

The hippocampus and language: Word to word prediction in terms of the successor representation

Master's Thesis in Computer Science

submitted
by

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Übersicht Den theoretischen Hintergrund der Masterarbeit bilden die Ort- und Rasterzellen des Hippocampus, die für verschiedenste Aufgaben der Orientierung zuständig sind. Das reicht von abstrakten Zuordnungen wie der Höchstgeschwindigkeit zu einem Fahrzeug auf Grundlage der Motorleistung und des Gewichts bis zur klassischen räumlichen Navigation in einer Stadt oder einem Gebäude. Da diese Resultate bereits per Maschinellern untersucht wurden, soll diese Arbeit davon handeln, ob diese Methoden auch dazu verwendet werden können, um Sprache zu verarbeiten, damit so ggf. Rückschlüsse auf die Orts- und Gitterzellen gezogen werden können. Zu diesem Zweck soll die Theorie der Projektiven Karten und deren mathematischer Formulierung der Successor Representation genutzt werden. Um dies zu erreichen, werden mehrere Architekturen eines Neuronalen Netzes untersucht und verschiedene Techniken des Natural Language Processing verwendet, wobei das Hauptaugenmerk auf der Verarbeitung von Büchern liegt, mit denen die Trainingsdaten generiert werden können, da sie plausible Sprachdaten darstellen.

Abstract The theoretical background of my master thesis is founded on the concept of the places and grid cells of the hippocampus, which control different tasks of orientation. They range from classical spatial navigation in a city or building to abstract mappings between velocity and vehicle based on engine power and mass. These results were already examined by the means of Machine Learning. Thus, this work wants to try to extend the methods to process language in hope to gain some conclusions on place and grid cells. For this purpose, the Successor Representation as application of the Projective Map theory is implemented by deploying a Neural Network under multiple architectures. Furthermore, different techniques of Natural Language Processing are used, because the training data is generated from two books to have plausible language data.

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Chapter 1

Introduction

Understanding and therefore modeling the human brain is a challenge as old as science itself. Through the centuries, mankind contemplated and associated the brain as a complex version of the technology they were surrounded by, starting by comparing it with an abacus up to the [Human Brain Project \(HBP\)](#)¹ founded by the EU, which tries to simulate and build a “silicon brain”. The first steps toward this venture were taken by Santiago Ramón y Cajal, who was rewarded with the Nobel Prize in 1906 [[Noba](#)]. Furthermore, his research includes a full description of a nerve cell and further related concepts, for instance that signals are processed mono-directionally. These results lead directly to Rosenblatt’s perceptron [[Ros58](#)] and from then on to the nowadays modern field of Deep Learning in Computer Science.

Next to large scaled research projects like the [HBP](#), there also exist smaller ones tackling different parts of the brain, for example the hippocampus (Section [2.1 Hippocampus](#)). It plays a fundamental role in forming new memories, processing emotions as part of the limbic system and in positioning, a result awarded with the Nobel Prize in 2014 (Section [2.1 Hippocampus](#) & Section [2.2 Predictive map theory](#)) [[Nobb](#)]. This abstract space, in which the navigation happens, is called cognitive room (Section [2.1 Hippocampus](#)) and Stachenfeld et al. provide an adequate mathematical theory, the [Successor Representation \(SR\)](#) (Section [2.3 Successor Representation](#)), to transfer the concept into a framework to work and do experiments with.

This master thesis tries to extend the application of the [SR](#), which is focused on spatial coordination in [[Sta⁺17](#)] to learning languages. For this purpose, some techniques of [Natural Language Processing \(NLP\)](#) are useful, necessary and applied (Section [3.2.1 Data preparation](#)). One motivating indication this plan might work out is given by Stachenfeld et al.,

¹<https://www.humanbrainproject.eu/en/>

who showed that their theory doesn't need well structured surroundings like a city but a topological/graphical environment is sufficient to retrieve viable results. Therefore, P. Stöwer did promising first experiments [Stö21], which will be used as a foundation to generalize his framework (Chapter 3 Framework) in an attempt to gain more precise results (Chapter 4 Methodology and Results).

Chapter 2

Theoretical Background

2.1 Hippocampus

The hippocampus is located in the brain and part of an old area called the archicortex. It is named after the greek word for seahorse, because it has the shape of one (Figure 2.1). This brain area can be divided into three parts: the dentate gyrus, the cornu ammonis and the subiculum [ORe⁺20; Gar18].

The hippocampus plays a fundamental role in forming new memories (not preserving them, which is done across the brain) and is highly capable of learning new information fast. Regarding its functions, one was already mentioned: It is the key area when it comes to establishing new memories. Patients with a damaged hippocampus, therefore lacking this ability, will lose spatial and temporal orientation. Moreover epilepsy, schizophrenia and Alzheimer’s disease are connected to this dysfunctional organ [Tre17]. The hippocampus is also important in emotional contexts because it is an integral unit of the limbic system [Gar18]. Another task, and for this thesis the most important one, is navigation/orientation, not just in spatial surroundings, but also in an abstract context, called cognitive room. Some examples for abstract contexts are: Danger of animals based on their appearance and speed of vehicles based on their weight and engine (Section 2.2 Predictive map theory). To achieve this skill, two types of cells in the hippocampus are active: place cells and grid cell. The first one encodes states/positions (one for each cell) and the latter resembles a coordinate system.

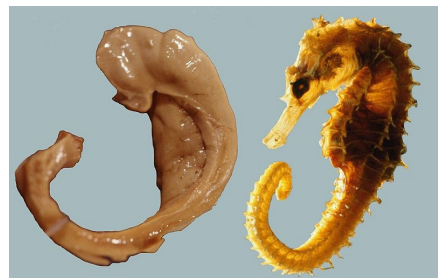


Figure 2.1: Hippocampus and seahorse [Ser10]

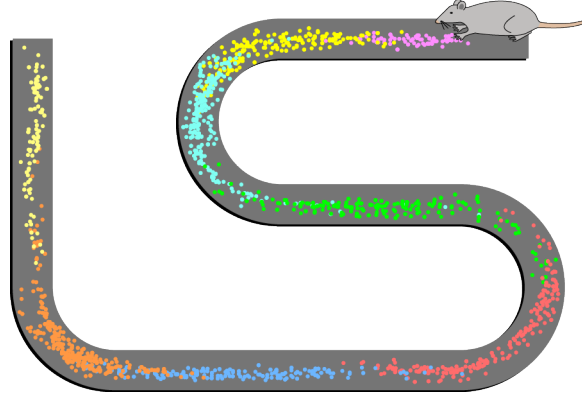


Figure 2.2: Activity pattern of color encoded place cell across a maze. Each place cell is exactly related to one distinct position of the corresponding environment e.g., turquoise to the first arch. Its activity spikes if the rat walks along the arch [Stu13].

Place cells Place cells are irregular distributed across the cognitive room. Their firing is tied to the location of the state, whereby the term location has not always its classic spatial meaning if we navigate in an abstract setting (as mentioned above). The place cell is active in case we encounter the associate state. As seen in Figure 2.2 different place cells (each is color coded) fire at different positions in the parkour e.g., turquoise is undoubtedly related to the first arch, meaning its activity spikes while the rat passes by. The remark of the thesis lies on place cells.

Grid cells This type of cell can be found in the entorhinal region and satisfies a more general purpose. They are regularly distributed and form a triangular lattice (Figure 2.3). It provides raw spatial information in terms of a metric or distance measure the hippocampus integrates with the place cells [ORe⁺20; Bel⁺18].

2.2 Predictive map theory

To explain the principle of the predictive map theory introduced in [Sta⁺17], it is necessary to illustrate the concept of a cognitive room, mentioned before in Section 2.1 *Hippocampus*. An example is of course a naive navigational task as presented by Stachenfeld et al. and similar to the setting of Figure 2.2. The authors even demonstrated that just a topological environment is sufficient to craft a cognitive room and apply the predictive map theory.

The concept becomes far more interesting when talking about experience based cognitive rooms i.e., the speed of vehicles based on weight and engine specifications. This category

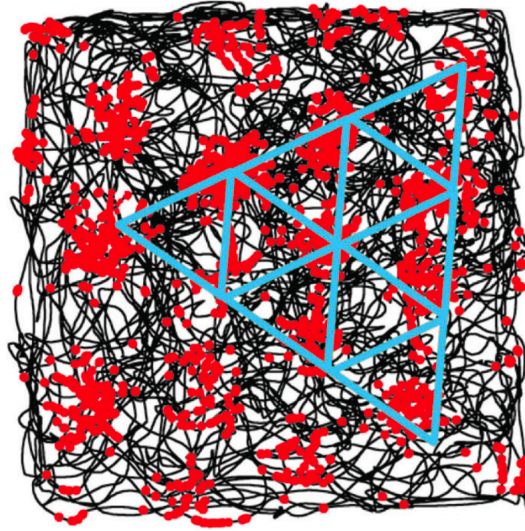


Figure 2.3: Sketched path of a rat moving in a square, while tracking firing grid cells. As their name suggests, they form a regular lattice over the space. Hence, they act as coordinate system. The information provided by grid cell is combined with that of the place cells to generate a full picture of the surroundings [Mos⁺15].

of a cognitive room also fits the topic of the thesis much better, since it aims to model language not a spatial environment. An illustrating example can be found in Figure 2.4. For instance, a “sports car” might be rather lightweight but has plenty of horse power. By using these two characteristics, the cognitive room has the shape of a $2d$ -plane. For instance, while reading about an alien car, it is immediately possible to compare it with different well-known vehicles and draw conclusions about its shape since the cognitive room has enough information to position the car within it. All these decisions of placing new objects in an appropriate context is done by place and grid cells (Section 2.1 Hippocampus). Expanding the example by the firing of cells results in the full illustration given in Figure 2.5.

2.3 Successor Representation

According to Stachenfeld et al., our behavior in an open spatial environment, or in general in a cognitive room e. g., a city, follows the predictive map theory introduced in Section 2.2 Predictive map theory. An active place cell encodes the next/successor state entered by the agent.

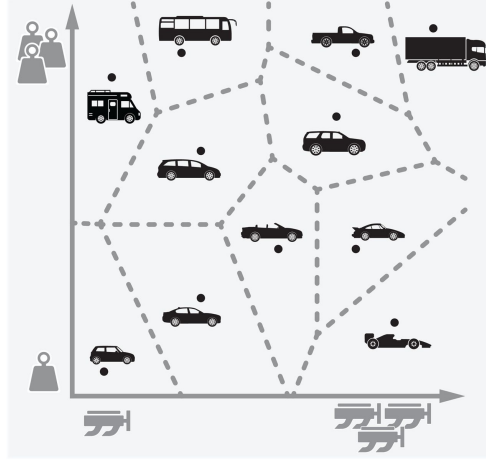


Figure 2.4: Exemplary cognitive room of vehicles according to their weight and engine power. An unknown car can be placed easily in the environment given the two parameters because there are already established place cells acting as abstract waypoints (the depicted cars) to support the orientation i. e., finding its place on the map. By doing so, it is immediately possible to derive information about the appearance of the automobile [Bel⁺18].

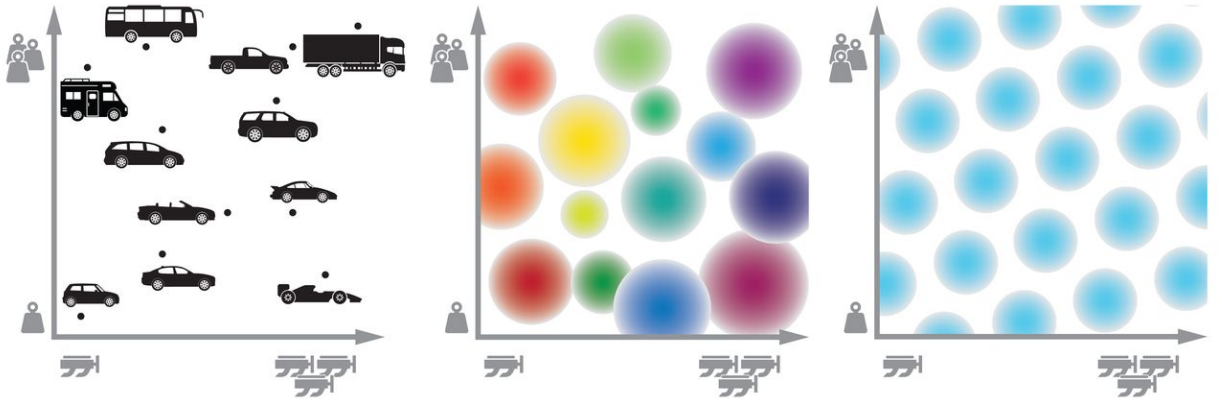


Figure 2.5: Left: cognitive room of vehicles according to weight and horse power. Middle: Firing pattern of place cells crafting the cognitive room i. e., the boundaries in Figure 2.4. Right: Corresponding lattice of grid cells. [Bel⁺18]

To model this or the general setting of predicting future states, the **SR** was developed by a **Reinforcement Learning (RL)** approach. Furthermore, the **SR** and the predictive map theory go hand in hand. The latter is an application regarding the former: The authors support the proposition that hippocampal mechanics, explained by the predictive map theory, can be described via the **SR**.

2.3.1 Mathematical Foundation

The basis lies largely in **RL**, in formula:

$$V(s) := E \left[\sum_{t=0}^{\infty} \gamma^t R(s_t) | s_0 = s \right]. \quad (2.1)$$

Here, V resembles a value function, expressed via reward function R , which operates on state s_t , encoded by the sum over t , starting in s . $\gamma \in [0, 1]$ serves as a discount factor to control the influence of states reached in distant future. High values permit distal states to play a larger role, whereas smaller values de facto limit the result to neighboring positions¹. By the reward function is obtained how beneficial the currently visited state s_t is. After the calculation of V , the function can be decomposed into a more intuitive representation, consisting of a state matrix M , called the **SR**-matrix, and the known reward function R :

$$V(s) = \sum_{s'} M(s, s') \cdot R(s'). \quad (2.2)$$

The first argument of M specifies the row, the latter the column. Each cell contains the discounted expected number of times the agent visits state s' starting from s . Additionally, Stachenfeld et al. mention that the **SR**-matrix can be derived from a transition probability matrix T for the positions s [Sta⁺17]. Having T , it follows

$$M = \sum_{t=0}^{\infty} \gamma^t T^t, \quad (2.3)$$

which is a geometric series and converges for $\gamma < 1$ towards

$$(I_n - \gamma T)^{-1}, \quad (2.4)$$

¹Short mathematical explanation: $p^t \xrightarrow{t \rightarrow \infty} 0$ for $p \in [0, 1)$, the greater p the slower happens the approach of the limit. For $p = 1$ the sequence is constant. In our case every state is taken into account equally.

where I_n is the corresponding identity matrix.

Although defining all formulae by infinite sums, it is seamlessly possible to calculate the SR-matrix in Equation (2.3) up to a finite index or starting at an arbitrary t i.e., $t = 1$. Doing so makes sense in a language environment. The identity matrix would imply that a word can follow itself, which is extremely rare². Therefore, the first summand will always be γT , where T is calculated by a Neural Network (Section 3 Framework). If the indices in Equation (2.3) are altered, the lines of the geometric series no longer applies directly and has to be adjusted by subtracting the first summands from Equation (2.4). The SR and thus the depicted formulas, especially the SR-matrix and the transition probability matrix, are policy dependent. This is reflected by the training data.

By definition, matrix M reveals all successor states with their particular probability because the summation combines the following positions, which are calculated by exponentiation, into one matrix. By examining a row (Figure 2.7) e.g., row k , it is possible to follow all paths starting from state k .

One advantage of the SR, i.e., describing the model by the SR-matrix M , is its high flexibility regarding the evaluation of different reward functions given by the Equation (2.2). The value of a state s can be calculated in an instant with a different reward function while no relearning is necessary.

SR and grid cells Although not further discussed in the thesis but an, interesting claim of Stachenfeld et al. is that the eigenvalue decomposition of the SR-matrix reveals the grid cell structure. They provide supplementary information depicting many examples [Sta⁺17].

2.3.2 Example for the Successor Representation

This subsection is dedicated to fill the concept of the SR and the SR-matrix M with some intuition. Stachenfeld et al. simulated a linear spatial environment built by six states with a simple policy merely consisting of two actions the agent can apply: Going one step to the right or pausing.

Rows In this scenario, a plot of single rows of M is shown in Figure 2.6. From the upper half of Figure 2.6, examining the row of s^1 , it is possible to deduce that the agent will most likely remain at its current position, with the values for distal locations disappearing. A different point of view results for the part of $M(s^5, s^i)$. It is obvious that going backwards

²Although sentences like “Ich hoffe, dass das das Richtige ist.” do occur in German.

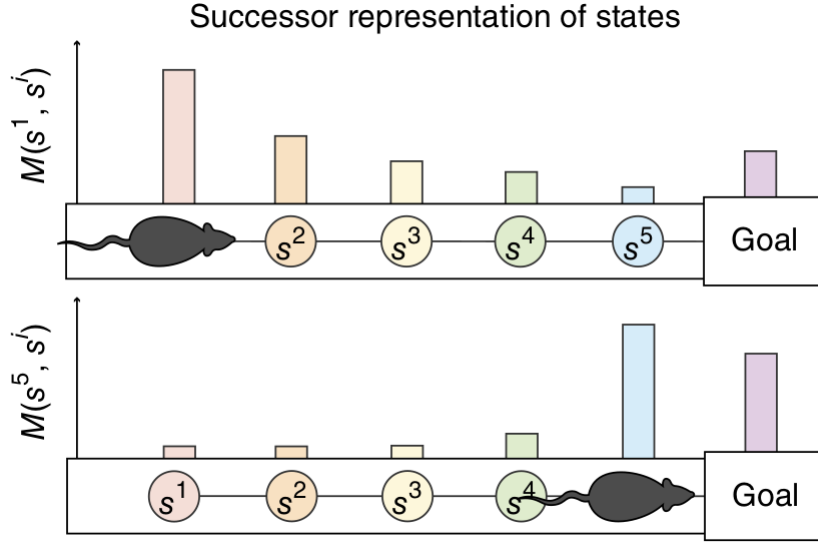


Figure 2.6: Schematic plot of the rows of state s^1 and s^5 respectively. By interpreting the ordinate values as probabilities for transitioning instead of a probability for the current state, it is possible to make assumptions on the future path the agent may take. Hence, matrix M describes all possible paths. In both cases the policy prefers pausing over changing the state.

is nothing to reckon with since the numbers for transitioning distribute over s^5 and **goal** by slightly favoring the former. This behavior was expected by the policy.

Columns It is also worth analyzing the column of M , called *place field* by Stachenfeld et al. (Figure 2.7). Having the policy in mind, it is no surprise that the values $M(s^i, s^5)$ ascend in parallel to the index i . The probability for entering s^5 grows by approaching it. In addition the plot shows how s^5 is probably reached best, simply by passing via s^3 and s^4 . This might seem obvious, but in a more complex cognitive room the graph won't look as ordinary and therefore will contain more further distributed information.

2.4 Multidimensional Scaling

The goal of **Multidimensional Scaling (MDS)** is to calculate a m -dimensional mapping, $m < n$, of a given point cloud in \mathbb{R}^n that preserves the original distances as good as possible [Has⁺17]. The result of the calculation is unique modulo rotation and scaling. Therefore, it is based on a metric and not exact coordinates. **MDS** is used to analyze similarities between the rows of the **SR**-matrix by determining clusters in the graph.

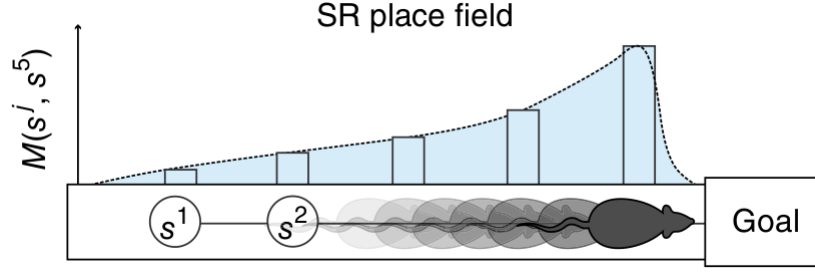


Figure 2.7: Schematic plot of the s^5 -column depicting how s^5 is reached by ascending probabilities. It is possible to recapitulate the policy consisting of pausing or taking one step to the right. Entering s^5 is most likely from s^4 and s^5 (due to resting).

The algorithm is simple and only uses basic linear algebra. **MDS** works with a distance matrix D , where each entry is equal to d_{ij}^2 , the squared distance between two points $x_i, x_j \in \mathbb{R}^n$, whose coordinates are (in principle) unknown. By double centering D it is possible to calculate the matrix product $X^\top X$, where X bears the coordinates in the desired dimension [Rie20]. Double centering means multiplying by a matrix $C := I_n - \frac{1}{n}J_n$, where J_n is a $n \times n$ -matrix of ones:

$$\underbrace{-\frac{1}{2}CDC}_{B:=} = X^\top X, \quad (2.5)$$

The centering matrix C has, after a multiplication with a column vector, the same effect of subtracting the mean of all components from the vector itself.

In the next step, the m largest eigenvalues B are calculated along with their corresponding eigenvectors. Finally, the m -dimensional coordinates are determined:

$$X_m = E_m V_m^{1/2}, \quad (2.6)$$

where E_m contains the m eigenvectors and V_m is a m -dimensional diagonal matrix with the associated eigenvalues.

2.5 Metric for quantifying the results

Throughout the presentation of the results in Chapter 4 **Methodology and Results** numerous matrices and **MDS** plots are used. Sometimes, they give a clarifying visual response, but not in all cases. When comparing different approaches, images lack the needed objectivity

and plausible criteria to rate the outcomes. To tackle this issue, a metric was developed to have the possibility to draw objective conclusions.

Since Neural Networks on languages are trained, a measure on the grade of the closeness to the real counterpart is necessary, which is referred by “ground truth (distribution)” in the following. The mathematical objects are in both cases squared matrices of dimension $n \in \mathbb{N}$ built by transposed probability vectors. Nevertheless, the presented mapping is made for $n \times m$ -matrices. Depending on the model type, the ground truth vectors are 1-hot-encoded vectors or share different fractions across all entries (Section 3.2 [Word to word models](#)).

Hence, the starting positions for the metric are probability vectors. The obvious way to quantify the results is by taking the euclidean norm d of the difference of the ground truth and the prediction. Consequentially, d takes values between 0 and $\sqrt{2 \cdot n}$ because the maximal difference for each row is $\sqrt{2}$ and there are n in total. $\sqrt{2}$ is derived by the following nonlinear program

$$\begin{aligned} \max \quad & \|\mathbf{x} - \mathbf{y}\|_2 = \sqrt{\sum_{i=1}^n (x_i - y_i)^2} \\ \text{s.t.} \quad & \sum_{i=1}^n x_i = 1, \sum_{i=1}^n y_i = 1 \\ & x_i, y_i \in [0, 1], \end{aligned} \tag{2.7}$$

which is solved by 1-hot-encoded vectors for \mathbf{x} and \mathbf{y} where $x_i = 1 \neq y_i$ for a $i \in \{1, \dots, n\}$. Or to put it bluntly, the difference takes its highest values for all scenarios in which the \mathbf{x} and \mathbf{y} are perpendicular and have a maximal euclidean norm, which means being a 1-hot-encoded vector. This relation is present n -times for the ground truth matrix and the learned one, implying that the maximal difference is $\sqrt{2 \cdot n}$.

Finally, it is possible to define the metric on the set \mathcal{P} of $n \times m$ -probability matrices:

$$d_A: \mathcal{P} \rightarrow [0, 1], \quad L \mapsto \frac{1}{\sqrt{2 \cdot n}} \|A - L\|_2, \tag{2.8}$$

where A describes a fixed matrix in \mathcal{P} . In the scope of this work the ground truth will play the role of A . By d_A , the learned matrix L is mapped to 0 if it matches the ground truth distribution perfectly and to 1 if the rows satisfy the conditions mentioned above.

Chapter 3

Framework

After setting up the theoretical basis for the tools needed to start the experiments, the code framework will be introduced. In general, it is a supervised dense Neural Network written in `python` [Van⁺09] with the help of `keras` [Cho⁺15] and `numpy` [Har⁺20]. The process is divided into two phases: One training phase and one for visualization of the result. The goal was to be able to calculate a decent `SR`-matrix showing visible clusters in the `MDS`-plot. To retrieve the `SR`, a Neural Network is trained, whose predictions serve as transition probability matrix T . If not otherwise stated, a discount factor $\gamma = 0.5$ is used.

Different scenarios were tested, hence various models were configured having distinct features e. g., some work with 1-hot-encoded vectors, while other use word vectors or made up rules and datasets.

3.1 First Model and Architecture

The first class of networks augments the results in [Stö21]. P. Stöwer's models rely on predefined rules, like

- Adjective \rightarrow Noun
- Verb \rightarrow Adjective
- Personal Pronoun \rightarrow Verb
- Question word \rightarrow Personal Pronoun

for building the dataset backed by a word database containing the corresponding information. Starting point is the cognitive room, which consists of a list reflecting the whole data. The

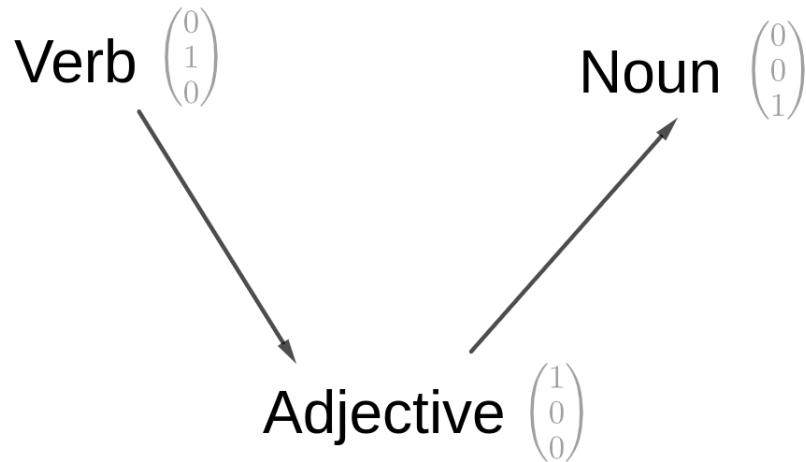


Figure 3.1: The first two rules depicted as graph. In gray are corresponding 1-hot-encoded vectors for the exemplary cognitive room [blue, to run, desk] denoted. The rules serve as edges and the word classes as vertices.

training data was crafted in accordance by randomly choosing respectively one of the four rules above and within the word class by chance an example. This information is used to initialize a 1-hot-encoded vector and is done for input and output of the network.

The goal was to attain results on the behavior of the model if it is extended by more rules and words. One can imagine this type of model as a graph (Figure 3.1).

3.2 Word to word models

The more difficult challenge lies in unannotated texts without a paradigm for pairing words of an example data set. In this manner a language normally occurs and is learned by humans. A priori one has to expect results of poorer quality in comparison to the configuration of Section 3.1 [First Model and Architecture](#) because they were tailored and NLP comes always with uncertainties.

3.2.1 Data preparation

The data is extracted from two books, namely “Gut gegen Nordwind”, written by Daniel Glattauer in German [Gla06] and from Jostein Gaarder “Sophie’s World” [Gaa96] in English. Two languages were chosen since German comes in general with a high degree of freedom in word order, whereas English is more restrictive. This distinction may be important, since

analyzing successive words is fundamental for this work. Because the books are available as pdf-file, the python module `pymupdf` [McK⁺] is used to generate a simple `String` containing the whole text, which is afterwards parsed by `spacy` [Hon⁺17]. This is a powerful tool in the area of NLP and some techniques are indispensable for further analysis, mainly

- Tokenization: segmenting text into words, punctuations marks etc.
- Part-of-speech (POS)-Tagging¹: assigning word types to tokens, like verb or noun
- Lemmatization: assigning the base forms of words²
- word2vec [Mik⁺13a; Mik⁺13b]: calculating a vector representation with real values of a word, in the following called *word vector*.

Additionally, a mechanism was implemented to extract an exact number of words having equal sized foundations in both languages. The training data consists of word pairs in their occurring order, for instance the sentence

Goethe remarked about Alexander von Humboldt to friends that he had never met anyone so versatile.³

gets tokenized, lemmatized and coupled having

("Goethe", "remark"), ("remark", "about"), ("about", "Alexander"), ...

where the first component serves as input and the second one as supervised output.

Clearly, not the actual word is fed into the Neural Network, but numerical representations: either a 1-hot-encoded vector or a word vector. To construct the former, the concept of the cognitive room is applied by building a list containing all words of the text i.e., one word resembles one state and states are encoded by place cells. To learn the transition probability matrix, as proclaimed at the beginning of the chapter, one has to transform the prediction of the Neural Network into a probability vector via division by its sum. This processing is done not during training because it is supervised via 1-hot-encoded vectors.

¹More information on [dMar⁺]

²For example, the lemma of “was” is “be”, and the lemma of “rats” is “rat”.

³Sentence taken from [Wul16]

3.2.2 1-hot-encoded vector approach

This configuration follows the principles of the first model (Section 3.1 [First Model and Architecture](#)) by using 1-hot-encoded vectors as input and output but there are no invented grammatical rules anymore. The training data is now directly related to concrete words and not to a word class. An illustration of the data structure is given in Figure 3.2.

3.2.3 Word vector approach

The Neural Network takes word vectors, a $300d$ -vector of real numbers, as input and omits them during training. Word vectors are calculated by `spacy`. To be precise, this step has two stages. Building the training data is easy because it is effortlessly possible to retrieve the real valued vector given a word. Since predictions aren't (and can't be) as accurate as the results `spacy` computes, it is impossible to query a dictionary or database to reshape the exact word. For such situations, the module offers the option to retrieve a list with the $n \in \mathbb{N}$ closest words. This list includes the n words whose vector representations have the smallest euclidean distance to the desired vector i. e., the prediction.

In the next step, a check is performed whether the word is part of the book i. e., the cognitive room. If so, the euclidean distance is taken as entry in the Transition Probability Matrix T , which will undergo a row-wise transformation to fit the criteria of a transition probability matrix. One disadvantage is an ambiguous prediction and therefore a less sharp T . But in comparison to the 1-hot-encoded vector, a word vector bears a lot more information, which hopefully can be exploited by the neural network. The data structure is shown in Figure 3.2 next to the 1-hot-encoded vector equivalent.

3.3 Average approach

Because the models become enormous and especially thus the evaluation difficult, this configuration aims to analyze the results on a rougher scale by taking averages of the predictions. While collecting the training data, the [POS](#)-tag of each one is saved and after training the cumulative outputs of a word class prediction are taken i. e., all 1-hot-encoded vectors of a [VERB](#) are mapped by the Neural Network, averaged into one vector and then checked for the most probable [POS](#)-tags (Section 4.3 [Averaging models](#)).

[POS](#)-tags were mentioned before in Section 3.2.1 [Data preparation](#) and are just another term for word classes. In detail, a subset of the UniversalDependencies [POS](#)-tags [dMar⁺]

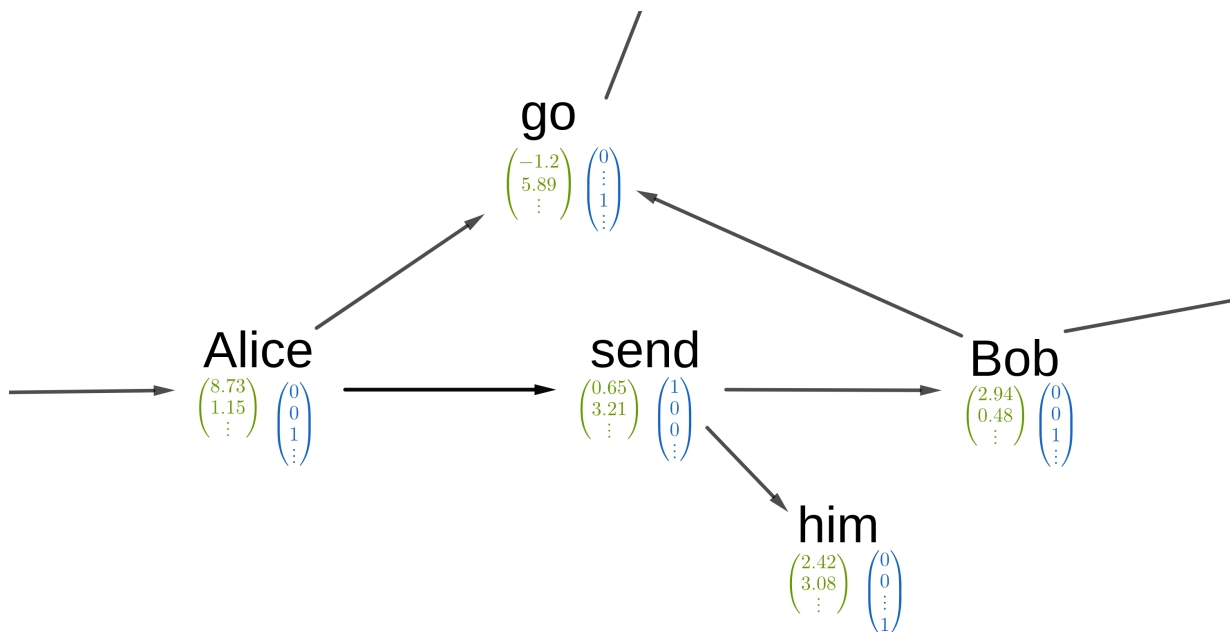


Figure 3.2: The word to word models can also be illustrated as graphs, though more complex. The lemmatized words of the text serve as vertices and the pairs mentioned before in Section 3.2.1 [Data preparation](#) as edges. In green are word vectors and in blue 1-hot-encoded vectors denoted. This cropped graph is generated by the bold passages of the text: “**Alice sends Bob** a message. **Alice goes** to the grocery store. Peter **sent him** a letter. **Bob went** to his friend.”

Table 3.1: List of relevant POS-tags including examples and short definition.

POS-tag	Definition & Example	POS-tag	Definition & Example
ADJ	Adjective: educated, hot	VERB	Verb: to run, to drink
ADV	Adverb: easily, everywhere	DET	Determiner: this, a, no
NOUN	Noun: car, bottle	PART	Particle: 's, not
AUX	Auxiliary: to have, should	ADP	Adposition (Pre- & Postpositions): in, on
PRON	Pronoun: she, ours	REST	Rest (Container for Conjunctions and additional residuals): and, if

are used (Table 3.1) because this project provides a rich dataset, good documentation and its guidelines are implemented by `spacy`.

Chapter 4

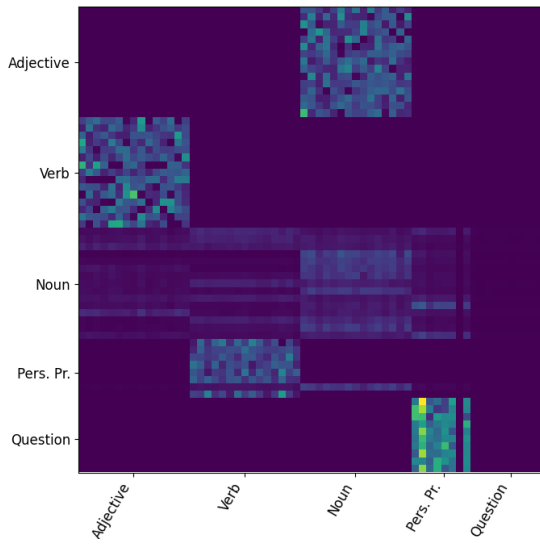
Methodology and Results

4.1 First Model and Architecture

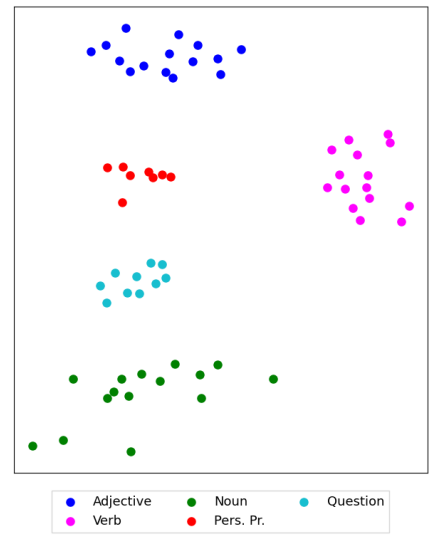
Starting with the predefined structures as mentioned in Section 3.1 [First Model and Architecture](#) i.e., a rule set was given which is equivalent to graphical model, where the rules describe the edges. The training data was composed by randomly choosing one of the five rules and the input as well as output word. The Neural Network was quite shallow because it contained only one hidden layer. By using eight words from each class the rules are easily learned (Figure 4.1). Since the rows encode the states, it is expected in the terms of the successor representation that the next position shows a high activation. Checking this behavior is simple because the environment (Section 3.1 [First Model and Architecture](#)) is clearly defined. The Noun part of Figure 4.1 is smeary because there is no rule for consecutive state (in graph theory it corresponds to a sink). The undefined behavior is also revealed in the [MDS](#) illustration where all nouns are distributed between the other word classes. By calculating the [SR](#) for additional time steps, the result incorporates all following rules or states (Figure 4.2). These matrices are interesting for analyzing the value function V (Equation (2.2)) which is beyond the scope of this work.

The principle also works out when using more rules and a larger data set. The enhancement is done by introducing four new rules

- Question word \rightarrow Verb
- Noun \rightarrow Personal Pronoun
- Adverb \rightarrow Possessive Pronoun

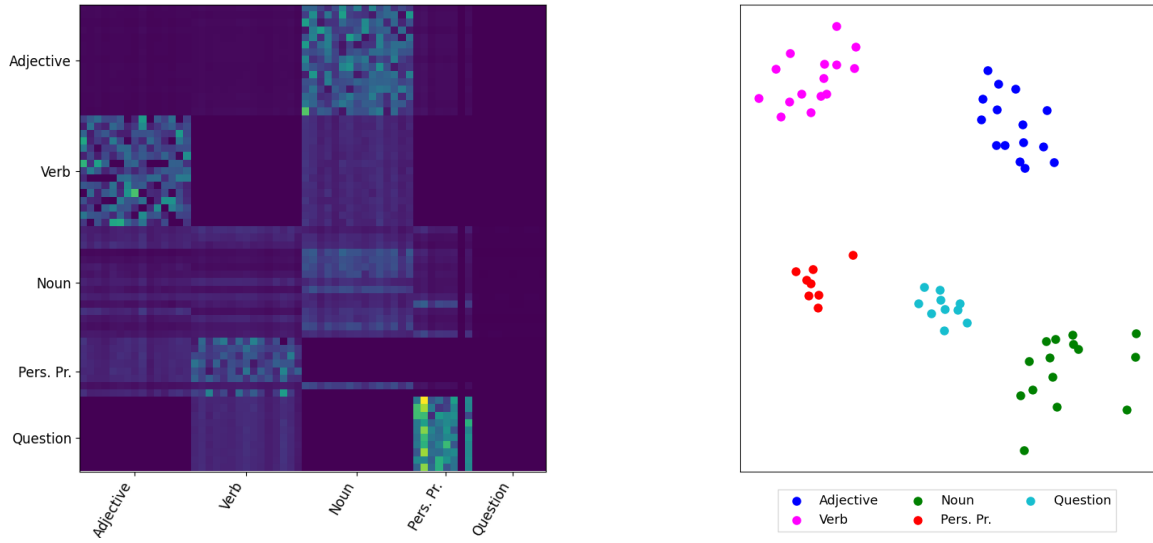


(a) Learned Successor Representation of a tailored cognitive room with apparent future states.



(b) MDS plot of the SR in (a) showing decent clusters.

Figure 4.1: Clearly visible are the successor positions of the states e.g., **Adjective** \rightarrow **Noun**. **Nouns** are smeary because the rule set in Section 3.1 **First Model and Architecture** doesn't provide one specifying starting on **Nouns**, so the Neural Network has to guess which results in less definite successors. Although there is a prediction made for each single word i.e., state in the cognitive room, only word classes are displayed to avoid clutter (Pers. Pr. = **Personal Pronoun**, Pos. Pr. = **Possessive Pronoun**).



(a) Calculated **SR** of a tailored cognitive room for $t = 2$ and $\gamma = 0.5$ using the matrix of Figure 4.1. (b) **MDS** plot of the **SR** in (a) with properly grouped word classes

Figure 4.2: Calculating the Successor Representation for one higher time step i. e., $t = 2$, already demonstrates the properties of the construction. For all states (visual aggregated into the word class) it is possible to derive successor states e. g., the two step rule **Question** \rightarrow **Pers. Pr.** \rightarrow **Verb**.

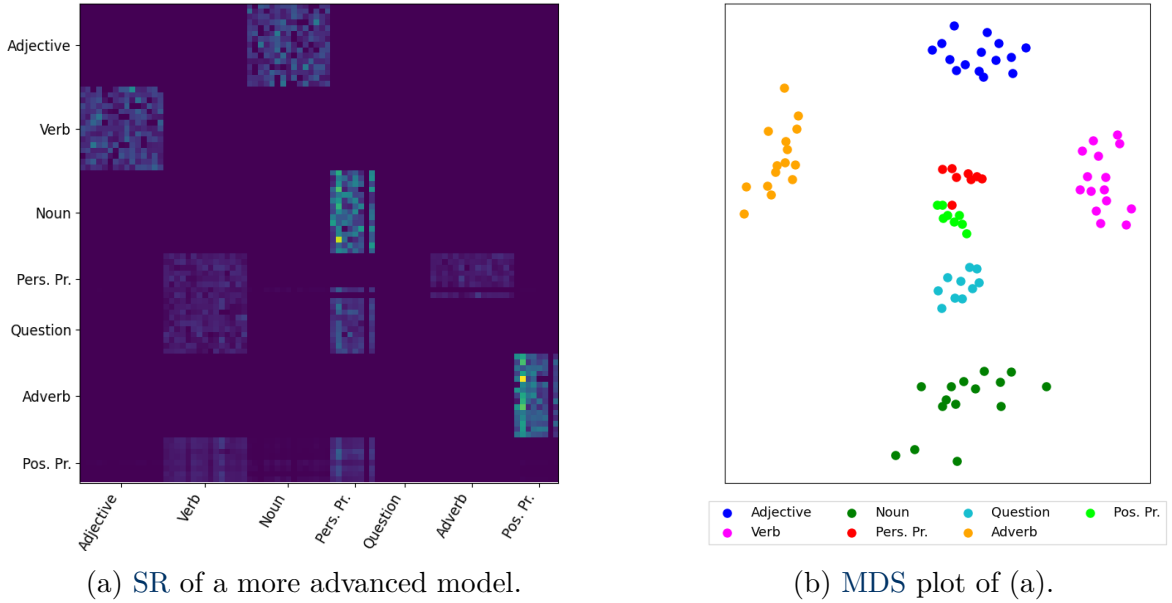


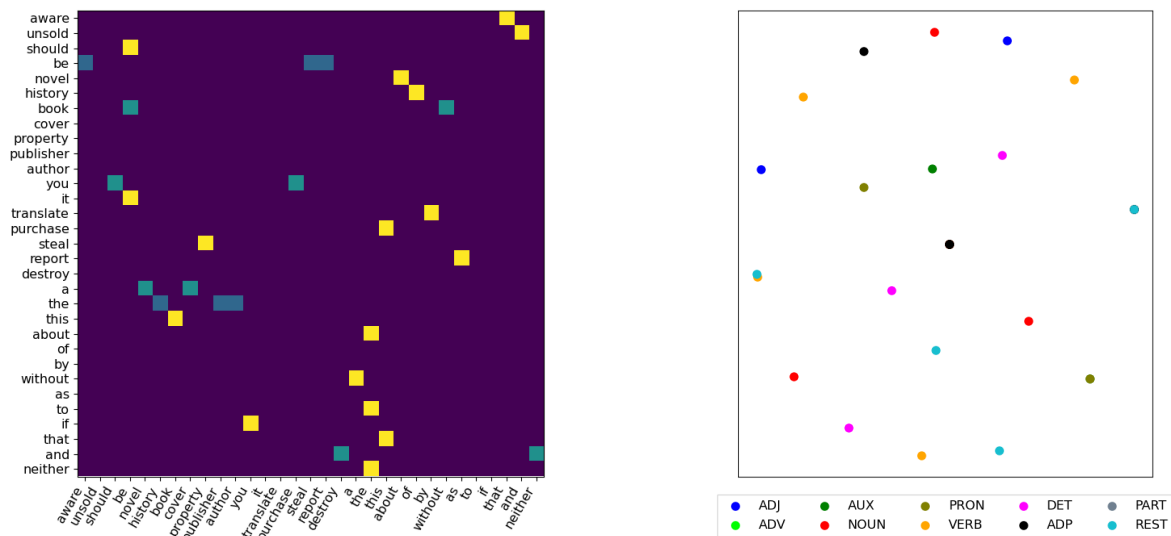
Figure 4.3: The illustrated plots stem from a model using additional rules backed by more word classes and a larger database to retrieve the training data. The outcomes are similar to Figure 4.1. The upcoming states are obvious. The model can handle ambiguous successors e. g., *Personal Pronoun* \rightarrow *Verb* and *Personal Pronoun* \rightarrow *Adverb* are deployed rules.

- *Personal Pronoun* \rightarrow *Adverb*,

more words for the already existing categories and two new word classes (*Adverb* and *Possessive Pronoun*). The result in Figure 4.3 is in clarity similar to Figure 4.1 but without having an obvious blurry row even though the word class *Possessive Pronoun* is without successor as *Noun* in the trial before but some similarities to *Question word* are detected. The only characteristic they seem to share is having exactly one edge. The clusters are in the MDS apparent. Although artificial, conceptually they serve as a standard to reach for the upcoming configurations.

4.2 Word to word models

The harder challenge lies in processing natural languages. For this purpose two different approaches, namely *1-hot-encoded vector approach* and *Word vector approach* were examined. The ambitious goal was to learn or get a sense of the grammatical structure of the text. In practice this means that after feeding e. g., an adjective into the Neural Network it



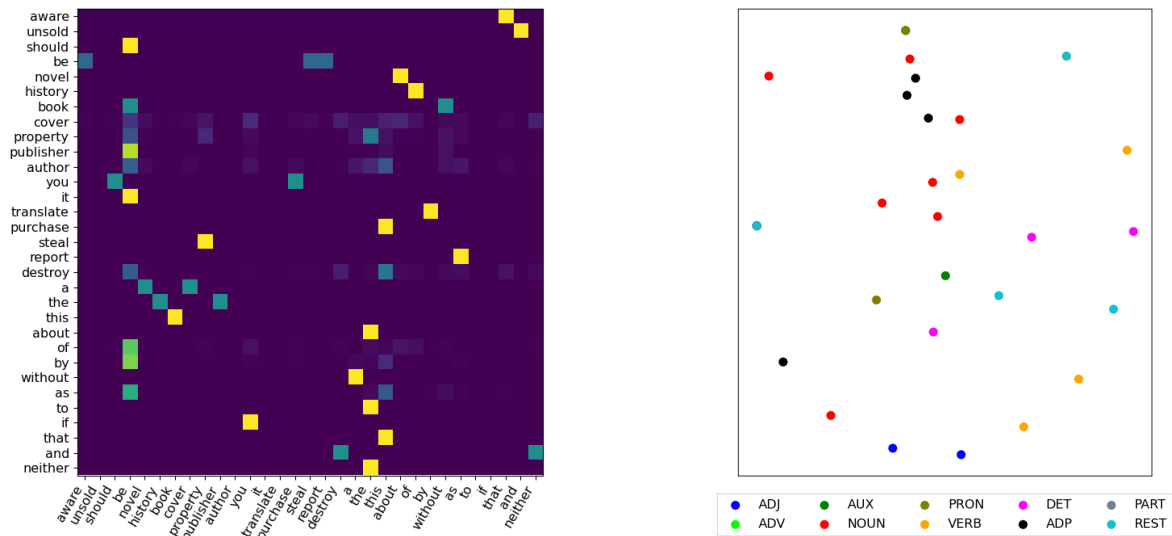
(a) Exemplary ground truth distribution of a tiny data set. (b) Corresponding MDS plot of the ground truth in (a).

Figure 4.4: For illustrative purposes only a tiny data set i. e., few words of the book were processed to calculate the ground truth distribution.

should propose words or word classes which follow this word. In the following paragraphs an schematic outline of the model will be given i. e., few data was involved to achieve more reasonable diagrams. The full book covers multiple thousands of states, leading to a sparse squared matrix in this dimension. Thus, depicting matrices no longer makes sense.

To be able to evaluate the results a ground truth distribution was calculated for gaining a qualitative and quantitative measure. In Figure 4.4 is one depicted. The data set is labeled on the axis. There is also a MDS plot next to it because on larger scaled models (> 500 words) it is impossible to get visual feedback just by looking at the matrix plot. The hope is that clusters of the same color emerge, as seen in Section 4.1 [First Model and Architecture](#), because some meta word pairs, for example *Noun* \rightarrow *Verb* i. e., *Alice* \rightarrow *goes* and *wood* \rightarrow *breaks*, should share some features and be mapped close to each other. Furthermore, similarities are to some extent also visible by looking at the MDS.

Having a reference now, the model was set up for training. In Figure 4.5 is an emblematic transition matrix illustrated. Whereas in Section 4.1 [First Model and Architecture](#) it was easy to recognize the rules in the SR, this will no longer be possible due to the sheer amount of states. Hence, the cluster plot is more important to gain visual intuition for the results.



(a) Learned SR-matrix of model using 1-hot-encoded vectors during training.

(b) MDS clustering of the Successor Representation in (a).

Figure 4.5: Transition probability matrix of model using rules constructed by processing a book und 1-hot-encoded vectors to learn. Hence, the environment is no longer manufactured. Whereas the results of the models in Section 4.1 [First Model and Architecture](#) were fully described by the matrix plot this will no longer be possible for large scale models because the matrix becomes to huge. As seen before can the MDS occupy this role. If sufficient learning happened, clusters or similarities to the corresponding plot of the ground truth should be recognizable. (Though not when illustrating with the tiny data set.)

Table 4.1: Trained models with metric values regarding their corresponding ground truth. “german” and “english” refer to the book which provided the data set (s. Section 3.2.1 [Data preparation](#)). The associated [MDS](#) plots for a qualitative feedback can be found in Figure B.1 and Figure B.2 of Appendix B [Cluster plots of word to word models](#).

Version	Metric
german, 1-hot-encoded vector	0.08
german, word vector	0.74
english, 1-hot-encoded vector	0.10
english, word vector	0.78

4.2.1 Word to word models: Evaluating the results

To achieve the best result four configurations were tested and compared in Table 4.1 by the metric introduced in Section 2.5 [Metric for quantifying the results](#). Surprisingly, the german and english 1-hot-encoded vector versions nearly don’t differ. Not only regarding the model used to collect the data illustrated in this thesis but in general. Due to the beforehand mentioned freer word order german incorporates, a better score for the english based models was expected.

It is obvious that the models using word vectors perform quite bad compared to the 1-hot-encoded vector variants. The cause may be on the one hand that language is a structural complex field and on the other that too many uncertainties are attached to word vectors, learning is more difficult since 300 distinct values are involved, whereas a 1-hot-encoded vector may be quite accurate if the learned version has its maximum near or at the index where the input vector is equal to 1. Also back-calculating the output to words is a process of compromises because it is guaranteed that `spacy` doesn’t provide a word vector with the exact same components and it is necessary to limit on the n closest word vectors/words. The disappointing outcome of the word vector model is furthermore frustrating since it is more probable that the hippocampus doesn’t process signals which are close to 1-hot-encoded vectors (or an analogy of it) but rather multiple stimuli decoding different characteristics which is thus more related to a word vector.

Additional configurations While searching for the best parameters, not just the four versions mentioned were examined. Most of the time was consumed by finding a promising setup. This is reflected by some parameters the framework provides (e.g., `nmb_hidden_layers`, Section D [Training parameters](#)) which aren’t necessary to reproduce the results presented

Table 4.2: Schematic sentences of the book used in Figure 4.6.

Rule	Sentence
ADP → NOUN	Sie hat mich zum Schmunzeln gebracht.
ADP → PRON	Es war überaus angenehm, sich mit Ihnen zu unterhalten.
ADP → DET	Ich bin nämlich eine gebürtige Linkshänderin, die in der Schule, [...]
ADJ → NOUN	Lieber Leo, ich habe drei fürchterliche Tage hinter mir.

in this work. A subset with illustrations and short documentation of all variants can be found in Appendix A [Additional configurations](#).

4.3 Averaging models

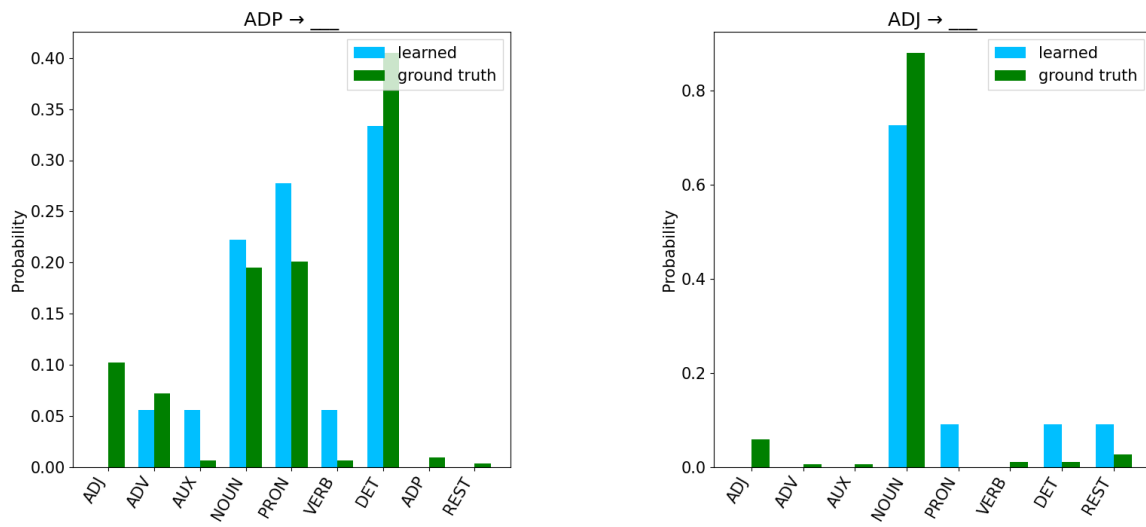
Because large scale word to word models seem to lack characteristics for a proper evaluation and interpretation of the results, the average approach was developed (Section 3.3 [Average approach](#)). The main idea is to rearrange the output of the formerly presented models, because general patterns like **Noun** → **Verb** or **Determiner** → **Adjective** appear significantly more frequently than certain instances as **sun** → **shines** or **an** → **old**. By averaging the predictions one might be able to catch the structure in general.

Since Section 3.3 [Average approach](#) only provided a rough description of the principle, it shall be extended in the following. After the collective prediction of one word class, all outputs are averaged having one vector resembling the complete data in the dimension of the cognitive room showing the associated frequencies. In the next step the n indices (in practice 10 was used) with the highest values are checked for their **POS**-tag. So, if index i is one of the n highest and encodes the word **fish**, its **POS**-tag i.e., **NOUN** will be counted. Finally, one has constructed a vector for all word classes where each component resembles the probabilities for the successor word class. Some final numbers are illustrated in Figure 4.6.

To get an idea of the learned results, some valid sentences are provided in german (the language of the training data of Figure 4.6) in Table 4.2. This short sanity check implies that there is no cacophony learned and the outputs are reasonable.

4.3.1 Averaging models: Evaluating the results

The same configurations as in Section 4.2.1 [Word to word models: Evaluating the results](#) were processed. By “configurations” is subsumed: german and english, 1-hot-encoded vector



(a) Averaged transitions of all ADPs compared to the ground truth.

(b) Averaged transitions of all ADJs compared to the ground truth.

Figure 4.6: Comparison of the averaged predictions (green) with the ground truth distribution (blue). The model was trained by 1-hot-encoded vectors and german data. If a POS-tag has no blue bar, it has a 0% probability to appear as successor e. g., after an ADJ comes no ADP. The remaining plots of the other POS-tags can be found in [Appendix C Barplots of the average approach](#).

Table 4.3: Averaged means of the difference between prediction and ground truth. As expected, the word vector versions have higher scores than the 1-hot-encoded vector counterpart. These values can't be used for a comparison with Table 4.1 because the underlying metrics are different.

Version	Mean in 10^{-2}	Standard deviation in 10^{-2}
german, 1-hot-encoded vector	7.3	2.0
german, word vector	14.0	2.1
english, 1-hot-encoded vector	8.1	3.3
english, word vector	10.2	3.6

or word vector version and the same number of epochs and words used for training. After the unsatisfactory performance of the word vector approaches (Table 4.1) everything else than a similar outcome would be surprising. A detailed illustration of the results offers Figure 4.7. By this plot it is also possible to talk about the outcomes a bit more specifically. All means are to some extent equal but the standard deviations differ. The free word order of german doesn't seem to be a problem because both models learn better than their english counterparts (Table 4.3). Surprisingly, there are some difficulties with adjectives (except for Ger. OHE), although adjectives are tied to NOUN and ADJ (Figure 4.6).

Sadly, the prepared visualizations i. e., Figure 4.7 and Table 4.3, lack the ability to grasp the full picture: The word vector configurations seem to work by checking the means for each POS-tag, although using german scratches the edge of the phrase, but when inspecting the matrices as a whole as in Figure 4.8, it is apparent that they don't. Whereas using the english book the model degenerates to the identical distribution and the german one contemplates NOUN as its personal 42.

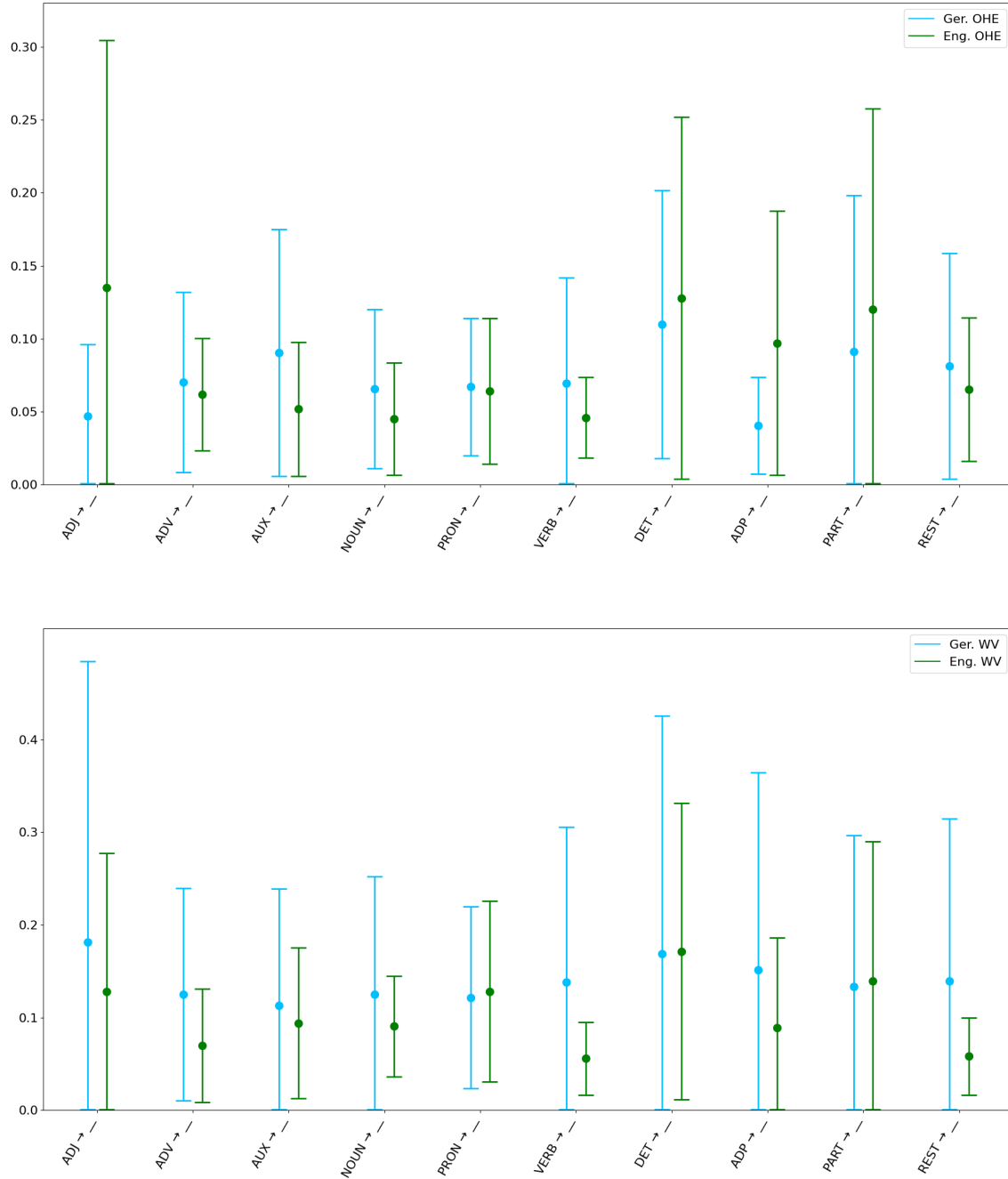
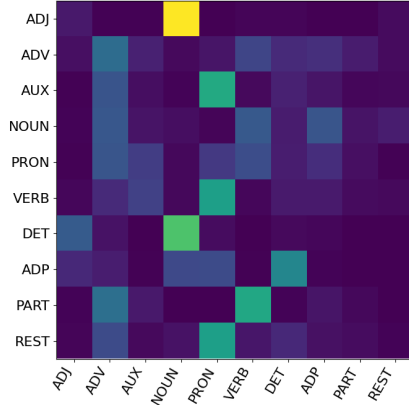
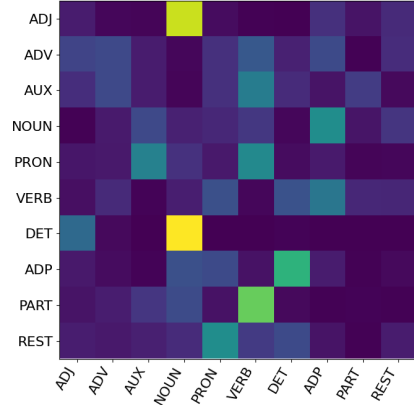


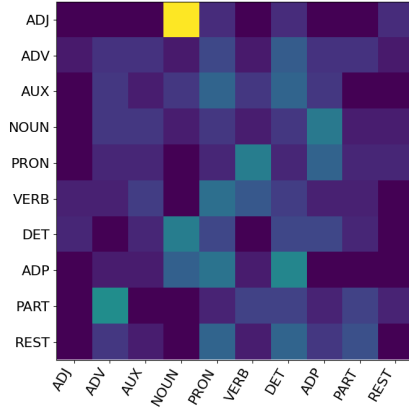
Figure 4.7: Mean and standard deviation of the configurations w.r. t. to the ground truth i.e., the difference between the ground truth matrix and the prediction matrix was used for the row wise calculations (matrices depicted in Figure 4.8). Clearly visible that 1-hot-encoded vector models (OHE) outperform word vector versions (WV). Both, mean and standard deviation are lower. Because a difference is assessed, smaller means are better.



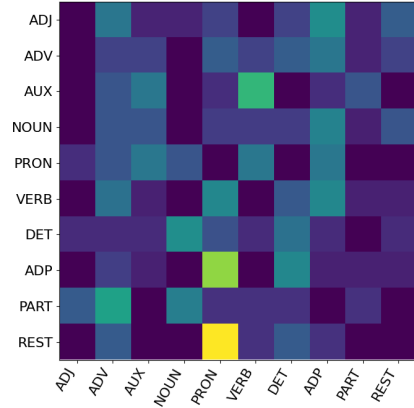
(a) German, ground truth of word class transitions.



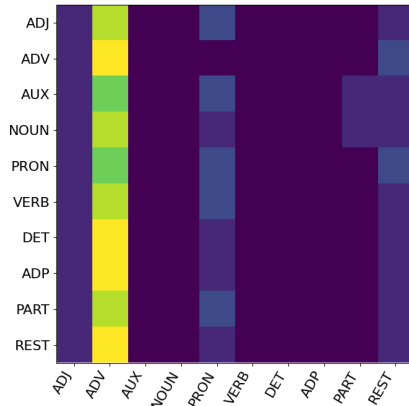
(b) English, ground truth of word class transitions.



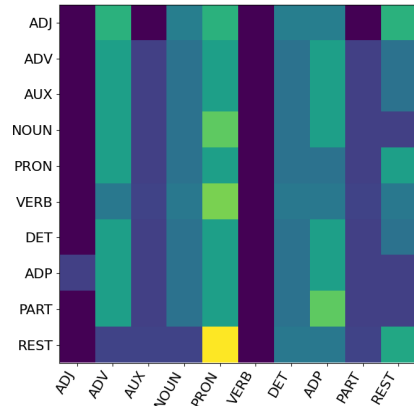
(c) German, learned SR using 1-hot-encoded vectors.



(d) English, learned SR using 1-hot-encoded vectors.



(e) German, learned SR using word vectors.



(f) English, learned SR using word vectors.

Figure 4.8: If word vectors are used for training the model has problems with both languages. When using German the predictions degenerate completely and will classify everything as NOUN. The outcome of precessing English is reversed: it is quite close to an identical distribution which equals mere guessing amidst the POS-tags.

Chapter 5

Conclusion

Since no data from valid neural scans researching the same or an similar topic was provided, the project is heavily theory based (in comparison to [Sta⁺17]) which makes the interpretation of the results a priori not easy because a quantitative and qualitative frame of reference is missing. There were sharp results produced in Section 4.1 [First Model and Architecture](#) but they are too artificial to draw relevant conclusions regarding the objective and neuroscientist won't collect data as clear.

While trying to reproduce them i. e., getting as close as possible, many architectures were unsuccessfully tested and evaluated as mentioned in Appendix A [Additional configurations](#). Therefore, the process of finding a proper one consumed many weeks with discussions between my advisor and me. Maybe, the goals were slightly too ambitious. Additionally, they more or less led to the same results covered in this thesis, especially in Section 4.2 [Word to word models](#). Although, the values calculated in Table 4.1 are relatively low and close to 0, which means a perfect fit according to Section 2.5 [Metric for quantifying the results](#), the metric d_A itself isn't justified for more than internal comparisons of the configurations. It was developed to have a sensible measure on the results because plots of high dimensional sparse matrices, which are just monochromatic squares, don't convince. From the figures in Table 4.1 & Table 4.3 can be deduced that models training with word vectors have an unsatisfactory performance in comparison to their equivalents working with 1-hot-encoded vectors. This is unsatisfying for two reasons: Firstly, getting the approach working costed much time because the implementation of the mechanics `spacy` offers and integrating them into the concept of the cognitive room were the most elaborate part in the process of building the framework, and secondly because the input the hippocampus receives is probably closer to a word vector than to a 1-hot-encoded vector. Translating it into a

neuroscience behavior, it can be compared with receiving plenty of signals as input against processing one (strong) activation from another cell.

By presenting the topic in front of my colloquium, further approaches were gathered. One of them, the idea of averaging the predictions of one word class and analyzing the outcome, paid off (s. Section 3.3 [Average approach](#) & Section 4.3 [Averaging models](#)). The results found there can function as addition to the plain word models because they prove that these models can grasp grammatical structure. Therefore, they can provide visual feedback even in large dimensional contexts and by calculating the ground truth distribution there is a useful reference.

But nevertheless, the 1-hot-encoded vector variant can serve as foundation for further (minor) research, for instance developing a better metric to have a mathematical notion of encoding a good and objective value or tweaking the learning with word vectors due to the better compatibility with hippocampal functions. Of great value would be collected data from an analogue survey conducted by neuroscientist i. e., analyzing the activity of the hippocampus, the place and grid cells while participants process new pieces of language. Then is a viable environment as in [\[Sta⁺17\]](#) is given and the theory may be expanded to language related topics as it is to spatial navigation.

Appendix A

Additional configurations

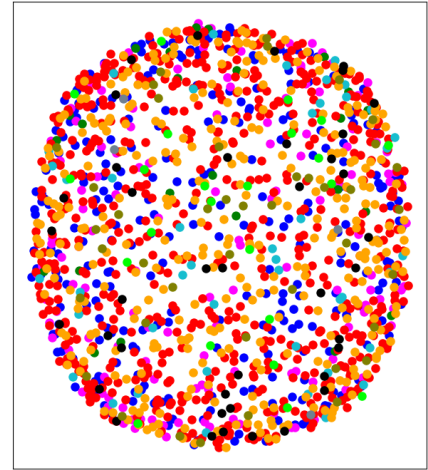
To draw a full picture, plenty of approaches which had the goal to improve the results will be mentioned in this chapter. Sadly, no one changed the outcome by any means. Facing this presented an enormous obstacle while researching. Some of them will be presented shortly in this chapter. In all cases it is obvious that these configurations were dead ends.

A.1 Multiple hidden layers

Different numbers of layers ranging from 1 to 100 were tested, some example results will be depicted.

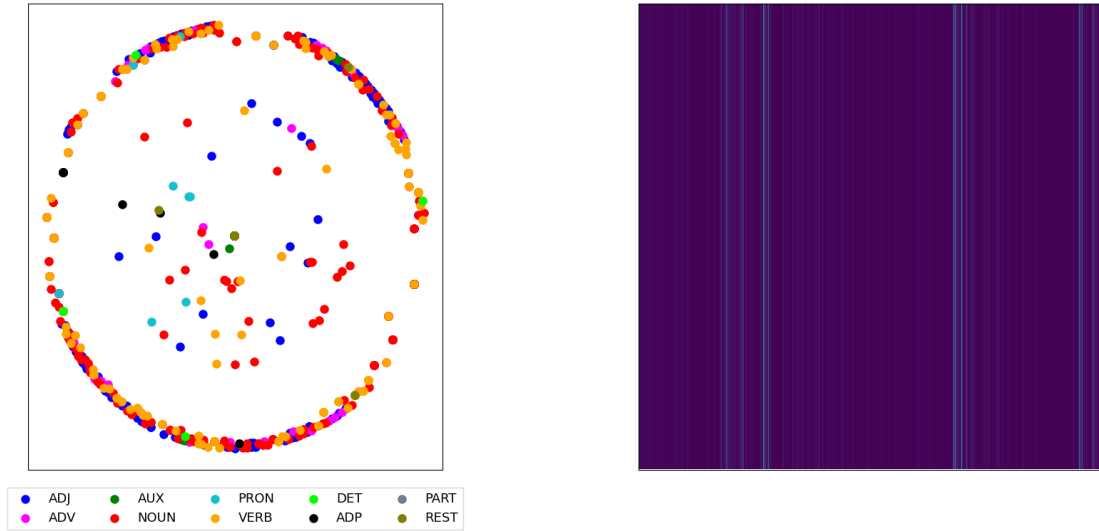


(a) **SR** of a model using english and 1-hot-encoded vectors with 40 hidden layers.



(b) **MDS** of the matrix in (a).

Figure A.1: Although mentioned that transition probability matrices don't show anything if too many words are used, they can be used sometimes to detect failure. The reference, at least for the **MDS**, is illustrated in Figure B.1b. The value of the metric is 0.50, the equivalent with one layer achieves 0.10. This could imply that more layers hamper learning.



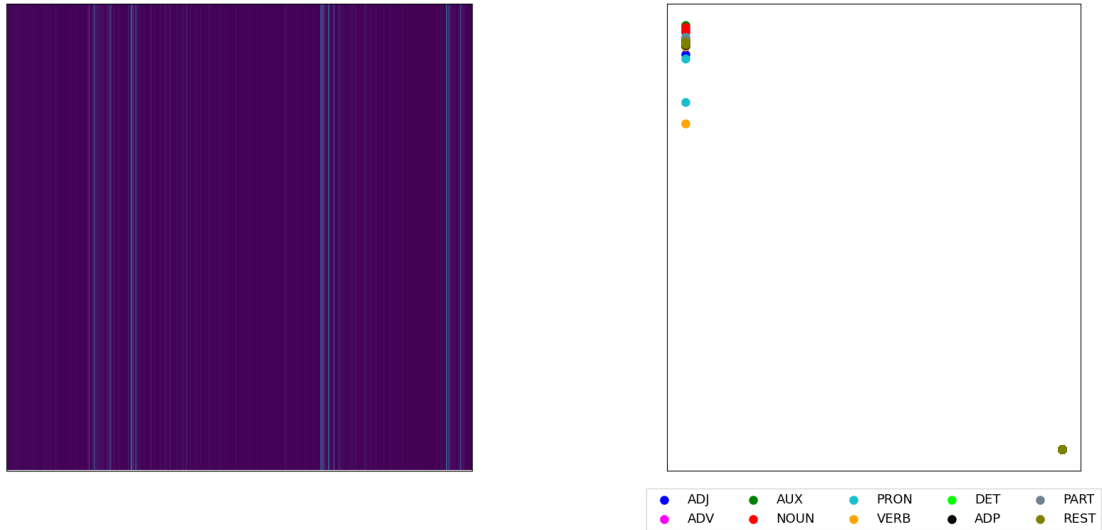
(a) MDS of a model using english and 1-hot-encoded vectors with 2 hidden layers.

(b) SR of a model using english and 1-hot-encoded vectors with 10 hidden layers.

Figure A.2: As mentioned before, more layers result in worse SRs. Already one additional hidden layer lowers the metric. The model in (a) reaches 0.22, whereas with one hidden layer the value is 0.10. The network in (b) was configured with 10 hidden layers and the successor representation looks indistinguishable from one training with 40 (Figure A.1).

A.2 Many epochs and multiple hidden layers

The example outputs stem from a model which trained with sixfold epochs and 40 hidden layers.



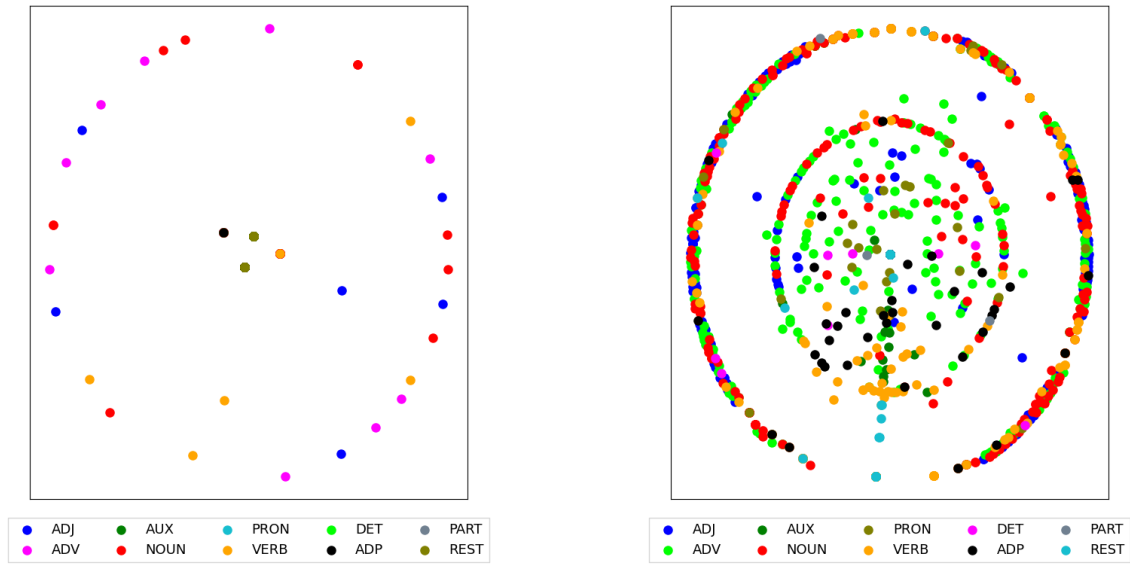
(a) English, 1-hot-encoded vectors, 25,000 epochs and 40 layers.

(b) MDS of a model using english, word vectors, 25,000 epochs and 40 layers

Figure A.3: The only conclusion to draw from this plot of two different models is that additional epochs might lead to a full degeneration of the results if word vectors are used for training. The 1-hot-encoded vector analogue shows no mismatch to them of Section A.1 Multiple hidden layers.

A.3 Using word vectors to learn an 1-hot-encoded vector

This configuration is combination of two mainly used in the thesis. It uses word vectors as input and 1-hot-encoded vectors as output i. e., it uses heterogeneous structured training data.



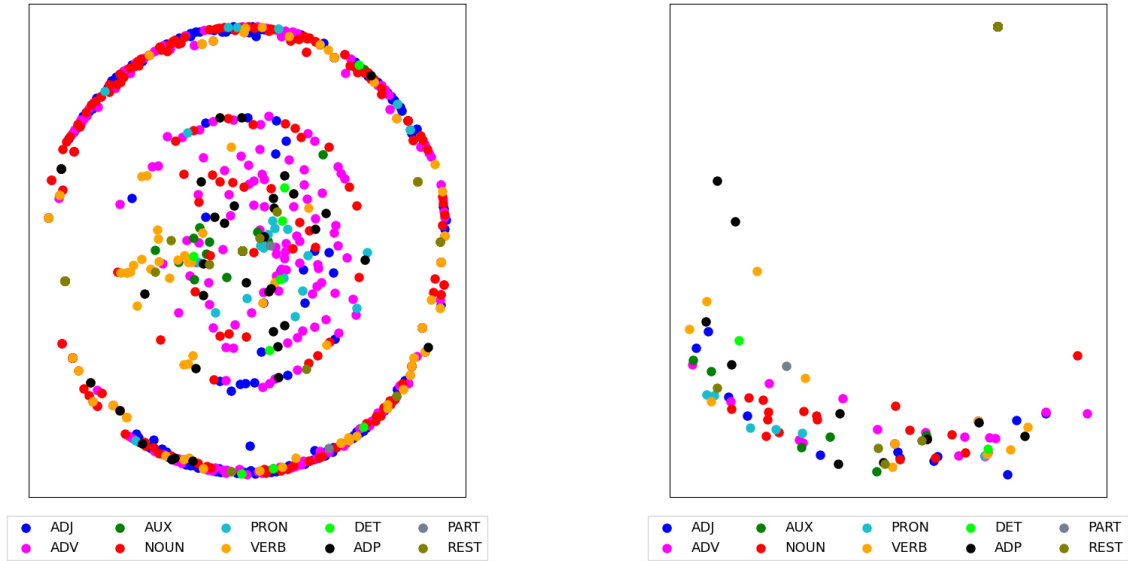
(a) English, word vector to 1-hot-encoded vector as MDS.

(b) German, ground truth MDS of word to word transitions.

Figure A.4: MDS plot of a model using german training data and word vectors as input to learn a 1-hot-encoded vector. The results lack characteristics to draw sensible conclusions from. Though it is possible to calculate the metric for the configuration: 0.47. By comparing with Table 4.1, it sits between its full 1-hot-encoded vector and word vector relatives.

A.4 Multiplying the training data

The goal of multiplying the training data i. e., concatenating the training data n times with itself, was to have the opportunity to see the training data more often during one epoch.



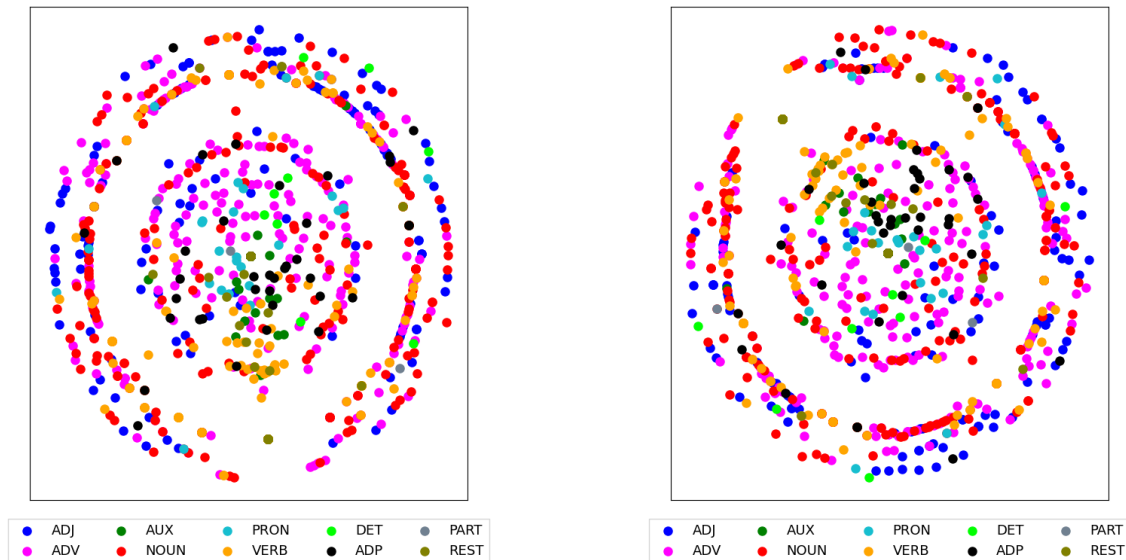
(a) German, 1-hot-encoded vectors with 5 concatenations.

(b) German, word vectors with 5 concatenations.

Figure A.5: Concatenating the training data 5 times with itself doesn't change outcomes (compare Figure B.2). This impression is fortified by the metrics both models achieve: 0.14 for 1-hot-encoded vectors and 0.72 with word vectors (0.08 and 0.74 without respectively, Table 4.1).

A.5 Calculating high time steps

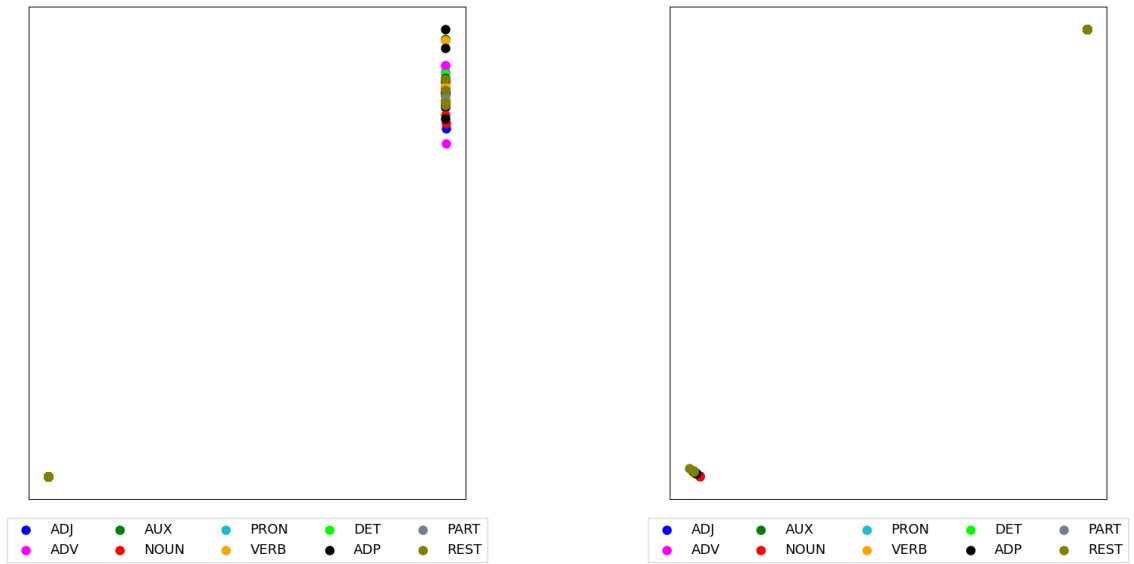
One idea was to calculate high time steps of the SR hoping the irregularities even out in distant future.



(a) MDS of a SR with $t = 20$. German and 1-hot-encoded vectors were used during training.

(b) MDS of a SR with $t = 50$. German and 1-hot-encoded vectors were used during training.

Figure A.6: High times also don't bring progress since no evident structure is recognizable within the plots. A comparison with the ground truth wouldn't bring additional insights too because the underlying matrices can't be interpreted as transition probability matrices.

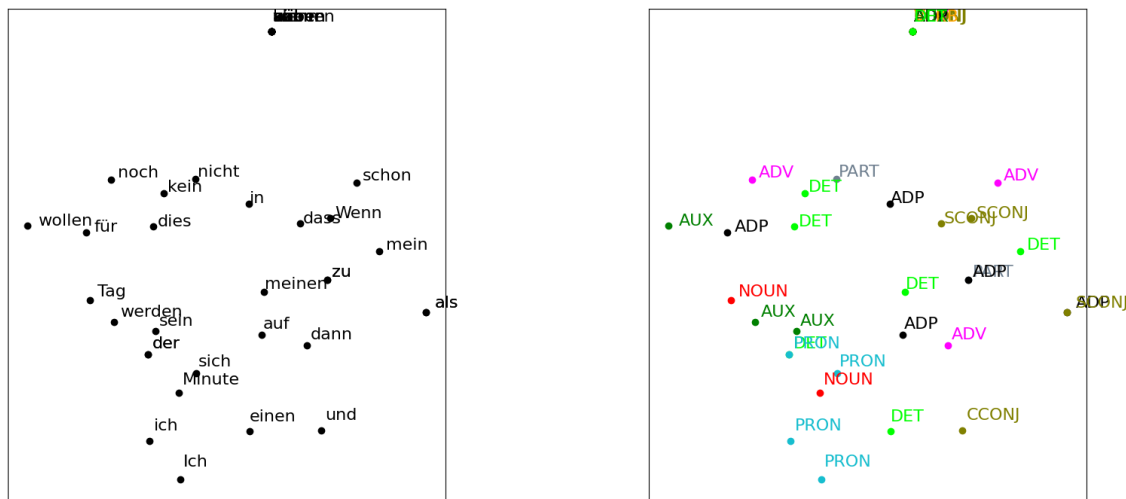


(a) MDS of a SR with $t = 20$. German and word vectors were used during training.

(b) MDS of a SR with $t = 50$. German and word vectors were used during training.

Figure A.7: As before in Figure A.6 no structure is recognizable to do further research on. Results relying on word vectors again seem to be very labile and degenerate.

Similar to Section A.4 [Multiplying the training data](#), the most frequent words of the text are seen more often by the network. Hence it might be able to learn these inputs better than ordinary ones.



(a) German with word vectors. MDS of the 40 most frequent words.

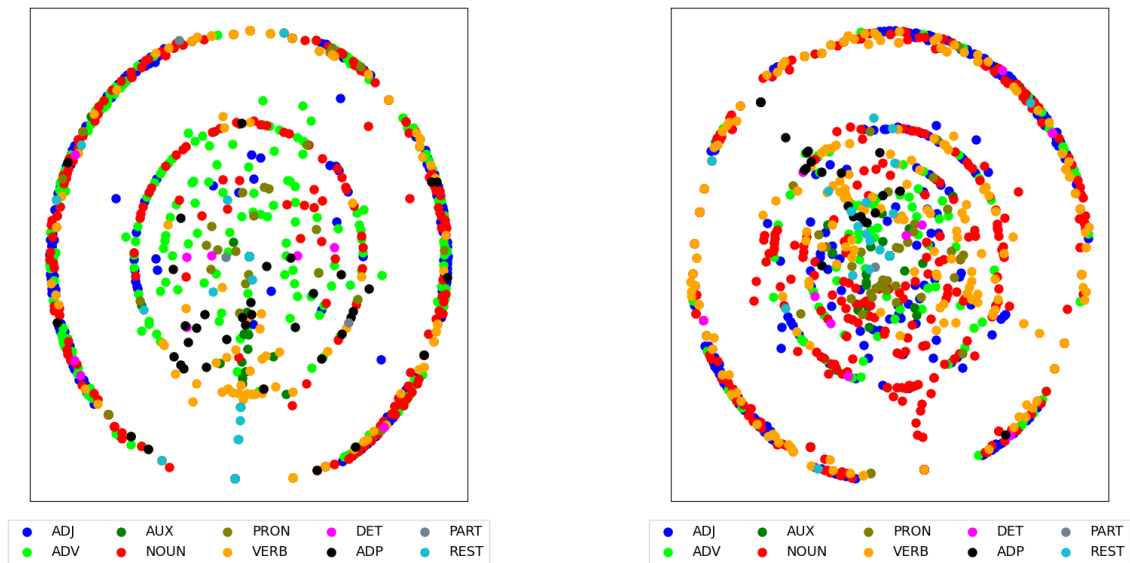
(b) Same MDS plot as in (a) but annotated with POS-tags instead of words.

Figure A.8: The same model with german data set and word vectors as in Section 4.2 [Word to word models](#) was trained. Predictions were limited to the 40 most frequent words. For a better overview the second plot was labeled with the corresponding POS-tags.

Appendix B

Cluster plots of word to word models

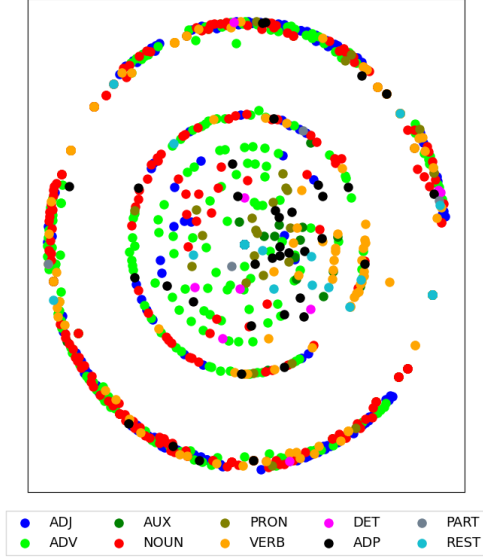
Visualizing matrices training with more than 500 words doesn't make sense, because the result is high dimensional and sparse. To get at least some visual feedback, MDS plots are calculated. To avoid a crowded picture, a compromise had to be made: depicting solely the POS-tag means a manageable overview but information on single words gets lost.



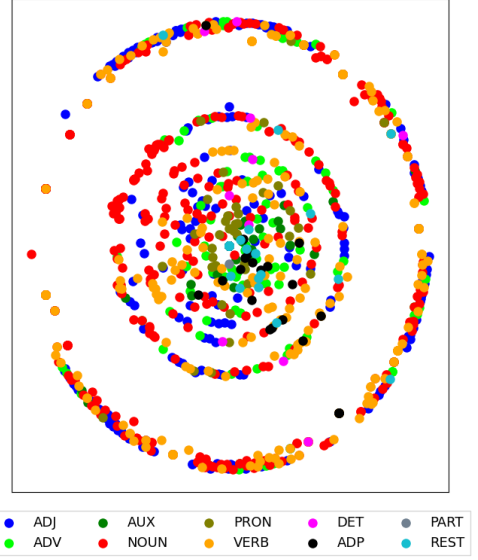
(a) German, ground truth MDS of word to word transitions.

(b) English, ground truth MDS of word to word transitions.

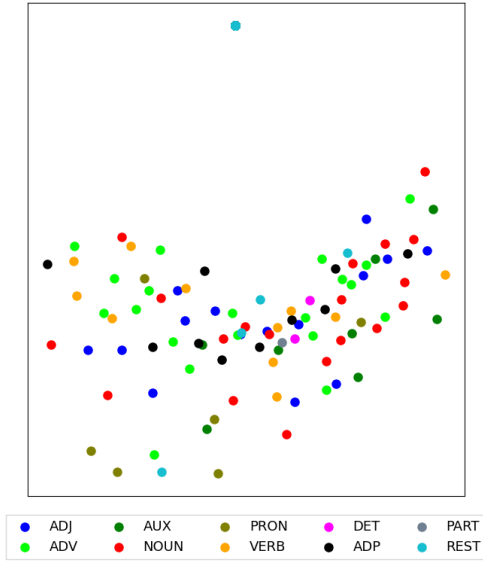
Figure B.1



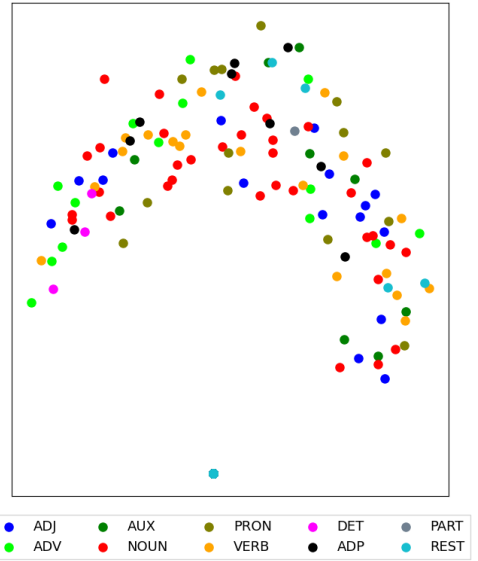
(a) German, MDS of learned SR using 1-hot-encoded vectors. Metric: 0.08.



(b) English, MDS of learned SR using 1-hot-encoded vectors. Metric: 0.1.



(c) German, MDS of learned SR using word vectors. Metric: 0.74.



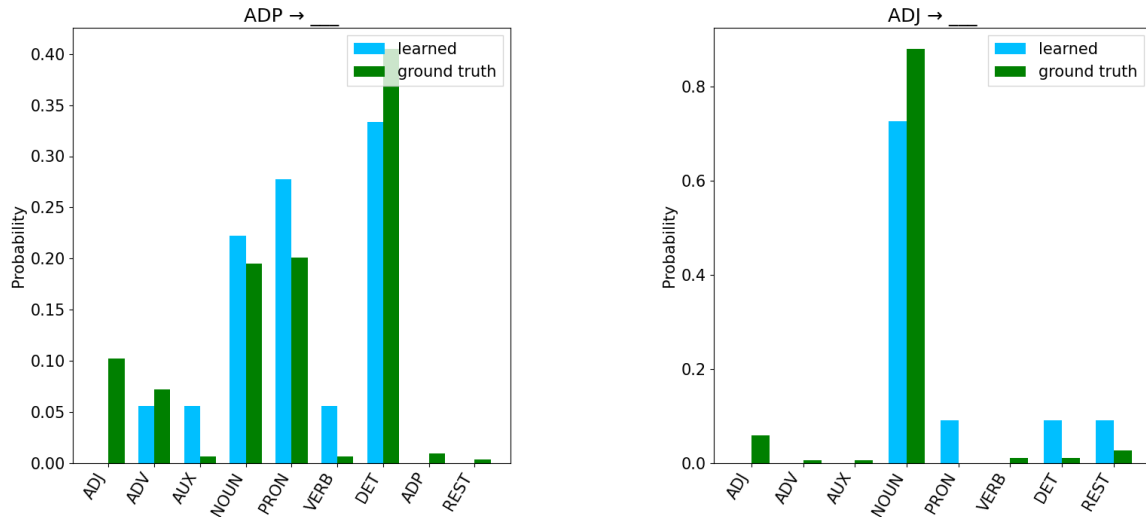
(d) English, MDS of learned SR using word vectors. Metric: 0.78.

Figure B.2: The 1-hot-encoded vector models show some resemblance with the ground truth in Figure B.1. The disappointing results of word vectors is not just visible by the different shape the dots occupy but also by their number, much less are visible i. e., many are mapped onto each other. Hence the Network produces the same output for different inputs.

Appendix C

Barplots of the average approach

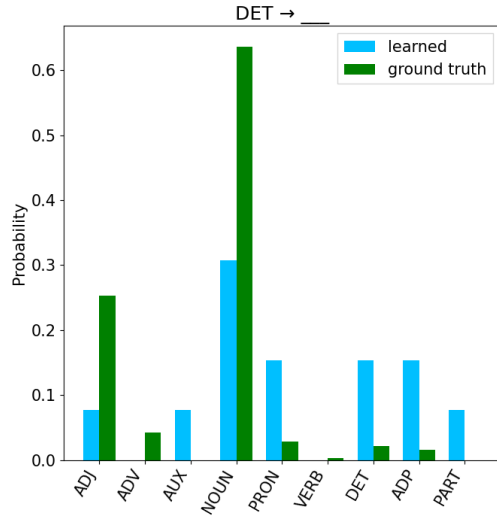
The barplots illustrated here stem from a 1-hot-encoded vector model using a german book to collect the training data. It achieved the best value ($7.3 \cdot 10^{-2}$) of all models tested. The scores are listed in Table 4.3. If a POS-tag doesn't appear in the plots i.e., having no green or blue bar, this means that it doesn't succeed the depicted POS-tag. The explanation of the POS-tags can be found in Table 3.1.



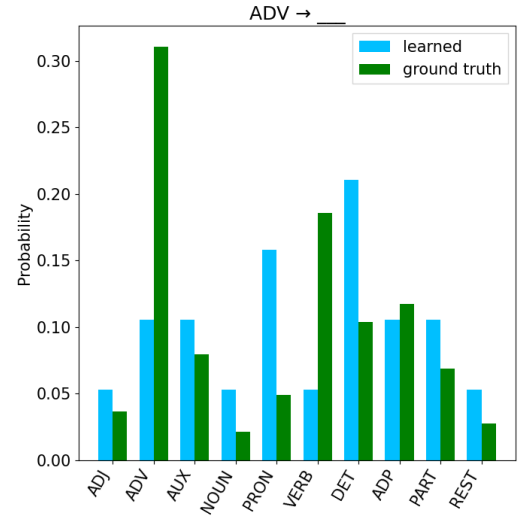
(a) Averaged transitions of all ADPs compared to the ground truth.

(b) Averaged transitions of all ADJs compared to the ground truth.

Figure C.1

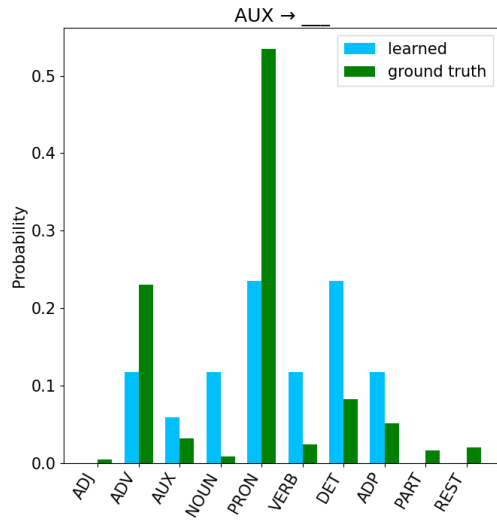


(a) Averaged transitions of all DETs compared to the ground truth.

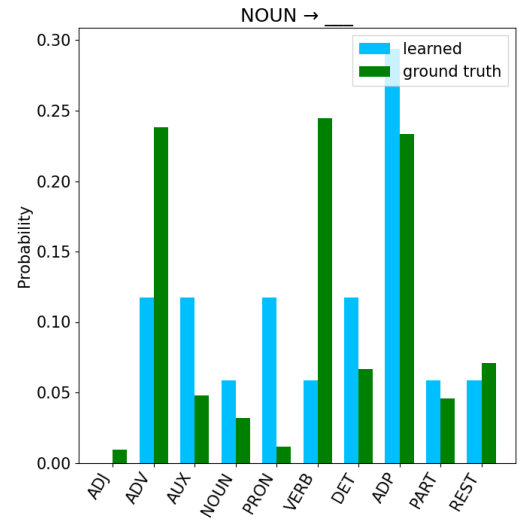


(b) Averaged transitions of all ADVs compared to the ground truth.

Figure C.2

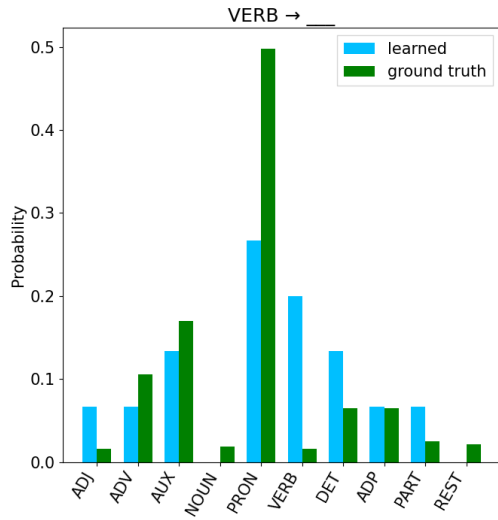


(a) Averaged transitions of all AUXs compared to the ground truth.

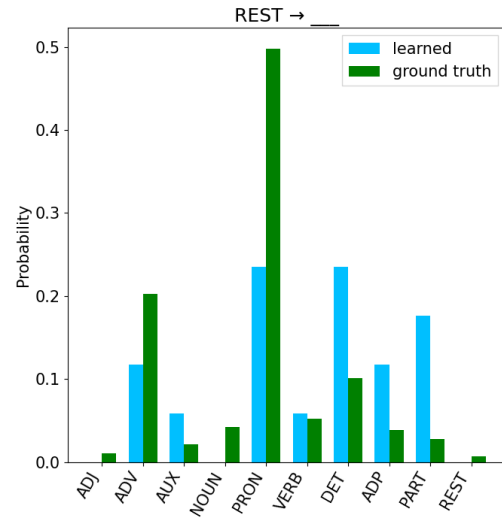


(b) Averaged transitions of all NOUNs compared to the ground truth.

Figure C.3

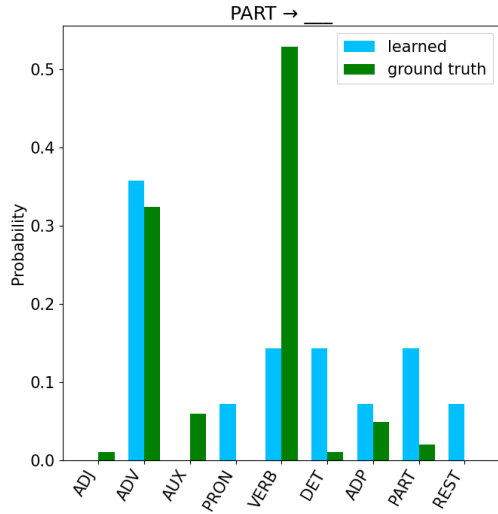


(a) Averaged transitions of all VERBs compared to the ground truth.

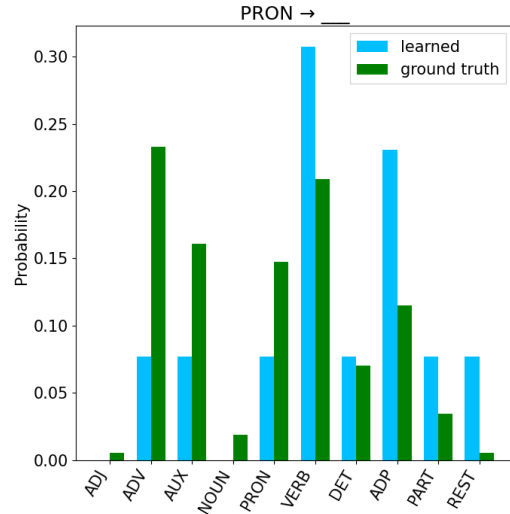


(b) Averaged transitions of all RESTs compared to the ground truth.

Figure C.4



(a) Averaged transitions of all PARTs compared to the ground truth.



(b) Averaged transitions of all PRONs compared to the ground truth.

Figure C.5

Appendix D

Training parameters

In case my results shall be reproduced with the framework I programmed, the parameters of Table D.1 were used. For the results in Appendix A [Additional configurations](#) the numbers differ e. g., more `epochs`, a higher `nmb_hidden_layers` or `nmb_concatenations`. The exact factor is mentioned there.

Table D.1: Training parameters of the network.

Parameter	Value
Learning rate <code>lr</code>	0.1
<code>epochs</code>	4000
<code>batch_size</code>	100
<code>pages</code>	200
<code>nmb_tokens</code>	1500
<code>nmb_hidden_layers</code>	1
<code>nmb_concatenations</code>	1
<code>book_name</code>	0 (german), 1 (english)

List of Abbreviations

HBP Human Brain Project

MDS Multidimensional Scaling

NLP Natural Language Processing

POS Part-of-speech

RL Reinforcement Learning

SR Successor Representation

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