
PID_control Documentation

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Philipp Schuette, Daniel Schuette

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INTRODUCTION TO PID_CONTROL'S DOCUMENTATION

This is a custom introduction for the PID_control documentation! At this point, it is simply a placeholder for something meaningful. The only actual information you can find here, are the following references: [\[Son98\]](#), [\[Fö90\]](#).

1.1 Example Section for the Spinx Documentation

Here is a section with a very complicated formula:

$$1 + 1 = 2 \tag{1.1}$$

PID_CONTROL MAIN MODULE

```
class PID_control.AnimatedPendulum(phi0, phi0_dot, alpha, beta, mu, max_control, frequency,  
                                     deadband, set_point, precision, t_start, t_end, N, L, func)
```

Class especially tailored to creating, solving and finally animating a controlled inverted pendulum. While the Pendulum class method *animate* can be called after solving the pendulum ODE with *solve*, the AnimatedPendulum class wraps these steps. Simply create an instance and call the *animate* method.

```
__init__(phi0, phi0_dot, alpha, beta, mu, max_control, frequency, deadband, set_point, precision,  
         t_start, t_end, N, L, func)
```

Parameters

- **phi0** (*float*) – initial angle value
- **phi0_dot** (*float*) – initial angle velocity value
- **alpha** (*float* > 0) – proportional control parameter
- **beta** (*float* > 0) – derivative control parameter
- **mu** (*float* > 0) – integral control parameter
- **max_control** (*float* > 0) – controller output bound
- **frequency** (*int* >= 1) – controller speed parameter
- **deadband** (*float*) – minimum difference between calculated control outputs
- **set_point** (*float*) – desired value of controlled system
- **precision** (*int* > 0) – measurement precision of controller input
- **t_start** (*float*) – starting time for pendulum dynamics
- **t_end** (*float* > *t_start*) – ending time for pendulum dynamics
- **N** (*int* > 0) – number of support points
- **L** (*float* > 0) – pendulum length
- **f** – right hand side for pendulum ODE, available are either “linear” or “nonlinear”

Output Creates an instance of a pendulum, waiting to be animated

```
__module__ = 'PID_control'
```

```
animate(anim_name)
```

Animates an instance of AnimatedPendulum.

Parameters **anim_name** (*string*) – name for the mp4 file, in which the animation gets stored

class `PID_control.PIDControl` (*alpha, beta, mu, frequency, max_control, set_point, deadband*)

Class implementation of a PID controller. This class is initialize from given data like parameters for P, I and D, controller speed with respect to the modelled system and a bound for controller ouput. Especially the latter two are quite important in practical applications. The set point, that the controller tries to reach, can also be adjusted manually. A parameter deadband reduces strain on possible machinery behind the controller; the control output is only changed, if the newly calculated output differs from the previous one by at least the amount specified by deadband.

__init__ (*alpha, beta, mu, frequency, max_control, set_point, deadband*)

Initialize PIDControl class.

Parameters

- **alpha** (*float > 0*) – proportional control parameter
- **beta** (*float > 0*) – derivative control parameter
- **mu** (*float > 0*) – integral control parameter
- **frequency** (*int >= 1*) – controller speed parameter
- **max_control** (*float > 0*) – controller output bound
- **set_point** (*float between 0 and 2*pi*) – desired valued of controlled system
- **deadband** (*float > 0*) – minimum difference for controller adjustment

```
>>> import numpy as np; from PID_control import *
>>> ALPHA = 4.4; BETA = 2.0; MU = 1.2; MAX_CONTROL = 2.6
>>> FREQUENCY = 30; DEADBAND = 0.01; SET_POINT = -0.0*np.pi
>>> controller = PIDControl(
... ALPHA, BETA, MU, FREQUENCY, MAX_CONTROL, SET_POINT, DEADBAND
... )
>>> print(controller)
PID Controller with alpha = 4.4, beta = 2.0, mu = 1.2
```

__module__ = `'PID_control'`

__repr__ ()

Return string representation of PID controller.

derivative_output (*x1, x2, t1, t2*)

Method returning the derivative or D controller output, depending on the attribute beta. A numerical approximation of the derivative value is necessary to compute the ouput. The trapezoid rule was chosen for that.

Parameters

- **x1** (*float*) – system value at time t1
- **x2** (*float*) – system value at time t2
- **t1** (*float*) – last time point
- **t2** (*float*) – current time point

Output derivative control value

integral_output (*x1, x2, t1, t2*)

Method returning the integral or I controller output, depending on the controller attribute mu. A numerical approximation of the integral value is necessary to compute the output.

Parameters

- **x1** (*float*) – system value at time t1

- **x2** (*float*) – system value at time t2
- **t1** (*float*) – last time point
- **t2** (*float*) – current time point

Output integral control value

proportional_output (*x, t*)

Method returning the proportional or I controller output, depending on the controller attribute alpha.

Parameters

- **x** (*float*) – system value at time t
- **t** (*float*) – current time point

Output Proportional control value

total_output (*x1, x2, x1mod, x2mod, t1, t2, precision=4*)

Method returning the total controller output in response to system value x at time t. The output is bounded by the max_control attribute and controller adjustment speed is bounded by the frequency attribute. Controller does not adjust, if successive outputs differ by less than the deadband attribute. Limited measurement precision is included by rounding controller input. The angle reduction modulo 2*pi for the pendulum is accounted for by additional parameter x1mod, x2mod, which are necessary for consistent derivative calculations.

Parameters

- **x1** (*float*) – system value at time t1
- **x2** (*float*) – system value at time t2
- **x1mod** (*float*) – unreduced system value at time t1
- **x2mod** (*float*) – unreduced system value at time t2
- **t1** (*float*) – last time point
- **t2** (*float*) – current time point
- **precision** (*int > 0*) – system measurement precision

Output total control value

class PID_control.**Pendulum** (*t_start, t_end, N, func, L=10.0, G=9.81*)

Class implementation of a simple ODE solver for the inverted pendulum. Intended to be used in conjunction with the PIDControl class. The solved ODE is of the form $x'(t) = f(x(t)) + u(t)$.

Initialize with time parameters t_start, t_end, number of support points N. Initial values are given to the solve method for flexibility in calculating solutions for different initial conditions. Right hand side can be adjusted, even though sine and identity are the most reasonable choices.

__init__ (*t_start, t_end, N, func, L=10.0, G=9.81*)

Initialize linear or nonlinear pendulum.

Parameters

- **t_start** (*float*) – starting time for ODE solving
- **t_end** (*float > t_start*) – final time for ODE solving
- **N** (*int > 0*) – number of numerical support points for ODE solving
- **func** (*string*) – right hand side for the second order pendulum ODE, available options are “linear” or “nonlinear”

- **L** (*float*) – pendulum length parameter in [m]
- **G** (*float* > 0) – gravitational constant in [m/s²]

Output object representing the second order pendulum ODE with right hand side f

__module__ = 'PID_control'

__repr__ ()

Return string representation of inverted pendulum.

animate (*anim_name*)

Method to animate solutions generated with Pendulum class. One needs to call the *solve* method, before *plot* makes sense.

Parameters **anim_name** (*string*) – name for the mp4 file, in which the animation gets stored

get_func_values ()

A convenience method that returns the calculated function values or an empty list if *solve* was never called on this pendulum.

Output array containing angle solution values (floats)

get_support_values ()

A convenience method that returns the support values (== time points) or an empty list if *solve* was never called on this pendulum.

Output array containing support values (floats)

get_xy_coordinates ()

A convenience method that returns the xy-coordinates corresponding to the pendulum angles phi or an empty list, if *solve* was never called on the particular instance.

Output array containing xy-coordinates (float pairs)

plot (*file_name*, *parameter=False*)

Method to plot solutions generated with Pendulum class. One needs to call the *solve* method, before *plot* can be called. PID parameters can be written in the filename. This might be useful for numerical experiments with several distinct sets of parameters.

Parameters

- **file_name** (*string*) – name for the .png file, in which the solution gets stored
- **parameter** (*bool*) – if true, controller parameters are written in the filename

Todo fix naming scheme (Linear vs Nonlinear; testing for (lambda x: x) == self.f is not implemented very nicely).

solve (*phi0*, *phi0_dot*, *alpha*, *beta*, *mu*, *max_control*, *frequency*, *deadband*, *set_point*, *precision*)

Method solving the ODE for given physical initial conditions, i.e. initial angle and velocity, and with PID controller, that has the given parameters.

Parameters

- **phi0** (*float*) – initial value
- **phi0_dot** (*float*) – initial angular velocity
- **alpha** (*float* > 0) – proportional control parameter
- **beta** (*float* > 0) – derivative control parameter
- **mu** (*float* > 0) – integral control parameter
- **max_control** (*float* > 0) – controller output bound

- **frequency** (*int* ≥ 1) – controller speed parameter
- **deadband** (*float*) – minimum difference between calculated control outputs
- **set_point** (*float*) – desired value of controlled system
- **precision** (*int* > 0) – measurement precision of controller input

Output numerically calculates the attributes (float arrays) `phi`, `output_array`, `P_array`, `I_array` and `D_array`

```
>>> import numpy as np; from PID_control import *
>>> ALPHA = 4.4; BETA = 2.0; MU = 1.2; MAX_CONTROL = 2.6
>>> FREQUENCY = 30; DEADBAND = 0.01; SET_POINT = -0.0*np.pi
>>> PRECISION = 5; t_start = 0.0; t_end = 45.0; N = 9000; LENGTH = 10.0
>>> phi0 = 0.5 * np.pi; phi0_dot = 0.3 * np.pi
>>> pendulum = Pendulum(t_start, t_end, N, "nonlinear", L=LENGTH)
>>> pendulum.solve(
... phi0, phi0_dot, ALPHA, BETA, MU, MAX_CONTROL, FREQUENCY, DEADBAND,
... SET_POINT, PRECISION
... )
>>> abs(pendulum._phi[0] - phi0) < 1e-8
True
>>> phi1 = phi0 + phi0_dot*pendulum.h
>>> abs(pendulum._phi[1] - phi1) < 1e-8
True
>>> controller = PIDControl(
... ALPHA, BETA, MU, FREQUENCY, MAX_CONTROL, SET_POINT, DEADBAND
... )
>>> u0 = controller.proportional_output(phi0, t_start)
>>> abs(u0 - (-ALPHA*phi0)) < 1e-8
True
>>> u1 = controller.derivative_output(
... phi0, phi1, t_start, t_start + pendulum.h
... )
>>> abs(u1 - (-BETA*(phi1 - phi0)/(pendulum.h))) < 1e-8
True
>>> u2 = controller.integral_output(
... phi0, phi1, t_start, t_start + pendulum.h
... )
>>> abs(u2 - (-MU*(phi0 + phi1)*pendulum.h/2.0)) < 1e-8
True
```

solve_from_angles (*phi0, phi1, alpha, beta, mu, max_control, frequency, deadband, set_point, precision*)

Method solving the ODE for given numerical initial conditions, i.e. two initial angles. Works exactly like the *solve* method.

Parameters

- **phi0** (*float*) – first initial value
- **phi1** (*float*) – second initial value
- **alpha** (*float* > 0) – proportional control parameter
- **beta** (*float* > 0) – derivative control parameter
- **mu** (*float* > 0) – integral control parameter
- **max_control** (*float* > 0) – controller output bound
- **frequency** (*int* ≥ 1) – controller speed parameter

- **deadband** (*float*) – minimum difference between calculated control outputs
- **set_point** (*float*) – desired value of controlled system
- **precision** (*int* > 0) – measurement precision of controller input

Output Numerically calculates the attributes (float arrays) phi, output_array, P_array, I_array and D_array

```
>>> import numpy as np; from PID_control import *
>>> ALPHA = 4.4; BETA = 2.0; MU = 1.2; MAX_CONTROL = 2.6
>>> FREQUENCY = 30; DEADBAND = 0.01; SET_POINT = -0.0*np.pi
>>> PRECISION = 5; t_start = 0.0; t_end = 45.0; N = 9000; LENGTH = 10.0
>>> phi0 = 0.5 * np.pi; phi0_dot = 0.3 * np.pi
>>> pendulum = Pendulum(t_start, t_end, N, np.sin, L=LENGTH)
Pendulum type must be either linear or nonlinear!
Default type linear was chosen!
>>> pendulum
Inverted Pendulum of Length 10.0
>>> phi1 = phi0 + phi0_dot*pendulum.h
>>> pendulum.solve(
... phi0, phi0_dot, ALPHA, BETA, MU, MAX_CONTROL, FREQUENCY, DEADBAND,
... SET_POINT, PRECISION
... )
>>> x = pendulum.phi[10]
>>> pendulum.solve_from_angles(
... phi0, phi1, ALPHA, BETA, MU, MAX_CONTROL, FREQUENCY, DEADBAND,
... SET_POINT, PRECISION
... )
>>> y = pendulum.phi[10]
>>> print(np.abs(x - y) < 5e-5)
True
```

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