Systems and Networking – Unit I

B.Sc. in Applied Computer Science and Artificial Intelligence 2021-2022

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Recap from Last Lecture

- Synchronization **primitives**:
 - Locks
 - Semaphores
 - Monitors

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- Synchronization **primitives**:
 - Locks
 - Semaphores
 - Monitors
- 2 fundamental synchronization problems:
 - Producers-Consumers
 - Readers-Writers

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- 5 philosophers sitting at a round table

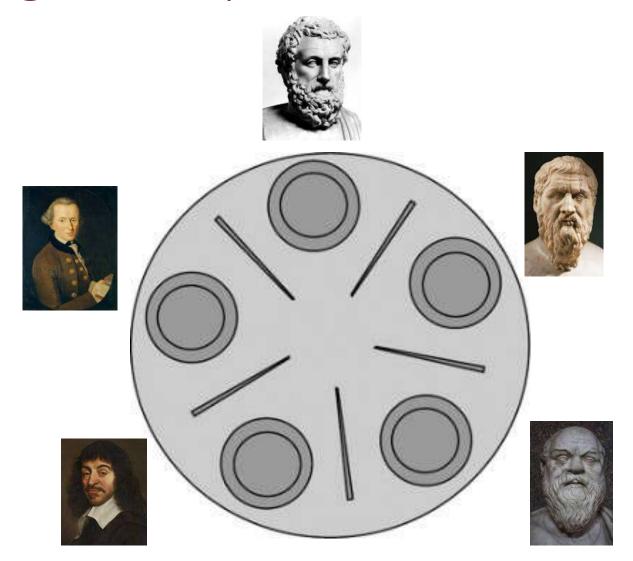
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- 5 philosophers sitting at a round table
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- 2 things philosophers are good at ②:
 - Eating
 - Thinking

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 - Block if a neighbour has already picked up a chopstick
- After eating, put down both chopsticks and go back thinking!





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We still want some concurrency here ©

The Dining Philosophers: Solution 1

```
Semaphore chopsticks[5];
while(True) {
   chopsticks[i].wait(); // wait on the left chopstick
   chopsticks[(i+1)%5].wait(); // wait on the right chopstick
   eat();
   chopsticks[i].signal(); // signal on the left chopstick
   chopsticks[(i+1)%5].signal(); // signal on the right chopstick
   think();
```

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   think();
```

Is this solution correct?

No! Possible deadlock if all philosophers take the left chopstick

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<u>Idea:</u> Before picking one chopstick be sure also the second one is available, otherwise wait for the neighbour to finish

Testing if either one of the two neighbours of a given philosopher is currently eating (condition variables)

Never gonna pick a single chopstick!

```
class Philosopher {
    enum Status {
        THINKING,
        HUNGRY,
        EATING
    }
    Status state;

    public Philosopher() {
        this.state = THINKING;
    }
}
```

```
void canEat(int i) {
    State state = this.philosophers[i].state;
    State left = this.philosophers[[(i-1)%5].state;
    State right = this.philosophers[[(i+1)%5].state;
    if(left != EATING && right != EATING && state == HUNGRY) {
        this.philosophers[i].state = EATING;
        this.philosophers[i].notify();
    }
}
```

```
class DiningPhilosophers {
    Philosopher[5] philosophers;

public DiningPhilosopers() {
    for(int i=0; i < 5; ++i) {
        this.philosophers[i] = new Philosopher();
    }
}
// continue implementation ----->
```

```
void synchronized pickup(int i) {
    this.philosophers[i].state = HUNGRY;
    canEat(i);
    if(this.philosophers[i].state != EATING) {
        this.philosophers[i].wait();
    }
}
```

```
void synchronized putdown(int i) {
    this.philosophers[i].state = THINKING;
    canEat((i - 1) % 5); // left neighbour
    canEat((i + 1) % 5); // right neighbour
}
```

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 - Banking system: read vs. update account balances

- The problems we have seen so far are interesting because they identify some patterns which are very common in practice
 - Producer-Consumer
 - Audio/Video player embedded in a web browser: shared data buffer + network and render threads
 - Reader-Writer
 - Banking system: read vs. update account balances
 - Dining Philosophers
 - Lock on multiple resources: e.g., travel reservation (hotel, airline, car rental databases)

Our Journey

- What is deadlock?
- Conditions for deadlock to happen
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"When two trains approach each other at a crossing, both shall come to a full stop and neither shall start up again until the other has gone."

Kansas legislation early 1900's

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```
Thread A

printer.wait();

disk.wait();

// copy from disk to printer

printer.signal();

disk.signal();
```

```
Thread B

disk.wait();
printer.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

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printer.signal();

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disk.wait();
printer.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

```
Thread A

printer.warcquires printer and context switch disk.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

```
Thread B

    disk.wait();
    printer.wait();

// copy from disk to printer
    printer.signal();
    disk.signal();
```

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

```
Thread A

printer.wait();

disk.wait();

// copy from disk to printer

printer.signal();

disk.signal();
```

```
Thread B

B takes over

disk.wait();

printer.wait();

// copy from disk to printer

printer.signal();

disk.signal();
```

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

```
Thread A

printer.wait();
disk.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

```
Thread B

disk.wafequires disk and context switch
printer.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

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Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

```
Thread A

printer.waiAteXecutes again and blocks
    disk.wait();

// copy from disk to printer

printer.signal();
    disk.signal();
```

```
Thread B

    disk.wait();
    printer.wait();

// copy from disk to printer

    printer.signal();
    disk.signal();
```

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printer.wait();

disk.wait();

// copy from disk to printer

printer.signal();

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Thread B

disk.walt();

// copy from disk to printer

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printer.wait();

// copy from disk to printer

printer.signal();
disk.signal();
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A waits B to release the disk

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

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printer.signal();

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```

```
Thread B

    disk.wait();
    printer.wait();

// copy from disk to printer

    printer.signal();
    disk.signal();
```

B waits A to release the printer

• Deadlock: it can occur when multiple threads compete for a finite number of resources

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- Deadlock detection: finds instances of deadlocks and tries to recover
- Deadlock prevention (offline): imposes restrictions/rules on how to write deadlock-free programs
- Deadlock avoidance (online): runtime support checks resource requests made by threads to avoid deadlocks

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- Related terms but each one refers to a specific situation
- Starvation occurs when a thread waits indefinitely for some resource but other threads are actually making progress using that resource
- The main difference with deadlock is that the system is not completely stuck!

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- What is deadlock?
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 - Circular Wait \rightarrow a set of waiting threads t_1, \ldots, t_n where t_i is waiting on $t_{(i+1)\%n}$

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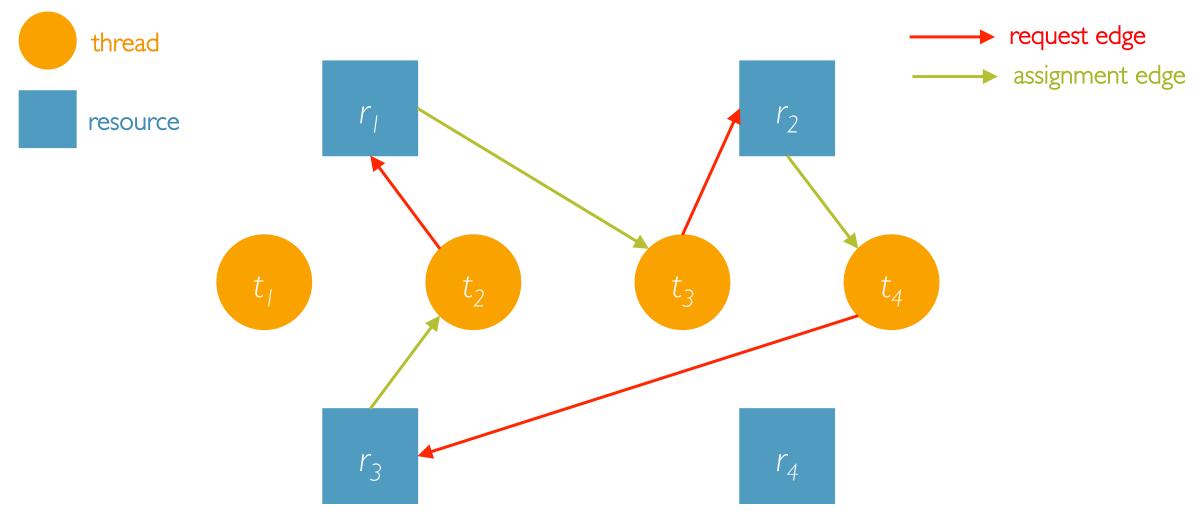
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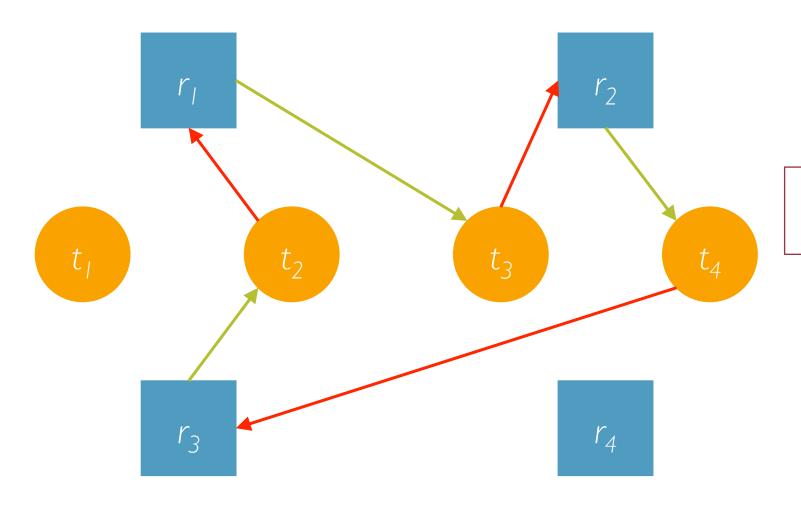
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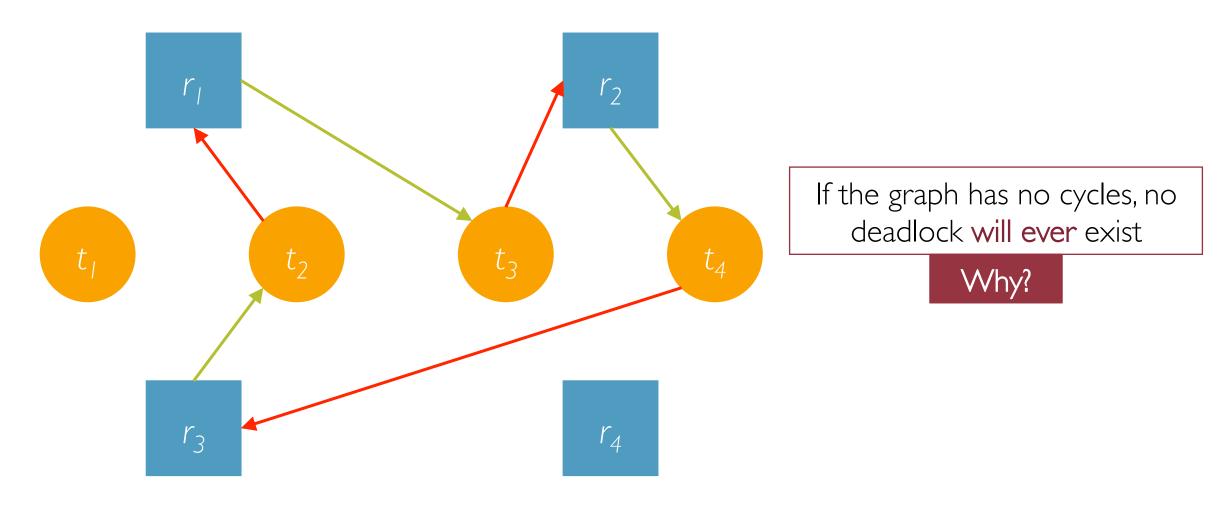
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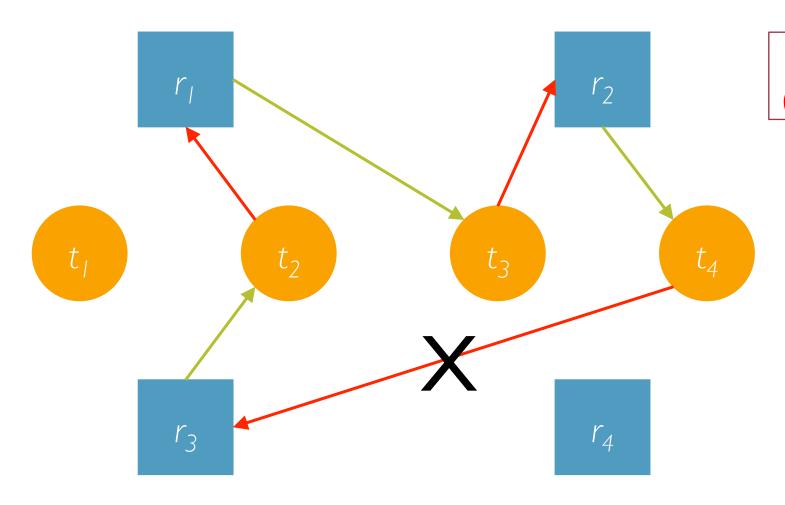


If the graph has no cycles, no deadlock will ever exist

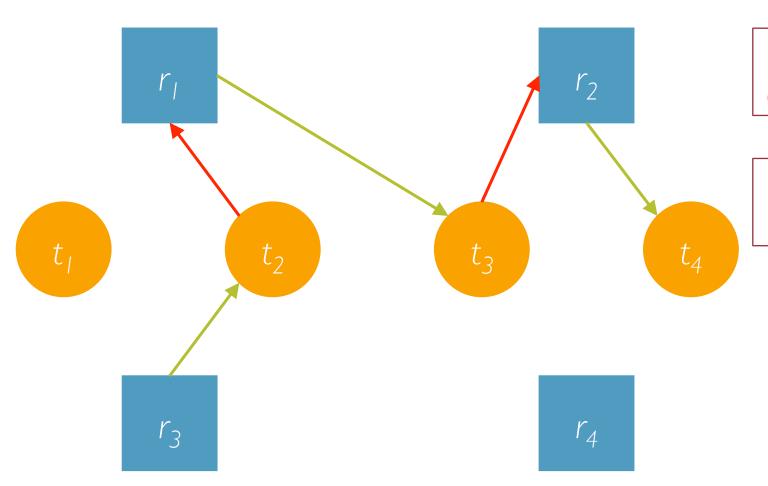
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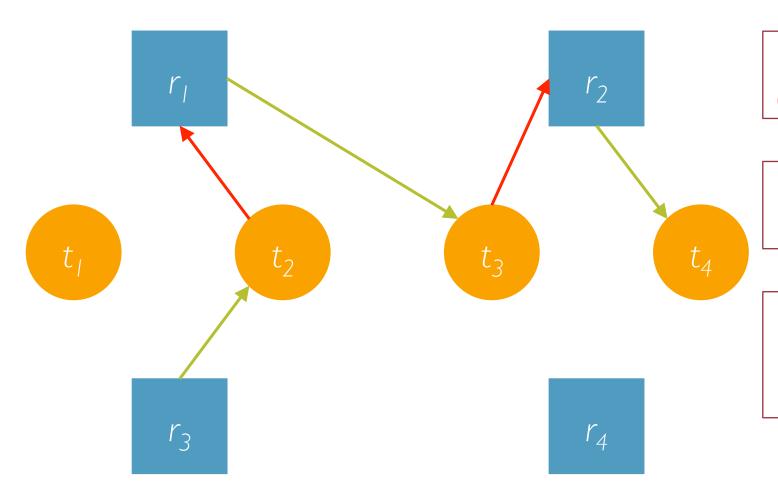


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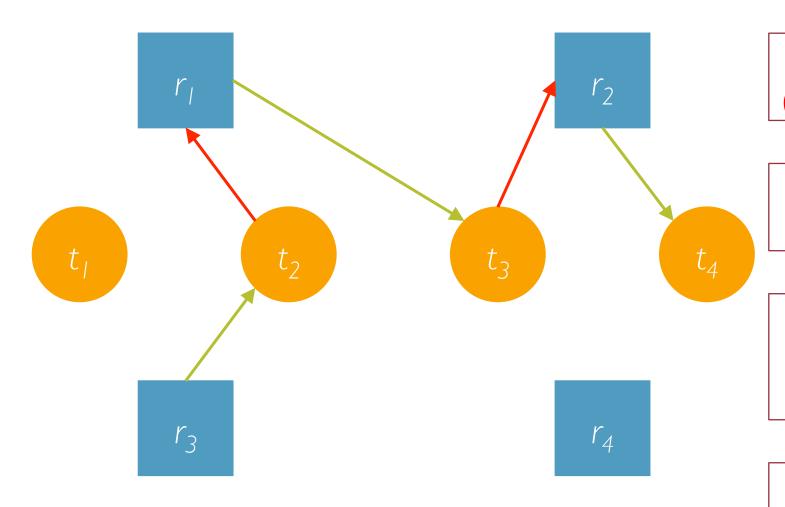
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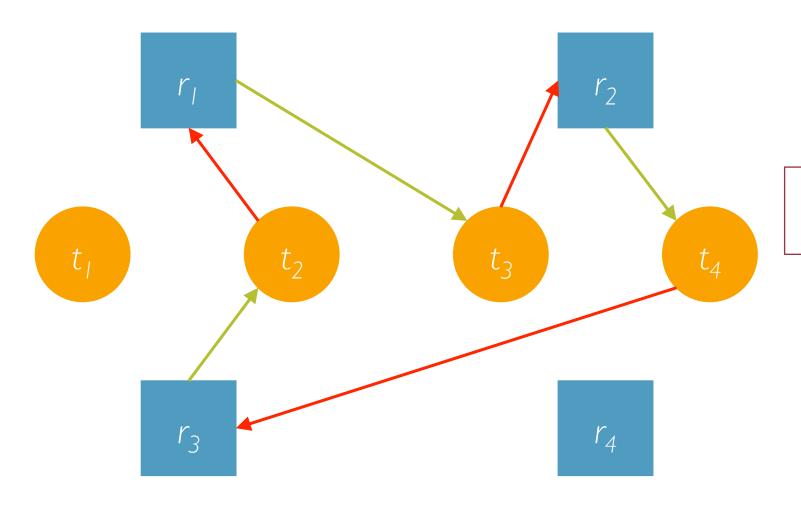


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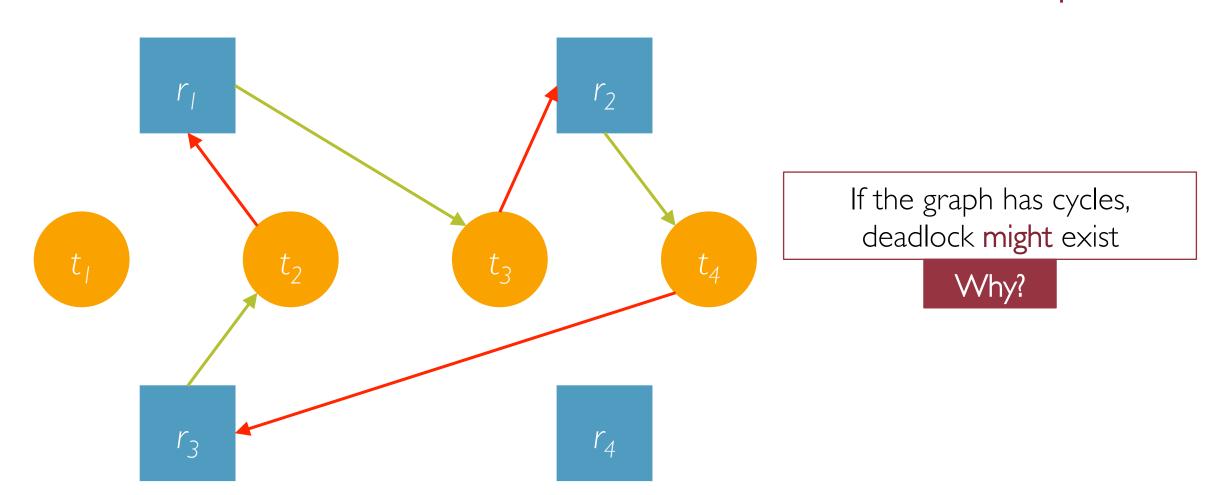
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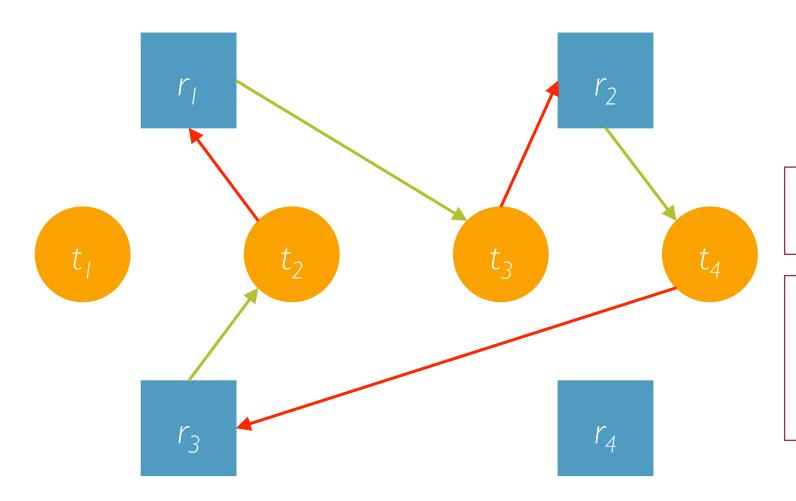
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And so on and so forth...



If the graph has cycles, deadlock might exist

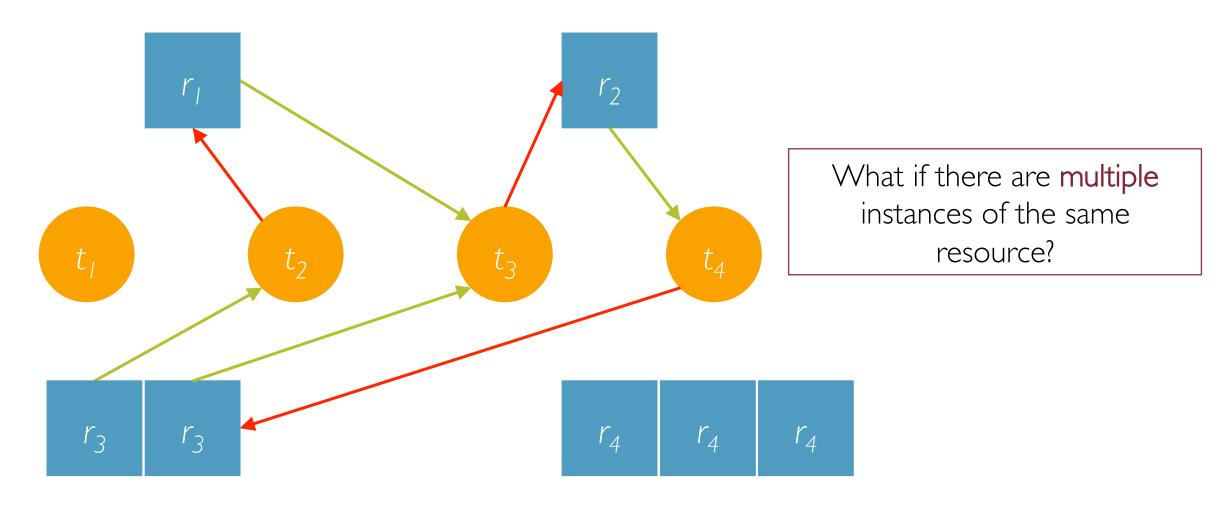




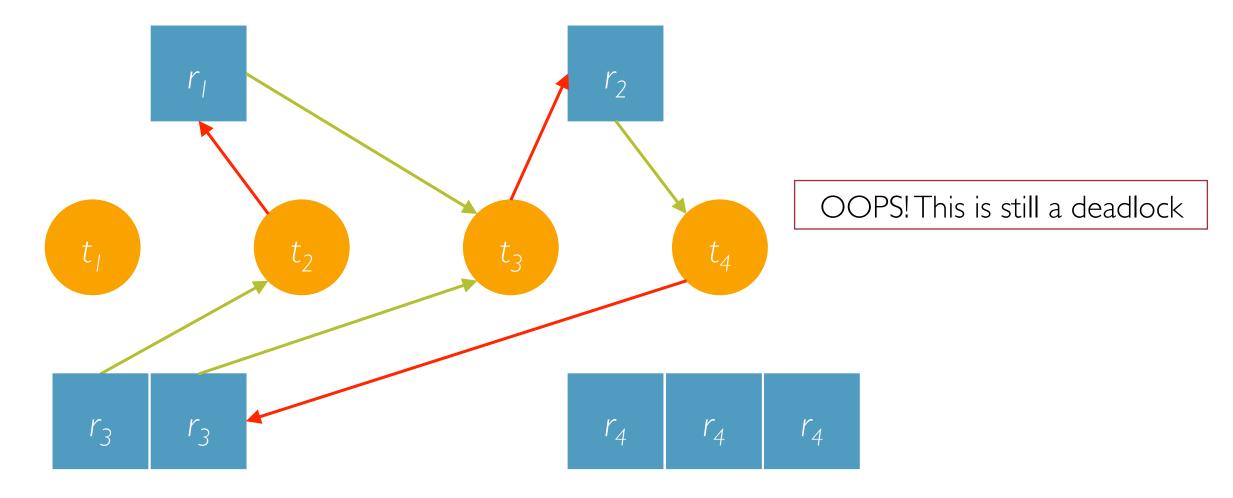
If the graph has cycles, deadlock might exist

We are implicitly assuming the multiplicity of each resource is I (i.e., we have one r_1 , one r_2 , etc.)

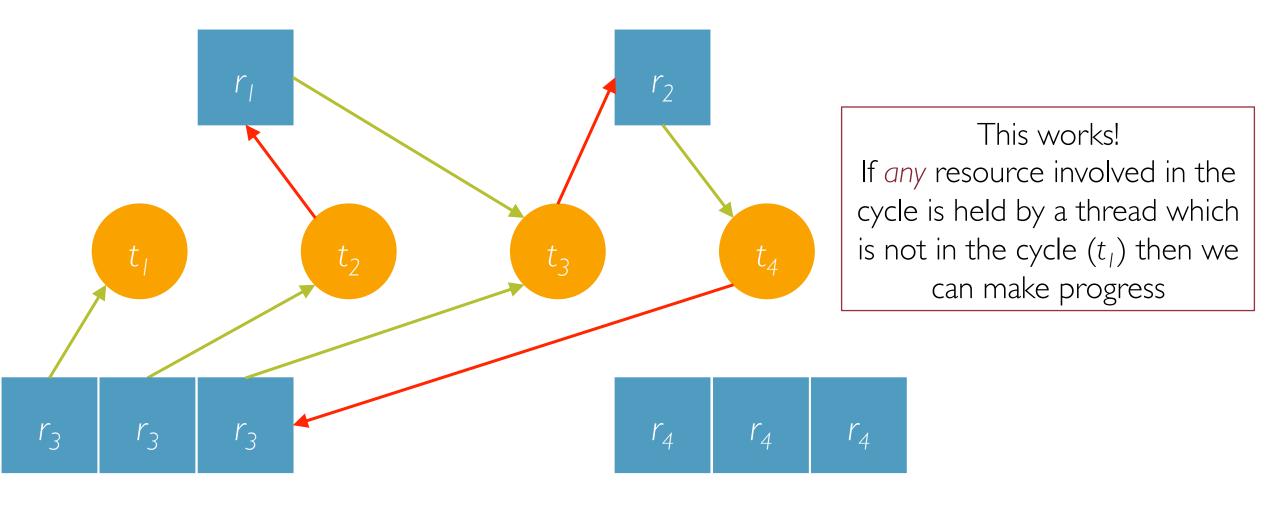
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- How? Several ways of doing it:
 - Kill all the threads in the cycle (quite harsh, ugh?)
 - Kill all the threads one at a time, forcing each one of them to release resource(s)
 - Preempt resources one at a time rolling back to a consistent status (e.g., common in database transactions)

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- We would like to be more precise than that...

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- When to run such a detection algorithm?
 - Before granting a resource \rightarrow each granted request will take $O(|V|^2)$
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- What do modern OSs do? Nothing! They leave it to the programmer!

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 - <u>Problem:</u> not all resources can be easily preempted (e.g., printers)

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 - <u>Problem:</u> not all resources can be easily preempted (e.g., printers)
 - Circular Wait → impose an ordering (i.e., numbering) on resources and enforce to request them in such order

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Deadlock Avoidance: Resource Reservation

Each thread provides information about the maximum number of resources it might need during execution

> $m_i = maximum$ number of resources that thread i might request $c_i = current$ number of resources that thread i is holding $C = \sum_{i=1}^{\infty} c_i = total$ number of resources currently allocated R = maximum number of resources overall available

Any thread sequence is **safe** if for each thread it holds that:

$$\underbrace{m_i - c_i}_{\text{resources } t_i \text{ might still request}} \leq \underbrace{R - C}_{\text{resources currently available}} + \underbrace{\sum_{j=1}^{i} c_j}_{\text{resources currently allocated up to } t_i, j < i}$$

Deadlock Avoidance: Safe State

- A state in which there is a safe sequence for the threads
- An unsafe state does not necessarily mean deadlock (i.e., some threads may not request the maximum number of resources as declared)
- Grant a resource to a thread if the new state is safe, otherwise make it wait even if the resource is available
- This policy ensures no circular-wait condition exists

- 3 threads: t₁, t₂, and t₃ are competing for 12 tape drives (resources)
- Currently, II drives are allocated to the threads, leaving I available

Thread	m _i	C _i	m _i — c _i
t _I	4	3	I
t_2	8	4	4
t_3	12	4	8

Is the current state safe?

Thread	m _i	c _i	$m_i - c_i$
t _I	4	3	
t_2	8	4	4
t_3	12	4	8

The current state is safe in that there exists a sequence of threads (t_1, t_2, t_3) where each one will get the maximum number of resources without waiting

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t₂ can use the current allocation, plus t₁'s resources and 1 drive left (4 drives)

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t₁ can complete using the current allocation and the I drive left

t₂ can use the current allocation, plus t₁'s resources and 1 drive left (4 drives)

t₃ can use the current allocation, plus t₁'s & t₂'s resources and 1 drive left (8 drives)

Thread	m _i	c _i	$m_i - c_i$
t _I	4	3	I
t_2	8	4	4
t_3	12	5	7

Suppose t₃ requests one more drive, then now there are no more available drives

Theoretically, everything might still work (e.g., t₁ may never request another drive)

However, t₃ must wait because allocating that extra drive would lead to an unsafe state, which in turn might lead to deadlock

• An extension of the original definition of resource allocation graph

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- Edges can now be of 3 types:
 - Request Edge \rightarrow a directed edge (t_i, r_j) indicates that t_i has requested r_j , but not yet acquired
 - Claim (dotted) Edge \rightarrow a directed edge (t_i, r_j) indicates that t_i might request r_j in the future
 - Assignment Edge \rightarrow a directed edge (r_j, t_i) indicates that the OS has allocated r_j to t_i

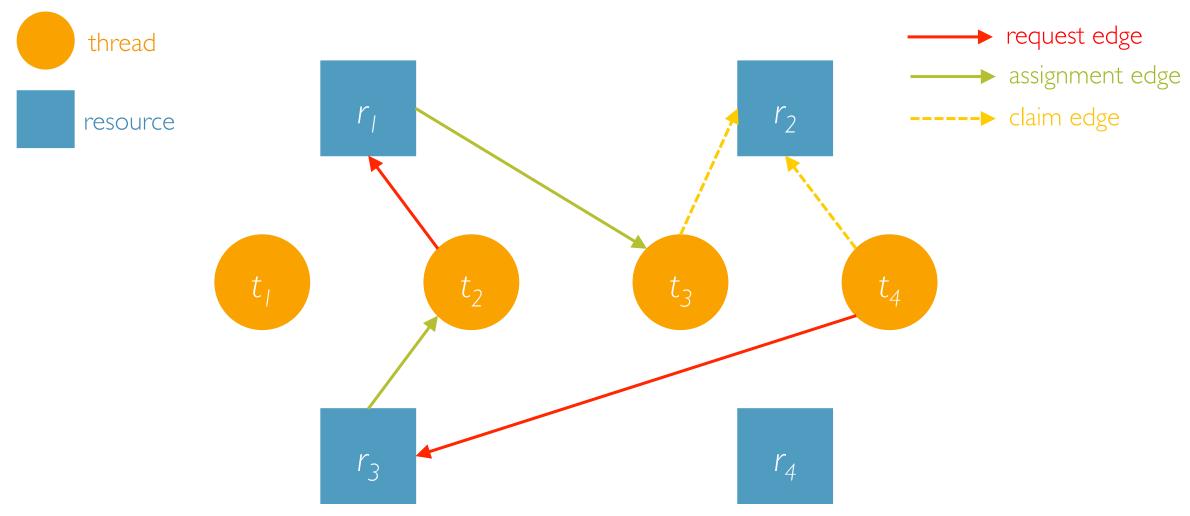
- An extension of the original definition of resource allocation graph
- Edges can now be of 3 types:
 - Request Edge \rightarrow a directed edge (t_i, r_j) indicates that t_i has requested r_j , but not yet acquired
 - Claim (dotted) Edge \rightarrow a directed edge (t_i, r_j) indicates that t_i might request r_j in the future
 - Assignment Edge \rightarrow a directed edge (r_j, t_i) indicates that the OS has allocated r_j to t_i
- Satisfying a request means converting a claim into an assignment edge

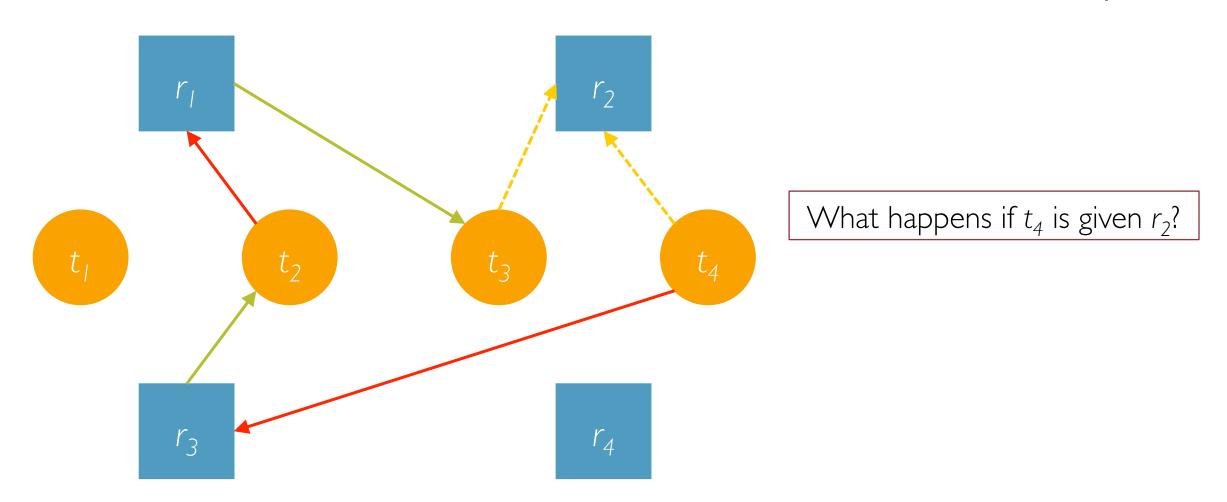
• A cycle in this extended RAG indicates an unsafe state

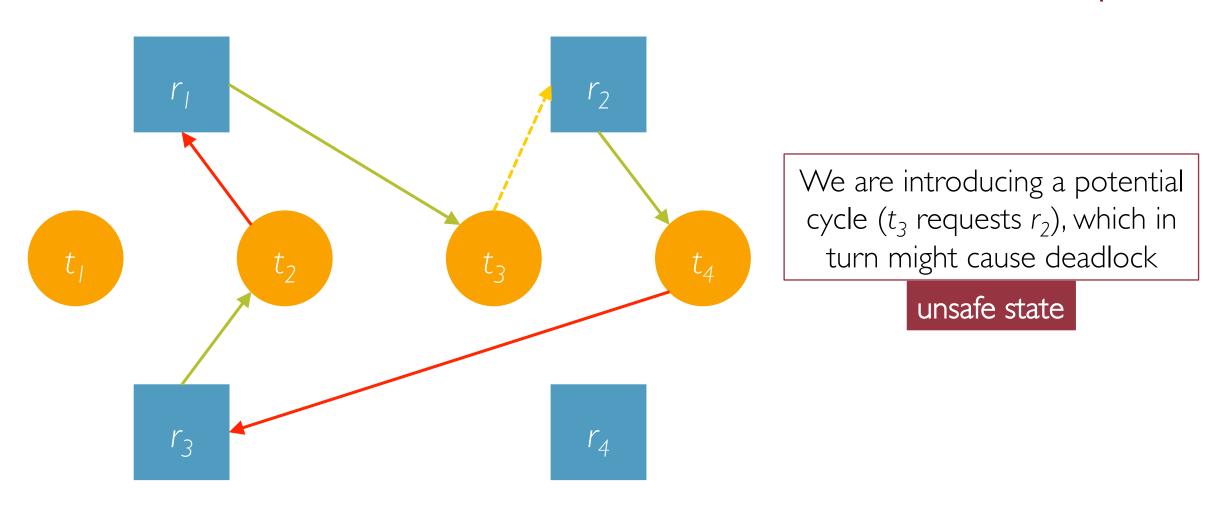
- A cycle in this extended RAG indicates an unsafe state
- If the allocation results in an unsafe state, this will be denied even if the resource is actually available

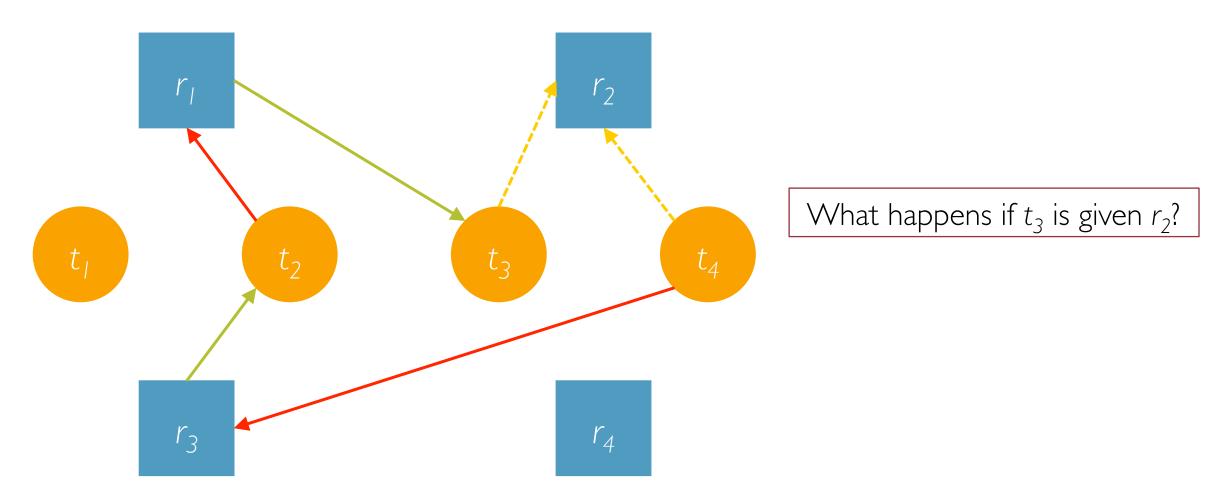
- A cycle in this extended RAG indicates an unsafe state
- If the allocation results in an unsafe state, this will be denied even if the resource is actually available
- In other words, the claim edge is converted into a request edge and the thread will wait

- A cycle in this extended RAG indicates an unsafe state
- If the allocation results in an unsafe state, this will be denied even if the resource is actually available
- In other words, the claim edge is converted into a request edge and the thread will wait
- <u>NOTE:</u> This solution does not work when there are multiple instances of the <u>same</u> resource

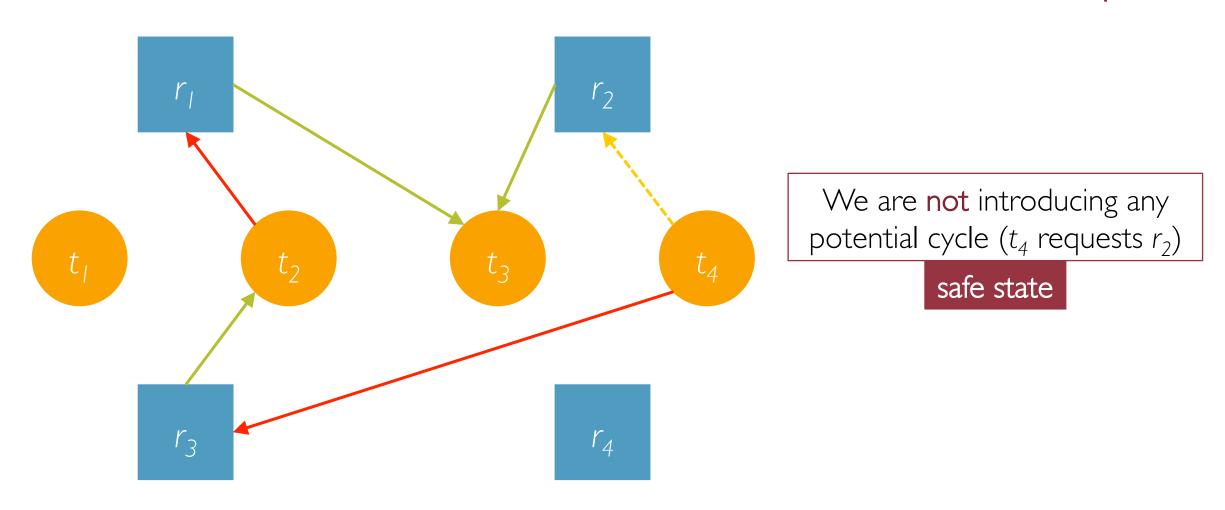




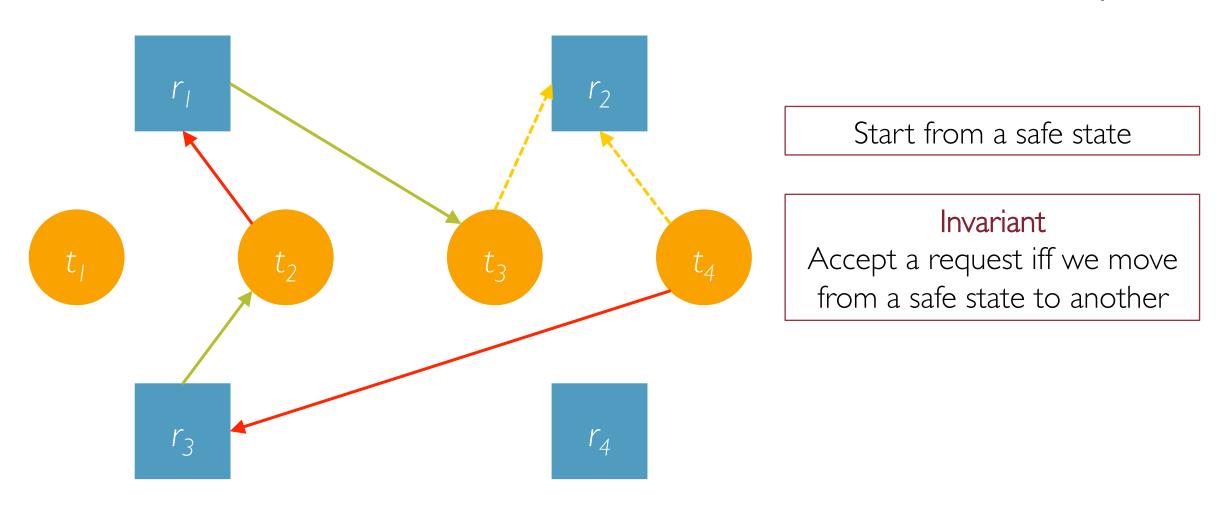




Deadlock Avoidance: Resource Allocation Graph



Deadlock Avoidance: Resource Allocation Graph



Banker's Algorithm

- Handles multiple instances of the same resource
- Forces threads to provide information on what resource they might need, in advance
- The resources requested must not exceed the total available in the system
- The algorithm allocates resources to a requesting thread if the allocation leaves the system in a safe state, otherwise the thread waits

Banker's Algorithm: Data Structures

- n = number of threads; m = number of resource types
- available [1..m]: m-dimensional vector
 - available [j] = k means there are k resources of type j available
- max[1..n, 1..m]:n x m matrix
 - max[i, j] = k means thread i may require at most k resources of type j
- allocation[1..n, 1..m]:nxm matrix
 - allocation[i, j] = k means thread i has allocated k resources of type j
- need [1...n, 1...m]: n x m matrix
 - need[i, j] = max[i, j] allocation[i, j] = k means thread i may need k
 more resources of type j to complete its task

Banker's Algorithm: Idea

- The algorithm is divided in 2 tasks:

 - resourceRequest → given a thread and its resource request decides if such a request can be satisfied

Banker's Algorithm: Idea

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 - isSafeState \rightarrow given the current status of allocation of resources, tests if this is a safe state
 - resourceRequest → given a thread and its resource request decides if such a request can be satisfied
- A request can be satisfied iff this leads to a safe state!

Banker's Algorithm: Idea

- The algorithm is divided in 2 tasks:
 - isSafeState \rightarrow given the current status of allocation of resources, tests if this is a safe state
 - resourceRequest → given a thread and its resource request decides if such a request can be satisfied
- A request can be satisfied iff this leads to a safe state!
- In other words, the second tasks uses the output of the first one in order to make a decision

Banker's Algorithm: isSafeState

- I. Let work and finish be vectors of length m and n, respectively Initialize: work = available; finish[i] = false; for all i
- 2. Find an i such that:

```
finish[i] = false && need[i] ≤ work

If no such i exists, go to step 4.
```

3. Assume thread i executes:

```
work = work + allocation[i]; finish[i] = true; go to step 2.
```

4. If finish[i] == true for all i, the system is in a safe state

Banker's Algorithm: requestResource

Input: i (thread) and request an m-dimensional vector of requests

- I. If request > need[i] raise an error as thread i is attempting to request more resources that it claimed, otherwise go to step 2.
- If request > available thread i must wait since resources are not available, otherwise go to step 3.
- 3. Even if resources are available, test if this allocation will lead to a safe state by simulating it

```
available -= request; allocation[i] += request; need[i] -= request;
isSafeState() ? OK : rollback() and wait()
```

A snapshot of the current state of the system

					RES	SOUR	CES			
			MAX		ALL	OCATI	ON	A۱	VAILAB	LE
		Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0		0	0				
R	T _I	-	7	5		0	0			
E A	T ₂	2	3	5		3	5			
D S	T ₃	0	6	5	0	6	3			
	Total				2	9	9	1	5	2

QI: How many resources of type A, B, and C are there overall?

					RES	SOUR	CES			
			MAX		ALL	OCATI	ON	A۱	VAILAB	LE
		Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0		0	0				
R	T ₁	1	7	5		0	0			
E A	T ₂	2	3	5		3	5			
D S	T ₃	0	6	5	0	6	3			
	Total				2	9	9	1	5	2

QI: How many resources of type A, B, and C are there overall?

					RES	SOUR	CES			
			MAX		ALL	OCATI	ON	A\	VAILAB	LE
		Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	1	0	0	- 1			
R	T ₁	I	7	5		0	0			
E A	T ₂	2	3	5		3	5			
D S	T ₃	0	6	5	0	6	3			
	Total				2	9	9		5	2

$$A = 2 + 1 = 3$$

 $B = 9 + 5 = 14$
 $C = 9 + 2 = 11$

Q2: What is the content of the NEED matrix?

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	0	0	I						
R	T ₁		7	5		0	0						
E A	T ₂	2	3	5		3	5						
D S	T ₃	0	6	5	0	6	3						
	Total				2	9	9	I	5	2			

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

					RES	SOUR	CES						
			MAX		ALL	OCAT	ON	A	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0		0	0							
R	T ₁	I	7	5		0	0						
E A	T ₂	2	3	5		3	5						
D S	T ₃	0	6	5	0	6	3						
	Total				2	9	9	I	5	2			

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0	l	0	0					0-0 = 0		
R	T ₁	I	7	5		0	0						
E A	T ₂	2	3	5		3	5						
D S	T ₃	0	6	5	0	6	3						
	Total				2	9	9	I	5	2			

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

					RE:	SOUR	CES						
			MAX		ALL	LOCATI	ON	A'	VAILAB	LE		NEED	
		Α	A B C 0 1			В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	0	0	I				0	0-0 = 0	
R	T _I	I	7	5	I	0	0						
E A	T ₂	2	3	5		3	5						
D S	T ₃	0	6	5	0	6	3						
	Total				2	9	9	I	5	2			

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0	1	0	0	1				0	0	I-I = 0
R	T ₁	I	7	5		0	0						
E A	T ₂	2	3	5		3	5						
D S	T ₃	0	6	5	0	6	3						
	Total				2	9	9	I	5	2			

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0	I	0	0	I				0	0	0
R	T ₁		7	5		0	0				0	7	5
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Q3: Is the system in a safe state? Why?

					RES	SOUR	CES						
			MAX		ALL	OCATI	ON	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	0	0					0	0	0
R	T ₁	- 1	7	5		0	0				0	7	5
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	- 1	5	2			

Let's start with T₀

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0	I	0	0	I				0	0	0
R	T ₁	I	7	5		0	0				0	7	5
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Eventually, To finishes and releases all its resources

					RES	SOUR	CES						
			MAX		ALL	OCAT	ON	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	0	0	I				0	0	0
R	T ₁	I	7	5		0	0				0	7	5
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

 T_1 can't execute as it still might NEED (0, 7, 5) and AVAILABLE = (1, 5, 3)

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	-	-	-				-	-	-
R	T_l	I	7	5	I	0	0				0	7	5
E A	T ₂	2	3	5	l	3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	8	1	5	3			

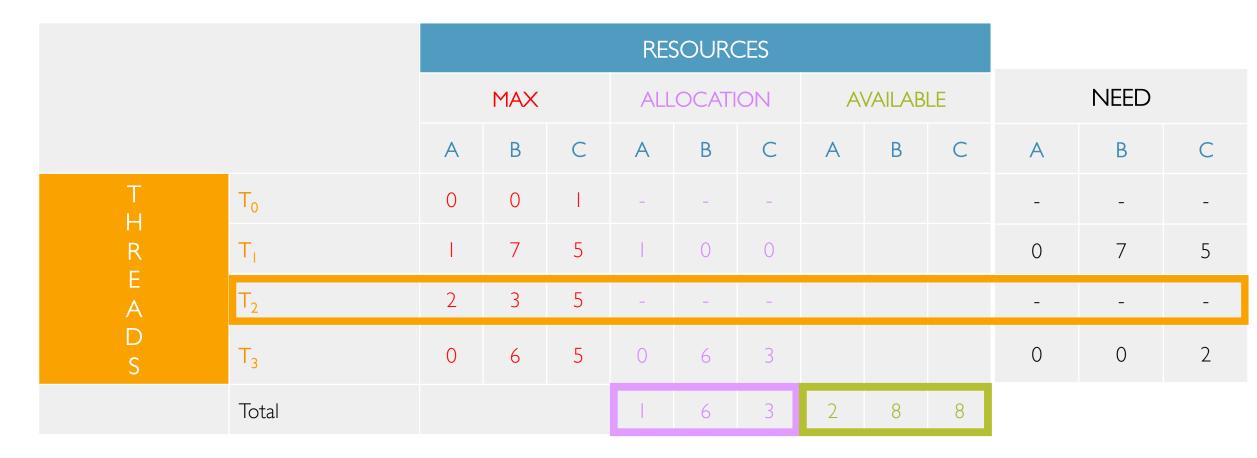
 T_2 can execute as it still might NEED (1,0,0) and AVAILABLE = (1,5,3)

					RES	SOUR	CES						
			MAX		ALL	LOCATI	ON	A	VAILAB	LE		NEED	
		A	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0	I	_	-	-				-	-	-
R	T ₁	1	7	5		0	0				0	7	5
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	8	1	5	3			

 T_2 can execute as it still might NEED (1,0,0) and AVAILABLE = (1,5,3)

					RES	SOUR	CES						
			MAX		ALL	.OCATI	ON	A	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	-	-	-				-	-	_
R	T _I	I	7	5	I	0	0				0	7	5
E A	T ₂	2	3	5	2	3	5				0	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				3	9	8	0	5	3			

T₂ eventually finishes and releases all its resources



 T_3 can execute as it still might NEED (0, 0, 2) and AVAILABLE = (2, 8, 8)

					RES	SOUR	CES						
			MAX		ALL	OCATI	ON	A'	VAILAB	LE		NEED	
		A	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	_	_	_				-	-	-
R	T _I	1	7	5		0	0				0	7	5
E A	T ₂	2	3	5	-	-	-				-	-	-
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total					6	3	2	8	8			

 T_3 can execute as it still might NEED (0, 0, 2) and AVAILABLE = (2, 3, 6)

					RES	SOURC	CES						
			MAX		ALL	LOCATI	ON	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0	I	-	-	_				-	-	-
R	T ₁	1	7	5		0	0				0	7	5
E A	T ₂	2	3	5	-	-	-				-	-	-
D S	T ₃	0	6	5	0	6	5				0	0	0
	Total				I	6	5	2	8	6			

T₃ eventually finishes and releases all its resources

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	-	-	-				-	-	-
R	T ₁	I	7	5	- 1	0	0				0	7	5
E A	T ₂	2	3	5	-	-	-				-	-	-
D S	T ₃	0	6	5	-	-	-				-	-	-
	Total				- 1	0	0	2	14	11			

 T_1 can now execute since NEED (0, 7, 5) and AVAILABLE = (2, 14, 11)

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0	I	-	-	-				-	-	-
R	T ₁	I	7	5	I	7	5				0	0	0
E A	T ₂	2	3	5	-	-	-				-	-	-
D S	T ₃	0	6	5	-	-	-				-	-	-
	Total					7	5	2	7	6			

We have found a sequence of execution T_0 , T_2 , T_3 , T_1 which leads to safe state!

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0		_	-	-				-	-	-
R	T ₁		7	5	_	-	-				-	-	-
E A	T ₂	2	3	5	-	-	-				-	-	-
D S	T ₃	0	6	5	_	_	_				-	-	-
	Total				-	-	-	3	14	11			

Q4: If T₁ issues a REQUEST (0, 5, 2), can this be granted immediately?

					RES	SOUR	CES						
			MAX		ALL	OCATI	ON	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0	I	0	0					0	0	0
R	T ₁		7	5		0	0				0	7	5
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

We have to ask ourselves: I. if the request can be satisfied; 2. if it will lead to a safe state

					RES	SOUR	CES						
			MAX		ALL	.OCATI	ON	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	То	0	0	I	0	0					0	0	0
R	T ₁	I	7	5		0	0				0	7	5
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

To answer I. check if: a. REQUEST <= NEED and b. REQUEST <= AVAILABLE

					RES	SOUR	CES						
			MAX		ALL	OCATI	ON	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	0	0					0	0	0
R	T ₁	I	7	5		0	0				0	7	5
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	- 1	5	2			

I.a. REQUEST <= NEED?

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0	I	0	0	I				0	0	0
R	T ₁		7	5		0	0				0	7	5
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

I.a. REQUEST <= NEED?

YES! $(0, 5, 2) \le (0, 7, 5)$

	RESOURCES												
		MAX			ALLOCATION			AVAILABLE			NEED		
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H R E A D S	T _o	0	0		0	0					0	0	0
	T ₁		7	5		0	0				0	7	5
	T ₂	2	3	5		3	5				I	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	- 1	5	2			

I.b. REQUEST <= AVAILABLE?

	RESOURCES												
		MAX			ALLOCATION			AVAILABLE			NEED		
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H R E A D S	T ₀	0	0	I	0	0					0	0	0
	T ₁	I	7	5		0	0				0	7	5
	T ₂	2	3	5		3	5				I	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	I	5	2			

I.b. REQUEST <= AVAILABLE?

YES! (0,5,2) <= (1,5,2)

					RES	SOUR	CES						
			MAX		ALL	OCATI	ON	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	То	0	0	I	0	0					0	0	0
R	T ₁	-	7	5		0	0				0	7	5
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

To answer 2. we simulate the request is granted and see if we are still in a safe state

					RES	SOUR	CES						
			MAX		ALL	OCATI	ON	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	0	0					0	0	0
R	T ₁	- 1	7	5		0	0				0	7	5
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	- 1	5	2			

To answer 2. we simulate the request is granted and see if we are still in a safe state

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	0	0	I				0	0	0
R	T ₁	I	7	5		5	2				0	2	3
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	14			0	0			

Let's start with T₀

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	0	0	I				0	0	0
R	T ₁		7	5		5	2				0	2	3
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	14	11	1	0	0			

Eventually, T₀ finishes and releases all its resources

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	-	-	-				-	-	-
R	T ₁	1	7	5	l	5	2				0	2	3
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	14	10	I	0	1			

 T_1 can't execute as it still might NEED (0, 2, 3) and AVAILABLE = (1, 0, 1)

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	A	В	С	Α	В	С
T H	T ₀	0	0	I	_	-	_				-	-	-
R	T_l	I	7	5	I	5	2				0	2	3
E A	T ₂	2	3	5		3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	14	10	1	0	- 1			

 T_2 can execute as it still might NEED (1,0,0) and AVAILABLE = (1,0,1)

					RES	SOUR	CES						
			MAX		ALL	.OCATI	ON	A'	VAILABI	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0	I	_	_	-				-	-	-
R	T ₁	1	7	5		5	2				0	2	3
E A	T ₂	2	3	5	- 1	3	5				I	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	14	10	I	0	1			

 T_2 can execute as it still might NEED (1,0,0) and AVAILABLE = (1,0,1)

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	-	-	-				-	-	-
R	T ₁	1	7	5	I	5	2				0	2	3
E A	T ₂	2	3	5	2	3	5				0	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				3	14	10	0	0	I			

T₂ eventually finishes and releases all its resources

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	-	-	-				-	-	-
R	T _I	I	7	5	-	5	2				0	2	3
E A	T ₂	2	3	5	-	-	-				-	-	-
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				-	11	5	2	3	6			

 T_3 can execute as it still might NEED (0, 0, 2) and AVAILABLE = (2, 3, 6)

					RES	SOUR	CES						
			MAX		ALL	OCATI	ON	A'	VAILAB	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0	I	-	-	-				_	-	-
R	T _I	1	7	5	I	5	2				0	2	3
E A	T ₂	2	3	5	-	-	-				-	-	-
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total					11	5	2	3	6			

 T_3 can execute as it still might NEED (0, 0, 2) and AVAILABLE = (2, 3, 6)

					RES	SOUR	CES						
			MAX		ALL	LOCATI	ION	A'	VAILABI	LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T _o	0	0	I	-	-	-				-	-	-
R	T ₁	1	7	5	- 1	5	2				0	2	3
E A	T ₂	2	3	5	-	-	-				-	-	-
D S	T ₃	0	6	5	0	6	5				0	0	0
	Total				1	П	7	2	3	4			

T₃ eventually finishes and releases all its resources

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	A'	VAILAB	LE		NEED	
		A	В	С	Α	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	I	_	-	-				-	-	-
R	T ₁	I	7	5		5	2				0	2	3
E A	T ₂	2	3	5	-	-	-				-	-	-
D S	T ₃	0	6	5	-	-	-				-	-	-
	Total				-	5	2	2	9	9			

 T_1 can now execute since NEED (0, 2, 3) and AVAILABLE = (2, 9, 9)

	RESOURCES												
		MAX			ALLOCATION			AVAILABLE			NEED		
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H R E A D S	T ₀	0	0	I	-	-	-					-	-
	T ₁	I	7	5	I	7	5				0	0	0
	T ₂	2	3	5	-	-	-				-	-	-
	T ₃	0	6	5	-	-	-				-	-	-
	Total				I	7	5	2	7	6			

We have found a sequence of execution T_0 , T_2 , T_3 , T_1 which leads to safe state!

	RESOURCES												
		MAX			ALLOCATION			AVAILABLE			NEED		
		Α	В	С	Α	В	С	Α	В	С	Α	В	С
T H R E A D S	То	0	0		-	-	-				-	-	-
	T ₁	I	7	5	_	-	-				-	-	-
	T ₂	2	3	5	_	-	-				-	-	-
	T ₃	0	6	5	_	-	_				-	-	-
	Total				-	-	-	3	14	11			

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- Prevention → design resource allocation strategies which guarantee at least one of the 4 necessary deadlock conditions never holds
- Avoidance -> runtime checks to avoid deadlock online
- In practice, most OSs don't do anything and leave it all to applications

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