

# Deep Neural Network

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## Abstract

The purpose of this report is to develop a neural net that can identify handwritten digits in the MNIST database at near human levels of accuracy. The neural net will be developed without the assistance of libraries such as Python's tensor flow or MATLAB's Deep Learning.

The author would like to express his gratitude to Professor Hicken for the suggestion of this project. The author would also like to thank Theodore Ross and Varun Rao for their assistance with artificial neural networks.

## 1 Introduction

The first computational models for neural networks were thought up in the 1940s, however it would take 50 years for computers to achieve the processing power to implement the first neural networks. Today neural networks can be used for a variety of tasks. One of these tasks is image recognition of numbers.

### 1.1 The MNIST database

The Modified National Institute of Standards and Technology database or MNIST database [5] is a database of handwritten numbers used to train image processing systems. It contains 60,000 training images and 10,000 testing images. The database is comprised of images that are made up of a grid of 28x28 pixels. Some of these are seen in figure 1.

A number of attempts have been made to get the lowest possible error rate on this dataset. As of August 2018 the lowest achieved so far is a error rate of 0.21% or an accuracy of 99.79%. For comparison human can accurately recognize digits at a rate of 98% - 98.5% [6].

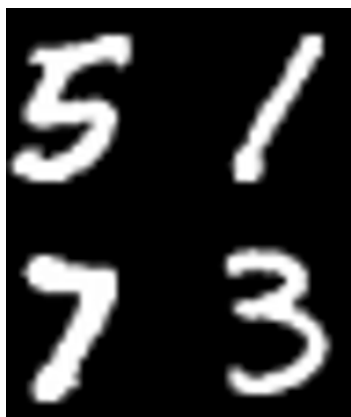


Figure 1: Sample numbers from MNIST [1].

### 1.2 Artificial neural network

An artificial neural network (referred to as a neural network in this paper) is a computation system that mimics the biological neural networks found in animal brains. A neural network is not an algorithm, but a general framework to solve problems. Artificial neural networks are based of layers of interconnected neurons that transmit signals to each other. Neural networks may be trained for tasks, such as the number recognition in this report.

The neural net implemented in this project had an input vector of  $784 \times 1$  and an output vector of  $10 \times 1$ . Different configurations were tried, with one hidden layer of  $250 \times 1$  producing the best results. A visualization of an example neural net is seen in figure 2.

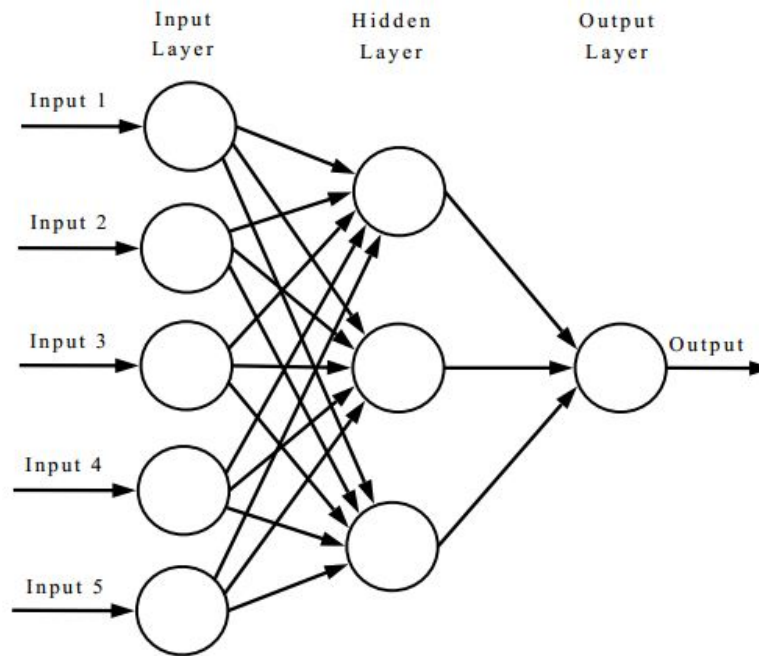


Figure 2: Visualization of a neural network with one hidden layer [2].

### 1.3 Neural Network Walkthrough

The training of a neural network involves four main steps:

1. Initialize weights and biases.
2. Forward propagation
3. Compute the loss
4. Backward propagation

#### 1.3.1 Parameter Initialization

The first step in training a neural net is to initialize the bias vectors and weight matrices. They are initialized with random numbers between 0 and 1, then multiplied by a small scalar around the order of  $10^{-2}$  so that the units are not on the region where the derivative of the activation function are close to zero. The initial parameters should be different values (to keep the gradients from being the same).

There are various forms of initialization such as Xavier initialization or He-et-al Initialization, but a discussion on methods of initialization outside the scope of this paper. In this paper we will stick with random parameter initialization.

#### 1.3.2 Forward Propagation

The next step is the forward propagation. The network takes the inputs from a previous layer, computes their transformation, and applies an activation function. Mathematically the forward propagation at level “i” is represented by equation 1.

$$\begin{aligned} z_i &= A_{i-1} * W_i + b \\ A_i &= \phi(z_i) \end{aligned} \tag{1}$$

Where  $z$  is the input vector,  $A$  is the layer,  $W$  is the weights going into the layer,  $b$  the bias, and  $\phi$  the activation function. This process then repeats for the next layer until it reaches the end of the neural net.

### 1.3.3 Compute loss

The loss is simply the difference between the output and the actual value. In this neural net it is computed by equation 2.

$$\text{loss} = A_{i=\text{end}} - y \tag{2}$$

This loss is used to begin the next step: backward propagation.

### 1.3.4 Backward propagation

After going forward through the neural net in the forward propagation step and computing the loss the final step is backwards propagation. Backwards propagation is the updating of the weight parameters via the derivative of the error function with respect to the weights of the neural net. For the output layer this is seen in equation 3 and equation 4 for all other layers.

$$dW_{i=\text{end}} = \phi'(z_{i=\text{end}}) * (A_{i=\text{end}} - y) \tag{3}$$

$$dW_i = \phi'(z_i) * (W_{(i+1)}^T * dW_{(i+1)}) \tag{4}$$

Once these derivatives have been computed, the weights are updated by equation 5

$$W_i = W_i - \alpha * dW_i * A_{(i-1)}^T \tag{5}$$

Where for the first layer  $z_{(i-1)}^T$  will be the input vector and for all the following layers it will be the vector from the previous layer.

At this point the neural net has completed a full run through. The next input vector is selected and the forward and backward propagation are run again. A visualization of forward and backward propagation is in figure 3.

## 1.4 Gradient Decent

Also known as steepest decent, gradient decent is a first order optimization algorithm. It is used to find the minimum of a function. Equation 6 shows gradient decent implemented in a neural net.

$$\Delta W(t) = -\alpha \frac{\partial E}{\partial W(t)} \tag{6}$$

Where  $\alpha$  is the learning rate, and  $\partial E / \partial W(t)$  is the error derivative with respect to the weight. As these derivatives must be computed for each node the more nodes there are in a neural net the longer it will take to train.

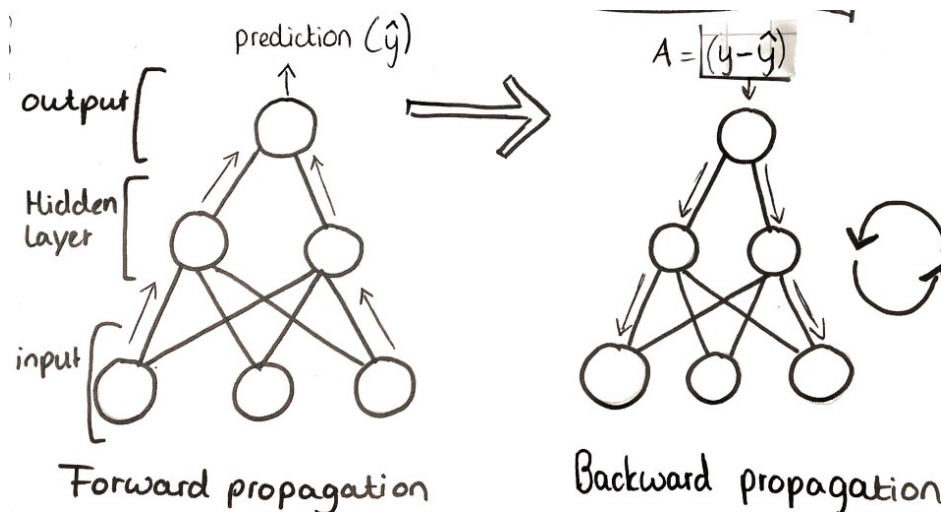


Figure 3: A visualization of forward and backward propagation [3].

## 1.5 Activation Function

The activation function was previously mentioned as a function used to convert the input signal to the output signal. Activation functions introduce non-linear properties to the neural net's functions, allowing the neural net to represent complex functions [3].

The two most common activation functions used in neural nets for the gradient decent are sigmoid and hyperbolic tangent (Tanh). The formula for Tanh is seen in equation 7, and the formula for it's derivative is seen in equation 8

$$\phi_{\text{Tanh}}(z) = \frac{1 - e^{-2z}}{1 + e^{-2z}} \quad (7)$$

$$\phi'_{\text{Tanh}}(z) = \frac{4}{(e^{-z} + e^z)^2} \quad (8)$$

The formula for the sigmoid function is seen in equation 9, the formula for it's derivative is seen in equation 10.

$$\phi_{\text{Sigmoid}}(z) = \frac{1}{1 + e^{-z}} \quad (9)$$

$$\phi'_{\text{Sigmoid}}(z) = \frac{e^{-z}}{(e^{-z} + 1)^2} \quad (10)$$

The sigmoid and Tanh function are visualized in figure 4.

Both functions have relatively simple mathematical formulas and are differentiable. In this paper the sigmoid function is used over the Tanh function as it had better results. Sigmoid and Tanh are not the only activation functions. Other functions that should be noted are the Rectified Linear Unit (ReLU) and the Leaky Rectified Linear Unit function. These functions have their own separate pros and cons, but a proper discussion of them is outside the scope of this paper.

## 1.6 Pitfalls

The most important thing to steer clear of is over training. Over training occurs when the neural net trains too much to the training data. While it will have a high accuracy for the training data, it's performance for the test data will decay, as it has become too well attuned to the training data.

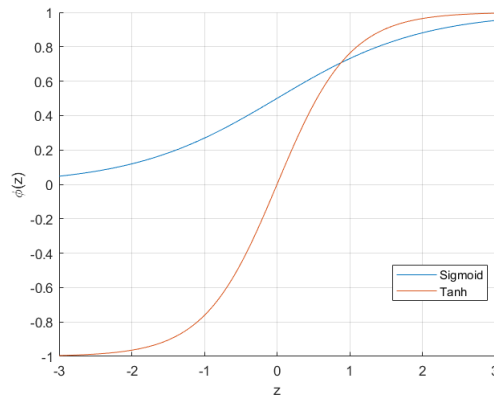


Figure 4: Visualization of sigmoid and Tanh function

ID	architecture	test error for	best test	simulation	weights
	(number of neurons in each layer)	best validation [%]	error [%]	time [h]	[milions]
1	1000, 500, 10	<b>0.49</b>	0.44	23.4	1.34
2	1500, 1000, 500, 10	<b>0.46</b>	0.40	44.2	3.26
3	2000, 1500, 1000, 500, 10	<b>0.41</b>	0.39	66.7	6.69
4	2500, 2000, 1500, 1000, 500, 10	<b>0.35</b>	0.32	114.5	12.11

Figure 5: Run times for various neural network architectures [4].

The other problem is the time it takes to train. A three layer neural net can be trained to 97% accuracy within 10 minutes, however it will not improve far beyond that. Larger nets will take longer to train, but will take far longer to train.

## 2 Implementation

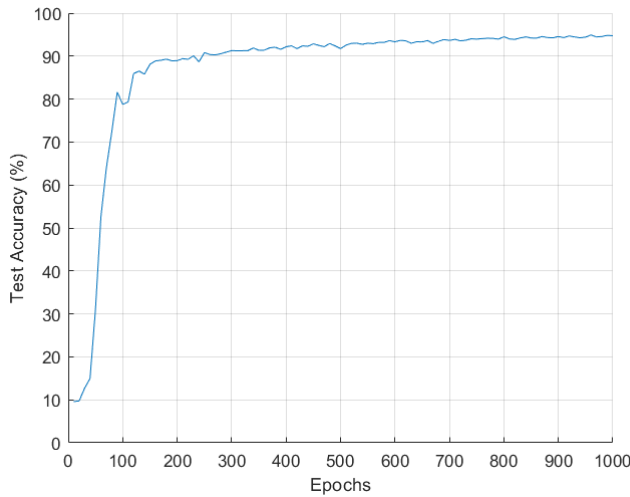
### 2.1 Object Oriented Programming in MATLAB

This neural net had to be made without the use of any built in libraries [7] and the code had to be modular [8]. To create code for neural network subject to these constraints the author decided to create their own neural net class in MATLAB.

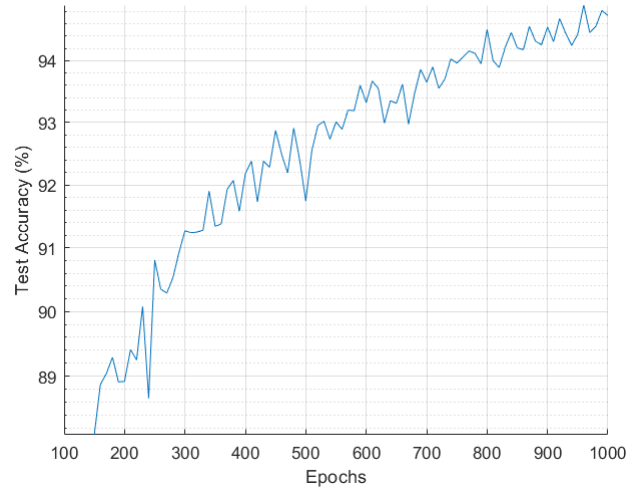
The MATLAB class `philipNeuralNet.m` was written for this neural net project. It has the parameters `learningRate`, `enableBias`, `actFunSwitch`, and `Level`. The `learningRate` parameter is obviously the learning rate. The `Level` parameter has four parameters attached to it: `W` (weight), `dW` (weight derivative), `z` (input), and `A` (the vector for the layer). By having this class we have avoided hard coding the propagation of the neural net and it is possible to test different neural net architectures on this code.

The MATLAB class also has an activation function and a derivative of the activation function. The `actFunSwitch` variable allows either the Sigmoid or the Tanh function to be selected. Additionally the `enableBias` variable allows for biases to be used or not used in the code's execution.

Finally it has a `outputVector` function that is simply an implementation of the neural net. It takes the input, runs it through the net, and returns the net's output.



(a) The results for the first 1000 epochs.



(b) The results for the first epochs scaled logarithmically

Figure 6: The results from the simple network for the first 1000 epochs.

## 2.2 MATLAB Code

The MATLAB code first initializes a neural net from given parameters. It obtains the MNIST data from a function [9]. It then uses the `handleTrainNet` function to train the net. This function implements batch training, using the forward and backward propagation functions. It then computes and displays the training error and the testing accuracy after a specified number of runs via the `testAcc.m` function. Once it has done this it plots the accuracy of the neural net via the `plot accuracy` function, generating the plots seen in the results section.

## 3 Results

### 3.1 Simple Neural Net

The best results were found for the simplest neural net examined; a one hidden layer with 250 nodes a learning rate of 0.1, and no biases. For this simple a test accuracy of 98% was achieved. The first 1000 epochs of this net are visualized in figure 6. To get the 98.37% accuracy it took approximately 12 hours of running the code and over three million neural net evaluations.

### 3.2 Comparison of different hidden layer sizes

From Shure [10], the optimal size for the hidden layer in a three layer neural network for the MNIST is 250 nodes. Comparing the results for hidden layers show in figure 7, different sizes of hidden layer do not have a large effect on the accuracy of these results. However what is different is the time it takes to run each net. The more nodes in a net, the longer it takes for the net to train, as there are more operations to perform. Thus if a neural net with 250 nodes will have the same accuracy as a net with 800 nodes, the first net is preferable, as it will be trained faster.

### 3.3 Multiple hidden layers

The best accuracy occurred when both layers had a size of  $250 \times 1$ . For network with two hidden layers of 250 each the best test accuracy was 96.49%. The accuracy from the first 2000 epochs is seen in figure

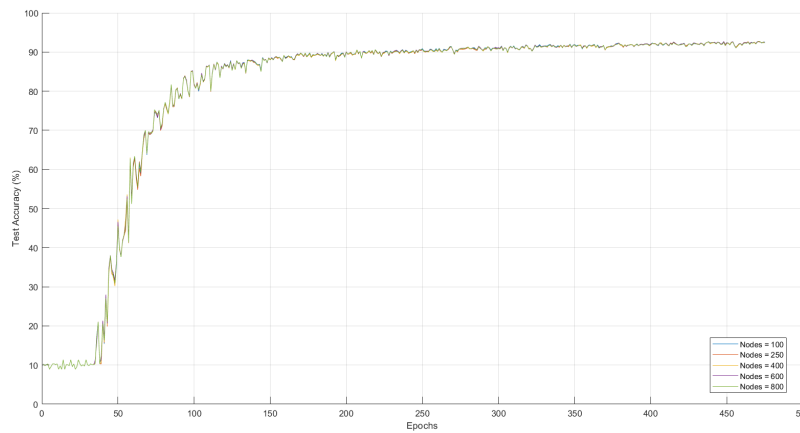
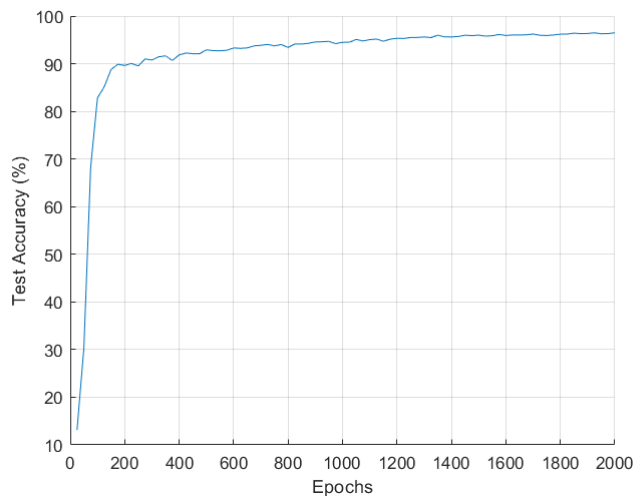
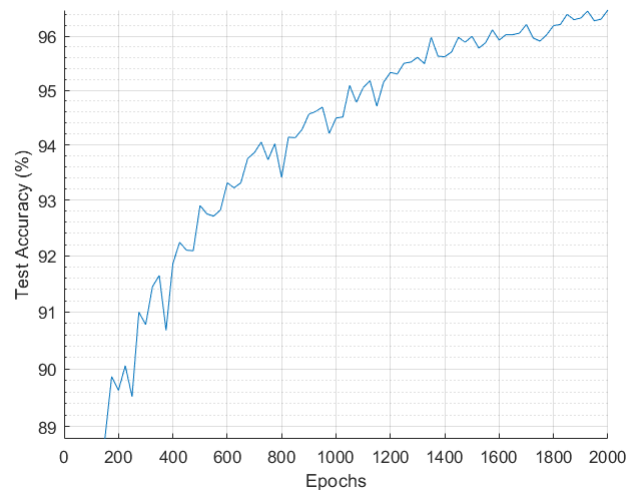


Figure 7: Net accuracy for different layer sizes.



(a) The results for the first 2000 epochs.



(b) The results for the first epochs scaled logarithmically

Figure 8: The results from the two layer network for the first 2000 epochs.

8.

The accuracy of two hidden layers was not as good as the accuracy of one hidden layer. No other configurations achieved an accuracy as high as this one.

## 4 Conclusion

The simple neural net achieved an accuracy of 98.37%. This is on par with human recognition, and is about as accurate as a simple neural net can achieve. Higher accuracy rates are achieved via the use of constitutional neural networks, such as the LeNet-5 [?]. Due to the long run time of large multi layered neural networks they were not studied, but could provide a more accurate identification with out convolution.

What is interesting is that the best results occurred with out biases and with one hidden layer. It was expected that adding more complexion to the neural net would increase the accuracy, however this was not the case. As neural nets are very much a trial and error process, it is possible that these more complex nets will achieve a better accuracy with more fiddling.



## References

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- [10] Loren Shure. Artificial neural networks for beginners. <https://blogs.mathworks.com/loren/2015/08/04/artificial-neural-networks-for-beginners/>, August 2015.

## Appendix 1 - MATLAB code

### NN\_Master.m

```

1 %% Philip Hoddinott NN
2 % Neural Net for MNIST numbers
3 %% Setup
4 clear all; close all;
5 %% load values
6 % These functions come from
7 % http://ufldl.stanford.edu/wiki/index.php/Using_the_MNIST_Dataset
8 inputValues = loadMNISTImages('train-images.idx3-ubyte');
9 labels = loadMNISTLabels('train-labels.idx1-ubyte');
10
11 inputValuesTest = loadMNISTImages('t10k-images.idx3-ubyte');
12 labelsTest = loadMNISTLabels('t10k-labels.idx1-ubyte');
13
14 % change labels
15 targetValues = 0.*ones(10, size(labels, 1));

```

```

16 for n = 1: size(labels, 1)
17     targetValues(labels(n) + 1, n) = 1;
18 end
19 % traing paramters
20 sizeArr=[250;10];
21 learningRate=.1;
22 batchSize = 100;
23 epochs = 500; numEpoch=1;
24 % net switches
25 enableBias=0; % 0 for off, 1 for on
26 actFunSwitch =0; % 0 for sigmoid, 1 for Tanh
27 % create net
28 pNet=philipNeuralNet(inputValues,sizeArr,learningRate,enableBias,actFunSwitch);
29 % train net
30 [pNet,pNetBest,errorM,testAccM]=handleTrainNet(pNet, inputValues, targetValues, ...
    epochs, batchSize, inputValuesTest, labelsTest,numEpoch,sizeArr);
31 % plot results
32 plotAcc
33
34 function [pNet,pNetBest,errorM,testAccM] = handleTrainNet(pNet, inputValues, ...
    targetValues, epochs, batchSize, inputValuesTest, labelsTest,numEpoch,sizeArr)
35 % handleTrainNet function to train net via batch traning
36 % Input
37 % pNet : net
38 % epochs : number of epochs
39 % numEpoch : epoch multiplier
40 % batchSize : size of batch
41 % inputVector : MNIST Input vector for training
42 % targetVector : MNIST Labels for traning validation
43 % sizeArr : net architecture
44 % inputValuesTest : MNIST Input vector for testing
45 % labelsTest : MNIST Labels for testing validation
46 %
47 % Output
48 % pNet : net
49 % pNetBest : pNet with best accuracy
50 % errorM : matrix of traning error
51 % testAccM : matrix of test accuracy
52 trainingSetSize = size(inputValues, 2); % get traning set size
53 errorM=[]; testAccM=[]; % init values
54
55 n = zeros(batchSize); % init values
56 errorBest=100; accBest=-1; % init values
57
58 figure; hold on; % init figure
59 ylabel('Training Error'); xlabel('Epochs');
60 tic
61 for t = 1: numEpoch*epochs
62     for k = 1: batchSize
63         % Select input vector to train on.
64         n(k) = floor(rand(1)*trainingSetSize + 1);
65         % get inputs and targets
66         inputVector = inputValues(:, n(k));
67         targetVector = targetValues(:, n(k));
68         % forward propogation
69         pNet = forwardProp(pNet,sizeArr,inputVector);
70         % backwards Propagation
71         pNet=backprop(pNet,sizeArr,inputVector,targetVector);
72     end % end for loop

```

```

73
74     % Calculate the error for plotting.
75     error = 0;
76     for k = 1: batchSize
77         inputVector = inputValues(:, n(k));
78         targetVector = targetValues(:, n(k));
79         outputVector = pNet.netOutput(inputVector, sizeArr);
80         error=error+norm(outputVector- targetVector, 2);
81
82     end
83     error = error/batchSize; errorM=[errorM,error];
84     plot(t,error,'*')
85
86     if error<errorBest
87         pNetBest=pNet; errorBest=error; % get best error
88     end
89
90     if mod(t,25)==0 %
91         [numCorrect, numErrors] = testAcc(pNet, inputValuesTest, ...
92             labelsTest,sizeArr);
93         acc=100*(numCorrect) / (numCorrect+numErrors); % get accuracy
94         if acc>accBest
95             accBest=acc; % get best accuracy
96         end
97         testAccM=[testAccM,acc];
98         fprintf('Epoch = %d,error = %.4f, best acc = %.4f\n',t, error,accBest)
99         grid on;
100        toc % time to run
101    end
102    drawnow % draw error
103
104 end
105
106 function pNet = forwardProp(pNet,sizeArr,inputVector)
107     % forwardProp function to perform forward propgation
108     %
109     % Input
110     % pNet : net
111     % inputVector : MNIST Input vector for training
112     % targetVector : MNIST Labels for traning validation
113     % sizeArr : net architecture
114     %
115     % Output
116     % pNet : net
117     for i=1:length(sizeArr)
118         if i==1 % 1st layer from input
119             pNet.Level(i).z=pNet.Level(i).W*inputVector;
120         else % all other layers
121             pNet.Level(i).z=pNet.Level(i).W* pNet.Level(i-1).A;
122         end
123         pNet.Level(i).A=pNet.actFunc(pNet.Level(i).z+pNet.Level(i).b); % handle bias
124     end
125 end
126
127 function pNet=backprop(pNet,sizeArr,inputVector,targetVector)
128     % backprop function to perform backpropagation
129     %
130     % Input

```

```

131 % pNet : net
132 % inputVector : MNIST Input vector for training
133 % targetVector : MNIST Labels for traning validation
134 % sizeArr : net architecture
135 %
136 % Output
137 % pNet : net
138 learningRate=pNet.learningRate; % get leraning rate
139 iArr=linspace(length(sizeArr),1,length(sizeArr)); % array to go backwards
140 for i=iArr
141     if i==length(sizeArr) % derivative from cost at output
142         pNet.Level(i).dW=pNet.dactFunc( pNet.Level(i).z).* ...
            (pNet.Level(i).A-targetVector);
143     else % derivative for other hidden layers
144         pNet.Level(i).dW = pNet.dactFunc( ...
            pNet.Level(i).z).*(pNet.Level(i+1).W'* pNet.Level(i+1).dW);
145     end
146     dz=pNet.dactFunc(pNet.Level(i).z); % vector deriv
147     pNet.Level(i).db=(1/length(dz))* sum(dz,2); % bias deriv
148 end
149
150 for i=iArr
151     if i≠1 % adjust weight for all hidden layers not at input
152         pNet.Level(i).W= ...
            pNet.Level(i).W-learningRate*pNet.Level(i).dW*pNet.Level(i-1).A';
153     else % adjust hidden layer weight at input
154         pNet.Level(i).W= ...
            pNet.Level(i).W-learningRate*pNet.Level(i).dW*inputVector';
155     end
156     if pNet.enableBias==1 % switch for enable bias
157         pNet.Level(i).b=pNet.Level(i).b-learningRate*pNet.Level(i).db;
158     end
159 end
160 end

```

## philipNeuralNet.m

```

1 classdef philipNeuralNet
2     %philipNeuralNet Class created for neural net
3     % Detailed explanation goes here
4
5     properties
6         learningRate; % learning rate
7         Level; % level, which has z, W, dW, b, db, and A
8         enableBias; % switch to toggle bias on /off
9         actFunSwitch; % switch for Tanh or Sigmoid
10    end
11
12    methods
13        function obj = ...
14            philipNeuralNet(inputValues,sizeArr,learningRate,enableBias,actFunSwitch)
15            % philipNeuralNet function to initzlied neural net
16            % Input
17            % inputValues : input values for net
18            % sizeArr : net architecture
19            % learningRate : net learningRate

```

```

19      % enableBias : switch to toggle bias on /off
20      % actFunSwitch : switch for Tanh or Sigmoid
21      %
22      % Output
23      % obj : pNet
24      inputDim = size(inputValues, 1); % get dim
25
26      for i =1:length(sizeArr)
27          if i==1
28              obj.Level(i).W=rand(sizeArr(i),inputDim);
29              obj.Level(i).W=( obj.Level(i).W)./size( obj.Level(i).W,2);
30          else
31              obj.Level(i).W=rand(sizeArr(i),sizeArr(i-1));
32              obj.Level(i).W=( obj.Level(i).W)./size( obj.Level(i).W,2);
33          end
34          obj.Level(i).z=learningRate*rand(sizeArr(i),1);
35          obj.Level(i).A=learningRate*rand(sizeArr(i),1);
36          obj.Level(i).dW=learningRate*rand(sizeArr(i),1);
37          obj.Level(i).b=learningRate*zeros(sizeArr(i),1);
38          obj.Level(i).db=learningRate*obj.Level(i).b;
39
40      end
41      obj.learningRate=learningRate;
42      obj.enableBias=enableBias;
43      obj.actFunSwitch=actFunSwitch;
44  end
45  function funcVal = actFunc(obj,x)
46      %actFunc activation function depending on the activation
47      %function switch, this performs sigmoid or TanH
48      % Input
49      % x : vector to perform function on
50      % obj : pNet
51      %
52      % Output
53      % funcVal: result of function(z)
54      if obj.actFunSwitch==0 % for sigmoid
55          funcVal = 1./(1 + exp(-x));
56      elseif obj.actFunSwitch==1 % for tanh
57          funcVal=tanh(x);
58      end
59  end
60
61  function funcD = dactFunc(obj,x)
62      %dactFunc activation func derivative
63      % depending on the activation function switch, this performs
64      % derivative of sigmoid or Tanh
65      %
66      % Input
67      % x : vector to perform function on
68      % obj : pNet
69      %
70      % Output
71      % funcD: result of function(z)
72      if obj.actFunSwitch==0
73          funcD = obj.actFunc(x).*(1 - obj.actFunc(x));
74      elseif obj.actFunSwitch==1
75          funcD=(1-tanh(x).^2);
76      end
77  end

```

```

78
79     function outputVector = netOutput(pNet, inputVector, sizeArr)
80         % netOutput get the output of the neural net given an input and
81         %
82         % INPUT:
83         % pNet : net
84         % inputVector : input to net
85         % sizeArr : net architecture
86         %
87         % OUTPUT:
88         % outputVector : output of net
89         for i=1:length(sizeArr)
90             if i==1
91                 pNet.Level(i).z=pNet.Level(i).W*inputVector;
92             else
93                 pNet.Level(i).z=pNet.Level(i).W*pNet.Level(i-1).A;
94             end
95             pNet.Level(i).A=pNet.actFunc(pNet.Level(i).z);
96         end
97         outputVector=pNet.Level(i).A;
98     end
99
100 end
101 end

```

## testAcc.m

```

1  function [numCorrect, numErrors] = testAcc(pNet, inputValues, labels, sizeArr)
2      % testAcc test the accuracy of a net using mnist validation set
3      %
4      % INPUT:
5      % pNet : net
6      % inputValues : MNIST Input values for training
7      % labels : MNIST Labels for validation
8      % sizeArr : net architecture
9      %
10     % OUTPUT:
11     % numCorrect : number of correctly classified numbers.
12     % numErrors : number of classification errors.
13     %
14     testSetSize = size(inputValues, 2);
15     numErrors = 0;    numCorrect = 0;
16
17     for n = 1:testSetSize
18         inputVector = inputValues(:, n);
19         outputVector = pNet.netOutput(inputVector, sizeArr);
20         max = 0; class = 1;
21
22         for i = 1: size(outputVector, 1)
23             if outputVector(i) > max
24                 max = outputVector(i);
25                 class = i;
26             end
27         end
28
29         if class == labels(n) + 1

```

```
30         numCorrect = numCorrect + 1;  
31     else  
32         numErrors = numErrors + 1;  
33     end  
34 end  
35 end
```