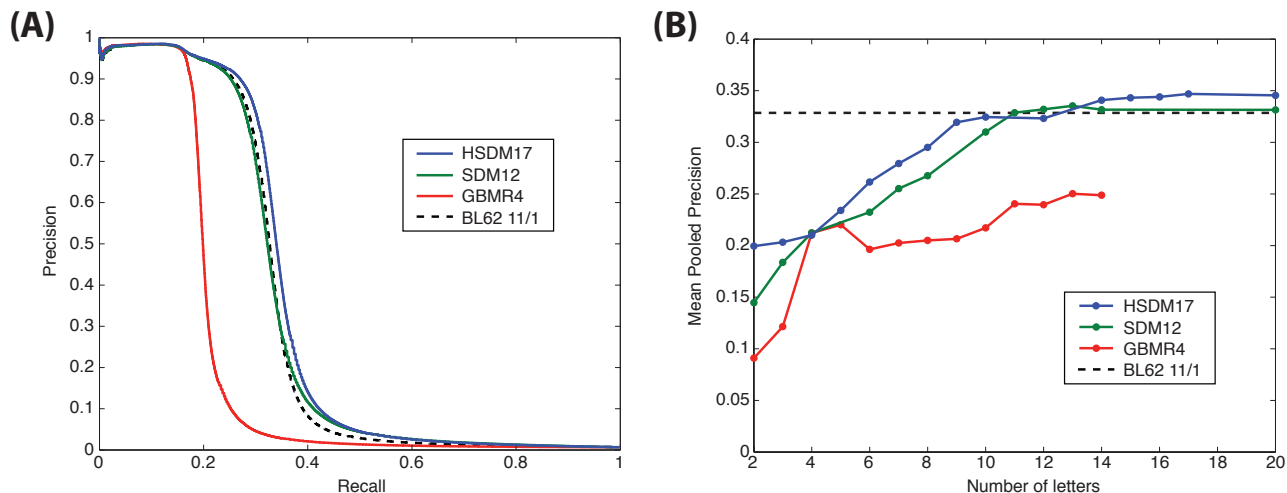
FIG. 2: **Reduced alphabet performance in mean pooled precision.**

(A) Precision versus recall curves for the top reduced alphabet performers. The mean pooled precision is the area under this curve and indicates the ability of a particular matrix to maintain high selectivity over a wide range of error rates. At some point, each matrix loses the ability to selectively reject false positives and the curve drops precipitously to low precision values.

(B) Mean pooled precision indicates the average precision achieved by a matrix over the entire range of recall. A perfect method would achieve a mean pooled precision value of unity, with all true positives ranked ahead of false ones. The HSDM17 matrix is the top performer in this metric; the dashed black lines in panels A and B show the performance of BL62 11/1 for reference. Points indicate reduced alphabets that were tested; the connecting lines are a guide to the eye.

the top ten with only six letters. Receiver Operating Characteristic curves are shown in Fig. 3(A) for SDM12, HSDM17 and GBMR4. The total area under the curve versus number of letters in these schemes is shown in panel B; note that the area under the ROC curve does not necessarily increase monotonically with alphabet size.

Although it is of interest that HSDM17 maintains the best selectivity as measured by mean pooled precision and SDM12 the best sensitivity as measured by the area under the ROC curve, what is of most interest to a pedestrian user of an alignment program with a query protein and a target database is to find a scoring matrix that will yield the most number of true positives at a fixed, low error rate. Operationally, a researcher will have an intuition for what E values indicate hits that are likely to be significant and will ignore hits below that intuitive threshhold. In the DALI database we used there are more than 150 times as many false positives as true positives, so much of the advantage shown by HSDM17 and SDM12 is in a regime beyond what could be reasonably processed "by hand". Therefore we also examine the performance of reduced alphabets

in recall of true relationships at an error per query rate of 0.01.
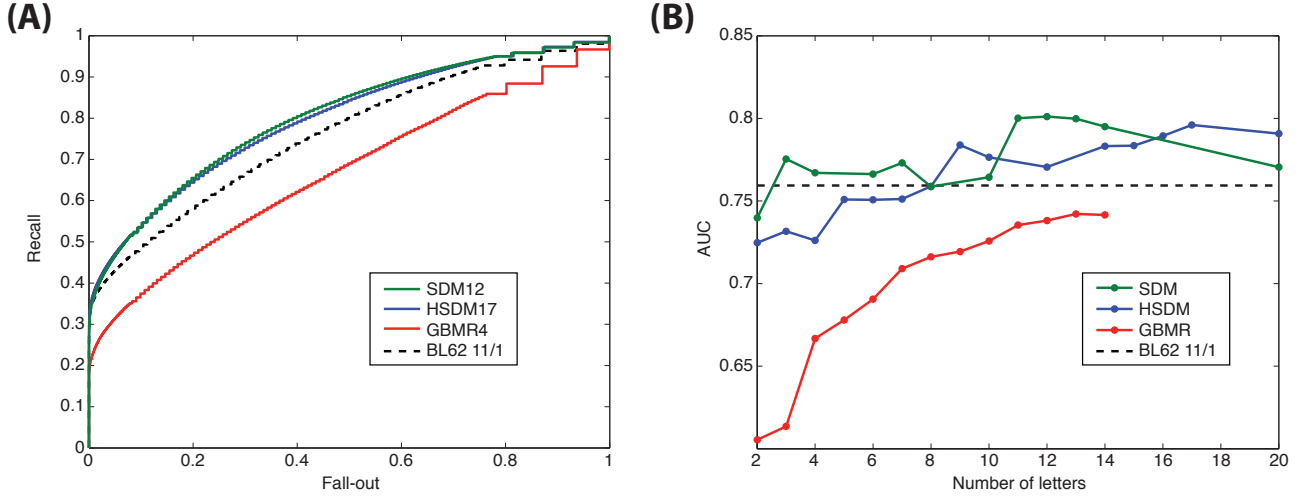
(A)

(B)

FIG. 3: **Reduced alphabet performance in area under the Receiver Operating Characteristic curve.**

(A) Receiver Operating Characteristic (ROC) curves for the top performing alphabets. The integral of this curve gives a measure of how well the entire pooled list of hits is sorted; a perfect method would have an ROC area of unity.

(B) Overall sensitivity of the SDM alphabets as measured by the area under the ROC curve. The level of sensitivity of BL62 11/1 is shown with the black dashed line. Points indicate reduced alphabets that were tested; the connecting lines are a guide to the eye.

	(A) Mean pooled precision			(B) Area under ROC curve		
Rank	*Scheme*	*Letters*	*MPP*	*Scheme*	*Letters*	*AUC*
1	HSDM	17	0.347	SDM	12	0.801
2	BL62 7/1	20	0.347	SDM	11	0.800
3	BL50 11/1	20	0.346	SDM	13	0.800
4	LZ-BL	16	0.346	HSDM	17	0.796
5	HSDM	20	0.345	SDM	14	0.795
6	HSDM	16	0.344	LZ-MJ	6	0.793
7	HSDM	15	0.343	HSDM	20	0.791
8	HSDM	14	0.341	HSDM	16	0.789
9	LZ-BL	15	0.339	HSDM	9	0.784
10	SDM	13	0.335	HSDM	15	0.783

TABLE III: Top 10 performers in mean pooled precision (MPP) and area under the Receiver Operating Characteristic curve (AUC). Mean pooled precision is a measure of the selectivity of a matrix i.e. its ability to retain high recall of true positive relationships at low error rates. The area under the ROC curve measures the sensitivity of a matrix to true positive alignments over the entire list of results.

Recall at 0.01 EPQ. The second measure of the selectivity of each reduced alphabet scheme was calculated as the recall (also called coverage) at 0.01 errors per query; this is the metric of the most practical interest. Panel A of Fig. 4 shows the recall versus error rate curves under linear normalization for GBMR4, HSDM17 and SDM12 with better-performing matrices generating curves that tend toward the lower-right hand corner indicating high recall at low error rates. Comparing this with panel A of Fig. 2 we can see that GBMR4 is able to maintain the highest level of precision initially, but it rapidly loses precision at higher recall values. Panel B of Fig. 4 shows the recall at 0.01 EPQ with linear normalization versus number of letters for the GBMR, SDM and HSDM alphabets. Table IV shows the top ten ranked matrices in recall at 0.01 EPQ under each of the normalizations described earlier with GBMR4 and other relatively small alphabets being the top performers.
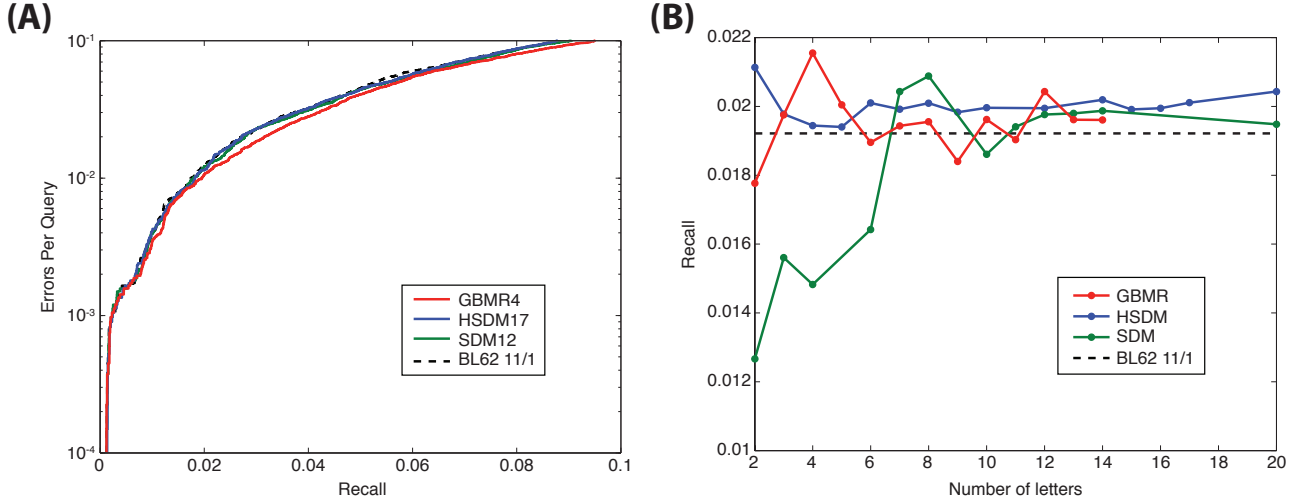

FIG. 4: **Reduced alphabet performance in recall versus errors per query with linear normalization.**

(A) Linearly normalized recall (or coverage) versus the number of errors per query (EPQ). Curves that tend toward the lower right-hand corner perform better, detecting more true positives at a given error rate. Small alphabets show good performance at lower error rates (EPQ < 0.1) with GBMR4 being the top performer. (B) Recall with linear normalization at 0.01 EPQ for various numbers of letters in the GBMR, HSDM and SDM reduced alphabet schemes. The level of performance of BL62 11/1 is shown with the black dashed line. Points indicate reduced alphabets that were tested; the connecting lines are a guide to the eye.

These results would seem to indicate that reduced alphabets offer an advantage of immediate practical value over currently used matrices based on the full alphabet. To further investigate this possibility we performed all vs. all alignments with HSDM17, SDM12, GBMR4 and BL62 11/1

	Recall at 0.01 EPQ								
	No normalization			Linear normalization			Quadratic normalization		
Rank	Scheme	Letters	Recall	Scheme	Letters	Recall	Scheme	Letters	Recall
1	GBMR	6	0.0097	GBMR	4	0.022	LZ-BL	7	0.036
2	GBMR	7	0.0089	CB/LW	2	0.021	GBMR	4	0.036
3	GBMR	8	0.0085	HSDM	2	0.021	HSDM	2	0.036
4	GBMR	9	0.0067	LZ-BL	7	0.021	HSDM	20	0.036
5	DSSP	2	0.0044	SDM	8	0.021	LZ-BL	8	0.036
6	GBMR	10	0.0038	TD	2	0.021	GBMR	12	0.035
7	ML	2	0.0036	BL50 11/1	20	0.021	LW-I	9	0.035
8	SDM	6	0.0030	LZ-BL	6	0.020	GBMR	3	0.035
9	GBMR	4	0.0029	HSDM	20	0.020	CB/LW	2	0.035
10	CB/LW	2	0.0029	SDM	7	0.020	SDM	8	0.035

TABLE IV: Top 10 performers in recall at 0.01 errors per query with default, linear and quadratic normalization. Like mean pooled precision, recall at 0.01 EPQ measures the selectivity of a matrix but is drawn from a limited set of hits such as a researcher might reasonably peruse manually, rather than the entire pooled list of search results which comprises approximately 170 million alignments.

using proteins belonging to the same SCOP superfamily to define true positives. The results of a preliminary study with the scop40 and scop95 sequence databases, containing sequences sharing no more than 40% and 95% sequence identity, respectively, are compared with DALI in Table V. We note that BL62 11/1 outperformed GBMR4 in linearly-normalized recall at 0.01 EPQ with both SCOP databases. However larger reduced alphabets maintained their advantage in selectivity and sensitivity with SCOP since HSDM17 and SDM12 both achieved higher mean pooled precision, area under the ROC curve and linear recall at 0.01 EPQ scores than BL62 11/1. This indicates that small reduced alphabets can show an increased sensitivity and selectivity for proteins that are *structurally* related, the only criteria used by DALI, but seem to lose selectivity when criteria such as function and evolution are taken into account, as is done with the human-curated SCOP superfamily classification [40]. To the extent that performance with the SCOP and DALI databases indicates real world performance, these results suggest that larger alphabets like SDM12 and HSDM17 offer increased sensitivity and selectivity over the standard BL62 11/1 matrix based on a full alphabet.

Statistical significance of results. The three top-performing alphabets (GBMR4, SDM12 and HSDM17) are shown in Table VI together with the results of BL62 11/1 shown for reference. We used the Bayesian bootstrap method developed by Price *et al.* [1] to evaluate the statistical significance of the successes of the reduced alphabets in comparison with the standard BL62 11/1 scoring matrix. First the differences in performance are tabulated between each pair of bootstrap replicas and then a z-statistic is calculated by dividing the mean of distribution of differences by its standard deviation. This statistic, rather than the difference in mean performance, was found

Scheme	scop40			scop95			DALI		
	MPP	AUC	Recall	MPP	AUC	Recall	MPP	AUC	Recall
GBMR4	0.089	0.658	0.100	0.259	0.727	0.204	0.212	0.667	0.022
SDM12	0.156	0.734	0.136	0.419	0.833	0.250	0.332	0.801	0.020
HSDM17	0.173	0.751	0.148	0.436	0.840	0.259	0.347	0.796	0.020
BL62 11/1	0.156	0.714	0.134	0.408	0.812	0.245	0.329	0.759	0.019

TABLE V: Comparison of results from all vs. all studies with scop40, scop95 and DALI. In the SCOP results GMBR4 is unable to maintain its advantage in linearly normalized recall at 0.01 EPQ over BL62 11/1. However both SDM12 and HSDM17 are able to match or better the results of BL62 11/1 in mean pooled precision (MPP), area under the ROC curve (AUC) and linearly normalized recall at 0.01 EPQ. Version 1.71 of the scop40 and scop95 sequence databases were used.

to be the most sensitive for evaluating the significance of differences in performance between two scoring matrices [1]. We find a strongly significant z-value of 6.17 for the superior performance of SDM12 relative to BL62 11/1 in area under the ROC curve and marginally significant z-values of 1.33 for HSDM17 versus BL62 11/1 in mean pooled precision and 1.49 for GBMR4 versus BL62 11/1 in recall at 0.01 EPQ with linear normalization.

		Recall	AUC	MPP
GBMR4	ADKERNTSQ YFLIVMCWH G P	**0.022(0.001)**	0.667(0.004)	0.212(0.006)
SDM12	A D KER N TSQ YF LIVM C W H G P	0.020(0.001)	**0.801(0.005)**	0.332(0.009)
HSDM17	A D KE R N T S Q Y F LIV M C W H G P	0.020(0.001)	0.796(0.004)	**0.347(0.008)**
BL62 11/1	A D K E R N T S Q Y F L I V M C W H G P	0.019(0.001)	0.759(0.005)	0.329(0.009)

TABLE VI: The top performing alphabets found in this study in linearly normalized recall at 0.01 errors per query (GBMR4), area under the ROC curve (SDM12) and mean pooled precision (HSDM17) with the standard deviation of 1000 bootstrap replicas given in parentheses. Results for BL62 11/1 are shown for comparison.

A.   Alignment Accuracy

We evaluated how well pairwise sequence alignments with reduced alphabets identified pairs of residues that are structurally equivalent as defined by DALI. The results are shown in Fig. 5, plotted as the fraction of structurally equivalent residue pairs identified by SSEARCH using the SDM, HSDM and GBMR reduced alphabet schemes. The curves tend to saturate at around 10 letters, implying that expanding the alphabet beyond this point does not improve the alignments but tends to increase their sensitivity to more recently diverged proteins. The top 10 finishers in alignment accuracy are shown in Table VII; HSDM and SDM show the best performance which is not surprising given that they were derived from structurally equivalent pairs of residues [26]. It

is interesting that the highly simplified GBMR4 alphabet is able to achieve nearly the same level of accuracy as the full BL62 11/1 matrix. The DALI database of structurally equivalent residues is an exceedingly challenging test of pairwise sequence comparison since the equivalenced residues share only 11% identity overall; even the best alphabet, HSDM17, achieves exact agreement with less than one tenth of all residues in the DALI structural alignments.
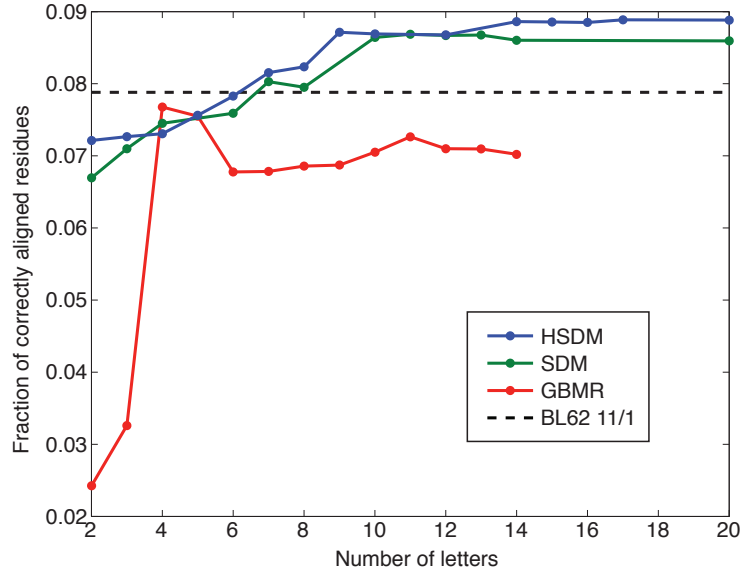

FIG. 5: Agreement of structural and sequence alignments. The fraction of DALI equivalent residue pairs found by SSEARCH alignment is shown for various reduced alphabet schemes. Most of the gains are made as classes are added up until around 10 classes, after which the performance levels off. Points indicate reduced alphabets that were tested; the connecting lines are a guide to the eye.

Rank	Scheme	Letters	Fraction aligned
1	HSDM	17	0.08887
2	HSDM	20	0.08882
3	HSDM	14	0.08862
4	HSDM	15	0.08857
5	HSDM	16	0.08849
6	HSDM	9	0.08714
7	HSDM	10	0.08691
8	SDM	11	0.08686
9	HSDM	12	0.08676
10	SDM	13	0.08675

TABLE VII: The top 10 performers in agreement between sequence and structural alignments, using DALI structurally equivalent residues as the "gold standard". As expected, the two structure-derived matrices, HSDM and SDM, completely dominate the results.

B. Comparison of detected relationships

It is also valuable to compare the hits returned by two matrices at a given errors per query level to see what types of relationships are more easily detected by one relative to another. We compared the hits returned by the SDM12 and BL62 11/1 matrices at or above 0.01 EPQ and found that each matrix finds about 3000 true positives at that error level. After separating out the hits that were unique to each matrix (they share 2724 hits in common) SDM12 was left with 271 unique hits and BL62 11/1 with 139. The approximate mean percent identity of the SDM12 unique hits is 60% whereas for BL62 11/1 it is 70%. Although SDM12 and BL62 have essentially identical relative entropy (-0.703 and -0.699 bits respectively) SDM12 is able to detect more distant relationships than BL62. A histogram of the hits unique to each matrix is shown in Fig. 6.
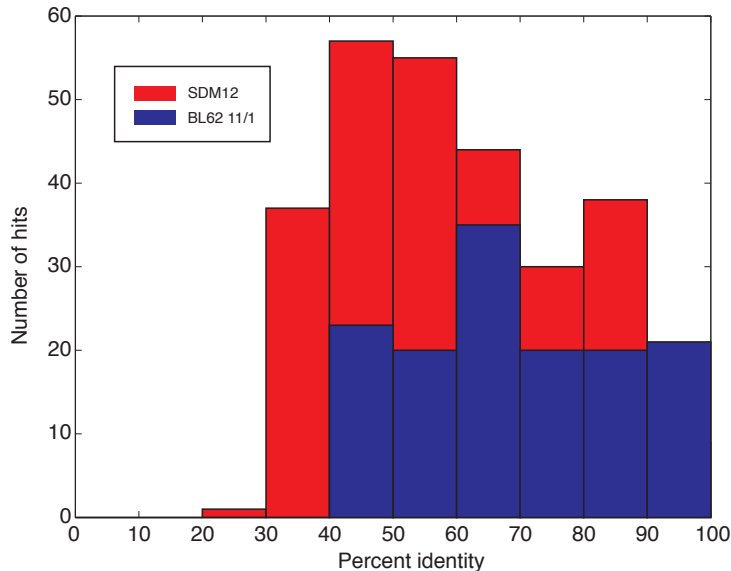
FIG. 6: Histogram of the hits at or above 0.01 errors per query unique to the SDM12 and BL62 11/1 matrices. The results from SDM12 are both more numerous and shifted towards lower identity, showing its increased ability to detect more remote relationships.

IV. DISCUSSION

We find, perhaps counter to common intuition, that reduced alphabets *increase* the selectivity and sensitivity to pairs of proteins with structural similarity as measured by the mean pooled precision, area under the ROC curve and recall at 0.01 errors per query (under all normalizations). In addition we found that reduced alphabets can return more distantly related pairs of proteins.

This is in contrast to some earlier studies [17, 18, 30] which found that reduced alphabets could only produce losses in performance relative to a full alphabet. Landès and Risler also observed improved sensitivity with reduced alphabets; in an early study with aminoacyl-tRNA synthetases, LR10 showed an increased ability to identify distant homologs over methods using the full alphabet [27]. This work also adds to the encouraging results with reduced alphabets found by Melo and Marti-Renom [28], who tested the 20 letter Johnson-Overington matrix against several small reduced alphabets: WW5, GBMR5, ML4, MM5 and 100 randomly reduced five-letter alphabets. They found that the GBMR5 alphabet produced performance gains over the full matrix in alignment accuracy as measured by the root-mean-square deviation of C^α atoms after using the pairwise alignment as the initial seed for an optimal structural superposition.

A point of diminishing returns is observed in mean pooled precision (Fig. 2, panel B), area under the ROC curve (Fig. 3, panel B) and alignment accuracy (Fig. 5) at an alphabet size of about 10 letters. For instance, we find that in area under the ROC curve, HSDM10 achieves 98% of HSDM20's performance, GBMR10 achieves 96% of the performance of BL62 11/1 and SDM10 slightly exceeds the total area achieved by SDM20. Similar results have been observed elsewhere in reduced alphabet studies. Weathers *et al.* found that a Support Vector Machine model using reduced alphabets (as small as 4 letters) retained nearly as much ability to detect intrinsically disordered proteins as the full 20 letter alphabet [41]. Rackovsky and coworkers showed that using seven groups of amino acids best conserves information about local backbone conformation [22] and in a separate work found that current knowledge-based statistical potentials, though often assumed to discriminate between all 20 amino acids, actually only distinguish at most between about eight classes of residues [42]. In their work testing the ENERGI method for building of statistical potentials, Dill and Thomas found that using a 20 letter alphabet was no more successful than a 5 letter alphabet for fold detection, with the peak of detection occurring at an alphabet of 10 letters [19]. In their study of pairwise sequence alignment, Murphy *et al.* estimated that a minimum of a 10-12 letter alphabet is necessary to design foldable sequences for most protein families [17]. Fan and Wang also found that the minimum alphabet size for protein folding requires approximately 10 types of amino acids [43]. The consensus seems to be the there is little to lose and possibly gains to be made by properly clustering the amino acids.

It is interesting that the top performing alphabets, shown in Table VI, are compatible with one another in the sense that SDM12 can be derived from GBMR4 and HSDM17 can be derived from SDM12 by simply breaking down larger clusters into smaller ones without needing to interchange the grouping of any of the amino acids. In the GBMR4 alphabet glycine and proline are singled out as being structurally dissimilar from the other amino acids; the remaining two groups reflect a

hydrophobic (YFLIVMCWH) and polar (ADKERNTSQ) classification. In this sense, the GBMR4 alphabet is a modest refinement of the simple HP concept. The SDM12 alphabet maintains clusters for acidic/basic (KER), polar (TSQ), aromatic (YF) and mostly aliphatic (LIVM) groups. Two non-intuitive results in these groupings are the omission of aspartic acid from the acidic/basic KER cluster and the inclusion of methionine in the otherwise aliphatic LIVM cluster. In HSDM17 only the strongest associations among these are maintained: acidic/basic (KE) and aliphatic (LIV). By clustering together amino acids with similar properties in this way we increase the signal to noise in our database searches and avoid over-assigning importance to differences among the naturally occurring amino acids.

We wish to note several promising avenues for further investigation but which could not be pursued in this work for lack of sufficient time and computing resources. In theory an optimum alphabet could be searched for at each alphabet size by e.g. Monte Carlo search. Likewise it would be ideal to optimize the gap penalties with respect to each reduced alphabet. Lack of sufficient computational resources made it impractical to carry out these optimizations. We chose to use the DALI database as our standard for determining structural relationships among proteins in the PDB over databases like e.g. SCOP [40] because its determinations are informed only by structural similarity and require no human curation. Although we obtained some preliminary results with SCOP it would be instructive to compare the results using the DALI database to what would be obtained by testing all the reduced alphabets in this work using SCOP superfamilies as the "gold standard" for structural relatedness. Given the encouraging results shown by SDM12 and HSDM17 with both SCOP and DALI we believe that further investigation into the practical advantages of reduced alphabets for general use with pairwise alignment matrices merits additional exploration.

Another promising area for application of the results of this study is in the building of protein profiles or hidden Markov models (HMMs). Such models are built up from a multiple alignment of many putatively homologous proteins. At each position in the alignment, a number can be assigned for the probability of observing a particular amino acid based on the sequences in the multiple alignment. The simplest type of protein profile is simply a consensus sequence of the most commonly occurring amino acid at each position. One current limitation of these methods is the limited sample of sequences with which to build up the multiple alignment; experimentally-determined sequences account for only a fraction of the total sequence space available to a given protein fold. By thinking of a protein as being made up of amino acids drawn from classes with particular physical properties we can leverage the physicochemical similarities of amino acids to help make up for this lack of statistics in our sampling of sequence space. This problem of undersampling was recognized by Sjölander *et al.* [44] who developed a method of Dirichlet mixtures for use with

multiple alignments to improve detection of remote homologs. The method of Dirichlet mixtures estimates the most likely expected distribution of amino acids at a given position in a multiple alignment and could be extended to estimate the most likely expected distribution of *classes* of amino acids, as studied here, instead of individual amino acids.

Applying the idea of searching for classes of amino acids was applied successfully by Bork *et al.* [47] to correctly predict in 1992 that MreB, FtsA and ParM would adopt the same ATPase fold as actin, nearly 10 years before any of those three proteins were crystallized. Bork *et al.* used a previously described "property pattern" approach [48] to build up a profile of 5 motifs from actin, HSP70 and sugar kinase sequences and were then able to sensitively identify structural homologs by searching for matches against those conserved motifs. A reduced alphabet approach to building up protein profiles may improve our ability to detect proteins with structural homology by leveraging our knowledge of the chemical properties of the amino acids in building up a physical picture of a fold.

V.   ACKNOWLEDGEMENTS

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