

# Project Details

## Geometry Description and Mesh Construction from Medical Imaging

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CNR-IMATI

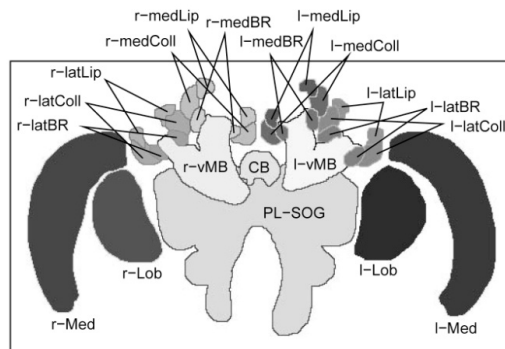


# Outline

- Image & atlas-based segmentation
- Atlas selection
  - Single, variable, and multiple individual atlas
  - Single average atlas
- Image registration & trasformations
  - Non-rigid transformations
  - Parametric transformations
- Registration error: distance
- 2D examples

## Image segmentation

- Segment an image = tag each pixel/voxel with a semantic label



- From the paper "Quo vadis, Atlas based segmentation" by T. Rohlfing, R. Brand, R. Menzel, D.B. Russakoff, C.R. Maurer jr

## Image segmentation

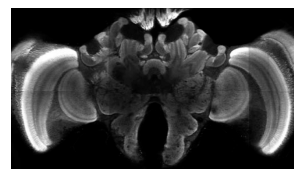
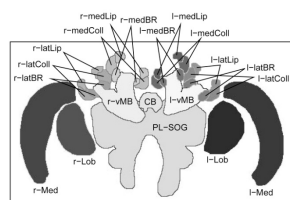
- Intensity based classification
  - Group the gray level space in clusters
  - Each cluster is identified with a label
  - Each pixel is tagged with the label of the corresponding cluster
- Ok for classifying tissue types
- Bad when classifying anatomical structures

## Image segmentation

- Force the geometry of the image to evolve using
  - Image properties (gradient)
  - Constraints (smoothness of the segmented curves)
- Examples
  - Active contours (snakes) [Kass, Witkin & Terzopoulos '87]
  - Level set method [Osher & Sethian '88, Sethian '99]
  - ...

## Image segmentation

- Atlas-based segmentation: template image T, already segmented



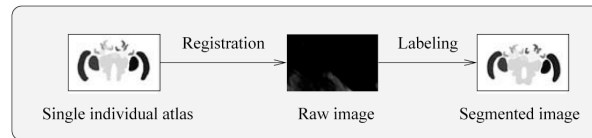
- Find a map transforming the template image in the image R to be segmented
- “Transfer” on R the segmentation of T

## Atlas Selection

### Atlas selection

- Choice of atlas has substantial impact on the result of the segmentation algorithm
- Four strategies
  - *Single atlas* for all images to be segmented
  - *Choice of best atlas* for each given image into an atlas set
  - *Average atlas* for all the images to be segmented
  - *Simultaneous use of multiple atlases*

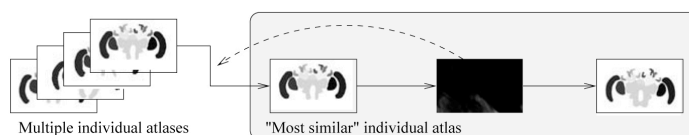
## Single individual atlas



IND: Segmentation using a single individual atlas.

- Selection of an individual atlas
- Registration of all the raw images with the selected atlas
- (individual atlas = obtained by a single raw image)

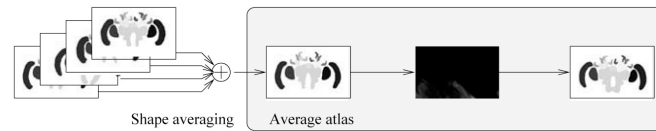
## Variable individual atlas



SIM: Segmentation using the "most similar" individual atlas.

- Set of atlases
- Segment R using all atlases
- Select the atlas that gives the best result
  - Maximum similarity
  - Minimum deformation

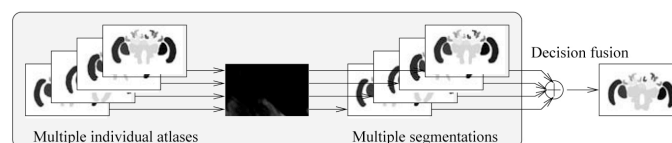
## Single average atlas



AVG: Segmentation using an average shape atlas.

- Construct an artificial “typical image” T from a set of images
- Construct corresponding atlas
- Register all images with T

## Multiple individual atlas



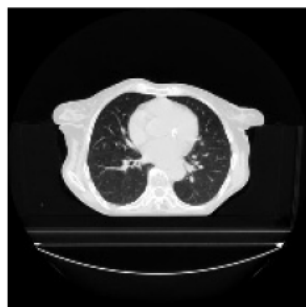
MUL: Independent segmentation using multiple individual atlases with decision

- Set of atlases
- Register R using each atlas
- Tag pixels with labels using all information
  - Ex: voting strategy  $\leftrightarrow$  tag with label chosen by highest number of atlases

## Image Registration

### Image registration

REFERENCE IMAGE

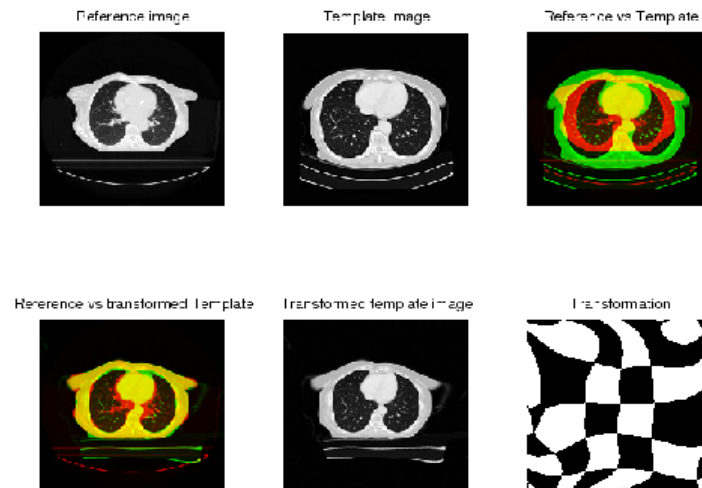


TEMPLATE IMAGE



CT studies, of the same patient by different CT machines

## Image registration



## Image registration

- Grey scale images  $\leftrightarrow$  real valued functions
- $R: \Omega_R \rightarrow \mathbf{R}^+$ ,  $T: \Omega \rightarrow \mathbf{R}^+$
- Find mapping  $\theta: \Omega_R \rightarrow \Omega$  such that  $T \circ \theta$  and  $R$  are as “close” as possible
- Huge number of approaches
- Huge number of algorithms

See [Brown '92; Zitova, Flusser '03]



## Image registration

- Huge number of algorithms obtained by combining
  - Different “distance” functionals
  - Different transformation classes
  - Different image models
  - Different optimization algorithms
- Huge number of possible combination

## The transformations

- Rigid transformations (translations, rotations)
- Affine transformation
- Non rigid transformations
  - Splines, B-splines [Thevenaz, Unser '98]
  - Thin plate splines [Bookstein, '89]
  - Interpolating wavelets [S.B., G. Maggi '13]
  - ...
  - Parametric transformations

## Parametric transformations

- N-dimensional parameter space
- Parameter  $\alpha \rightarrow$  mapping  $\theta_\alpha$
- (Ex:  $\theta_\alpha = \sum \alpha_i e_i$ )
- $\theta_\alpha = \Theta(x; \alpha)$ 
  - $x$  : spatial coordinate (in  $\mathbf{R}^2$ )
  - $\alpha$  : parameter (in  $\mathbf{R}^N$ )
  - $\Theta : \mathbf{R}^2 \times \mathbf{R}^N$  function (represents the selected class of transformations)

## The “distance”

- **Im**: space of images
- $d: \mathbf{Im} \times \mathbf{Im} \rightarrow \mathbf{R}$  functional measuring the discrepancy between the two images
- $\delta: \mathbf{Im} \rightarrow \mathbf{R}$  defined as  $\delta(X) = d(X, R)$
- $c: \mathbf{R}^N \rightarrow \mathbf{R}$  cost functional
- $c(\alpha) = d(T^0 \theta_\alpha, R) = \delta(T^0 \theta_\alpha)$

## The “distance”

- Many different possibilities
  - Least square error
  - Human Visual System model distance [Mannos, '74]
  - Structural similarity index SSI  
[Wang et al, '04, Brunet, Vrsnay, Wang '11]
  - Besov functional norm
  - Besov norm + divisive renormalization (generalised SSI) [S.B., G. Maggi, '14]
  - Mutual information [Viola, Wells '97; Thevenaz, Unser '98]
  - ...

## The optimization problem

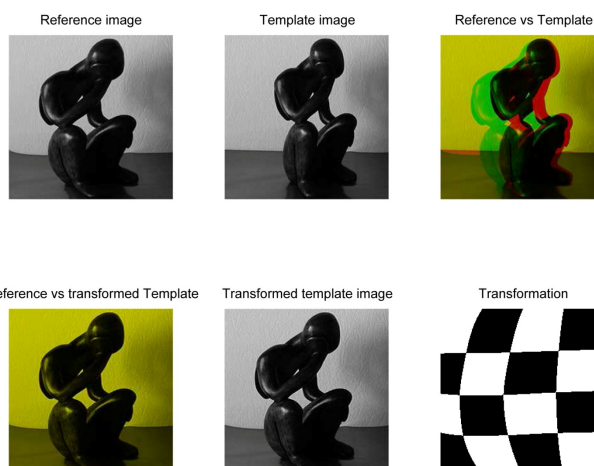
- Find  $\alpha_0$  in  $\mathbf{R}^N$ 

$$\alpha_0 = \arg \min_{\alpha} c(\alpha)$$
- Unconstrained optimization problem
- Several possible optimization algorithms
- Choice depends on the characteristics of
  - Transformation
  - Distance functional

## Image model

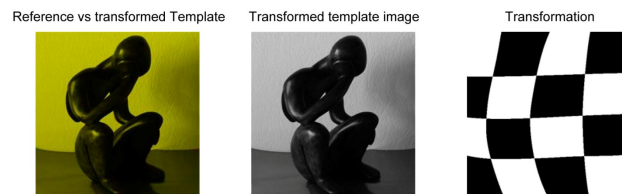
- Need rules to
  - Evaluate images out of their domain of definition (*extrapolation*)
  - Compute values of (deformed) images at pixels (*interpolation*)
  - Compute the values of derivative of images at pixels (*numerical differentiation*)
- Many different possibilities

## Results



No noise  
Distance: LS

## Results



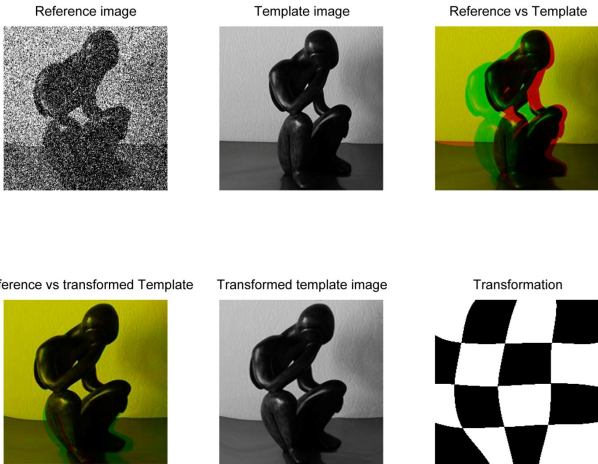
No noise  
Distance: SSIM  
p=2

## Results



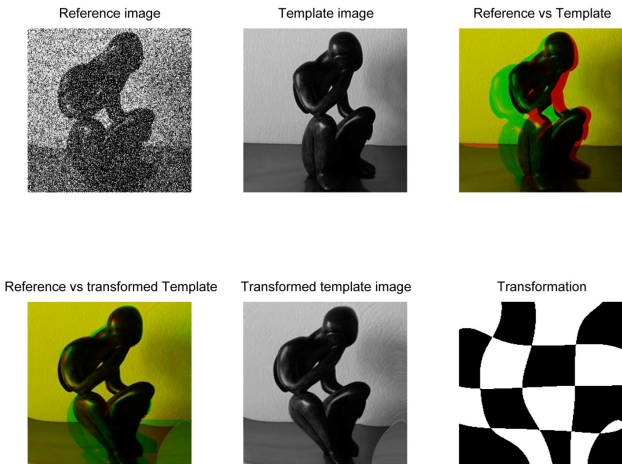
No noise  
Distance: GSSIM  
p=2

# Results



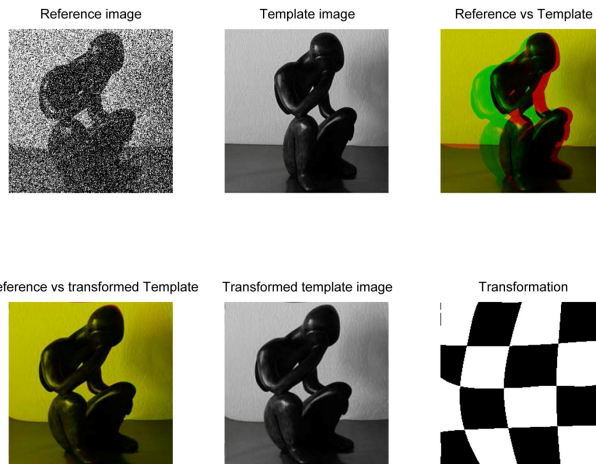
Gaussian noise  
Distance: LS

# Results



Gaussian noise  
Distance: SSIM  
p=2

## Results



Gaussian noise  
Distance: GSSIM  
 $p=2$