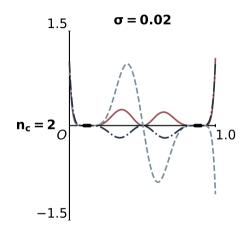
Sharpened CG Iteration Bound for Schwarz-preconditioned High-contrast Heterogeneous Scalar Elliptic PDEs

Going Beyond Condition Number

P. Soliman¹

EEMCS-DIAM Numerical Analysis MSc. Thesis Presentation, April, 2025

¹ Delft University of Technology





Opening Darcy Problem



Opening

Conjugate Gradient Method



Opening

Condition Number



Opening Preconditioners



Opening Research Gap



- Research Questions
- Mathematical Background
- Related Work
- Preliminary Results
- Outlook



- Research Questions
- Mathematical Background
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Research Questions

Main Research Question

How can we sharpen the CG iteration bound for Schwarz-preconditioned high-contrast heterogeneous scalar elliptic PDEs?



- Research Questions
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Mathematical Background

Conjugate gradient method



Mathematical Background

Schwarz preconditioners



- Research Questions
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Related Work

Tailored Coarse Spaces for High-Contrast Problems



Related Work

CG convergence in case of non-uniform spectra



- Research Questions
- Mathematical Background
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Preliminary Results

Two-cluster case



Preliminary Results

Generalization to multiple clusters



Preliminary Results

Numerical example



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Research Question 1 answered



Research question 3 answered



Next steps

Work on answering research questions 4, 5, and 6.



Open Challenge

• How to answer research question 2?

