# Internet infrastructure and competition in digital markets

Philip Hanspach\*

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Preliminary: Latest version <u>here</u> (comments welcome).

#### Abstract

Large digital platform companies increasingly integrate vertically by building Internet infrastructure. These proprietary infrastructures confer quality advantages in markets for digital services. I model investment incentives for an infrastructure firm and a vertically-integrated firm facing a rival without proprietary infrastructure. Small changes in the marginal cost of investment lead to a discontinuous jump in investment incentives both for the infrastructure firm and the vertically-integrated firm if the latter has more infrastructure than the former. The infrastructure firm benefits from "commoditization" when its infrastructure is smaller. I derive conditions under which the resulting increase in investment is socially efficient. As the market share of the rival firm decreases, a trade-off arises between efficiency and "contestability", a key objective in European competition policy for digital markets.

**JEL Codes:** L13, L42, L51, L63, L86

**Keywords:** vertical integration, competition policy, net neutrality, Internet, Internet infrastructure, commoditization

<sup>\*</sup>European University Institute, philip.hanspach@eui.eu. Funding by the German Academic Exchange Service, the International Center for Law and Economics, and Lear is gratefully acknowledged. The author thanks Giacomo Calzolari, David K. Levine, Zeinab Aboutalebi, Pierre Regibeau, Volker Stocker, Sean Ennis, as well as participants at the DG COMP Chief Economist Team internal seminar, CLEEN 2022, ITS 2022, CRESSE 2022, ICLE Market Structure Roundtable 2022, Lear Competition Festival 2022 and at EUI for helpful comments and discussion. All errors and views are my own.

# 1 Introduction

Reigning in and regulating "big tech", a catch-all for diverse companies known by acronyms such as GAMAM or BAT, is on the political agenda in China, the EU, and the US. Economists have explained the size and power of "big tech" with features that generate "winner-takes-all" markets: (indirect) network effects, platform economics, or the use of big data analytics. One less well-researched aspect of "big tech" market power is the role of proprietary Internet infrastructures. This paper seeks to fill this gap by proposing a theory of vertical integration in digital markets to study the effect of proprietary Internet infrastructure on competition.

The scale and ownership structure of the physical aspect of the Internet - data centers, Internet exchange points, backbone - have undergone drastic changes in the past decade. Traditionally, large voice carriers connected local networks. These carriers deliver data packages based on principles of net neutrality and best-effort. The largest Internet Service Providers (ISP) interconnect with each other free of payment, creating a global network of networks, the Internet.

More recently, consumer-facing firms such as Google, Netflix or Meta, have increasingly complemented this so-called "public Internet" (operated by private companies nonetheless) with their own investments.<sup>1</sup> Some of the largest digital companies have made joint investments with traditional carriers and also created parallel, proprietary infrastructures.<sup>2</sup> These networks enable higher quality or guaranteed reliability contracts without violating net neutrality rules. This is essential for quality- or latency-sensitive applications, ranging from entertainment to corporate and security-related applications that require near 100% uptime.

Researchers and competition authorities are increasingly aware of proprietary Internet infrastructure but there is little knowledge about its implications. The EU's Digital Markets Act (DMA) recognizes that large platforms, which it calls "gatekeepers", can steer and block access to certain infrastructures. The DMA calls for openness and free choice in its pursuit of "fairness" and "contestability" in digital markets.<sup>3</sup> The German competition authority in its report on "Competition 4.0" singles out content delivery networks (CDN) as a piece of Internet infrastructure which has been increasingly used

<sup>&</sup>lt;sup>1</sup>An article by the Financial Times describes investors' diverging views on the competitive dynamics between data center operators that can be broadly summarized as belonging to the "public Internet" and those operated by "big tech groups". Financial Times, Will the cloud kill the data centre? Jim Chanos thinks so (2022), last accessed 31.10.2022.

<sup>&</sup>lt;sup>2</sup>Examples include ocean-crossing submarine cables, such as *JUPITER*, connecting the United States, Japan, and the Philippines, owned by a consortium including Amazon Web Services, Meta, NTT, PCCW, PLDT, and Softbank Corp. A transatlantic example, *Havfrue/AEC-2* connects the United States, Ireland, Denmark and Norway and is owned by Aqua Comms, Bulk, Meta, and Google. Both cables became ready for service in 2020.

<sup>&</sup>lt;sup>3</sup>The DMA discusses network access in recitals 14 and 51 of the preamble. Article 6(1)(e) proposes an unspecified obligation for "gatekeeper" firms not to restrict the choice of Internet access providers. However, it is not clear how the DMA will treat proprietary networks operated by gatekeepers.

by content firms.<sup>4</sup> However, neither text draws conclusions for the application of competition policy to Internet infrastructure based on economics principles.

This paper presents a theoretical model of vertical integration with a novel demand structure that represents Internet infrastructure as an (upstream) input to (downstream) digital services. A pure upstream firm, the infrastructure firm, invests in infrastructure and sells access to it to a pure downstream firm and to a vertically integrated firm. The latter further expands its available infrastructure through an investment in proprietary infrastructure. The resulting difference in infrastructure between the vertically integrated firm and the pure downstream firm allows the former to sell additional digital services for which it is a monopolist. When the cost structure of the industry results in this proprietary infrastructure being larger than that of the infrastructure firm, both firms' investment incentives jump upwards.

The model explains the incentives for "commoditization" of the infrastructure industry, a common fear in industrial policy, not only in telecommunications but also, for example, in automotive. It furthermore sheds light on the trade-off between contestability (the market share of the pure downstream firm) and efficiency (social welfare). The model suggests to account for the role of infrastructure in the review of vertical mergers in digital markets. It explains the side-payments that have occurred between vertically integrated firms and infrastructure firms such as Netflix and Comcast. Finally, it suggests that expanding net neutrality to certain kinds of infrastructure, such as CDN, would likely harm consumers. I show robustness to assumptions on congestion, the bargaining procedure, and product differentiation.

<sup>&</sup>lt;sup>4</sup>Bundeskartellamt (2016) Working Paper: Market power and platforms [in German]. The authors mention that on-demand server and network services allow small scale entry, while many large firms invest additionally in CDN to reduce response times. The report does not contain conclusions for the competitive assessment of these CDN.

# 2 Literature

This paper relates to the emerging literature on the economics of Internet infrastructure (Greenstein, 2020). Wilson, Xiao, and Orazem (2021) analyze the investment decisions of ISP and find long-term effects of investment delays on infrastructure quality. Greenstein and Fang (2020) find that data centers are being built primarily where customers are located, rather than in locations with favorable (land- and energy-)cost structure. Chaturvedi, Dutta, and Kanjilal (2021) investigate ISP pricing, in the presence of complementarity between broadband and content. These papers typically focus on the monopoly standing of last-mile ISP with respect to residential connections. By contrast, the infrastructure I am describing appears at an earlier stage in the value chain where big tech firms are vertically integrating.

This paper is closest to Buehler, Schmutzler, and Benz (2004) and Avenali, Matteucci, and Reverberi (2014). The former studies investment incentives by an upstream industry when network quality is not verifiable and the downstream (retail) industry is one-sided. They argue that vertical separation enhances incentives to invest in network quality most of the time. One main channel here is the quality sensitivity of retail demand. However, Buehler, Schmutzler, and Benz (2004) study a chain of monopolies and do not consider vertical integration.

Avenali, Matteucci, and Reverberi (2014) analyze functional and ownership separation for broadband networks and find ambiguous effects of vertical integration. By contrast, my setup focuses on competing investment by a pure infrastructure firm (for example, Akamai, a CDN operator) and a vertically integrated firm (for example, Google). I do not analyze the last-mile connections in which broadband providers have monopoly access<sup>5</sup> but focus on the digital services for which large content firms integrate vertically.

These infrastructure investments improve data management in the presence of net neutrality. Net neutrality is the imposition of zero-termination fees<sup>6</sup> and non-discrimination of data by carriers. Even though net neutrality is controversial and not uniformly enforced (for an early overview of the literature, see Schuett, 2010), it poses economic questions and trade-offs as described by Greenstein, Peitz, and Valletti (2016). Current net neutrality regulation is uneven, focusing on ISP while leaving open bypass opportunities and loopholes for cloud services and content providers (Stocker, Smaragdakis, and W. Lehr, 2020). This paper studies the investments into infrastructure that enables network management practices that arise to cope with the limitations of net neutrality.<sup>7</sup> It contributes to the debate on net neutrality by modeling investment incentives into the

<sup>&</sup>lt;sup>5</sup>Some attempts at competing in this area by content providers, such as Google Fibre, have failed in the past and do not play a large role in the marketplace.

<sup>&</sup>lt;sup>6</sup>For example, an ISP such as AT&T cannot charge Netflix for traffic that terminates in an AT&T network such as a residential building where Netflix customers live. The price paid by the final consumer to the ISP is understood to compensate the terminating network, no matter where data packages originate.

<sup>&</sup>lt;sup>7</sup>For example, infrastructure that ensures that one content provider's data packages arrive earlier and in a specific order at a router from where on they are treated on a first-come-first-served basis with the data packages of other content providers. Thus this infrastructure improves speed at the stage preceding the point where the net neutrality principle comes into play. See Easley, Guo, and Krämer (2018).

network management practices that already exist to adapt to net neutrality restrictions.

My setting where advertisement is served alongside digital services can be seen as a "reduced form" of Armstrong (2006)'s competitive bottleneck in two-sided markets. My paper introduces a true vertical structure with an intermediate input, in contrast with other papers on two-sided markets that call agreements with one market side "vertical" (Lee, 2013; D'Annunzio, 2017; Carroni, Madio, and Shekhar, 2018). The infrastructure firm is not a platform member, but an input supplier. Its inability to commit against opportunistic renegotiation rules out exclusivity. Instead, I show how the infrastructure firm benefits when its network is smaller than the vertically integrated firm's (corresponding to a platform with market power in a two-sided market model). Even though the infrastructure firm loses its strategic role and essentially sells a "commodity", it ends up extracting a greater surplus from the vertically integrated firm.

The phenomena studied in this paper are well-documented in a growing descriptive literature that has been largely ignored by economists. Some large digital services firms have pursued vertical integration strategies through the construction of private backbone networks, edge computing facilities, and owned CDN that improve their ability to expand and change their digital infrastructure to improve the performance and quality of their services (Arnold et al., 2020; Arnold, 2020; Sermpezis, Nomikos, and Dimitropoulos, 2017; Motamedi et al., 2019). Depending on the business model, private infrastructure can result in cost decreases because of hardware that is fit for purpose or increasing connection quality from faster delivery of data packages at the router of the last-mile ISP.

This paper is a first approach to analyze the effects of this shift in Internet ownership structure. Stocker, Knieps, and Dietzel (2021) document the geographic and virtual dimension of private networks and their implications for firm costs, service quality, and innovation. Lehr et al. (2019) and Balakrishnan et al. (2021) describe the functional disparities between services that rely on the public Internet versus services that are supported by proprietary networks and clouds. Using publicly available data, we add to the description of proprietary networks by showing that increasing numbers and shares of submarine cables have firms including Amazon, Meta, Microsoft, and Google among their owners (see Appendix B). By analyzing the previously overlooked competitive effect of a feature of digital markets that mainly concerns the largest digital firms, this paper contributes to the academic debate on regulation and antitrust towards large technology companies (see also Petit, 2020).

## 3 Model

This model has two key components:

- 1. Infrastructure, which is a capital investment either of an infrastructure firm or of a vertically integrated firm. The size of a firm's infrastructure is denoted k. An example are CDN, which are decentralized networks of servers that are used to distribute files, such as large media files, to consumers.
- 2. Digital services, which are provided to consumers by a digital services firm or by a vertically integrated firm using infrastructure as an input. Quantities of digital services are denoted q. An example of digital services are video streaming services which are offered both by vertically integrated firms and pure digital services firms.

Firms sell digital services (in the "downstream" market) to consumers, generating revenue through these sales and advertisement. To sell digital services, a firm needs infrastructure as an input, either owned or rented (the "upstream" market). Firms can rent infrastructure from an infrastructure firm. In addition, we assume one firm to be vertically integrated and able to build some infrastructure for its own use.

There are three players:

- 1. A vertically integrated firm (V) that makes a costly investment in infrastructure, purchases access to additional infrastructure from an infrastructure firm, sells digital services to consumers and shows advertisement alongside these digital services. A well-known example would be Google's YouTube, a video-sharing platform.
- 2. A digital services firm (Q) that purchases infrastructure access from an infrastructure firm, sells digital services to consumers and shows advertisement alongside these digital services. Think of this as a smaller rival to YouTube, such as Dailymotion.
- 3. An infrastructure firm (I) that makes a costly investment in proprietary infrastructure and sells access to its infrastructure to V and Q. Think of this as a CDN operator, such as Akamai or Limelight.

The vertical structure is represented in Figure 1.

Downstream there are potentially unlimited consumers, but firms are limited in their ability to sell services by their available infrastructure (either their own or rented infrastructure). Adding one unit of infrastructure allows firms to serve exactly one more unit of services to consumers at zero marginal cost and to show one more unit of advertisement alongside these services.<sup>8</sup>

Firms compete over consumers for services that they both sell, while the firm with more infrastructure has a monopoly for those services that only it can sell. This results in a "competitive segment" and a "monopolistic segment" on which firms can set separate

<sup>&</sup>lt;sup>8</sup>Zero marginal cost is a common assumption to focus on pricing in two-sided markets (Hagiu and Lee, 2011; D'Annunzio, 2017).

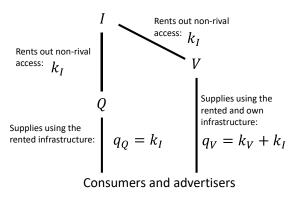


Figure 1: Infrastructure rental and downstream service supply

prices and face different demand. Firm Q can only choose whether to rent firm I's infrastructure  $k_I$ , so its downstream capacity is  $q_Q = \{k_I, \emptyset\}$ . Firm V can choose to rent access to  $k_I$  in addition to its own infrastructure  $k_V$ , so it offers  $q_V = \{k_I + k_V, k_V\}$ . Under this capacity structure, the size of the competitive segment is  $min(q_V, q_Q)$  and the size of the monopolistic segment is  $max(q_V, q_Q) - min(q_V, q_Q)$ . The relationship between available infrastructure and competition for consumers is visualized in Figure 2. In this example,  $\bar{q}_Q = k_I$  and  $\bar{q}_V = k_I + k_V$ . Therefore, Q and V compete Bertrand-style over the first  $k_I$  units of demand, while over the remaining  $k_V$ , V acts as a monopolist.

In the base model, access to infrastructure is non-rival, so I can sell its infrastructure to both V and Q simultaneously. While infrastructure in reality is capacity-limited (for example, storage space in a data center, capacity on a fibre-optic cable), in the base model we focus on the type of infrastructure that enables new kinds of services (for example, enabling latency-sensitive applications by building additional servers closer to final users) rather than congestion.

In our example, I offers a CDN for storing large media files to video-streaming services. In this example, infrastructure investment would correspond to building additional servers in local networks closer to consumers. The model emphasizes the quality advantage from being able to reach consumers locally (and thus decreasing latency) which enables higher quality services (such as live-streaming, higher video resolutions) for which platforms can charge through premium services (such as YouTube Premium). We consider congestion in a robustness check in Section 6.1.

Firms compete in prices and their products (on the competitive segment) are perfect substitutes to consumers. Hence, consumers buy services from the cheapest firm up to their willingness-to-pay a. When two firms set identical prices for their services, they split consumer demand equally. The digital services firm and the vertically integrated firm sell advertisement space alongside services to advertisers at a constant price of r

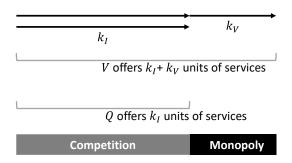


Figure 2: Market segmentation for differently-sized infrastructure

(irrespective of the segment on which the advertisement is displayed).<sup>9</sup>

I's objective is to maximize profits which are the sum of rental transfers  $t_V, t_Q$  minus the investment cost  $c_I(k_I)$ . V's objective is to maximize profits which are the revenue from selling digital services and advertisement downstream, minus the rental transfer  $t_V$  and investment cost  $c_V(k_V)$ . Q maximizes profits by selling digital services and advertisement downstream, minus its rental transfer  $t_Q$ . Firms' outside options are normalized to zero, and they accept transfers that allow them to at least break even. We indicate the monopolistic and competitive segments by subscript h = c (for competition), m (for monopoly). Firm j's demand on k is k0, and its price to consumers is k1, thence the payoffs:

$$\Pi_I = t_Q + t_V - c_I(k_I) \tag{1}$$

$$\Pi_V = \sum_{h=c,m} d_{V,h}(p_{V,h} + r) - t_V - c_V(k_V)$$
(2)

$$\Pi_Q = \sum_{h=c,m} d_{Q,h}(p_{Q,h} + r) - t_Q \tag{3}$$

The cost function for the creation of infrastructure is firm-specific and entails diminishing returns. We consider a convex cost function of the form  $c_i(k) = k^{\alpha} + \beta_i(k - k_0)$ ,  $\alpha > 1$ ,  $\beta_i > 0$  for some exogenous values  $\beta_i, k_0 \in \mathbb{R}_+$ ,  $k \geq 0$ , i = V, Q.

The timing is as follows: First, V and I simultaneously choose non-negative levels of investment. Second, I simultaneously posts take-it-or-leave-it offers to buy access to

<sup>&</sup>lt;sup>9</sup>This is equivalent to the "competitive bottleneck" configuration (Armstrong and Wright, 2007) in two-sided markets. The pricing is similar to the "per-reader advertising charges" in Armstrong (2006). The downstream market of our model is a simplified version of this two-sided market. A secondary source of revenues enables Q to pay a positive transfer to the infrastructure firm, which is required for competition in equilibrium.

<sup>&</sup>lt;sup>10</sup>From the demand structure above it follows that only one firm, either V or Q, can offer services on the monopolistic segment and serve consumers thereon.

 $k_I$  at transfers  $t_V, t_Q$  to V and Q, respectively. V and Q choose whether to accept or reject these offers. Player I cannot commit not to renegotiate prices opportunistically, so V and Q are accepting prices expecting competition by the other firm. Third, firms set prices to consumers and advertisers. Fourth, consumers and advertisers decide simultaneously from which firm to buy and payoffs are realized.

# 4 Analysis

We start by defining a subgame-perfect Nash equilibrium (SPNE) of this game.

**Definition SPNE:** A subgame-perfect Nash equilibrium of this game is a profile of prices  $p_{j,h}$ , transfers  $t_j$  j = V, Q, rental decisions, and investment levels  $k_i$ , i = I, V, such that these are optimal in every sub-game.

Now, we state the first main result regarding the types of equilibria of this game (Theorem 1). We state the main propositions regarding the existence of equilibria (Proposition 1) and an important feature of these equilibria (Proposition 2). Then, we state the second main result regarding social welfare in this model (Theorem 2). We then analyze the game, proving propositions 1 and 2, which together imply Theorem 1, followed by an analysis of social welfare. The proof of Theorem 2 is not interesting in itself, however, so it appears in the Appendix.

**Theorem 1:** There are two types of equilibrium in which either  $k_I > k_V$  or  $k_V \ge k_I$ .  $k_V \ge k_I$  in equilibrium if  $\beta_V - \beta_K \le r/2$ . The converse is true otherwise.

First, we show:

**Proposition 1:** Both I's and V's optimal level of investment are higher in the equilibrium when  $k_V \ge k_I$  than in the equilibrium where  $k_I > k_K$ .

and

**Proposition 2:** When  $\beta_V > \beta_I - \frac{r}{2} \ (\beta_V < \beta_I - \frac{r}{2})$  there is a unique equilibrium where

 $<sup>^{11}</sup>$ More precisely, after V and Q have announced whether to accept the take-it-or-leave-it offer, if any of them rejected the offer, I can make one additional, revised take-it-or-leave-it offer. This prevents I from initially announcing a high transfer that can only be recouped under monopoly, but not under competition, and thereby attempting to create a downstream monopoly. Any firm facing such a transfer would anticipate an opportunistic offer to its rival and reject. In equilibrium V and Q correctly anticipate that the rival will enter. The idea is similar to franchising where the franchiser would like to commit to limit downstream competition but has an incentive to opportunistically award more franchises after a contract has been made (McAfee and Schwartz, 1994). With a similar logic a durable goods monopolist is disciplined by competition from its future self (Bulow, 1982). In our model, upstream competition could alternatively be a second infrastructure firm or a competitive fringe of infrastructure firms but given our demand structure, this is a convenient way of limiting upstream market power.

$$k_I > k_V \ (k_I < k_V).$$

**Theorem 2:** Social welfare is decreasing in marginal costs  $\beta_I$ ,  $\beta_V$  but has a discontinuity when  $\beta_V - \beta_I = r/2$ . Social welfare increases at this point if

$$(a+r)^{\alpha-1} \left[ \frac{2a+r}{\alpha} \right] > \left[ \frac{2a+r}{\alpha} \right]^{\alpha} + (\beta_I + \beta_V)^{\alpha-1} \left( \frac{a+\frac{r}{2}}{\alpha} \right)$$
 (4)

and decreases otherwise.

We start by analyzing the game.

**Proof of proposition 1:** At the third and final stage, firm j = V, Q choose consumer prices  $p_{j,h}$  for h = c, m. On the monopoly segment, firm j maximizes profits by setting  $p_{j,m}^* = a$ . On the competitive segment  $p_{i,c}^* = 0$  is the only equilibrium: firms have zero marginal cost and products are perfect substitutes, so Bertrand pricing prevails.

If both firms decide to rent infrastructure access from I (we'll verify next that they do so in equilibrium), the resulting available infrastructure is as in Figure 2 and resulting demand is:

$$d_{Q,c} = d_{V,c} = k_I/2 \tag{5}$$

$$d_{Vm} = k_V \tag{6}$$

$$d_{Q,m} = 0. (7)$$

Given these prices and demand, profits are

$$\Pi_Q = k_I(r/2) - t_Q \tag{8}$$

$$\Pi_V = k_I(r/2) + (r+a)k_V - t_V - c_V(k_V). \tag{9}$$

Recall that when setting transfers, I cannot commit not to renegotiate. For example, if Q rejects the initial offer, I can always offer  $t'_Q = k_I(r/2)$  which allows Q to break even (anticipating  $d_{Q,c} = k_I/2$  and revenues  $rd_{Q,c}$ ) and is accepted. Anticipating that it will face competition for the first  $k_I$  units of services, the highest price that V is willing to pay to I is

$$t_V = \frac{r}{2}k_I + k_V(a+r) - k_V\frac{r}{2} - \max(0, (k_V - k_I)(r/2 + a))$$
(10)

which can be rewritten as

$$t_V = \begin{cases} (k_I + k_V)\frac{r}{2} + k_V a & \text{if } k_I > k_V \\ k_I(a+r) & \text{if } k_V \ge k_I. \end{cases}$$
 (11)

Importantly, V's willingness-to-pay for access to  $k_I$  depends on whether its own infrastructure is greater than I's. Levels of infrastructure are selected in the first period and are fixed and observed when I makes its offers. When  $k_I$  is larger than  $k_V$  and V does

not rent access to  $k_I$ , V can only serve  $k_V$  units of digital services and it faces competition from Q on this range. V's revenue in this case is  $k_V \frac{r}{2}$ , the third term in equation 10. Its willingness-to-pay is therefore the difference between the total revenue it makes with  $k_I$  minus this outside option.

If  $k_V$  exceeds  $k_I$ , V will be able to act as a monopolist for some part of demand  $(k_V - k_I)$  even without access to I's infrastructure. At the margin, one additional unit of infrastructure allows V to serve one more unit of digital services at the monopolist's markup a + r.

At the first stage, V and I make their investment decisions. We now set up the profit functions and solve for the profit-maximizing level of investment. V's first period problem is

$$\max_{k_V} \Pi_V = d_{V,c}(p_{V,c} + r) + d_{V,m}(p_{V,m} + r) - t_V - c_V(k_V). \tag{12}$$

Now we can write

$$\frac{\partial \Pi_V}{\partial k_V} : a + r - c_V'(k_V) - \frac{\partial t_V}{\partial k_V} = 0 \tag{13}$$

$$\frac{\partial t_V}{\partial k_V} = \begin{cases} \left(\frac{r}{2} + a\right) & \text{if } k_I > k_V \\ 0 & \text{if } k_V \ge k_I \end{cases}$$
 (14)

$$c_V'(k_V) = \alpha k_V^{\alpha - 1} + \beta_V \tag{15}$$

which yields the first order conditions for  $k_V$ :

$$\begin{cases}
\frac{r}{2} = c'_V(k_V) & \text{if } k_I > k_V \\
a + r = c'_V(k_V) & \text{if } k_V \ge k_I
\end{cases}
\leftrightarrow
\begin{cases}
k_V = \left(\frac{r/2 - \beta_V}{\alpha}\right)^{\frac{1}{\alpha - 1}} & \text{if } k_I > k_V \\
k_V = \left(\frac{a + r - \beta_V}{\alpha}\right)^{\frac{1}{\alpha - 1}} & \text{if } k_V \ge k_I
\end{cases}$$
(16)

The second order conditions are fulfilled from the convexity of  $c_V(k_V)$ .

I's first stage problem is

$$\max_{k_I} \Pi_I = t_Q - t_V - c_I(k_I) \tag{17}$$

with

$$\frac{\partial \Pi_I}{\partial k_I}: \quad \frac{r}{2} + \frac{\partial t_V}{\partial k_I} - c_I'(k_I) = 0 \tag{18}$$

$$\frac{\partial t_V}{\partial k_I} = \begin{cases} \frac{r}{2} & \text{if } k_I > k_V \\ a+r & \text{if } k_V \ge k_I. \end{cases}$$
 (19)

which yields the first order conditions for  $k_I$ :

$$\begin{cases}
 r = c_I'(k_I) & \text{if } k_I > k_V \\
 a + (3r/2) = c_I'(k_I) & \text{if } k_V \ge k_I
\end{cases}$$

$$\begin{cases}
 k_I = \left(\frac{r - \beta_I}{\alpha}\right)^{\frac{1}{\alpha - 1}} & \text{if } k_I > k_V \\
 k_I = \left(\frac{a + (3r/2) - \beta_I}{\alpha}\right)^{\frac{1}{\alpha - 1}} & \text{if } k_V \ge k_I
\end{cases}$$
(20)

Comparing the upper and lower branches of equations 16, 20, we see that there are two types of equilibrium and that these are characterized by either  $k_I > k_V$  or  $k_V \ge k_I$ . In the former case, investment is lower than in the latter case, as stated in Proposition 1.

One interpretation of the case  $k_I > k_V$  is that I plays a strategic role by "pushing" V into the region where it has market power - without it, V faces tough competition and only reaps low profits. In the second case,  $k_I$  does not have such a strategic role: Q's ability to constrain V's pricing power is limited and additional infrastructure at the margin allows V to increase its revenue by a + r, independent of whether it makes this investment privately or whether I makes this investment (as long as  $k_I < k_V$ ).

I call the intuition behind the case  $k_V > k_I$  "commoditization": I's infrastructure becomes interchangeable with marginal investment for V because it only adds to the monopolistic segment. For this reason, V's willingness-to-pay is higher in this scenario.<sup>12</sup>

In equations 16, 20 we assume implicitly that investment is as in the case of  $k_V > k_I$  if the condition holds with equality. This is purely for completeness, there is nothing in the model that tells us that this particular equilibrium will be chosen when the condition holds with equality. The following section shows that there is a set of parameters for which either outcome (the upper or lower branch of these equations) is possible.

#### 4.1 Existence of equilibria

So far, we have computed the transfers and prices that maximize firm profits for given levels of investment as well as the optimal levels of investment as a function of model parameters and whether  $k_I$  or  $k_V$  is larger. Without further restrictions, there is no guarantee that the optimal levels of investment are indeed consistent with the size-ordering of the two infrastructures.

From equations 16 and 20 we see that I(V) will never choose a level of investment greater than 0 if  $\beta_I > a + (3r/2)$  ( $\beta_V > a + r$ ). In general, strictly positive levels of investment only arise in equilibrium if  $\beta_V < r/2$  and  $\beta_I < r$ . To investigate only interesting cases, we are going to restrict the parameter space accordingly. Furthermore, for any set of parameters to result in an equilibrium, the parameters also need to result in the correct size ordering of the two infrastructures, i.e.,  $k_I > k_V$  or the converse must be true when computing equilibrium investment levels. We now show that such equilibria exist.

<sup>&</sup>lt;sup>12</sup>The idea of commoditization, in the more general sense of converting a product into a standardized and interchangeable input, is common in the discussion of industrial policy surrounding vertical integration of some big tech firms, both for Internet infrastructure firms and also with regards to other industries such as the automotive sector. One concern is whether automotive firms will become mere suppliers of hardware as the value generation shifts to the digital sphere and the data generated by cars and drivers. A major German daily compares the fear of Internet infrastructure firms like Deutsche Telekom to become "dumb tubes", or commoditized suppliers to data-driven consumer-facing platform companies. The corresponding fear of car companies and other manufacturing companies is to become "dumb wheels" or "extended workbenches" as profit shifts to digital platform companies. FAZ, Autobranche im Spagat (2021) [in German], last accessed 31.10.2022.

**Proof of proposition 2:** Take the first-order conditions from the upper cases of equations 16 and 20, impose  $k_I > k_V$ , and some algebra yields

$$\beta_V > \beta_I - \frac{r}{2}.\tag{21}$$

Therefore, given marginal costs that fulfill the above inequality, the infrastructure firm has indeed the larger network. Similarly, comparing the lower cases of equations 16 and 20 and solving for  $k_V \geq k_I$  yields

$$\beta_V \le \beta_I - \frac{r}{2}.\tag{22}$$

Now, setting the upper and lower cases of equations 16 and 20 equal yields:

$$\left(\frac{r/2 - \beta_V}{\alpha}\right)^{\frac{1}{\alpha - 1}} = \left(\frac{r - \beta_I}{\alpha}\right)^{\frac{1}{\alpha - 1}} \qquad \leftrightarrow \quad \beta_V = \beta_I - \frac{r}{2} \tag{23}$$

$$\left(\frac{r/2 - \beta_V}{\alpha}\right)^{\frac{1}{\alpha - 1}} = \left(\frac{r - \beta_I}{\alpha}\right)^{\frac{1}{\alpha - 1}} \qquad \leftrightarrow \quad \beta_V = \beta_I - \frac{r}{2} \qquad (23)$$

$$\left(\frac{a + r - \beta_V}{\alpha}\right)^{\frac{1}{\alpha - 1}} = \left(\frac{a + (3r/2) - \beta_I}{\alpha}\right)^{\frac{1}{\alpha - 1}} \qquad \leftrightarrow \quad \beta_V = \beta_I - \frac{r}{2}. \qquad (24)$$

The profit functions are strictly concave  $(c_I''(k_I) < 0, c_V''(k_V) < 0)$ , so the first-order conditions are sufficient to describe the unique values of  $k_I$ ,  $k_V$  where  $\Pi_I$ ,  $\Pi_V$  attain their global maxima. Also, the equilibrium value of  $k_I$  does not depend on  $k_V$  and vice versa except through the ordering of size of these two variables. Therefore, when either  $\beta_V > \beta_I - \frac{r}{2}$  or  $\beta_V < \beta_I - \frac{r}{2}$ , the equilibrium is unique. 

It is not surprising that the firm with lower marginal costs will generally have the larger infrastructure. Also the "wedge" of r/2 that separates the marginal cost values which equalize investment is not interesting in itself - it is a consequence of the nocongestion-assumption which allows I to charge Q an additional r/2 for every unit of  $k_I$ added in addition to charging its contribution to V's profit.<sup>13</sup>

There is one combination of parameters where both orderings of the two infrastructure variables are an equilibrium. When  $\beta_V = \beta_I - \frac{r}{2}$ , both  $k_V > k_I$  and  $k_I > k_V$  can be optimal. For completeness, I have defined the conditional functions above such that that  $k_V > k_I$  will be chosen. However, there is nothing inherent in the model which tells us that this equilibrium will be chosen. This is interesting because it gives us a configuration of parameters for which we can directly compare the two types of equilibrium. We will use this below to compare social welfare for the two types of equilibrium, holding parameters constant.

Figure 3 illustrates equilibrium investment values as a function of  $\beta_I$  for some set of parameters.  $k_V$  does not depend on  $\beta_I$ , so it can only take two values for a given set of parameters, represented by horizontal black lines: one corresponding to the case  $k_V > k_I$  and one where  $k_I > k_V$ . We denote V's optimal level of investment  $k_V^*$  in the former case and  $k_V^{**}$  in the latter case.  $k_I$  depends on I's cost parameter  $\beta_I$  as well as

<sup>&</sup>lt;sup>13</sup>Accordingly, this wedge decreases in robustness checks (in Section 6) that afford less bargaining power to I or that consider congestion.

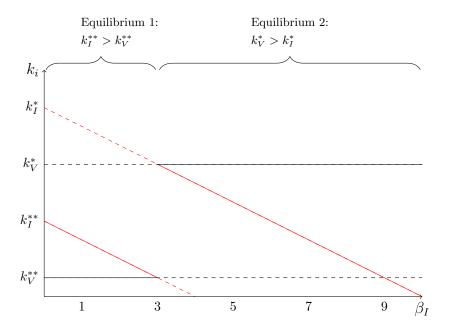


Figure 3: Equilibrium investment decisions as a function of  $\beta_I$  for  $\beta_V = 1, a = 4, r = 4, \alpha = 2$ .

other parameters and on which firm has the larger infrastructure, so it is represented by two decreasing functions. Given all other parameter values, a value of  $\beta_I$  admits an equilibrium in which infrastructure levels are  $k_V^*, k_I^*$  ( $k_V^{**}, k_I^{**}$ ) whenever it is true that  $k_V^* > k_I^*$  ( $k_I^{**} > k_V^{**}$ ). These regions are marked with solid black lines. When  $\beta_I = \beta_V + r/2$ , both equilibria are possible.

The model is silent on which equilibrium to expect in case of indifference. However, we are going to compare the two equilibria and show that  $k_V > k_I$  dominates the other in terms of firm profits and sometimes on social welfare. The presence of the two different kinds of equilibria is consistent with the increasingly large role played by vertically integrated firms in infrastructure which is documented in the literature (see Section 2) and Appendix B.

### 4.2 Social welfare

We consider whether the equilibria we just found maximize social welfare. We define social welfare as the total sum of surplus minus costs. This implies that both parts of the network are used to supply services. In terms of the game we presented in the previous section, this is the case whenever  $q_V = k_I + k_V$ . We define social welfare S as follows:

$$S = (k_I + k_V)(a+r) - c_I(k_I) - c_V(k_V)$$
(25)

It is easy to show that social welfare is maximized when

$$c_I'(k_I) = c_V'(k_V) = a + r (26)$$

Comparing this optimum to the outcome of the decentralized model, we see that social welfare is generally not maximized. Furthermore, social welfare is a function both of the parameters (higher costs clearly imply lower social welfare) as well as the two different types of equilibrium described in Theorem 1. As mentioned before, we want to compare social welfare when the parameters admit both types of equilibria. This allows us to ignore the levels of marginal cost parameters  $\beta_I$ ,  $\beta_V$  to analyze the role of the two different cases where either V or I owns more infrastructure.

#### **Proof of Theorem 2:** In the Appendix.

It is unsurprising that social welfare decreases when marginal costs increase. The interesting question is what happens with social welfare when we jump between the two equilibria of the decentralized game that we have identified earlier, either because we have marginal cost parameters that admit both types of equilibria as shown above in Propositions 1 and 2, or if we consider a small change of  $\beta_V$ ,  $\beta_I$  such that we move between these two equilibria (while having a negligible direct effect of the change). This proposition shows that the benefit from the increased investment incentives in the  $k_V > k_I$ -equilibrium dominates additional investment cost if  $\beta_I$ ,  $\beta_V$  are low or if  $\alpha$ ,  $\alpha$  and r fulfill certain conditions jointly.

Now compare the socially optimal investment with the Nash-equilibrium investment levels which we have computed in equations 16 and 20. In the case where  $k_I > k_V$ , we have underinvestment, as  $c'_I(k_I) = r$ ,  $c'_V(k_V) = r/2$ . In the case where  $k_V > k_I$ , we have overinvestment as  $c'_I(k_I) = a + (3r/2)$ ,  $c'_V(k_V) = a + r$ . The reason for overinvestment is that absent congestion, I's private return exceeds the public return from each additional unit of investment, as it gets to charge Q r/2 for the additional investment (which correspondingly lowers V's profit by r/2 due to competition). However, the net effect on social welfare is positive as long as the condition in equation 4 is fulfilled.

The problem could also be viewed as a social planner's problem who chooses  $k_V$  and  $k_I$  to maximize social surplus. Here, it is necessary to explicitly state a side-condition that the total sum of demand equals the maximum capacity from the combined networks of V and I. This planner problem can be written as

$$\max_{k_I, k_V} S = (k_I + k_V)(a+r) - c_I(k_I) - c_V(k_V)$$
(27)

subject to 
$$\sum_{i=V,Q} \sum_{h=c,m} d_{i,h} = k_I + k_V.$$
 (28)

and it is clearly also maximized where  $c'_I(k_I) = c'_V(k_V) = a + r$ . The side-condition in equation 28 is also fulfilled in the Nash equilibrium as both Q and V find it optimal to sign the contract with I. This side-condition rules out inefficient configurations for the social planner's problem in which V would not have access to  $k_I$  and the total quantity of digital services served downstream would be lower than in the Nash-equilibrium.

# 5 Applications

#### 5.1 Contestability

How does vertical integration into Internet infrastructure by V impact the "contestability" of the downstream market? Contestability is a policy objective in the regulation of digital markets. The European Commission implicitly defines contestability as the absence of "very high barriers to entry or exit, including high investment costs, which cannot, or not easily, be recuperated in case of exit, and the absence of, or reduced access to, some key inputs in the digital economy, such as data", also referring to the network effects implied by access to more data.  $^{14}$ 

The justification for pursuing contestability is that in its absence, platform markets in particular are prone to "tipping", resulting in entrenched market power, leading to higher costs for consumers and less innovation. <sup>15</sup> A straightforward way to approach this question in the context of this model is to look at how the market shares of V and Q (both on the advertising side and the consumer side) behave between the two equilibria.

Market shares in an antitrust context are typically measured in terms of revenue (rather than profit). Revenue on the advertising side is proportional to the number of connected users for both V and Q. Revenue on the consumer side is nil for Q due to Bertrand competition and  $k_V a$  for V due to market power for digital services on the monopolistic segment.

We denote the market shares of firm j as  $MS_j$ . It is measured in terms of revenue in the digital services market across both sides. It can be simplified by dividing by r and substituting infrastructure levels for demand. Now, market share is a function of infrastructure levels  $k_V$ ,  $k_I$  as well as the ratio of the value generated by digital services and advertisement (a/r).

$$MS_Q = \frac{r(k_I/2)}{r(k_I + k_V) + ak_V} = \frac{(k_I/2)}{(k_I + k_V) + (a/r)k_V}$$
(29)

$$MS_V = 1 - MS_O \tag{30}$$

We analyze the change in  $MS_Q$  in the case where two equilibria are possible. Denoting the equilibrium where  $k_V \ge k_I \ (k_V < k_I)$  with superscript \*\* (\*) we find:

**Proposition 3:**  $MS_Q^{**} - MS_Q^*$  is negative and decreasing in r,  $\beta_I$ .

 $<sup>^{14}</sup>$ The DMA discusses contestability repeatedly without giving a simple definition. Its meaning is implicitly explained most clearly in recitals 3 and 13 of the preamble.

<sup>&</sup>lt;sup>15</sup>For example, the preamble of the EU's DMA asserts that "specific features of core platform services make them prone to *tipping*: once a service provider has obtained a certain advantage over rivals or potential challengers in terms of scale or intermediation power, its position may become unassailable and the situation may evolve to the point that it is likely to become durable and entrenched in the near future." (emphasis added), DMA, preamble, paragraph 25.

#### **Proof:** In the Appendix.

For the cases when we find that social welfare increases at the higher levels of vertical integration that come with the  $k_V > k_I$ -case, the model illustrates a trade-off: the dynamics of Internet infrastructure and vertical integration that can lead to increased efficiency and greater social welfare come at the cost of lower market share for non-integrated rival platforms. Pursuing the EU's policy goal of contestability in digital markets comes at a cost in terms of efficiency. It is at odds with the equilibrium that arises when V's infrastructure dominates.

High market shares are not harmful to consumers per se but often serve as shortcuts to market power analysis by competition authorities. Under some conditions, such as incomplete capital markets or network effects, high market shares can constitute and further enhance market power, however, which may justify concerns about the market structure of the downstream market.

## 5.2 Merger: I buys Q

What happens when I is not a pure upstream player but can integrate downstream as well and provide digital services? While there is no notable example of a CDN operator offering consumer-facing services, such as media entertainment, there are traditional Internet infrastructure firms active in downstream consumer markets. For example, Deutsche Telekom operates on multiple levels of Internet infrastructure for business customers (including data centers and cloud computing) but also has media offerings including sports and streaming for final consumers.<sup>16</sup>

To remain as close as possible to the base model, we consider a merger between I and Q, forming a new merged entity, M. Now, the two firms V and M are symmetric except for the potentially different marginal cost variables  $\beta_M, \beta_V$ . In the first stage, M and V invest in infrastructure  $k_M, k_V$ . At the second stage M makes a take-it-or-leave-it-offer to V for access to  $k_M$ . Both firms anticipate downstream competition at the third stage. We analyze M's decision to rent its infrastructure to V as well as M's and V's infrastructure investment decisions.

In the base model, a firm never has an incentive to provide less digital services than its available infrastructure allows (as infrastructure costs are sunk at the phase of downstream competition and digital services are provided at zero marginal cost). Now, however, if M offers more digital services downstream while it has the smaller network, it provides additional competition to its rival V which may decrease V's ability to pay high transfers for network access. The equilibrium depends on whether M can commit to a level of downstream services  $q_M$  alongside the transfer  $t_V$  at the second stage.<sup>17</sup>

<sup>&</sup>lt;sup>16</sup>See Deutsche Telekom website, for business customers, for media and entertainment [both in German], last accessed 31.10.2022.

<sup>&</sup>lt;sup>17</sup>While the base model allowed no commitment of I towards V not to renegotiate transfers with Q, it seems more plausible that an integrated entity could credibly commit not to compete with its own business customers which is why we check both cases.

This is described in Proposition 4 which comes in two parts, 4a) describes the case without commitment by M for the quantity  $q_M$ , while 4b) describes the case with commitment:

**Proposition 4a:** If M cannot commit to a level of  $q_M$  at the second stage,  $q_M = k_M$  in equilibrium. Furthermore,

$$\begin{pmatrix}
 c'_{M}(k_{M}) & = r \\
 c'_{V}(k_{V}) & = r/2 \\
 t_{V} & = (k_{M} - k_{V})(r/2) + k_{V}(a+r)
 \end{pmatrix} \text{ if } \beta_{V} > \beta_{M} + r/2$$

and

$$\begin{pmatrix}
c'_{M}(k_{M}) &= (3r/2) + a \\
c'_{V}(k_{V}) &= a + r \\
t_{V} &= k_{M}(a + r)
\end{pmatrix} \text{ if } \beta_{V} < \beta_{M} + r/2$$

**Proposition 4b:** If M can commit to a level of  $q_M$  at the second stage, M offers

$$\begin{cases} t_V &= k_M(a+r) \\ q_M &= k_M \end{cases}$$
 if  $\beta_V < \beta_M + r/2$ 

at the second stage and first-stage investment is given by  $c'(k_M) = a + (3r/2)$  and  $c'(k_V) = a + r$ .

$$\begin{cases} t_V &= k_M(a+r) \\ q_M &= 0 \end{cases}$$
 if  $\beta_V > \beta_M + r/2$ 

at the second stage and first-stage investment is given by  $c'(k_M) = a + r$  and  $c'(k_V) = a + r$ . In both cases, if  $\beta_V = \beta_M + r/2$ , either one of these sets of investment levels and transfers can arise in equilibrium.

#### **Proof:** In the Appendix.

The first part of the proposition tells us that without commitment to a quantity level, we obtain the same result as in the base model. As M will always find it attractive at the third stage to offer digital services on its infrastructure and V anticipates this at the second stage, we have similar equilibrium profits and transfers and the condition on the difference in marginal cost that determines the equilibrium outcome is identical.

The second part of the proposition tells us that when the newly merged entity can commit in advance to a downstream strategy, it may find it useful to set  $q_M = 0$ , or shut down its digital services operations and become a pure infrastructure provider. This is the case when its infrastructure is larger than that of the vertically integrated firm. The intuition is that in this case, it can create a downstream monopoly and participate in its

profits by charging monopoly prices for access to  $k_M$ . As now the size of the competitive segment is  $\emptyset$  and the size of the monopolistic segment is  $k_M + k_V$ , consumer welfare is 0 and lower than in the base model when  $\beta_V > \beta_I + r/2$ .

This result does not have novel implications per se, competition authorities already investigate vertical mergers for the ability and incentive of a merged entity to divert business either upstream or downstream. While harmful to consumers, M shutting down its downstream business maximizes social welfare and increases investment (as marginal investment fulfills the conditions of equation 26). The proof also involves checking that the foregone downstream revenue is smaller than the additional transfer fee but this is implied by the condition  $\beta_V > \beta_M + r/2$ .

### 5.3 Efficient side-payments

One question of current interest is the contribution of digital content firms to telecommunication networks. We observe side payments between some large content platforms, such as Netflix, and traffic carriers such as Comcast. This model can explain why such side payments can occur when I's network is only used to a limited extent by Q. There are several reasons why smaller competitors may be limited in their ability to compete with a large digital platform even in the presence of sufficient infrastructure: intellectual property (patents, technology or media content), network effects, brand attraction, or internal technical ability. For example, the lack of exclusive content may limit a video-streaming platform's attractiveness to consumers.

We think of these various limitations as some exogenous limit to the demand served by Q. If Q cannot serve more than some amount  $\bar{q}_Q$  of services and V and I can agree, before t=1 of the base game, that V will pay a transfer  $t'_V$  (in addition to  $t_V$ ) to I conditional on choosing a certain value  $k_I$ . To make the model interesting, we only consider cases where  $\bar{q}_Q$  is binding in equilibrium.

**Proposition 5:** If Q is capacity-constrained and conditional side-payments are possible and  $\beta_V > \beta_I + r/2$ , I's and Q's incentives to invest align. Investment levels are given by  $c'_V(k_V) = c'_I(k_I) = a + r$ .

**Proof:** When Q is capacity-constrained so that it can serve only a portion of the demand that is smaller than the size of I's network, every unit  $k_I > \bar{q}_Q$  can be rented out only to V. V generates a profit of  $(a+r)(k_V+k_I-\bar{q}_Q)+r/2\bar{q}_Q-k_V(k_V)-t_V'-t_V$ . In equilibrium, I and V can jointly maximize their surplus by setting a value of  $k_I$  such that  $c_I'(k_I) = a + r$ . Call this value  $k_I^{**}$  and  $k_I^*$  the equilibrium level of I's investment. Then this can be implemented and is incentive compatible when V offers any value of  $t_V'$  such that  $(k_I^{**} - k_I^*)(a+r) > t_V' > c_I(k_I^{**}) - c_I(k_I^*)$  if and only if  $k_I = k_I^{**}$ . This value

<sup>&</sup>lt;sup>18</sup>See Reuters, EU's Vestager assessing if tech giants should share telecoms network costs (2022), last accessed 01.05.2023.

<sup>&</sup>lt;sup>19</sup>See Wall Street Journal, Netflix to Pay Comcast for Smoother Streaming (2014), last accessed 01.05.2023.

exists and is positive from the fact that  $c_I(k_I)$  is increasing and convex and its marginal value is a + r only at  $c_I(k_I^{**})$  and lower at any lower level.

This result illustrates that in the base model, competition from Q serves as a friction that prevents I and V from maximizing their joint surplus. Absent this constraint, the value  $k_I$  that maximizes total surplus is simply the one that equates marginal cost and revenue. An enforceable contract on the choice of  $k_I$  is a simple mechanism to implement the efficient investment levels  $k_V$ ,  $k_I$ .

#### 5.4 Net neutrality

Net neutrality is the absence of termination charges, i.e., content providers do not pay those Internet service providers (ISP) into whose network their traffic is delivered. According to other definitions, net neutrality does not allow ISP to offer a "fast lane" in exchange for payment.

The model only translates to this setup approximately as I does not represent an ISP operating last-mile-networks (we generally do not observe competition at this stage due to fixed costs that imply a natural monopoly). However, there is some discussion as to whether certain infrastructure operators should follow the same rules as ISP. For example, in the US CDN managed to be exempted from net neutrality rules by lobbying.<sup>20</sup>

Consider a net neutrality scenario in which I is constrained to charge a single price  $t_Q = t_V = t$ . Then, access to this infrastructure can be described as a price posted by the upstream industry instead of the bilateral bargaining of the base model. More precisely, after investment decisions in  $k_V, k_I$  have been made, I posts a price under which platforms can purchase non-rival access to  $k_I$ . V and Q decide simultaneously whether to pay the price, and finally downstream competition takes place. Here, we do not consider renegotiation of the transfer t (as there is only a single profit-maximizing price, renegotiation makes no difference in this case).

**Proposition 6:** Under net neutrality, I charges  $t = k_I(a+r)$  and chooses  $c'(k_I) = a+r$ . In equilibrium, Q chooses not to pay this price and  $q_Q = \{\emptyset\}$ ,  $q_V = k_V + k_Q$ .  $p_{V,m} = a$ ,  $d_{V,m} = q_Q$ .

#### **Proof:** In the Appendix.

Net neutrality for infrastructure providers thus harms downstream competition as Q is essentially excluded from the market and consumers pay higher prices due to the absence of a competitive segment. The intuition behind this result is that I has no

<sup>&</sup>lt;sup>20</sup>See the FCC's NPRM in 2014 which introduces their thinking on CDN. Protecting and Promoting the Open Internet NPRM (2014). Akamai and other CDNs lobbied to FCC to amend the Open Internet Order which would exempt them from regulation See filings received by Akamai between 02.02.2014 and 31.03.2015. This was reflected in the final order. FCC Releases Open Internet Order (2015). All links last accessed 17.01.2023.

interest in downstream competition as it reduces industry profit. There is no equilibrium where Q accepts the offer and V rejects because in this case, V's best response would be to invest at least up to the point where  $c'_V(k_V) = r/2$ . However, due to the presence of competition, Q cannot operate profitably when  $t = k_I(a+r)$ . The resulting outcome maximizes social welfare as the resulting equilibrium levels of investment fulfill the conditions of equation 26.

## 6 Robustness

#### 6.1 Congestion

So far, we have abstracted from the possibility of congestion. Each unit of infrastructure could be used as a non-rival input in the provision of digital services by both V and I. This most accurately describes investments that enhance capabilities rather than capacity. For example, in a network that does not suffer from congestion, additional investment may represent new network nodes that reduce the average (physical) distance that data packages travel between digital services firms and consumers. In such a case, it may be reasonable to abstract away from congestion and to focus on the role of the network in increasing demand through enhanced quality.

In reality, there are few examples of infrastructure that are truly non-rival, and the aspect of congestion may just be more or less important. To reflect this, we consider a robustness check in which returns on the competitive segment of the market are decreased. We introduce a *congestion factor*  $1/2 \le \phi < 1$ . We consider adjusted demand functions on the competitive segment:

$$d'_{V,c} = \phi d_{V,c}$$
 and  $d'_{Q,c} = \phi d_{Q,c}$ . (31)

The closer  $\phi$  is to 1, the smaller is the role played by congestion and for  $\lim_{\phi \to 1}$ , we are back in the base model. As  $\phi$  moves closer to 1/2, congestion reduces the returns on the competitive segment.

Simultaneous use of infrastructure (i.e., on the competitive but not on the monopolistic segment), decreases the quantity of digital services the lower is  $\phi$ . For example, the time that videos buffer before playing increases or the time that websites take to load and consumers switch away.<sup>21</sup> As firms compete Bertrand-style on the competitive segment, this results in lower advertisement revenues.

**Proposition 7:** Under congestion, investment is given by

$$\begin{cases} k_{V} = \left(\frac{(r\phi/2) - \beta_{V}}{\alpha}\right)^{\frac{1}{\alpha - 1}} & \text{if } k_{I} > k_{V} \\ k_{V} = \left(\frac{a + r - \beta_{V}}{\alpha}\right)^{\frac{1}{\alpha - 1}} & \text{if } k_{V} \ge k_{I} \end{cases} \text{ and } \begin{cases} k_{I} = \left(\frac{r\phi - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}} & \text{if } k_{I} > k_{V} \\ k_{I} = \left(\frac{a + (1 + \phi/2)r - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}} & \text{if } k_{V} \ge k_{I} \end{cases}$$

$$(32)$$

**Proof:** In the Appendix.

<sup>&</sup>lt;sup>21</sup>A leaked e-mail by Mark Zuckerberg about Facebook from February 14, 2008 is instructive about the relationship between transmission quality and the quantity of services consumed: "We have a lot of stats that show that usage of the site is basically tied to how fast the site is. The faster we make the site, the more activity we see. I believe the latest data I saw was that if we made the site 100ms faster we'd have about 3% more activity and if we made the site a second faster we'd have about 20% more activity. That's a really big deal. What it means is that even if users don't consciously notice the speed, it's subconsciously making them do fewer pager views and less activity." The Zuckerberg Files, "Six4Three v. Facebook sealed exhibits", last accessed 27.02.2023.

The overall impact of congestion on the model is low. Investment in the case  $k_I > k_V$  is decreased overall for both V and I. The part of the equations for  $k_I$ ,  $k_V$  related to revenues is multiplied by  $\phi$ . When I has the larger network, the transfer it gets from V reflects that marginal investment by V allows V not only to sell more services but also to escape the "congestion tax" (the term  $k_V(1-\phi/2)r$  in equation 63 is greater than the corresponding term  $k_V(r/2)$  in the base model, equation 11). Interestingly, in the case where  $k_V \geq k_I$ , investment by V is unaffected and investment by I is reduced to a lesser degree: only the part of the expression that pertains to the transfer paid by Q is multiplied by  $\phi$  in equation 61. The intuition is that the transfer  $t_V$  is solely determined by the returns of V on the monopolistic segment which are unaffected by congestion.

### 6.2 Nash-in-Nash bargaining

In the preceding analysis, we have not focused on surplus division between I on the one hand and V and Q on the other hand. In the base model, I proposes a take-it-or-leave-it offer that allows it to extract the entire surplus from the rental of  $k_I$ , only being disciplined by future competition from itself, due to the lack of commitment. Focusing on revenues instead of profits, for example in the analysis of market shares in Section 5.2, has allowed us to side-step this issue.

This assumption is less credible the more we think of the upstream industry as competitive. Nevertheless, intuitively it is not clear that limiting I's ability to extract surplus from the transaction should fundamentally change the model, rather than modifying the marginal-revenue conditions that determine equilibrium investment. Having introduced a source of interdependence of bargaining outcomes in the form of congestion, it seems desirable, however, to study the effect of an alternative surplus-division rule on the outcome of the model.

The Nash-in-Nash bargaining framework seems to be the most reasonable alternative surplus division rule for our model. The model satisfies the conditions of weak conditional decreasing marginal contributions, feasibility, and gains from trade posed by Collard-Wexler, Gowrisankaran, and Lee (2019). Alternative frameworks to intensify competition upstream, such as entry from a competitive fringe or adding one or several additional upstream firms, would require additional assumptions on the timing of investment and combinatorics for the now exponentially increased number of constellations in which V and Q can have access to different subsets of networks. These assumptions may drive results in addition to any potential effect from alternative modes of surplus division, making the model less tractable.

Again we consider the case with congestion, in which demand on the competitive segment is modified by a congestion parameter  $1/2 \le \phi < 1$ . In addition, we define bargaining weights  $0 < \delta_j < 1$ , j = V, Q which represent the share of the surplus that firm I can extract in the negotiation with V and Q, respectively. The impact of these changes on the model is that we now assume agreements in period 2 to occur immediately

and transfers  $t_Q$ ,  $t_V$  to be given by the following expressions:

$$t_Q = \delta_Q \phi k_I(r/2) \tag{33}$$

$$t_{V} = \begin{cases} \delta_{V} (k_{I} \frac{r\phi}{2} + k_{V} (a + r(1 - \frac{\phi}{2}))) & \text{if } k_{I} > k_{V} \\ \delta_{V} k_{I} (a + r) & \text{if } k_{V} \ge k_{I} \end{cases}$$
(34)

**Proposition 8:** In the case with congestion and Nash-in-Nash bargaining, equilibrium investments are given by

$$\begin{cases}
k_{V} = \left(\frac{(1-\delta_{V})a + r(1-\delta_{V}(1+(\phi/2))) - \beta_{V}}{\alpha}\right)^{\frac{1}{\alpha-1}} & \begin{cases}
k_{I} = \left(\frac{(\delta_{V} + \delta_{Q})\frac{r\phi}{2} - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha-1}} & \text{if } k_{I} > k_{V} \\
k_{V} = \left(\frac{a + r - \beta_{V}}{\alpha}\right)^{\frac{1}{\alpha-1}} & \text{if } k_{V} \ge k_{I}
\end{cases}$$

$$\begin{cases}
k_{I} = \left(\frac{\delta_{V}(a + r) + (\delta_{Q}\phi r/2) - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha-1}} & \text{if } k_{V} \ge k_{I}
\end{cases}$$
(35)

**Proof:** In the Appendix.

V's marginal investment when  $k_V \geq k_I$  does not depend on  $\delta_V$ . When  $k_I > k_V$ , however, V's investment now also depends on a as I no longer extracts the whole surplus on this margin. The new expressions reinforce the intuition about the cases in which V's profit drives investment by V and I, respectively. Unsurprisingly, I is now left with lower investment incentives although cases in which I over-invests are still possible (but ruled out in cases where  $\delta_V + \frac{\delta_Q \phi}{2} \leq 1$ .

Overall, modeling surplus division via Nash-in-Nash bargaining makes the model

Overall, modeling surplus division via Nash-in-Nash bargaining makes the model richer as it highlights the cases in which individual parameters do (a for V in the case  $k_I > k_V$ ) or don't ( $\delta_V$  for V's investment in the case  $k_V \ge k_I$ ) matter. It does not fundamentally change the model however, reassuring us that the upstream monopoly is a relatively innocent assumption.

#### 6.3 Product differentiation

Finally, we are interested how the introduction of product differentiation impacts the model. Until now, V and Q have offered undifferentiated services in the downstream market. On the competitive segment, consumers view their offers as perfect substitutes. Now, we consider that consumers have an innate preference for the products offered by one firm or the other. This may be due to personal preference, for example, as a result of branding, or differentiated product offering, such as exclusive content in the case of video-streaming platforms.

We follow the well-known framework of Shubik and Levitan (1980) for a differentiated goods model. This framework has the advantage that the total market size is unaffected by the number of products or their degree of substitutability. We have already considered a modification of total market size through congestion which shrinks the total amount of services sold on the competitive segment of the downstream market. We maintain both congestion and Nash-in-Nash bargaining as in the previous two subsections.

Denoting the degree of substitutability  $\mu \in [0, \infty]$  for n = 2 products (digital services by firms V and Q, respectively), following the notation of Motta (2004) with a as the demand scaling parameter, we write indirect demand for i = V, Q as

$$p_{i,c} = a - \frac{1}{1+\mu} \left( nq_i + \mu \sum_{j=1}^n q_j \right),$$
 (36)

and direct demand as

$$d_{i,c} = \frac{1}{n} \left[ a - p_i(1+\mu) + \frac{\mu}{n} \sum_{j=1}^n p_j \right].$$
 (37)

We leave demand on the monopolistic segment unaffected. On the competitive segment, price competition will now not generally result in marginal-cost pricing because a firm that increases its price above marginal cost will still face positive demand. However, due to the presence of advertisement revenues r, it is not clear that this price increase will be profitable. It could be that the marginal loss of advertisement revenue, which is linear in  $q_{i,c}$ , outweighs the marginal gain from a price increase for any price above marginal cost.

Under price competition for two firms and interpreting r as a negative marginal cost (as in Gans, 2022), equilibrium prices are

$$p_{i,c} = \frac{2a - r(2 + \mu)}{4 + \mu} \tag{38}$$

First, note that if advertisement revenues are too large, firms will indeed lower their price below marginal cost (0). As the model only allows non-negative prices, to rule out this case, we impose

$$r < \frac{2a}{2+\mu}. (39)$$

**Proposition 9:** Equilibrium investments are now given by

$$\begin{cases}
k_{I} = \left(\frac{(\delta_{Q} + \delta_{V}) \frac{\phi}{2} \left(\frac{2a + 2r}{4 + \mu}\right) - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}} \\
k_{I} = \left(\frac{\delta_{Q} \frac{\phi(a + r)}{4 + \mu} + \delta_{V} \left(\frac{4 + (a + r)(\mu - \phi)}{4 + \mu}\right)}{\alpha}\right)
\end{cases}
\begin{cases}
k_{V} = \left(\frac{a + r - \delta_{V} \left(\frac{4 + (a + r)(\mu - 2\phi)}{4 + \mu}\right) - \beta_{V}}{\alpha}\right)^{\frac{1}{\alpha - 1}} \text{ if } k_{I} > k_{V} \\
k_{V} = \left(\frac{a + r - \beta_{V}}{\alpha}\right)^{\frac{1}{\alpha - 1}} \text{ if } k_{V} \ge k_{I}
\end{cases}$$
(40)

The  $k_I > k_V$ -equilibrium arises if

$$\beta_I \ge \beta_V + \delta_Q \left( \frac{\phi(a+r)}{4+\mu} \right) + \delta_V \left( \frac{4+(a+r)(\mu-\phi)}{4+\mu} \right) - (a+r) \tag{41}$$

and the  $k_V \geq k_I$ -equilibrium arises otherwise.

#### **Proof:** In the Appendix.

The resulting expressions for equilibrium investment levels and the parameter thresholds that give rise to the different equilibria are now more complicated but have some interesting properties. The new parameter  $\mu$  does not merely shift all outcomes. Product differentiation always increases the share of the surplus that I can capture when  $k_I > k_V$ . In the case  $k_V \ge k_I$ , it also increases  $t_Q$  but decreases (increases) the share captured by I from V if a + r > (<) 1. Notably, investment by V is still at the efficient level if  $k_V \ge k_I$ . When  $k_I > k_V$ , the deviation from the efficient level of  $k_V$  is governed by the share of surplus captured by V and only this part is affected by congestion (the intuition for which was given in the previous section) and product differentiation.

#### 6.4 Discussion

The key prediction of the model is a change in the relationship between the traditional carriers of data on the Internet and vertically integrated platform companies. Depending on the role that the upstream firm plays for the vertically integrated firm's value creation, we observe a drastic, non-continuous change in investment incentives. I argue that this mechanism points to issues beyond digital services. Collaborations between digital platform companies and other industries, such as the automotive industry, have led to fears about the future focus of value creation. This model shows that the shift in outside options through vertical integration can have a disruptive impact on an industry.

This model is intended as a first attempt to analyze the questions posed by the vertical integration of digital platforms through proprietary infrastructures. Both competition in downstream markets as well as Internet infrastructure are complex and technical issues, and sector-specific regulation differs between Europe, North America, and other regions of the world. As such, it is not the purpose of this model to predict exactly the behavior and contracts that will arise in any specific geographic or product market. Instead, the model illustrates key features of proprietary Internet infrastructure: the potential efficiency and new goods and services provided by big tech investment, but also the interaction in the market place with smaller players which can be harmed by well-intended regulation or marginalized through increased efficiency.

The setup is standard except for the way that upstream investment determines the size of the downstream market. Intuitively, this one-dimensional measure of consumer demand can be read either as the intensive margin of demand (existing customers demanding additional services as bandwidth increases) or the extensive margin of demand (new customers are won as networks improve and bandwidth increases). For a more stringent exposition, I have focused only on the first interpretation in this paper but note that investment can also affect the extensive margin, especially for new services.

I make several simplifications for the purpose of approaching this complex environment. This model illustrates the incentives for a large digital services company to invest in proprietary Internet infrastructure. Even when applying this model to an example as specific as video-on-demand streaming, we are still folding several kinds of differentiated products downstream and different kinds of infrastructure upstream into a simple framework that relates the amount of the available infrastructure to the effective quantity of services that can be provided.

What is k? We are looking at proprietary networks that consist of many different parts. For the purpose of this model, we are not interested, for example, what share of investment goes towards data centers vs. submarine cables. Instead, we are interested in the service improvement that can be purchased at a given price. Therefore, infrastructure k can be thought of as a measure of real quality gain from a given level of investment. This only requires downstream demand to be at least somewhat elastic to the quality improvement induced by investment which seems a reasonable assumption (see also Footnote 21).

The 1:1 ratio between investment and downstream capacity is a free variable, as even relatively inelastic consumer demand can be expressed in the slope of  $c_i(k_i)$ . A steep investment cost function means that it is very costly to expand the market through further investment, and a low elasticity of demand with respect to quality improvements implies that large investments are needed to expand downstream demand. The main assumptions on investment in the model are therefore that investment costs are convex (increasing demand through additional infrastructure becomes more expensive as efficient and low-cost investment opportunities are realized) and potentially different for I and V.

The model is balanced on a "knive's edge" as for given  $\beta_I$  there is only one value of  $\beta_V$  that gives rise to the two types of equilibria that we compare in our analysis. The key mechanism, also throughout the robustness checks, is the change in the outside option. A more elegant but much more complicated approach would assume that the own-price elasticity of demand differs along the dimension of  $q_i$  independent of whether a particular level of infrastructure is reached by one firm or many, and potentially decreases at higher levels of  $q_i$ . This would also generate higher markups in the area where the vertically integrated firm does not face competition. This kind of demand could correspond to markets where infrastructure supports innovative and novel services that have fewer alternatives than basic ones.

This alternative formulation might be useful to model the entire ecosystem of a large digital services company, where the range of services offered through increasingly sophisticated infrastructure could range from e-mail, over online search, and real-time virtual realities (a "Metaverse") to future technologies. Such a demand structure would, however, assume the existence of a wider market with substitutes of varying qualities for all kinds of services offered by such a firm. For a tighter exposition and a more specific example, I choose to concentrate on a market in which the consumers' choice of options is always well-defined, as each segment of demand represents a product that is offered either by a monopolist or a Bertrand oligopolist and an outside option of 0.

The most promising avenue for future research appears to be innovation in proprietary networks: While the motivation to study proprietary networks is partly also the ability of platforms to steer innovation in their ecosystems, innovation is not an explicit feature of the model. In part, the increased demand as a result of increased investment can be understood as demand for innovative services that only become feasible with increased infrastructure. However, a practical concern around proprietary networks owned by big tech firms (e.g., deployment of software products through the cloud services of firms such as Microsoft, Amazon, Google) is that innovation might shift into their "walled gardens", decreasing overall benefits from innovation by limiting spillover and network effects.

# 7 Conclusion

The Internet has affected the global economy on many levels. It has enabled some platform businesses to grow to spectacular size in a short amount of time. Understanding the economics underpinning its infrastructure is key to successful economic policy and regulation. In particular, an effects-based assessment of regulation, potential anticompetitive conduct and merger review needs economic guidance. This paper illustrates the economic effects of the increasing vertical integration into Internet infrastructure by digital platform companies.

The model illustrates investment incentives for Internet infrastructure that impacts competition in a digital market downstream. I show that investment incentives increase both for a pure upstream player and a vertically integrated firm when the latter owns more infrastructure. The intuition is that in this case, the vertically integrated firm has market power over the additional demand generated by its investment even absent the additional infrastructure from the infrastructure firm.

Marginal investment by the infrastructure firm increases the total surplus to be shared between it and the vertically integrated firm. As each unit of upstream investment results in a constant increase in revenue for the vertically integrated firm, the infrastructure of the infrastructure firm becomes fully commoditized. An important exception is the case when the infrastructure firm has lower investment costs and fringe players cannot compete with the vertically integrated firm over the whole range of services, for example because of a lack of technical ability, patents or exclusive content. In this case, the vertically integrated firm may prefer to subsidize investment by the infrastructure firm directly. At least in this model, there is no market failure and no need for intervention for this to happen.

As a consequence, this model explains different aspects of the rise of private, proprietary infrastructure. I predict that this additional investment is socially desirable but might increase the market shares of the largest companies. High market shares are not problematic per se but often serve as shortcuts to market power analysis by competition authorities. Under specific circumstances, such as incomplete capital markets, present strength can beget future strength, however, justifying a concern about the market structure of the downstream market.

Expanding net neutrality, a pet policy of some Internet activists, to the infrastructure firms currently not covered, may lead to exclusion of rivals and harm to consumers. Entry downstream by the upstream firm may also have the surprising effect of reducing the amount of downstream services whenever the newly vertically integrated firm prefers infrastructure separation, yielding the inefficient outcome that does not occur in the equilibrium of the base model.

Caution is advised before drawing policy conclusions from a literal reading of the model. It is understood that this model is not a full simulation of any particular downstream market with its generic features such as paid-for premium services and advertisement revenues. Nor does it necessarily describe the market structure for the upstream industry. Instead I purposefully aggregate infrastructure investment into a black box

variable to study the effect of quality-improving infrastructure investment. Intervention in any particular market would need to carefully evaluate the sources of revenue and business models of firms in the downstream market and to identify the most important components of Internet infrastructure related to an industry.

Nevertheless, this paper can help policy makers and enforcers ask the right questions both for a competitive analysis of a digital market and for a forward-looking market investigation: First, it describes how even efficient and increasing investment in proprietary and public networks can enhance the unequal footing on which vertically integrated firms and smaller rivals compete. Second, it illustrates the kingmaker role of third-party infrastructure providers, especially when they become active downstream themselves.

Finally, the model points at questions beyond digital services. Large technology firms have begun vertical integration in other fields, including automotive, where questions about the future focus of value creation have also been asked. The model allows for many rich expansions as discussed above. In addition, the analysis can be expanded by appropriate data to test model predictions empirically.

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## A Proofs

### A.1 Proof of Theorem 2

For given  $\beta_V$ ,  $\beta_I$ , we can write social welfare when  $k_V \geq k_I$  as

$$S|_{k_{V} \geq k_{I}} = (a+r) \left[ \left( \frac{a + \frac{3}{2}r - \beta_{I}}{\alpha} \right)^{\frac{1}{\alpha-1}} + \left( \frac{a+r - \beta_{V}}{\alpha} \right)^{\frac{1}{\alpha-1}} \right]$$

$$- \left[ \left( \frac{a + \frac{3}{2}r - \beta_{I}}{\alpha} \right)^{\frac{\alpha}{\alpha-1}} + \beta_{I} \left( \left( \frac{a + \frac{3}{2}r - \beta_{I}}{\alpha} \right)^{\frac{1}{\alpha-1}} - k_{0} \right) \right]$$

$$- \left[ \left( \frac{a+r - \beta_{V}}{\alpha} \right)^{\frac{\alpha}{\alpha-1}} + \beta_{V} \left( \left( \frac{a+r - \beta_{V}}{\alpha} \right)^{\frac{1}{\alpha-1}} - k_{0} \right) \right]$$

$$(42)$$

while if the inequality is reversed, we have

$$S|_{k_I > k_V} = (a+r) \left[ \left( \frac{r-\beta_I}{\alpha} \right)^{\frac{1}{\alpha-1}} + \left( \frac{r/2 - \beta_V}{\alpha} \right)^{\frac{1}{\alpha-1}} \right]$$

$$- \left[ \left( \frac{r-\beta_I}{\alpha} \right)^{\frac{\alpha}{\alpha-1}} + \beta_I \left( \left( \frac{r-\beta_I}{\alpha} \right)^{\frac{1}{\alpha-1}} - k_0 \right) \right]$$

$$- \left[ \left( \frac{r/2 - \beta_V}{\alpha} \right)^{\frac{\alpha}{\alpha-1}} + \beta_V \left( \left( \frac{r/2 - \beta_V}{\alpha} \right)^{\frac{1}{\alpha-1}} - k_0 \right) \right]$$

$$(43)$$

Now, for  $S|_{k_V \ge k_I} - S|_{k_I > k_V} > 0$ , it must be that

$$(a+r)\left(\left[\frac{2a+\frac{5}{2}r-\beta_{I}-\beta_{V}}{\alpha}\right]^{\frac{1}{\alpha-1}}-\left[\frac{\frac{3}{2}r-\beta_{I}-\beta_{V}}{\alpha}\right]^{\frac{1}{\alpha-1}}\right)$$
(44)
$$-\left[\left(\frac{a+\frac{3}{2}r-\beta_{I}}{\alpha}\right)^{\frac{\alpha}{\alpha-1}}+\beta_{I}\left(\frac{a+\frac{3}{2}r-\beta_{I}}{\alpha}\right)^{\frac{1}{\alpha-1}}\right]$$

$$-\left[\left(\frac{a+r-\beta_{V}}{\alpha}\right)^{\frac{\alpha}{\alpha-1}}+\beta_{V}\left(\frac{a+r-\beta_{V}}{\alpha}\right)^{\frac{1}{\alpha-1}}\right]$$

$$+\left(\frac{r-\beta_{I}}{\alpha}\right)^{\frac{\alpha}{\alpha-1}}+\beta_{I}\left(\frac{r-\beta_{I}}{\alpha}\right)^{\frac{\alpha}{\alpha-1}}+\left(\frac{\frac{r}{2}-\beta_{V}}{\alpha}\right)^{\frac{\alpha}{\alpha-1}}+\beta_{V}\left(\frac{\frac{r}{2}-\beta_{V}}{\alpha}\right)^{\frac{1}{\alpha-1}}>0$$

$$\leftrightarrow (a+r)\left[\frac{2a+r}{\alpha}\right]^{\frac{1}{\alpha-1}}-\left(\frac{2a+r}{\alpha}\right)^{\frac{\alpha}{\alpha-1}}-\beta_{I}\left(\frac{a+\frac{r}{2}}{\alpha}\right)^{\frac{1}{\alpha-1}}-\beta_{V}\left(\frac{a+\frac{r}{2}}{\alpha}\right)^{\frac{1}{\alpha-1}}>0$$
(45)
$$\leftrightarrow (a+r)^{\alpha-1}\left[\frac{2a+r}{\alpha}\right]>\left[\frac{2a+r}{\alpha}\right]^{\alpha}+(\beta_{I}+\beta_{V})^{\alpha-1}\left(\frac{a+\frac{r}{2}}{\alpha}\right)$$
(46)

which is the expression in the proposition.

#### A.2 Proof of proposition 3

Substitute the expressions from equations 16, 20 into

$$MS_{Q}^{**} - MS_{Q}^{*} = \frac{k_{I}^{*}/2}{k_{I}^{**} + (1 + a/r)k_{V}^{**}} - \frac{k_{I}^{*}/2}{k_{I}^{*} + (1 + a/r)k_{V}^{*}}$$

$$= \frac{\frac{1}{2} \left(\frac{a + \frac{3r}{2} - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}}}{\left(\frac{a + \frac{3r}{2} - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}}} + \left(1 + \frac{a}{r}\right) \left(\frac{a + r - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}}} - \frac{\frac{1}{2} \left(\frac{r - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}}}{\left(\frac{r - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}}} + \left(1 + \frac{a}{r}\right) \left(\frac{\frac{r}{2} - \beta_{V}}{\alpha}\right)^{\frac{1}{\alpha - 1}}}$$

$$= \frac{1}{2} \left(\frac{a + \frac{3}{2}r - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}} \left[\left(\frac{r - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}} + \left(1 + \frac{a}{r}\right) \left(\frac{\frac{r}{2} - \beta_{V}}{\alpha}\right)^{\frac{1}{\alpha - 1}}\right]$$

$$- \frac{1}{2} \left(\frac{r - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}} \left[\left(\frac{a + \frac{3r}{2} - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}} + \left(1 + \frac{a}{r}\right) \left(\frac{a + r - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}}\right]$$

$$= \left(a + \frac{3}{2}r - \beta_{I}\right) \left(r - \beta_{I} + \left(1 + \frac{a}{r}\right)^{\alpha - 1} \left(\frac{r}{2} - \beta_{V}\right)\right)$$

$$- \left(r - \beta_{I}\right) \left[a + \frac{3}{2}r - \beta_{I} + \left(1 + \frac{a}{r}\right)^{\alpha - 1} \left(a + r - \beta_{I}\right)\right]$$

which, after multiplying out the brackets and some simplifications, becomes

$$\left(a + \frac{3r}{a} - \beta_I\right) \left(\frac{r}{2} - \beta_V\right) - (r - \beta_I)(a + r - \beta_I)$$

$$= -\frac{ra}{2} - \frac{r^2}{4} + \beta_I \frac{r}{2} + (\beta_I - \beta_V)a + \beta_I - \beta_V \frac{3}{2}r + \beta_I \beta_V - \beta_I^2.$$
(48)

As we consider the case where both equilibria can exist, we substitute  $\beta_V = \beta_I - \frac{r}{2}$ .

$$-\frac{ra}{2} - \frac{r^2}{4} + \beta_I \frac{r}{2} + (\beta_I - \beta_I + \frac{r}{2})a + \beta_I r - \frac{3}{2}\beta_I r - \frac{3}{4}r + \beta_I^2 - \beta_I \frac{r}{2} - \beta_I^2$$

$$= -\frac{r^2}{4} - \frac{3}{4}r - \beta_I \frac{r}{2}$$

$$(49)$$

which is clearly negative, given that r > 0,  $\beta_I > 0$ , proving the proposition.

#### A.3 Proof of proposition 4

First, note that in the case without commitment, at the third stage, M will always compete downstream, so  $q_M = k_M$  because doing so strictly increases M's profit, at least by  $k_M(r/2)$  if  $k_M \leq k_V$  and  $k_M(r/2) + max(0, (k_M - k_V)(a + r/2))$  otherwise, while withholding its capacity at the third stage yields no profit. Anticipating this, the highest transfer  $t_V$  that V is willing to pay is the difference between the profit with or without  $k_M$  given that the competitive segment downstream will be  $k_M$  if V agrees

to rent access to M's infrastructure or  $k_V$  if it does not and  $k_V \leq k_M$ . But then the analysis is equivalent to the base model with  $k_I$  instead of  $k_M$ .

In the case with commitment, if  $k_M > k_V$ , offering  $q_M = k_M$  limits M to charge  $t_V \leq (k_M - k_V) \frac{r}{2} + k_V (a+r)$ , or the additional profit V would make competing when M's infrastructure is larger. If M commits to  $q_M = 0$ , the highest transfer  $t_V$  that V would accept is  $k_M(a+r)$ . There are only these two candidate values of  $q_M$  as profits and the highest transfer  $t_V$  are linear in the value of  $q_M$  that M offers. Comparing profit under these two candidate commitments, we find

$$k_M(a+r) > k_M \frac{r}{2} + k_V(a + \frac{r}{2})$$
 (50)

which is true only if  $k_M > k_V$ . The proposition follows from this.

## A.4 Proof of proposition 6

There are two candidate prices for t, either the highest price that both Q and V are willing to pay or the highest price that a single firm is willing to pay. The highest price that both Q and V are willing to pay must be  $min(k_I(r/2), (k_I+k_V)(r/2)+max(0, (k_V-k_I)(a+r/2))$ , that is, Q's revenue under competition,  $k_I(r/2)$ . The highest revenue that V could make renting  $k_I$  is the monopoly profit  $k_I(a+r)$  which is evidently higher. The highest revenue that Q could make, given  $k_V$ , is  $k_I(r/2) + max(0, (k_I - k_V)(a + r/2))$ . This is lower than  $k_I(a+r)$  for all  $k_V > 0$ . Whenever V sets  $k_V > 0$ , only V will accept. By setting  $t = k_I(a+r)$ , I ensures that V agrees to rent at the proposed price. Off-path, V never has an incentive to choose  $k_V = 0$  as  $c'_V(0) = \beta_V$  which is smaller than the marginal revenue of r/2 by assumption.

#### A.5 Proof of proposition 7

We now analyze the model and its applications under congestion. Third stage prices conditional on available infrastructure remain unchanged: as products are still perfect substitutes and marginal costs are zero, the only prices that can emerge in equilibrium are  $p_{V,c} = p_{Q,c} = 0$ . However, revenues on this segment are now lower. Given that both firms rent access to I's infrastructure, V's price on the monopolistic segment remains unchanged at  $p_{V,m} = a$ .

The resulting profits are

$$\Pi_Q = \phi k_I(r/2) - t_Q \tag{51}$$

$$\Pi_V = \phi k_I(r/2) + (a+r)k_V - t_V - c_V(k_V)$$
(52)

Following the analysis from the base model, resulting transfers are

$$t_O = \phi k_I(r/2) \tag{53}$$

$$t_{V} = \begin{cases} k_{I} \frac{r\phi}{2} + k_{V} \left( a + r(1 - \frac{\phi}{2}) \right) & \text{if } k_{I} > k_{V} \\ k_{I}(a+r) & \text{if } k_{V} \ge k_{I} \end{cases}$$

$$(54)$$

Note that the expression for  $t_V$  if  $k_V \ge k_I$  is identical to the base model but if  $k_I > k_V$ , the expression for the transfer is different and lower.<sup>22</sup> In particular, the contribution of  $k_I$  to the transfer that I can demand is now lower, as each additional unit of  $k_I$  that increases the competitive segment has a lower return due to congestion. At the same time, the return to investment by V is higher because an increase in  $k_V$  and therefore an expansion of V's monopolistic segment allows V not only to escape competition with Q but also to escape the congestion "tax".

The resulting first-period investments follow:

$$\max_{k_V} \Pi_V = d'_{V,c}(p_{V,c} + r) + d'_{V,m}(p_{V,m} + r) - t_V - c_V(k_V)$$
(55)

$$\frac{\partial \Pi_V}{\partial k_V} = a + r - c_V'(k_V) - \frac{\partial t_V}{\partial k_V} = 0 \tag{56}$$

$$\frac{\partial t_V}{\partial k_V} = \begin{cases} a + r(1 - \frac{\phi}{2}) & \text{if } k_I > k_V \\ 0 & \text{if } k_V \ge k_I \end{cases}$$
 (57)

$$\frac{\partial \Pi_V}{\partial k_V} = \begin{cases} c_V'(k_V) = \frac{r\phi}{2} \\ c_V'(k_V) = a + r \end{cases} \leftrightarrow \begin{cases} k_V = \left(\frac{r\phi - \beta_V}{2\alpha}\right)^{\frac{1}{\alpha - 1}} & \text{if } k_I > k_V \\ k_V = \left(\frac{a + r - \beta_V}{\alpha}\right)^{\frac{1}{\alpha - 1}} & \text{if } k_V \ge k_I \end{cases}$$
(58)

$$\max_{k_I} \Pi_I = t_Q + t_V - c_I(k_I) \tag{59}$$

$$\frac{\partial \Pi_I}{\partial k_I} = \frac{\phi r}{2} + \frac{\partial t_V}{\partial k_I} - c_I'(k_I) \tag{60}$$

$$= \begin{cases} c'_{I}(k_{I}) = r\phi \\ c'_{I}(k_{I}) = a + (1 + \phi/2)r \end{cases} \leftrightarrow \begin{cases} k_{I} = \left(\frac{r\phi - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}} & \text{if } k_{I} > k_{V} \\ k_{I} = \left(\frac{a + (1 + \phi/2)r - \beta_{I}}{\alpha}\right)^{\frac{1}{\alpha - 1}} & \text{if } k_{V} \ge k_{I} \end{cases}$$

$$(61)$$

#### A.6 Proof of proposition 8

Working from the expressions for  $t_V$ ,  $t_Q$ ,

$$t_Q = \delta_Q \phi k_I(r/2) \tag{62}$$

$$t_{V} = \begin{cases} \delta_{V} \left( k_{I} \frac{r\phi}{2} + k_{V} \left( a + r \left( 1 - \frac{\phi}{2} \right) \right) \right) & \text{if } k_{I} > k_{V} \\ \delta_{V} k_{I} (a + r) & \text{if } k_{V} \ge k_{I} \end{cases}$$
 (63)

Which can be easily seen from solving  $(k_V + k_I)\frac{1}{2} > k_I\frac{\phi}{2} + k_V(1-\frac{\phi}{2}) \leftrightarrow k_I\frac{1-\phi}{2} > k_V\frac{1-\phi}{2}$  which is true when  $k_I > k_V$ .

we work out the resulting first-period investments:

$$\frac{\partial t_V}{\partial k_V} = \begin{cases} \delta_V \left( a + r \left( 1 - \frac{\phi}{2} \right) \right) & \text{if } k_I > k_V \\ 0 & \text{if } k_V \ge k_I \end{cases}$$
 (64)

$$\frac{\partial \Pi_V}{\partial k_V} : \begin{cases} c_V'(k_V) = (1 - \delta_V)a + r\left(1 - \delta_V\left(1 + \frac{\phi}{2}\right)\right) & \text{if } k_I > k_V \\ c_V'(k_V) = a + r & \text{if } k_V \ge k_I \end{cases}$$
(65)

(66)

Using the cost function, we obtain the following levels of investment:

$$\leftrightarrow \begin{cases}
k_V = \left(\frac{(1-\delta_V)a + r(1-\delta_V(1+(\phi/2))) - \beta_V}{\alpha}\right)^{\frac{1}{\alpha-1}} & \text{if } k_I > k_V \\
k_V = \left(\frac{a + r - \beta_V}{\alpha}\right)^{\frac{1}{\alpha-1}} & \text{if } k_V \ge k_I
\end{cases}$$
(67)

Similarly for firm I:

$$\frac{\partial \Pi_I}{\partial k_I} = \frac{\partial t_Q}{\partial k_I} + \frac{\partial t_V}{\partial k_I} - c_I'(k_I) \tag{68}$$

$$\frac{\partial t_Q}{\partial k_I} = \frac{\delta_Q \phi r}{2} \tag{69}$$

$$\frac{\partial \Pi_I}{\partial k_I} : \begin{cases} c_I'(k_I) = (\delta_V + \delta_Q) \frac{r\phi}{2} & \text{if } k_I > k_V \\ c_I'(k_I) = \delta_V(a+r) + \frac{\delta_Q\phi_I}{2} & \text{if } k_V \ge k_I \end{cases}$$
(70)

(71)

Using the cost function, we obtain the following levels of investment:

$$\leftrightarrow \begin{cases}
k_I = \left(\frac{(\delta_V + \delta_Q)\frac{r\phi}{2} - \beta_I}{\alpha}\right)^{\frac{1}{\alpha - 1}} & \text{if } k_I > k_V \\
k_I = \left(\frac{\delta_V(a + r) + (\delta_Q \phi r/2) - \beta_I}{\alpha}\right)^{\frac{1}{\alpha - 1}} & \text{if } k_V \ge k_I
\end{cases}$$
(72)

# A.7 Proof of proposition 9

V and Q charge identical prices on the competitive segment and face demand  $d'_{V,c} = d'_{Q,c} = \phi k_I/2$ . From this, we can compute third-period profits for given transfers and

infrastructure size.

$$\Pi_{Q} = \phi \frac{k_{I}}{2} (p_{Q,c} + r) - t_{Q} 
= \phi \frac{k_{I}}{2} \left( \frac{2a + 2r}{4 + \mu} \right) - t_{Q}$$
(73)

$$\Pi_{V} = \phi \frac{k_{I}}{2} (p_{V,c} + r) + (r+a)k_{V} - t_{V} - c_{V}(k_{V}) 
= \phi \frac{k_{I}}{2} \left( \frac{2a+2r}{4+\mu} \right) + (r+a)k_{V} - t_{V} - c_{V}(k_{V})$$
(74)

(75)

Given these profits, we can now write transfers

$$t_Q = \delta_Q \phi \frac{k_I}{2} \left( \frac{2a + 2r}{4 + \mu} \right) \tag{76}$$

$$t_{V} = \begin{cases} \delta_{V} \left( \frac{2a+2r}{4+\mu} \phi \frac{k_{I}}{2} + k_{V} \frac{4+(a+r)(\mu-2\phi)}{4+\mu} \right) & \text{if } k_{I} > k_{V} \\ \delta_{V} k_{I} \left( \frac{4+(a+r)(\mu-\phi)}{4+\mu} \right) & \text{if } k_{V} \ge k_{I} \end{cases}$$
 (77)

Finally, first period investment follows from the FOC:

$$\frac{\partial t_V}{\partial k_V} = \begin{cases} \delta_V \frac{4 + (a+r)(\mu - 2\phi)}{4 + \mu} & \text{if } k_I > k_V \\ 0 & \text{if } k_V \ge k_I \end{cases}$$
 (78)

$$\frac{\partial \Pi_V}{\partial k_V} : \begin{cases} c_V'(k_V) = r + a - \delta_V \left( \frac{4 + (a+r)(\mu - 2\phi)}{4 + \mu} \right) & \text{if } k_I > k_V \\ c_V'(k_V) = a + r & \text{if } k_V \ge k_I \end{cases}$$
 (79)

Similarly for firm I:

$$\frac{\partial \Pi_I}{\partial k_I} = \frac{\partial t_Q}{\partial k_I} + \frac{\partial t_V}{\partial k_I} - c_I'(k_I) \tag{80}$$

$$\frac{\partial t_Q}{\partial k_I} = \frac{\delta_Q \phi}{2} \left( \frac{2a + 2r}{4 + \mu} \right) \tag{81}$$

$$\frac{\partial \Pi_I}{\partial k_I} : \begin{cases}
c_I'(k_I) = (\delta_Q + \delta_V) \frac{\phi}{2} \left(\frac{2a+2r}{4+\mu}\right) & \text{if } k_I > k_V \\
c_I'(k_I) = \delta_Q \frac{\phi}{2} \left(\frac{2a+2r}{4+\mu}\right) + \delta_V \left(\frac{4+(a+r)(\mu-\phi)}{4+\mu}\right) & \text{if } k_V \ge k_I
\end{cases}$$
(82)

The parameter values underpinning the  $k_I > k_V$  equilibrium are:

$$k_I = \left(\frac{(\delta_Q + \delta_V)\frac{\phi}{2}\left(\frac{2a+2r}{4+\mu}\right) - \beta_I}{\alpha}\right)^{\frac{1}{\alpha-1}}$$
(83)

$$k_V = \left(\frac{r + a - \delta_V \left(\frac{4 + (a + r)(\mu - 2\phi)}{4 + \mu}\right) - \beta_V}{\alpha}\right)^{\frac{1}{\alpha - 1}}$$
(84)

$$k_I > k_V \leftrightarrow$$
 (85)

$$(\delta_Q + \delta_V) \frac{\phi}{2} \left( \frac{2a + 2r}{4 + \mu} \right) - \beta_I > r + a - \delta_V \left( \frac{4 + (a + r)(\mu - 2\phi)}{4 + \mu} \right) - \beta_V \leftrightarrow \tag{86}$$

$$\beta_V > \beta_I + (\delta_Q + \delta_V) \frac{\phi}{2} \left( \frac{2a + 2r}{4 + \mu} \right) + r + a - \delta_V \left( \frac{4 + (a + r)(\mu - 2\phi)}{4 + \mu} \right) \leftrightarrow \tag{87}$$

$$\beta_V > \beta_I + r + a + \delta_Q \left( \frac{\phi(a+r)}{4+\mu} \right) - \delta_V \left( \frac{4 + (a+r)(\mu - \phi)}{4+\mu} \right) \tag{88}$$

And for the  $k_V \geq k_I$  equilibrium:

$$k_I = \left(\frac{\delta_Q \frac{\phi(a+r)}{4+\mu} + \delta_V \left(\frac{4+(a+r)(\mu-\phi)}{4+\mu}\right)}{\alpha}\right)$$
(89)

$$k_V = \left(\frac{a + r - \beta_V}{\alpha}\right)^{\frac{1}{\alpha - 1}} \tag{90}$$

$$k_V \ge k_I \leftrightarrow a + r - \beta_V \ge \delta_Q \left( \frac{\phi(a+r)}{4+\mu} \right) + \delta_V \left( \frac{4 + (a+r)(\mu - \phi)}{4+\mu} \right) - \beta_I$$
 (91)

$$\beta_I \ge \beta_V + \delta_Q \left( \frac{\phi(a+r)}{4+\mu} \right) + \delta_V \left( \frac{4 + (a+r)(\mu - \phi)}{4+\mu} \right) - (a+r)$$
(92)

(93)

# B Submarine cable ownership

In this Section I present data on submarine cable ownership by some firms that are traditionally labeled "big tech" firms. The purpose of this exercise is firstly, to motivate the model describing vertical integration by firms offering digital services, and secondly, to justify the assumption that only either very large or specialized infrastructure firms have the scale to make these investments.

Bischof, Fontugne, and Bustamante (2018) describe the increasing role of these firms in the submarine cable infrastructure: "The latest construction boom, however, seems to be driven by content providers, such [as] Google, Facebook, Microsoft, and Amazon. According to Telegeography's Research Director Alan Mauldin, the amount of capacity deployed by content providers has risen 10-fold between 2013 and 2017, outpacing all other customers of international bandwidth."

I analyze data from Telegeography on submarine cables underlying the Submarine Cable Map.<sup>23</sup> The data is publicly available and as of September 2022 contains data on 516 submarine cables. The data set also includes location data on the cables which I do not use. Each observation of the data set includes the name of the cable, its length in kilometers, a list of its owners, a list of suppliers, and the year (and sometimes month) when the cable became or will become ready for service, ranging from 1989 to 2026.

# Description

I search among the list of owners in our data set for Google, Amazon, Meta, Apple, Microsoft, Baidu, Alibaba, and Tencent. These firms are sometimes referred to with catch-all abbreviations such as GAMAM (GAFAM, before Facebook changed its name to Meta in 2021) or BAT. Neither Apple nor any of the BAT firms appear on the list of owners, but only Meta, Microsoft, Google, and Amazon Web Services. However, Alibaba does own terrestrial backbone within Asia (Corneo et al., 2021) Thus I identify cables that have one of the above-mentioned firms among its owners. This does not indicate sole ownership. Indeed, except for 7 purely Google-owned cables, all cables listed here as having "GAMAM owners" have co-owners. This is unsurprising, given that submarine cables typically include several fibre-optic cables and firms can own individual fibres.

I also search the list of owners for other firms and as a general observation, I remark that the list of owners includes mostly telecommunications firms and governments, as well as a few electricity companies, but no other firms that mainly sell digital services. While this is just one example of Internet infrastructure, it is consistent with the data previously collected in the literature (see references in this Section and Section 2) that describes the emergence of proprietary networks as a phenomenon driven by just a few of the largest technology firms.

Extending the range of the data of the previous paper by 7 years, I find that among submarine cables getting ready for service 2022-2024, the share of GAMAM climbs to

<sup>&</sup>lt;sup>23</sup>https://www.submarinecablemap.com/

between 20 and 27% (see Figure 4).<sup>24</sup> This is higher than the share of new cables owned by these first in the previous decade, which only exceeded 20% in one year (2018).

At the same time, the absolute number of new GAMAM-owned cables has quadrupled, from 1.1 new cables per year between 2010 - 2019, to 4.4 new cables for 2020 - 2024 (Figure 5). The overall increase in cables going ready for service has increased by a third during this period, from 15.7 new cables per year to 21 new cables for year. In other words, the cables added with the large technology firms as co-owners contribute more than half of the increase in the number of added cables between the the period before and after 2020. The phenomenon of these firms owning submarine cables is not a recent one, however, with the first such cable registered in 2010. Overall, the data confirms the increasing role of content firms among investors of infrastructure.

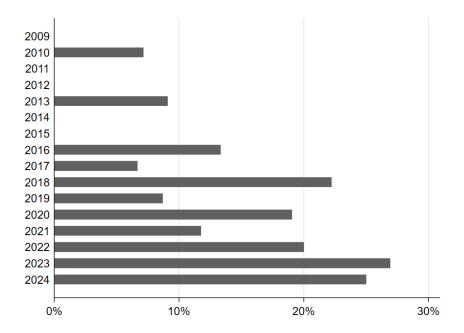


Figure 4: Share of submarine cables with GAMAM owners by ready-for-service date

<sup>&</sup>lt;sup>24</sup>Only 7 announcements have been made regarding cables that are ready for service in 2025 and only 1 for 2026, none of them involving any of the above-mentioned firms.

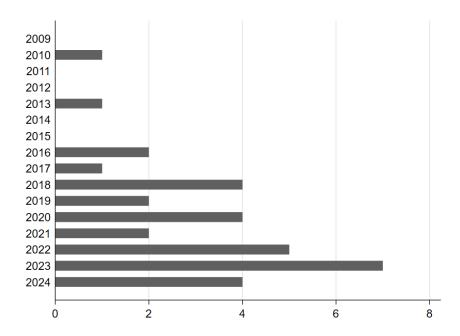


Figure 5: Sum of submarine cables with GAMAM owners by ready-for-service date