

# Deep Neural Network

Philip Hoddinott

December 17, 2018

## Contents

<b>1</b>	<b>Introduction</b>	<b>2</b>
1.1	The MNIST database . . . . .	2
1.2	Artificial neural network . . . . .	2
1.3	Neural Network Walkthrough . . . . .	3
1.3.1	Parameter Initialization . . . . .	3
1.3.2	Forward Propagation . . . . .	3
1.3.3	Compute loss . . . . .	4
1.3.4	Backward propagation . . . . .	4
1.4	Gradient Decent . . . . .	4
1.5	Activation Function . . . . .	5
1.6	Pitfalls . . . . .	5
<b>2</b>	<b>Implementation</b>	<b>6</b>
2.1	Object Oriented Programming in MATLAB . . . . .	6
2.2	MATLAB Code . . . . .	7
<b>3</b>	<b>Results</b>	<b>7</b>
3.1	Simple Neural Net . . . . .	7
3.2	Comparison of different hidden layer sizes . . . . .	7
3.3	Multiple hidden layers . . . . .	8
<b>4</b>	<b>Conclusion</b>	<b>8</b>
	<b>Appendix</b>	<b>9</b>

## List of Figures

1	Sample numbers from MNIST [1]. . . . .	2
2	Visualization of a neural network with one hidden layer [2]. . . . .	3
3	A visualization of forward and backward propagation [3]. . . . .	5
4	Visualization of sigmoid and Tanh function . . . . .	6
5	Run times for various neural network architectures [4]. . . . .	6
6	The results from the simple network for the first 1000 epochs. . . . .	7
7	Net accuracy for different layer sizes. . . . .	8
8	The results from the two layer network for the first 2000 epochs. . . . .	8

## Abstract

The purpose of this report is to develop a neural net that can identify handwritten digits in the MNIST database at near human levels of accuracy. The neural net will be developed without the assistance of libraries such as Python's tensor flow or MATLAB's Deep Learning.

The author would like to express his gratitude to Professor Hicken for the suggestion of this project. The author would also like to thank Theodore Ross and Varun Rao for their assistance with artificial neural networks.

## 1 Introduction

The first computational models for neural networks were thought up in the 1940s, however it would take 50 years for computers to achieve the processing power to implement the first neural networks. Today neural networks can be used for a variety of tasks. One of these tasks is image recognition of numbers.

### 1.1 The MNIST database

The Modified National Institute of Standards and Technology database or MNIST database [5] is a database of handwritten numbers used to train image processing systems. It contains 60,000 training images and 10,000 testing images. The database is comprised of images that are made up of a grid of 28x28 pixels. Some of these are seen in figure 1.

A number of attempts have been made to get the lowest possible error rate on this dataset. As of August 2018 the the lowest achieved so far is a error rate of 0.21% or an accuracy of 99.79%. For comparison human can accurately recognize digits at a rate of 98% - 98.5% [6].

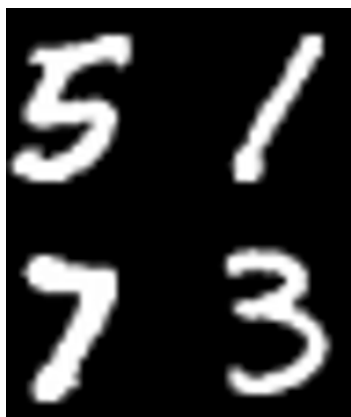


Figure 1: Sample numbers from MNIST [1].

### 1.2 Artificial neural network

An artificial neural network (referred to as a neural network in this paper) is a computation system that mimics the biological neural networks found in animal brains. A neural network is not an algorithm, but a general framework to solve problems. Artificial neural networks are based of layers of interconnected neurons that transmit signals to each other. Neural networks may be trained for tasks, such as the number recognition in this report.

The neural net implemented in this project had an input vector of  $784 \times 1$  and an output vector of  $10 \times 1$ . Different configurations were tried, with one hidden layer of  $250 \times 1$  producing the best results. A visualization of an example neural net is seen in figure 2.

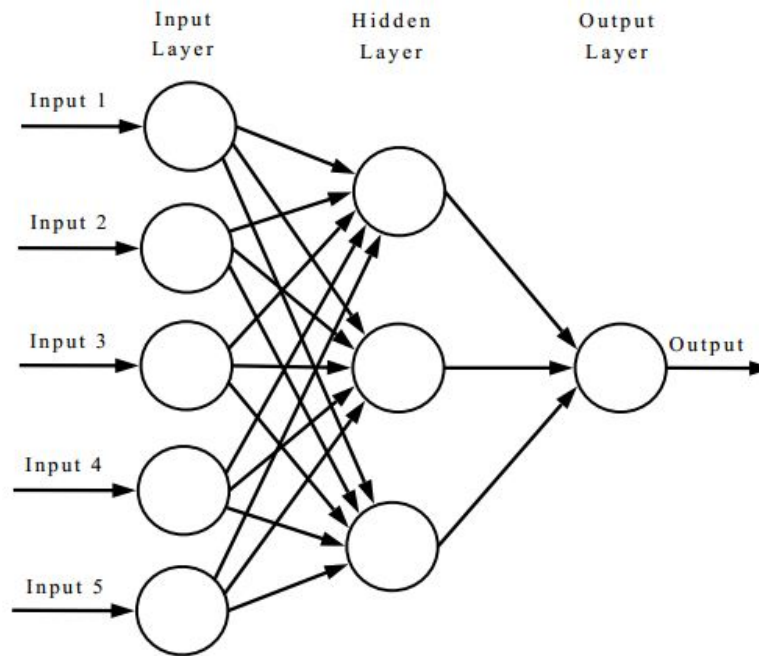


Figure 2: Visualization of a neural network with one hidden layer [2].

### 1.3 Neural Network Walkthrough

The training of a neural network involves four main steps:

1. Initialize weights and biases.
2. Forward propagation
3. Compute the loss
4. Backward propagation

#### 1.3.1 Parameter Initialization

The first step in training a neural net is to initialize the bias vectors and weight matrices. They are initialized with random numbers between 0 and 1, then multiplied by a small scalar around the order of  $10^{-2}$  so that the units are not on the region where the derivative of the activation function are close to zero. The initial parameters should be different values (to keep the gradients from being the same).

There are various forms of initialization such as Xavier initialization or He-et-al Initialization, but a discussion on methods of initialization outside the scope of this paper. In this paper we will stick with random parameter initialization.

#### 1.3.2 Forward Propagation

The next step is the forward propagation. The network takes the inputs from a previous layer, computes their transformation, and applies an activation function. Mathematically the forward propagation at level “i” is represented by equation 1.

$$\begin{aligned} z_i &= A_{i-1} * W_i + b \\ A_i &= \phi(z_i) \end{aligned} \tag{1}$$

Where  $z$  is the input vector,  $A$  is the layer,  $W$  is the weights going into the layer,  $b$  the bias, and  $\phi$  the activation function. This process then repeats for the next layer until it reaches the end of the neural net.

### 1.3.3 Compute loss

The loss is simply the difference between the output and the actual value. In this neural net it is computed by equation 2.

$$\text{loss} = A_{i=\text{end}} - y \tag{2}$$

This loss is used to begin the next step: backward propagation.

### 1.3.4 Backward propagation

After going forward through the neural net in the forward propagation step and computing the loss the final step is backwards propagation. Backwards propagation is the updating of the weight parameters via the derivative of the error function with respect to the weights of the neural net. For the output layer this is seen in equation 3 and equation 4 for all other layers.

$$dW_{i=\text{end}} = \phi'(z_{i=\text{end}}) * (A_{i=\text{end}} - y) \tag{3}$$

$$dW_i = \phi'(z_i) * (W_{(i+1)}^T * dW_{(i+1)}) \tag{4}$$

Once these derivatives have been computed, the weights are updated by equation 5

$$W_i = W_i - \alpha * dW_i * A_{(i-1)}^T \tag{5}$$

Where for the first layer  $z_{(i-1)}^T$  will be the input vector and for all the following layers it will be the vector from the previous layer.

At this point the neural net has completed a full run through. The next input vector is selected and the forward and backward propagation are run again. A visualization of forward and backward propagation is in figure 3.

## 1.4 Gradient Decent

Also known as steepest decent, gradient decent is a first order optimization algorithm. It is used to find the minimum of a function. Equation 6 shows gradient decent implemented in a neural net.

$$\Delta W(t) = -\alpha \frac{\partial E}{\partial W(t)} \tag{6}$$

Where  $\alpha$  is the learning rate, and  $\partial E / \partial W(t)$  is the error derivative with respect to the weight. As these derivatives must be computed for each node the more nodes there are in a neural net the longer it will take to train.

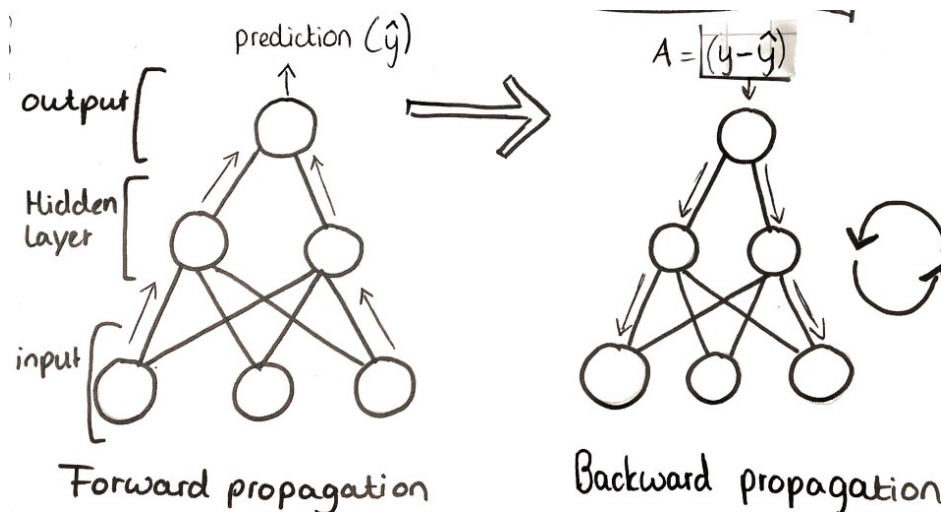


Figure 3: A visualization of forward and backward propagation [3].

## 1.5 Activation Function

The activation function was previously mentioned as a function used to convert the input signal to the output signal. Activation functions introduce non-linear properties to the neural net's functions, allowing the neural net to represent complex functions [3].

The two most common activation functions used in neural nets for the gradient decent are sigmoid and hyperbolic tangent (Tanh). The formula for Tanh is seen in equation 7, and the formula for it's derivative is seen in equation 8

$$\phi_{\text{Tanh}}(z) = \frac{1 - e^{-2z}}{1 + e^{-2z}} \quad (7)$$

$$\phi'_{\text{Tanh}}(z) = \frac{4}{(e^{-z} + e^z)^2} \quad (8)$$

The formula for the sigmoid function is seen in equation 9, the formula for it's derivative is seen in equation 10.

$$\phi_{\text{Sigmoid}}(z) = \frac{1}{1 + e^{-z}} \quad (9)$$

$$\phi'_{\text{Sigmoid}}(z) = \frac{e^{-z}}{(e^{-z} + 1)^2} \quad (10)$$

The sigmoid and Tanh function are visualized in figure 4.

Both functions have relatively simple mathematical formulas and are differentiable. In this paper the sigmoid function is used over the Tanh function as it had better results. Sigmoid and Tanh are not the only activation functions. Other functions that should be noted are the Rectified Linear Unit (ReLU) and the Leaky Rectified Linear Unit function. These functions have their own separate pros and cons, but a proper discussion of two more activation functions is outside the scope of this paper.

## 1.6 Pitfalls

The most important thing to steer clear of is over training. Over training occurs when the neural net trains too much to the training data. While it will have a high accuracy for the training data, it's performance for the test data will decay, as it has become too well attuned to the training data.

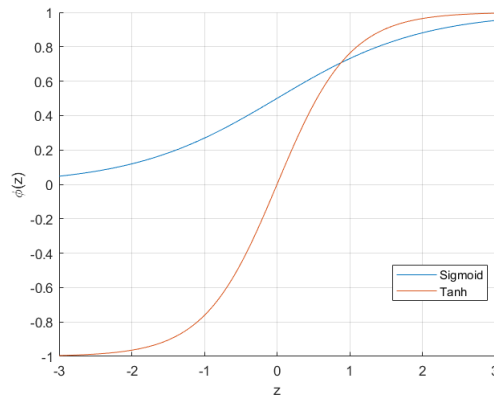


Figure 4: Visualization of sigmoid and Tanh function

ID	architecture	test error for	best test	simulation	weights
	(number of neurons in each layer)	best validation [%]	error [%]	time [h]	[milions]
1	1000, 500, 10	<b>0.49</b>	0.44	23.4	1.34
2	1500, 1000, 500, 10	<b>0.46</b>	0.40	44.2	3.26
3	2000, 1500, 1000, 500, 10	<b>0.41</b>	0.39	66.7	6.69
4	2500, 2000, 1500, 1000, 500, 10	<b>0.35</b>	0.32	114.5	12.11

Figure 5: Run times for various neural network architectures [4].

The other problem is the time it takes to train. A three layer neural net can be trained to 97% accuracy within 10 minutes, however it will not improve far beyond that. Larger nets will take longer to train, but will take far longer to train.

## 2 Implementation

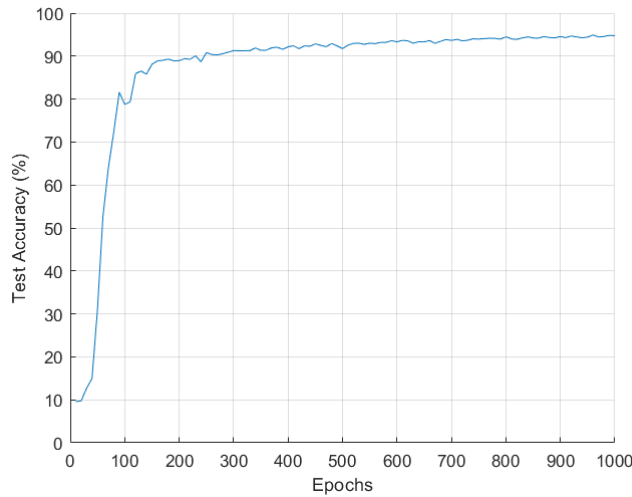
### 2.1 Object Oriented Programming in MATLAB

This neural net had to be made without the use of any built in libraries [7] and the code had to be modular [8]. To create code for neural network subject to these constraints the author decided to create their own neural net class in MATLAB.

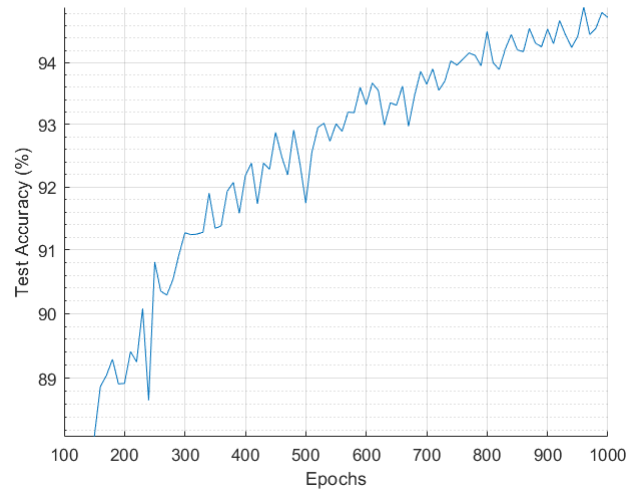
The MATLAB class `philipNeuralNet.m` was written for this neural net project. It has the parameters `learningRate`, `enableBias`, `actFunSwitch`, and `Level`. The `learningRate` parameter is obviously the learning rate. The `Level` parameter has four parameters attached to it: `W` (weight), `dW` (weight derivative), `z` (input), and `A` (the vector for the layer). By having this class we have avoided hard coding the propagation of the neural net and it is possible to test different neural net architectures on this code.

The MATLAB class also has an activation function and a derivative of the activation function. The `actFunSwitch` variable allows either the Sigmoid or the Tanh function to be selected. Additionally the `enableBias` variable allows for biases to be used or not used in the code's execution.

Finally it has a `outputVector` function that is simply an implementation of the neural net. It takes the input, runs it through the net, and returns the net's output.



(a) The results for the first 1000 epochs.



(b) The results for the first epochs scaled logarithmically

Figure 6: The results from the simple network for the first 1000 epochs.

## 2.2 MATLAB Code

The MATLAB code first initializes a neural net from given parameters. It obtains the MNIST data from a function [9]. It then uses the `handleTrainNet` function to train the net. This function implements batch training, using the forward and backward propagation functions. It then computes and displays the training error and the testing accuracy after a specified number of runs via the `testAcc.m` function. Once it has done this it plots the accuracy of the neural net via the `plot accuracy` function, generating the plots seen in the results section. The code used in this report may be downloaded from <https://github.com/PhilipHoddinott/DesignOpt/tree/master/designOpNN>

# 3 Results

## 3.1 Simple Neural Net

The best results were found for the simplest neural net examined; a one hidden layer with 250 nodes a learning rate of 0.1, and no biases. For this simple a test accuracy of 98% was achieved. The first 1000 epochs of this net are visualized in figure 6. To get the 98.37% accuracy it took approximately 12 hours of running the code and over three million neural net evaluations.

## 3.2 Comparison of different hidden layer sizes

From Shure [10], the optimal size for the hidden layer in a three layer neural network for the MNIST is 250 nodes. Comparing the results for hidden layers show in figure 7, different sizes of hidden layer do not have a large effect on the accuracy of these results. However what is different is the time it takes to run each net. The more nodes in a net, the longer it takes for the net to train, as there are more operations to perform. Thus if a neural net with 250 nodes will have the same accuracy as a net with 800 nodes, the first net is preferable, as it will be trained faster.

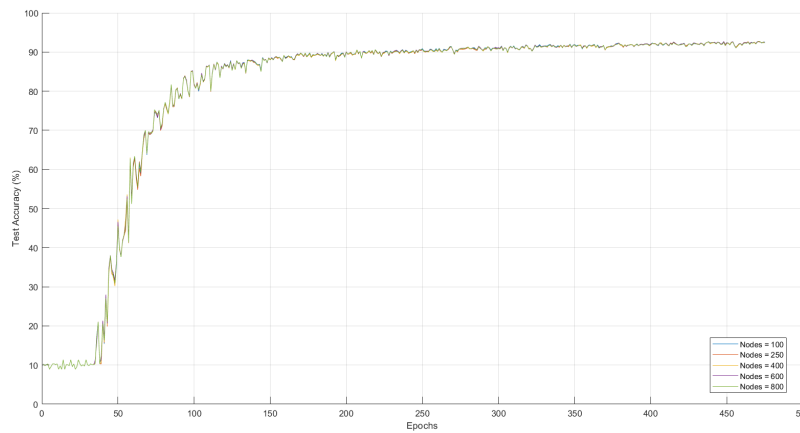
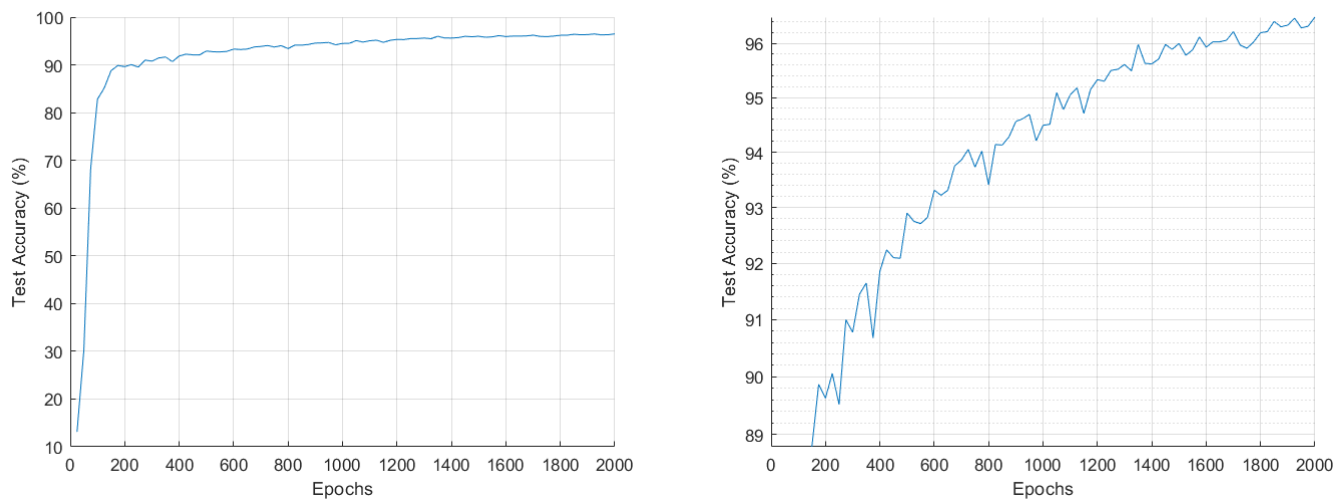


Figure 7: Net accuracy for different layer sizes.

### 3.3 Multiple hidden layers

The best accuracy occurred when both layers had a size of  $250 \times 1$ . For network with two hidden layers of 250 each the best test accuracy was 96.49%. The accuracy from the first 2000 epochs is seen in figure 8.



(a) The results for the first 2000 epochs.

(b) The results for the first epochs scaled logarithmically

Figure 8: The results from the two layer network for the first 2000 epochs.

The accuracy of two hidden layers was not as good as the accuracy of one hidden layer. No other configurations achieved an accuracy as high as this one.

## 4 Conclusion

The simple neural net achieved an accuracy of 98.37%. This is on par with human recognition, and is about as accurate as a simple neural net can achieve. Higher accuracy rates are achieved via the use of constitutional neural networks, such as the LeNet-5 [11]. Due to the long run time of large multi layered neural networks they were not studied, but could provide a more accurate identification with out convolution.



What is interesting is that the best results occurred with out biases and with one hidden layer. It was expected that adding more complexion to the neural net would increase the accuracy, however this was not the case. As neural nets are very much a trial and error process, it is possible that these more complex nets will achieve a better accuracy with more fiddling.

## References

- [1] Deep learning for classification on the mnist dataset. <https://www.mathworks.com/examples/computer-vision/community/36153-deep-learning-for-classification-on-the-mnist-dataset>, 2018.
- [2] Diagram of an artificial neural network. <https://tex.stackexchange.com/questions/132444/diagram-of-an-artificial-neural-network>, September 2013.
- [3] Daphne Cornelisse. <https://bit.ly/2rFQEhh>, February 2018.
- [4] Luca Maria Gambardella Jurgen Schmidhuber Dan Claudiu Ciresan, Ueli Meier. Deep big simple neural nets excel on handwritten digit recognition. <https://arxiv.org/pdf/1003.0358.pdf>, March 2010.
- [5] Christopher J.C. Burges Yann LeCun, Corinna Cortes. The mnist database of handwritten digits. <http://yann.lecun.com/exdb/mnist/>.
- [6] John Denker Patrice Simard, Yann Le Cun. Efficient pattern recognition using a new transformation distance. <https://papers.nips.cc/paper/656-efficient-pattern-recognition-using-a-new-transformation-distance.pdf>.
- [7] Jason Hicken. Mane 6963 independent study description, December 2018.
- [8] Jason Hicken. Rubric for mane 6963 independent study, December 2018.
- [9] Using the mnist dataset. [http://ufldl.stanford.edu/wiki/index.php/Using\\_the\\_MNIST\\_Dataset](http://ufldl.stanford.edu/wiki/index.php/Using_the_MNIST_Dataset), may 2011.
- [10] Loren Shure. Artificial neural networks for beginners. <https://blogs.mathworks.com/loren/2015/08/04/artificial-neural-networks-for-beginners/>, August 2015.
- [11] Yann LeCun. Lenet-5, convolutional neural networks. <http://yann.lecun.com/exdb/lenet/>.

## Appendix 1 - MATLAB code

### NN\_Master.m

```

1 %% Philip Hoddinott NN
2 % Neural Net for MNIST numbers
3 %% Setup
4 clear all; close all;
5 %% load values
6 % These functions come from
7 % http://ufldl.stanford.edu/wiki/index.php/Using_the_MNIST_Dataset

```

```

8  inputValues = loadMNISTImages('train-images.idx3-ubyte');
9  labels = loadMNISTLabels('train-labels.idx1-ubyte');
10
11 inputValuesTest = loadMNISTImages('t10k-images.idx3-ubyte');
12 labelsTest = loadMNISTLabels('t10k-labels.idx1-ubyte');
13
14 % change labels
15 targetValues = 0.*ones(10, size(labels, 1));
16 for n = 1: size(labels, 1)
17     targetValues(labels(n) + 1, n) = 1;
18 end
19 % traing paramters
20 sizeArr=[250;10];
21 learningRate=.1;
22 batchSize = 100;
23 epochs = 500; numEpoch=1;
24 % net switches
25 enableBias=0; % 0 for off, 1 for on
26 actFunSwitch =0; % 0 for sigmoid, 1 for Tanh
27 % create net
28 pNet=philipNeuralNet(inputValues,sizeArr,learningRate,enableBias,actFunSwitch);
29 % train net
30 [pNet,pNetBest,errorM,testAccM]=handleTrainNet(pNet, inputValues, targetValues, ...
    epochs, batchSize, inputValuesTest, labelsTest,numEpoch,sizeArr);
31 % plot results
32 plotAcc
33
34 function [pNet,pNetBest,errorM,testAccM] = handleTrainNet(pNet, inputValues, ...
    targetValues, epochs, batchSize, inputValuesTest, labelsTest,numEpoch,sizeArr)
35 % handleTrainNet function to train net via batch traning
36 % Input
37 % pNet : net
38 % epochs : number of epochs
39 % numEpoch : epoch multiplier
40 % batchSize : size of batch
41 % inputVector : MNIST Input vector for training
42 % targetVector : MNIST Labels for traning validation
43 % sizeArr : net architecture
44 % inputValuesTest : MNIST Input vector for testing
45 % labelsTest : MNIST Labels for testing validation
46 %
47 % Output
48 % pNet : net
49 % pNetBest : pNet with best accuracy
50 % errorM : matrix of traning error
51 % testAccM : matrix of test accuracy
52 trainingSetSize = size(inputValues, 2); % get traning set size
53 errorM=[]; testAccM=[]; % init values
54
55 n = zeros(batchSize); % init values
56 errorBest=100; accBest=-1; % init values
57
58 figure; hold on; % init figure
59 ylabel('Training Error'); xlabel('Epochs');
60 tic
61 for t = 1: numEpoch*epochs
62     for k = 1: batchSize
63         % Select input vector to train on.
64         n(k) = floor(rand(1)*trainingSetSize + 1);

```

```

65         % get inputs and targets
66         inputVector = inputValues(:, n(k));
67         targetVector = targetValues(:, n(k));
68         % forward propogation
69         pNet = forwardProp(pNet, sizeArr, inputVector);
70         % backwards Propagation
71         pNet=backprop(pNet, sizeArr, inputVector, targetVector);
72     end % end foor loop
73
74     % Calculate the error for plotting.
75     error = 0;
76     for k = 1: batchSize
77         inputVector = inputValues(:, n(k));
78         targetVector = targetValues(:, n(k));
79         outputVector = pNet.netOutput(inputVector, sizeArr);
80         error=error+norm(outputVector- targetVector, 2);
81
82     end
83     error = error/batchSize; errorM=[errorM,error];
84     plot(t,error,'*')
85
86     if error<errorBest
87         pNetBest=pNet; errorBest=error; % get best error
88     end
89
90     if mod(t,25)==0 %
91         [numCorrect, numErrors,acc] = testAcc(pNet, inputValuesTest, ...
92             labelsTest,sizeArr);
93         if acc>accBest
94             accBest=acc; % get best accuracy
95         end
96         testAccM=[testAccM,acc];
97         fprintf('Epoch = %d,error = %.4f, best acc = %.4f\n',t, error,accBest)
98         grid on;
99         toc % time to run
100     end
101     drawnow % draw error
102 end
103
104
105 function pNet = forwardProp(pNet, sizeArr, inputVector)
106     % forwardProp function to perform forward propogation
107     %
108     % Input
109     % pNet : net
110     % inputVector : MNIST Input vector for training
111     % targetVector : MNIST Labels for traning validation
112     % sizeArr : net architecture
113     %
114     % Output
115     % pNet : net
116     for i=1:length(sizeArr)
117         if i==1 % 1st layer from input
118             pNet.Level(i).z=pNet.Level(i).W*inputVector;
119         else % all other layers
120             pNet.Level(i).z=pNet.Level(i).W* pNet.Level(i-1).A;
121         end
122         pNet.Level(i).A=pNet.actFunc(pNet.Level(i).z+pNet.Level(i).b); % handle bias

```

```

123     end
124 end
125
126 function pNet=backprop(pNet,sizeArr,inputVector,targetVector)
127     % backprop function to perform backpropagation
128     %
129     % Input
130     % pNet : net
131     % inputVector : MNIST Input vector for training
132     % targetVector : MNIST Labels for training validation
133     % sizeArr : net architecture
134     %
135     % Output
136     % pNet : net
137     learningRate=pNet.learningRate; % get learning rate
138     iArr=linspace(length(sizeArr),1,length(sizeArr)); % array to go backwards
139     for i=iArr
140         if i==length(sizeArr) % derivative from cost at output
141             pNet.Level(i).dW=pNet.dactFunc( pNet.Level(i).z).* ...
                (pNet.Level(i).A-targetVector);
142         else % derivative for other hidden layers
143             pNet.Level(i).dW = pNet.dactFunc( ...
                pNet.Level(i).z).*(pNet.Level(i+1).W'* pNet.Level(i+1).dW);
144         end
145         dz=pNet.dactFunc(pNet.Level(i).z); % vector deriv
146         pNet.Level(i).db=(1/length(dz))* sum(dz,2); % bias deriv
147     end
148
149     for i=iArr
150         if i≠1 % adjust weight for all hidden layers not at input
151             pNet.Level(i).W= ...
                pNet.Level(i).W-learningRate*pNet.Level(i).dW*pNet.Level(i-1).A';
152         else % adjust hidden layer weight at input
153             pNet.Level(i).W= ...
                pNet.Level(i).W-learningRate*pNet.Level(i).dW*inputVector';
154         end
155         if pNet.enableBias==1 % switch for enable bias
156             pNet.Level(i).b=pNet.Level(i).b-learningRate*pNet.Level(i).db;
157         end
158     end
159 end

```

## philipNeuralNet.m

```

1 classdef philipNeuralNet
2     %philipNeuralNet Class created for neural net
3     % Detailed explanation goes here
4
5     properties
6         learningRate; % learning rate
7         Level; % level, which has z, W, dW, b, db, and A
8         enableBias; % switch to toggle bias on /off
9         actFunSwitch; % switch for Tanh or Sigmoid
10    end
11
12    methods

```

```

13     function obj = ...
14         philipNeuralNet(inputValues,sizeArr,learningRate,enableBias,actFunSwitch)
15         % philipNeuralNet function to initialize neural net
16         % Input
17         % inputValues : input values for net
18         % sizeArr : net architecture
19         % learningRate : net learningRate
20         % enableBias : switch to toggle bias on /off
21         % actFunSwitch : switch for Tanh or Sigmoid
22         %
23         % Output
24         % obj : pNet
25         inputDim = size(inputValues, 1); % get dim
26
27         for i =1:length(sizeArr) % initialize neural net variables
28             if i==1
29                 obj.Level(i).W=rand(sizeArr(i),inputDim);
30                 obj.Level(i).W=( obj.Level(i).W)./size( obj.Level(i).W,2);
31             else
32                 obj.Level(i).W=rand(sizeArr(i),sizeArr(i-1));
33                 obj.Level(i).W=( obj.Level(i).W)./size( obj.Level(i).W,2);
34             end
35             obj.Level(i).z=learningRate*rand(sizeArr(i),1);
36             obj.Level(i).A=learningRate*rand(sizeArr(i),1);
37             obj.Level(i).dW=learningRate*rand(sizeArr(i),1);
38             obj.Level(i).b=learningRate*zeros(sizeArr(i),1);
39             obj.Level(i).db=learningRate*obj.Level(i).b;
40
41         end
42         obj.learningRate=learningRate;
43         obj.enableBias=enableBias;
44         obj.actFunSwitch=actFunSwitch;
45     end
46     function funcVal = actFunc(obj,x)
47         %actFunc activation function depending on the activation
48         %function switch, this performs sigmoid or TanH
49         % Input
50         % x : vector to perform function on
51         % obj : pNet
52         %
53         % Output
54         % funcVal: result of function(z)
55         if obj.actFunSwitch==0 % for sigmoid
56             funcVal = 1./(1 + exp(-x));
57         elseif obj.actFunSwitch==1 % for tanh
58             funcVal=tanh(x);
59         end
60     end
61     function funcD = dactFunc(obj,x)
62         %dactFunc activation func derivative
63         % depending on the activation function switch, this performs
64         % derivative of sigmoid or Tanh
65         %
66         % Input
67         % x : vector to perform function on
68         % obj : pNet
69         %
70         % Output

```

```

71         % funcD: result of function(z)
72         if obj.actFunSwitch==0
73             funcD = obj.actFunc(x).*(1 - obj.actFunc(x));
74         elseif obj.actFunSwitch==1
75             funcD=(1-tanh(x).^2);
76         end
77     end
78
79     function outputVector = netOutput(pNet, inputVector, sizeArr)
80         % netOutput get the output of the neural net given an input and
81         %
82         % INPUT:
83         % pNet : net
84         % inputVector : input to net
85         % sizeArr : net architecture
86         %
87         % OUTPUT:
88         % outputVector : output of net
89         for i=1:length(sizeArr)
90             if i==1
91                 pNet.Level(i).z=pNet.Level(i).W*inputVector;
92             else
93                 pNet.Level(i).z=pNet.Level(i).W*pNet.Level(i-1).A;
94             end
95             pNet.Level(i).A=pNet.actFunc(pNet.Level(i).z);
96         end
97         outputVector=pNet.Level(i).A;
98     end
99
100 end
101 end

```

## testAcc.m

```

1 function [numCorrect, numErrors, acc] = testAcc(pNet, inputValues, labels, sizeArr)
2     % testAcc test the accuracy of a net using mnist validation set
3     %
4     % INPUT:
5     % pNet : net
6     % inputValues : MNIST Input values for training
7     % labels : MNIST Labels for validation
8     % sizeArr : net architecture
9     %
10    % OUTPUT:
11    % numCorrect : number of correctly classified numbers.
12    % numErrors : number of classification errors.
13    %
14    testSetSize = size(inputValues, 2);
15    numErrors = 0;    numCorrect = 0;
16
17    for n = 1:testSetSize
18        inputVector = inputValues(:, n);
19        outputVector = pNet.netOutput(inputVector, sizeArr);
20        maxV = 0; class = 1;
21
22        for i = 1: size(outputVector, 1)

```

```
23         if outputVector(i) > maxV
24             maxV = outputVector(i); % get maxV
25             class = i; % get class
26         end
27     end
28
29     if class == labels(n) + 1
30         numCorrect = numCorrect + 1; % count correct
31     else
32         numErrors = numErrors + 1; % count error
33     end
34 end
35 acc=100*(numCorrect) / (numCorrect+numErrors); % get accuracy
36 end
```

## plotAcc.m

```
1 %% PlotAcc
2 % Function to plot accuracy. No inputs, as it is run from the NN_master.m
3 % file
4 figure; hold on
5 plot(25.*(1:1:length(testAccM)),testAccM)
6 xlabel('Epochs')
7 ylabel('Test Accuracy (%)')
8 grid on
9
10 figure; hold on
11 plot(25.*(6:1:length(testAccM)),testAccM(6:end))
12 xlabel('Epochs')
13 ylabel('Test Accuracy (%)')
14 grid on
15 set(gca, 'YScale', 'log')
```