

# Predicting Ultrafast Nonlinear Dynamics in Fibre Optics with a Neural Network

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# Introduction

## Project Overview

- Topic: Nonlinear pulse propagation in optic-fibre - a typical case of [nonlinear Schrodinger equation system \(NLSE\)](#).
- Target: Predicting the propagation of pulses in optical fibre using [Recurrent Neural Network \(RNN\)](#).
- Method: [Long Short Term Memory \(LSTM\)](#) Network and [Complex Gated Recurrent Unit \(CGRU\)](#) Network.

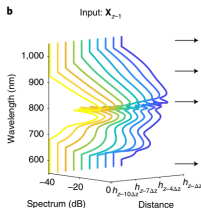


Figure: Predicting propagation of pulses

# Introduction

## Motivation of Using RNN in Nonlinear Schrodinger Equation (NLSE) System

**Challenges** for traditional numerical methods in studying nonlinear Schrodinger equation (NLSE) system :

- Require extensive numerical simulations.
- Computationally demanding.
- Creates server bottleneck in using them in experiments in real time.

**Motivation** of using RNN to study NLSE system:

- Similar idea as traditional numerical methods - Use earlier intensity of a signal to predict temporal intensity at particular distance.
- Less computational burden after training.
- Better performance in real time application.

## Solution 1

A solution using LSTM inspired by the work of L. Salmela et al<sup>1</sup>.

<sup>1</sup>L. Salmela, et al., "Predicting ultrafast nonlinear dynamics in fibre optics with a recurrent neural network," Nature Machine Learning Intelligence, 2021

# Introduction

## Motivation of Using Complex Representation of Pulses and Complex Neural Networks

**Motivation** of using **complex time domain representation** in pulse propagation prediction:

- **Amplitude/Power** representation suffers a potential loss of information.
- **Complex representation** provides complete information about spectra, power, and phase of the pulse.

**Challenges** of implementing **complex neural networks**:

- No existing libraries.
- Difficulty lies in implementing **complex operations**, especially in calculating complex gradients.
- Split complex approach. Real-valued non-linear activations are applied separately to the real and imaginary parts of the complex number.

# Introduction

## Motivation of Using Complex Recurrent Neural Network

**Motivation** of using **Complex Gated Recurrent Unit (CGRU)** Network:

- Use complex operation to **replace** the real number operation in a typical **Gated Recurrent Unit (GRU)** cell.
- **GRU** has a simpler structure comparing to **LSTM**.
- Easier to implement a complex version.

### Solution 2

A solution using Complex Gated Recurrent Unit (CGRU) Network inspired by the work of M. Wolter and A. Yao<sup>2</sup>.

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<sup>2</sup>M. Wolter, et al., “Complex Gated Recurrent Neural Networks” , CoRR, abs/1806.08267, 2018.

# Methodology

## LSTM Solution

The **LSTM** model is composed of 3 functioning layers:

- 1 **LSTM** layer with 250 neuron
- 2 **Dense** layer with 250 neuron
- Input data is **real** number data (power/amplitude)

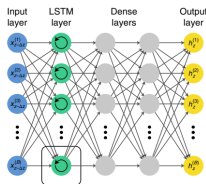


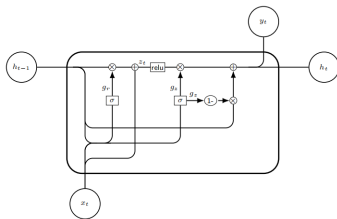
Figure: LSTM Model Structure

## Methodology

## Complex Gated Recurrent Unit (CGRU) Solution

A primitive **CGRU** model is composed of 1 layer:

- **CGRU** layer with 100 neuron
- Input data is **complex** number data (Complex time domain representation)



### Figure: CGRU Cell Structure



# Experiment

## Data

**Simulation generated** time domain power data and complex time domain data is used for the two solution separately:

- 1300 different input pulses
- 101 steps of propagation along the optic fibre
- 101 (for power data)/512 (for complex data) sampling points per signal

# Experiment

## LSTM Results

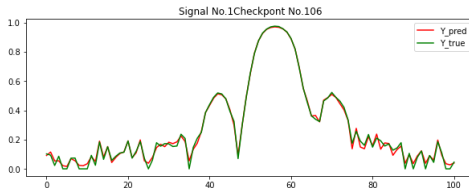


Figure: Example Prediction vs Truth Plot

TABLE II: Experiment Result on Dataset 1

Experiment Index	Optimizer	Window Size	learning Rate	Epochs	MSE (test)	MAE (test)
l_1_0	RMSprop	10	1e-4	5	8.2850e-05	0.0069
l_1_1	RMSprop	10	1e-4	10	6.7079e-05	0.0063
l_1_2	RMSprop	10	1e-4	20	5.3493e-05	0.0055
l_1_3(Early Stopping)	RMSprop	10	1e-4	29	5.9736e-05	0.0060
l_3_0	Adam	10	1e-4	10	4.7846e-05	0.0050
l_3_1	SGD	10	1e-4	10	0.0011	0.0196
l_5_0	RMSprop	15	1e-4	10	6.4968e-05	0.0060

Figure: LSTM Result

# Experiment

## Complex Gated Recurrent Unit (CGRU) Results

CGRU model has a less accurate prediction results comparing to LSTM, further study is needed to increase its performance.

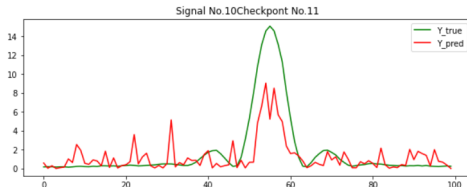


Figure: Example Prediction vs Truth Plot

# Limitation

Possible reasons for the relatively poor performance of **CGRU** model:

- **GRU** has a simpler structure comparing to **LSTM**.
- Possible information loss in complex operations.
- Not enough data samples.
- Further tuning may be needed.

# Conclusion

Using **Recurrent Neural Network** to predict pulse propagation in optic fibre proved to be a **feasible** solution:

- **LSTM** solution is **satisfactory** with regard to its prediction accuracy.
- **CGRU** solution points out a **feasible** and **promising** direction of future study using **complex representation** of pulses.

# References

- [1] L. Salmela, N. Tsipinakis, A. Foi, et al., “Predicting ultrafast nonlinear dynamics in fibre optics with a recurrent neural network,” *Nature Machine Learning Intelligence* 3, 344–354 (2021).
- [2] M. Wolter and A. Yao, “Complex Gated Recurrent Neural Networks” , *CoRR*, abs/1806.08267, 2018. [Online]. Available: <http://arxiv.org/abs/1806.08267>

# Thank You!