Saliency assessment of topological features extracted from the temporal region for Alzheimer's disease characterization

Philip Hartout November 25, 2020

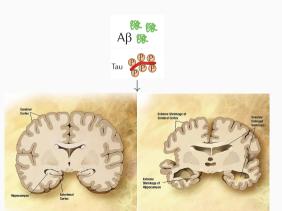
Alzheimer's disease:



- Nearly 40 million people live with AD
- Cost in US alone \$ 2 trillion by 2030
- Among leading causes of death in EU

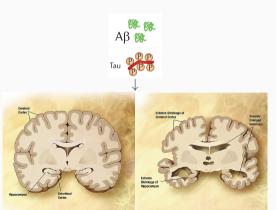
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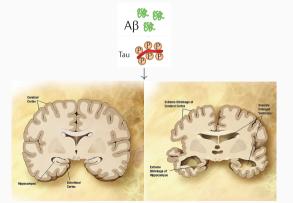
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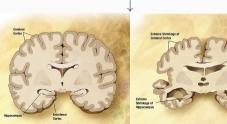
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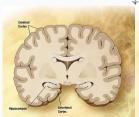


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- Concerned with "properties of a geometric object that are preserved under continuous deformations, such as [...] crumpling."
- Recently, persistent homology has emerged to quantify (differences in) the shape of data.
- How can we apply persistent homology to quantify changes in shape due to Alzheimer's disease?

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1. Classification

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- 2. Subtype identification

Topology in AD - Research Avenues @

- 1. Classification
- 2. Subtype identification
- 3. Progression & forecasting

Raw T1-weighted sMRI







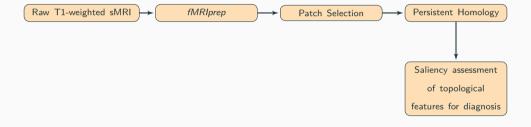




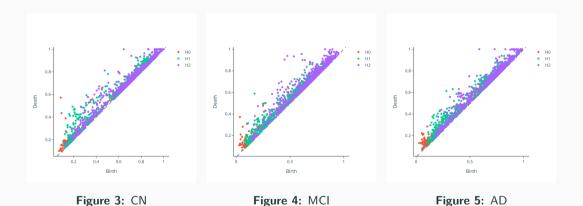
Figure 2: AUCPRC on each patch, achieved using a model described in earlier work. Chosen patch for analyses is boxed in red (patch with highest accuracy).

Computed the cubical filtration to obtain persistence image for each patch

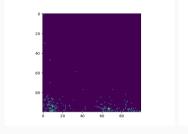
- Computed the cubical filtration to obtain persistence image for each patch
- Simple CNN to classify AD/CN patients.

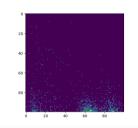
- Computed the cubical filtration to obtain persistence image for each patch
- Simple CNN to classify AD/CN patients.
- Use same partition as NeurIPS submission, train ANN 3 times on each partition

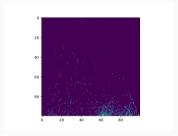
I - Persistent homology



I - Diagnosis prediction - Persistence Images







I - Diagnosis prediction - Persistence Images

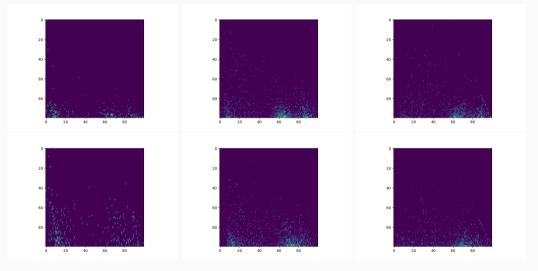
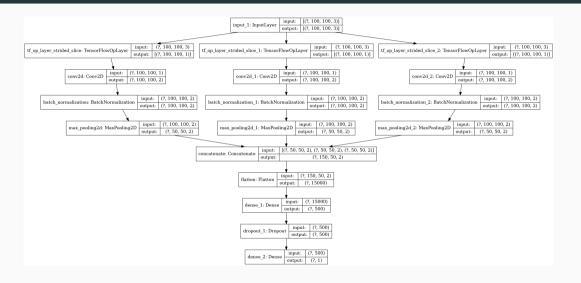


Figure 6: Columns: hom. dimension (0,1,2); Row: Diagnostic category (CN top, AD bottom).

I - Diagnosis prediction - Network architecture



I - Diagnosis prediction - Performance

Performance metric	DL model trained on PIs
Training accuracy	0.83 ± 0.01
Validation accuracy	0.79 ± 0.02
Precision	0.81 ± 0.04
Recall	0.81 ± 0.02
AUC	0.85 ± 0.03

 $\textbf{Table 1:} \ \ \mathsf{Performance} \ \ \mathsf{metrics} \ \ \mathsf{of} \ \ \mathsf{the} \ \ \mathsf{deep} \ \ \mathsf{learning} \ \ \mathsf{model}.$

I - Diagnosis prediction - Performance

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Table 1: Performance metrics of the deep learning model.

 \rightarrow using a normal CPU, training takes <5 minutes!

 Performance can be enhanced by taking local features from other patches and passing them through convolutions. Especially useful when dealing with subtypes of Alzheimer's which show atrophy in other brain regions.

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- Neural architecture could be made more complex to capture more complex features of the persistence images
- Can persistence images be used to diagnose prodromal forms of AD?
- Use other representations for prediction.
- Use topology-based embeddings for subtype identification?

Summary

GitHub repository of the project

github.com/pjhartout/TDA_ADNI_MLCB

With thanks to Bastian Rieck for the supervision and Sarah Brueningk, Felix Hensel, Catherine Jutzeler, Merel Kuijs and Louis Lukas for insightful discussions, code, and data.



II - Distance analysis among patients in CN, MCI & AD

Median persistence landscape.

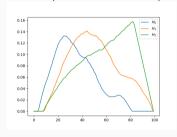


Figure 7: CN

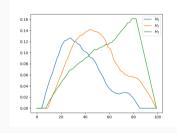


Figure 8: MCI

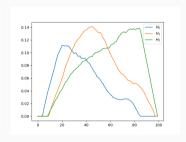


Figure 9: AD

II - Distance analysis among patients in CN, MCI & AD

Question: How topologically heterogenous is the data?

	Mean	Median	Standard deviation	Q3	Max	Skewness
CN H ₀	2.16	2.00	0.78	2.50	7.41	1.78
$CN H_1$	2.61	2.27	1.17	2.93	9.47	1.92
$CN H_2$	2.38	2.23	0.88	2.79	7.19	1.39
$MCIH_0$	2.24	2.04	0.82	2.55	6.21	1.71
$MCIH_1$	2.57	2.19	1.29	2.80	11.87	2.57
$MCIH_2$	2.40	2.27	0.83	2.82	6.55	1.18
AD H_0	2.40	2.18	0.96	2.77	7.77	1.97
AD H_1	2.47	2.13	1.15	2.77	9.28	2.10
AD H ₂	2.36	2.20	0.80	2.75	8.39	1.64

Table 2: Summary statistics of the distribution of distances

Question: Among the patients who deteriorate, do we see higher average pairwise distances compared to patients who don't deteriorate?

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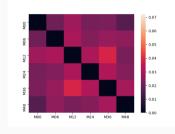
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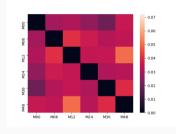
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- The data is a longitudinal dataset (multiple timepoints are available for each patient)
- Some patients deteriorate (transition from CN→MCI or from MCI→AD)
- Compute pairwise distance between patients (L^1 PL distance, Wasserstein distance and bottleneck distance), and average for each patient.

Example of L^1 norm between PLs of a deteriorating patient.





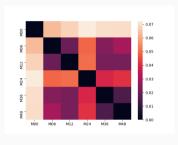
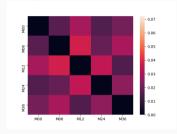


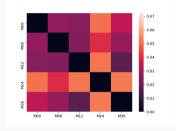
Figure 10: H_0

Figure 11: H_1

Figure 12: H_2

Example of L^1 norm between PLs of a subject who does *not* deteriorate.





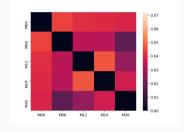
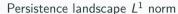


Figure 13: H_0

Figure 14: H_1

Figure 15: H_2



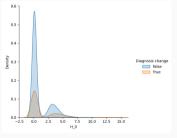


Figure 16: H_0

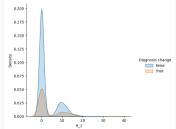


Figure 17: H_1

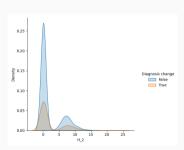


Figure 18: H_2

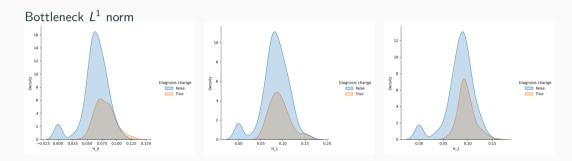
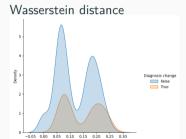
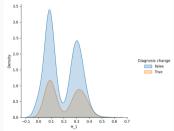


Figure 20: H_1

Figure 19: H_0

Figure 21: H_2





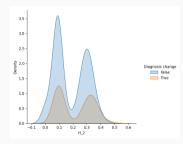


Figure 22: H_0

Figure 23: H_1

Figure 24: H_2