

PRACTICAL CONSIDERATIONS IN EXPERIMENTAL COMPUTATIONAL SENSING

by

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SIGNED: Phillip K. Poon

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ABSTRACT

Implementing computational optical sensors often comes with various issues that many traditional sensors may not encounter.

CHAPTER 1

Introduction

This chapter introduces the reader to the concept of isomorphic sensing, multiplexing, indirect imaging, compressive sensing and computational sensing and provides the motivation for the need to address the practical issues in experimental computational sensing.

Isomorphic sensing is the concept that a sensor's measurements resemble the signal of interest. Isomorphic sensing is often called traditional sensing. In isomorphic sensing the analog hardware, analog-to-digital converter (ADC), and processing algorithms are all separate components, see Figure 1.1. Computational sensing is the concept that a joint design of the sensor, often through coding of the analog signal, with task-specific algorithms can exceed the performance of an isomorphic sensor. Computational sensors exist at the intersection of these processes, see figure 1.2 [1]. While isomorphic sensors can provide flexible sensing in multiple applications, a computational sensor's joint design naturally leads to performance increases. Throughout this chapter and the rest of this dissertation we will provide many examples that highlight the differences between computational and isomorphic sensing.

Rather than a rigorous discussion, this chapter will discuss some of the major developments and concepts in the field of computational sensing on an intuitive level. This will familiarize the reader with important terminology and techniques common in the field of computational sensing. A rigorous discussion with mathematical

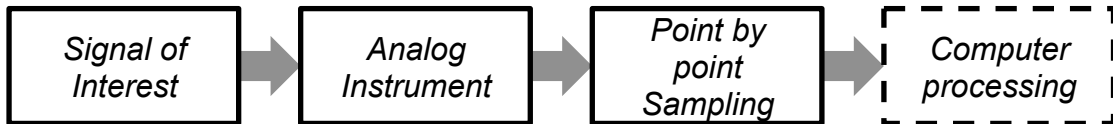


Figure 1.1: A systems view of a traditional sensing scheme. The signal-of-interest is incident upon the analog instrument. The analog instrument forms an isomorphism of the signal which is then periodically sampled point-by-point through an ADC device. Once the signal is in digital form, post-processing algorithms are often used to perform various tasks such as noise reduction, detection, and classification. Notice that the analog instrument, sampling scheme, and processing are all separated.

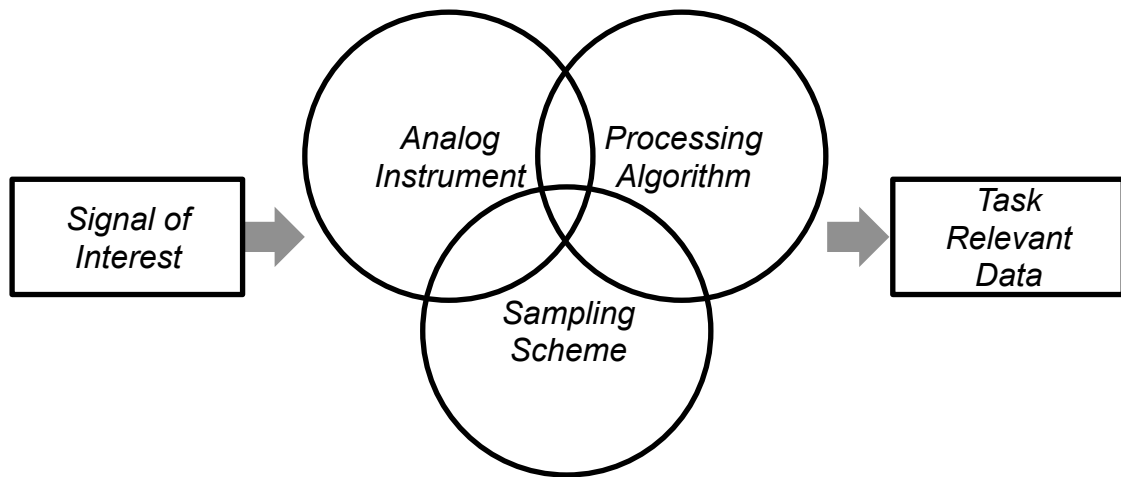


Figure 1.2: A systems view of a computational sensing scheme. The signal-of-interest is incident upon the analog instrument.

formalism of the concepts is given in chapter 2. This chapter will also discuss some of the challenges I and many other experimentalists and engineers have faced when developing computational sensing prototypes. I will close this chapter with a brief look ahead to the rest of the dissertation.

1.1 Isomorphic Sensing

In Greek, the word isomorphic loosely translates to equal in form. Traditional sensors perform isomorphic sensing. In the context of this dissertation, an isomorphic sensor is any sensor which attempts to produce an output signal that resembles the signal-of-interest. In this paradigm, the analog instrument, sampling scheme, and post-processing algorithms are separated.

We will discuss three important examples of isomorphic sensors: the pinhole camera, the photographic camera and the optical spectrometer (which I will just call a spectrometer from now on, even though there are many instruments called spectrometers that not concerned with optical spectra). These sensors have had major roles throughout the history of optics and in the physical sciences so it is natural that they have also been the main focus of computational sensing. Therefore it is important we first understand the isomorphic version of these sensors.

In the photographic camera, the signal-of-interest is the object that is being photographed. This can be anything that is scattering or emitting light, a person,

a tree or a distant group of stars. The analog instrument consists of the lens which is designed and fabricated to produce an image that looks like the object at the focal-plane array (FPA). The more that the image resembles the object the better the optics. The FPA then samples and quantizes the image and produces a digital representation of the object, measurement data. The measurement data is often post-processed to perform such tasks as noise removal or to locate the object.

There are two major sub-systems in the photographic camera which determine how well it performs: the optics and the FPA. Ideally, the optics (the analog instrument in this case) will produce a point spread function (PSF) which is infinitely small in diameter. For example, in a task such as the detection of a star from several neighboring stars in the night sky, if the PSF is much larger than the center to center separation of the two stars in the optical image, it will be quite difficult to detect. A careful reader will note that this is the same argument used by Lord Raleigh in proposing his resolution criterion [2]. Even if the PSF is small enough, the FPA must sample at a fine enough pixel-to-pixel spacing, called the *pixel pitch*, to accurately reproduce the intensity variations at the scale which is pertinent to the task. Intuitively, this makes sense because if the image of both stars and the decreased intensity which signifies a certain amount of separation between the two stars is imaged onto a single pixel, the one cannot ever hope to be able to accurately detect the star without some other prior or side information.

The pinhole camera predates the photographic camera over a thousand years, mostly due to its simplicity. It consists of a small hole and a box which prevents any light except from the pinhole to enter, see Figure 1.3. The pinhole camera is useful for imaging in parts of the electromagnetic spectrum and particles for which there is no direct analog to refractive lens or reflective mirror.

In the spectrometer, the signal of interest is the spectrum of the object. The optics are designed to take the incoming light and separate various wavelength components, see Figure 1.4. The part of the spectrometer which is used to physically isolate the wavelengths is called a *spectrograph*. The result is a spectral intensity as a function of position at the FPA. The FPA and post-processing algorithms are used in the same manner as the photographic camera, which is to sample the optical spectrum creating digital version of it and to perform various tasks on the measurement data. For now, we will concentrate on the slit spectrometer, which measurements spectrum at a single point on the object.

In the spectrometer, one of the important performance metrics is *spectral res-*

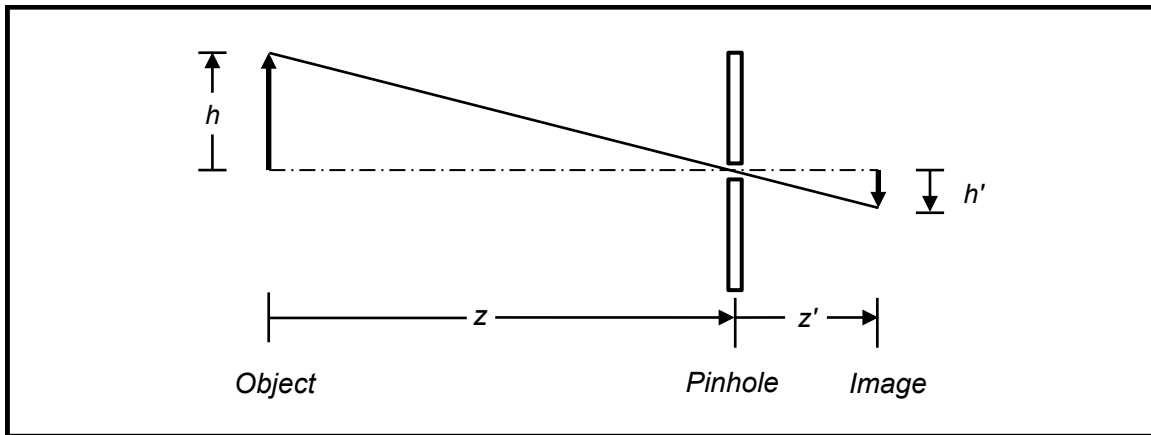


Figure 1.3: A pinhole camera.

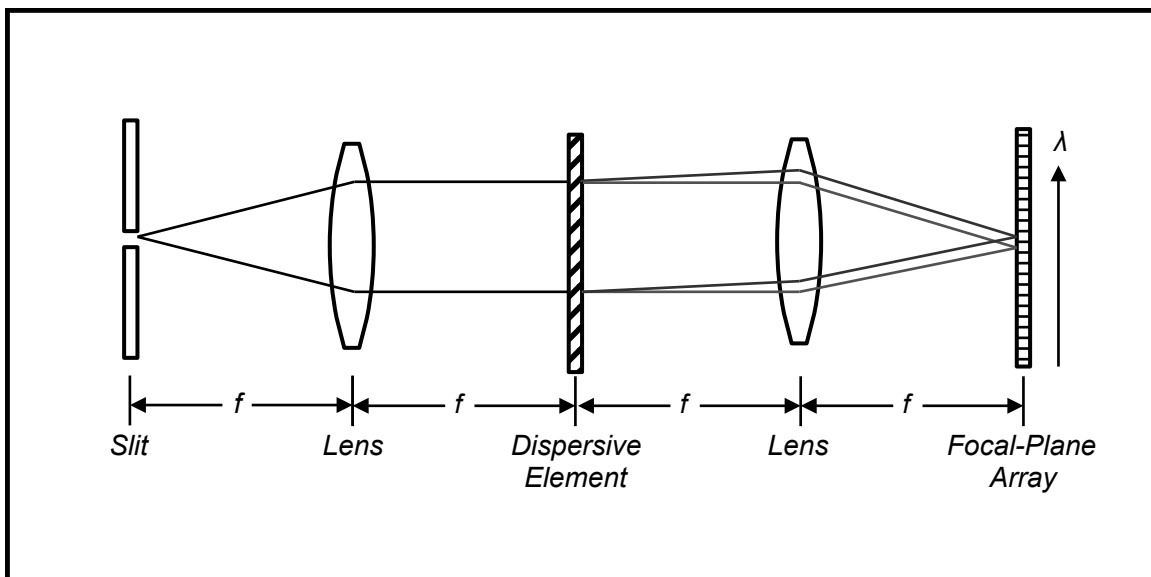


Figure 1.4: An isomorphic slit spectrometer with a 4F configuration.

olution, which we denote $\delta\lambda$. The spectral resolution is the smallest difference in wavelength the instrument can discern. Large spectral resolutions can degrade the spectrometers ability to discern important parts of the spectrum. Similarly with the camera, the FPA must have a pixel pitch which is small enough in order to correctly sample the variations in the spectrum.

The point-by-point nature of isomorphic sensing is both a strength and a source of weakness.

The strength comes from the straightforward and intuitive architecture of the isomorphic sensor. Each subsystem: the optics, the focal-plane array (FPA), and the post-processing can be designed and constructed seperately as long as they meet their individual specifications. As long as the Signal-To-Noise Ratio (SNR) is sufficient and the sampling rate is high enough we are guaranteed to recover the signal.

One of the weaknessess of the isomorphic approach however is the the ability to measure low SNR signals. Because the image is sampled in a completely parallel fashion at each exposure, each pixel contributes a certain amount of noise (which is independent of the signal strength). If the noise dominates, the measurement fidelity decreases often forcing the operator to incease the exposure time. For weak signals the exposure time can become prohibitive and for temporally dynamic signals this may lead to a loss of resolution. Indeed, one of the major engineering trade-offs faced by traditional spectrometer designers and users is that when one attempts to increase the light collection (increased slit-width) the spectral resolution $\delta\lambda$ degrades (increases). Similarly, in the pinhole camera, there is a throughput versus spatial resolution trade-off, increasing the size of the pinhole degrades the PSF.

It would be easy to assume that with the recent revolution in machine learning and statistical signal processing combined with the dramatic increase in computing power that we could simply post-process poor measurments and obtain useful data. However, this isn't possible due to the an important theorem in information theory called the data processing inequality [3]. In layman's term it means "garbage in, garbage out".

Another weakness of isomorhic sensing is that the seperation of the analog instrument, the sampling scheme, and the data processing algorithms lead to increased Size, Weight and Power-Cost (SWAP-C). As we mentioned in the photographic camera, the optics must be designed to produce a small PSF. For demanding applications, the optical design and fabrication can be the most expensive component

of the sensor. While FPA prices in the visible have fallen recently, FPAs in certain parts of the electromagnetic spectrum can be quite expensive or non-existent [4].

In many cases, the signal is redundant and high resolution sampling becomes a waste of resources such as data storage and communications bandwidth. A good example is in photography where often the post-processing takes the digital image and applies a compression algorithm which looks for patterns in the signal and reduces the file size, discarding much of the sample data [5].

The isomorphic sensor has served humanity well, however with all the weakness that have been discussed I will now begin to discuss some of major techniques in computational sensing that can be used to address some or all of the issues that I just stated.

1.2 Development of Multiplexing in Sensing

Multiplexing in sensing allows each measurement sample to be a combination of multiple points of the signal-of-interest. Multiplexing is a powerful tool that can be exploited by the sensor designer to eliminate or relax design trade-offs.

A simple example which illustrates the usefulness of multiplex sensing is weighing objects. In this example, we are given a 100 sheets of paper. Let's assume that the scale's measurement error is insignificant. Isomorphic measurement sensing means one would need to measure each sheet of paper individually. Requiring 100 measurements.

Now, let's say the scale's measurement error is on the order of the weight of the sheet. Measuring each sheet individually produces a large measurement error. In order to reduce the error to an acceptable SNR we need to make several measurements per sheet to reduce the error to an acceptable level.

However, we can be a little smarter. We can measure all 100 sheets at the same time. Since the weight of all 100 sheets is much larger than the measurement error of the scale, we can dramatically increase the precision of the measurement. If we can assume that each sheet is the same weight, then we are done.

The weighing problem is analogous to the spectroscopy example. As discussed earlier in section 1.1, there is trade-off between light collection and spectral resolution. Increasing the slit-width to increase the amount of light has the effect of degrading the spectral resolution $\delta\lambda$. Around the late 1940's and early 1950's, several important papers and inventions demonstrated the effectiveness of multiplexing

in spectroscopy. At the time the FPA was non-existent, so in the slit spectrometer shown in 1.4, where the FPA is pictured, there was actually another slit. To record the intensity at each spectral channel, either the dispersive element or the exit slit had to be mechanically translated, making the measurements even slower by a factor of N_λ , the number of spectral channels of interest.

Golay was the first to propose multiplexing the slit spectrometer by creating a pattern of binary (1's and 0's) entrance and exit slits [6]. The idea borrowed heavily from communications theory which is concerned with the reliable transmission of information over a noisy channel. In the Golay multi-slit spectrometer, the patterns of entrance and exit slits are matched based on mathematically useful properties, this is similar to coding and decoding signals in communications. The entrance slits act to code the spectrum while the exit slits decoded the coded spectrum. Intuitively, the ability to use multiple entrance and exist slits increases the optical throughput of the spectrometer. Golay's idea dramatically increased the optical throughput without degrading the spectral resolution.

Fellgett devised an alternative approach to multiplex spectroscopy, the Fourier Transform spectrometer, and was the first to note that multiplex measurements compared to isomorphic measurements improve the signal-to-noise ratio on the order of $\sqrt{N_\lambda}$ [7]. He is generally credited with discovering the multiplex advantage, so it is often called the Fellgett advantage instead.

Another example that is pertinent to this dissertation is coded aperture imaging. Coded aperture imaging can be thought of as the multiplexed version of a pinhole camera. As mentioned earlier in section 1.1, there is a trade-off between the throughput and spatial resolution. However in many fields, such as high-energy particle imaging, refractive lenses and reflective mirrors are non-existent or underdeveloped. By using multiple pinholes the throughput is increased without sacrificing spatial resolution. However, the pattern of the pinholes, which is the code, in this case must be carefully designed to achieve optimal object reconstruction. Fenimore, Canon, and Gottesman were the first to create an elegant solution to coded aperture design called uniformly redundant arrays [8, 9].

In summary, multiplexing has the ability to eliminate classic trade-offs in isomorphic sensors: signal strength or resolution. Modern researchers are still actively developing novel ways to implement multiplexing to increase resolution and sensitivity in the spatial domain [10, 11], spectral domain [12, 13], and temporal domain [14, 15]. However, multiplexing is not without its own set of problems. We now

discuss inverse problems in computational sensing.

1.3 Forward Models and Inverse Problems

In the computational sensing community, a model which maps the signal-of-interest to the measurement data is called the *forward model*. The problem of taking the observed data and calculating a reconstruction of the signal-of-interest or task-specific parameters is called the *inverse problem*.

As you can imagine, solving inverse problems of isomorphic measurements, when one is concerned with reconstruction of the signal-of-interest, tend to be straight forward. In the weighing problem, the measurement is also the reconstruction. In the slit spectrometer, where the forward model can be simply the continuous to discrete mapping of the spectrum. The spectrum is the interpolated measurement.

Of course, we can begin to add various levels of complexity to the forward model to account for various physical aspects of the sensor, such as the fact the FPA can't measure certain wavelength regions or the noise in our measurements. But again, assuming proper sampling and enough SNR, the reconstruction of the isomorphic signal is the measurement. This simplicity is one reason why isomorphic sensing still dominates at the consumer level despite all of the drawbacks I discussed earlier in section 1.1.

However, the multiplexing of signal information forces us to develop computational steps to reconstruct or infer the parameters of the signal that caused the measurements. In the multiplexed weighing problem, a significant complication occurs when each sheet has a different weight. Now solving the inverse problem is not as straight forward. A single measurement of all 100 sheets in this case is an *underdetermined problem* since we have 1 equation and 100 unknowns. What we can do is try measuring different combinations of the 100 sheets, each new combination provides us with a new equation to work with reducing the error. Naively, we might assume that we can randomly choose 100 unique combinations and solve 100 equations using the algebra we were taught in high school. However when there is measurement error, in many applications including the weighing problem, random combinations are not the best way to conduct the coding, they are sub-optimal in terms of reconstruction error. This lead many to begin working on optimal coding strategies of signals for sensing and is major topic in this dissertation.

In fact, the idea of multiplexing was not invented by Golay or Fenimore, what

they contributed was the creation of computationally simple ways to code and decode their signal-of-interest, making their sensors more appealing to a broader community of scientists and engineers. A good example is the Hadamard matrix based code [16]. The Hadamard code is appealing because reconstruction is simply the transpose of the original matrix. Unfortunately, not all multiplexing forward models have mathematically elegant inversion steps. Often the physics of the situation force non-isomorphic measurements which require a computational step to solve the inverse problem.

1.4 Indirect Imaging

While Golay, Fennimore, and others were leveraging multiplexing to eliminate trade-offs in traditional sensors, an entirely disparate group of researchers were working on imaging techniques for which there was no isomorphic analog. In these cases the physics of the sensing modality prevents a point-by-point sampling of the signal-of-interest. These techniques are called indirect imaging.

Perhaps one of the most successful early examples of indirect imaging and the rise of inverse problems in sensing is the development of radar. While early radar was concerned with the detection and distance of an object, development of imaging radar began after World War II. Imaging radar and specifically Synthetic Aperture Radar (SAR) can use time delay information combined with the doppler effects and interference patterns of coherent radio waves to create high resolutions of terrain and buildings.

In medicine, an imaging modality that now common is X-Ray Computed Tomography (CT), one is forced into this situation since the task is to reconstruct a 2 or 3-dimensional function from 1 or 2 dimensional measurement data. The forward model can be simple: In a collimated beam architecture with a 1-dimensional detector array, we say that each sample from each pixel on the array is proportional to the total number of x-ray photons that have not been absorbed by the object [17] plus noise. The inversion of course is not straight forward. The culmination of the work related to the inversion techniques and the actual prototype resulted in the Nobel Prize for Physiology or Medicine in 1979 [18].

In general, non-isomorphic sensing such as indirect imaging schemes which include X-ray CT, Single-Photon Emission Computed Tomography (SPECT), Positron Emission Tomography (PET), Magnetic Resonance Imaging (MRI) and

certain forms of sonic and radio wave imaging all require a data-processing or reconstruction step to solve an inverse problem [19]. In summary, the forward model of a sensor is essentially accounting for the physics which govern the measurement while the solving the inverse problem is a mathematical problem which attempts to either reconstruct the object or to calculate task-specific data of the object.

We now turn to what are arguably the most important inventions of optical sensing in the last several centuries, the digital image sensor.

1.5 The Digital Imaging Revolution

In 1969 Boyle and Smith invented the Charge-Coupled Device (CCD) [20]. The CCD is the first integrated circuit device which using a 2-dimensional arrangement of pixels which could reliably convert an image's intensity distribution to a digital signal. The CCD is a type of FPA.

The CCD was a major breakthrough for entire fields and industries who depended on the reliable sampling, storage and transmission of optical phenomena. Until then one either had to use film or bulky tubes that required an electron beam to be scanned across an image scene, such as the Image orthicon [21]. For their invention, Boyle and Smith both received the Nobel Prize in Physics in 2009 [22]

The invention of the digital camera by Sasson followed shortly after [23]. In the spectrometer, replacing the exit slit by the CCD allowed for simultaneous measurement of the entire spectrum in a compact architecture [24].

The development of the Complementary Metal–Oxide–Semiconductor (CMOS) FPA was also important. While in scientific settings, it could not rival the quality of the CCD, its cheaper cost brought digital imaging to the consumer level. Other technology like the digital computers and computer networking also provided major contributions to the democratization of imaging and optical sensing. While optical instrumentation was and is still expensive, the researcher could at least capture, process, and share data with significantly less effort.

Algorithms for efficient and reliable storage and transmission of digital images became important. Over time the pixel count continued to increase and the sheer volume of digital image and video data being generated and transmitted over networks began to outpace improvements in storage and transmission capacity. While many engineers developed new technology to combat the hardware limitations of storage and transmission. This also led to a renewed effort by researchers to develop

more efficient image and video compression algorithms [25, 26].

As mentioned in at the beginning of this chapter, computational sensing lies at the intersection of the design of the analog hardware, sampling schemes, and processing algorithms. Many of the algorithms used in computational sensing are the same as or inspired by the techniques used by the image processing community. This is because a major effort of computational sensing is the desire to make more resource efficient measurements.

1.6 From Multiplexing to Compressive Sensing

1.7 Practical Considerations in Computational Sensing

Decoding the signal, which we can also think of as solving the inverse problem is not necessarily straight forward. Unfortunately the coded of the analog signal and inversion steps are often seperately designed in computational sensing. This becomes especially frequency because the practicing sensor engineer must piece together various techniques from theorestist. This

1.8 Dissertation Overview

CHAPTER 2

Formalism

This chapter introduces the reader to the more rigorous concepts and mathematical background that will be required to fully understand the material presented in the later chapters of this dissertation.

A rigorous discussion of multiplexing and signal-to-noise ratio will be discussed, as well as various coding schemes used in various notable computational sensors as well as the ones in this dissertation.

Since the AFSSI-C relies on a variation of Principal Component Analysis (PCA) and a Bayesian algorithm for coding design we will discuss some of the fundamentals of Bayesian probability and the Log-Likelihood Ratios.

2.1 Isomorphic Sensing

$$\mathbf{g} = \mathbf{H}\mathbf{r} \tag{2.1}$$

where \mathbf{g} is the measurement vector.

2.2 Multiplexing

2.3 Principal Component Analysis

2.4 Bayesian Rules and Log-Likelihood Ratios

2.5 Compressive Sensing

2.5.1 The Nyquist-Shannon Sampling Theorem

The Nyquist-Shannon Sampling Theorem states one must sample a signal with a sampling rate that is at least twice the maximum frequency of the signal to prevent aliasing [27].

2.5.2 Sparsity, Incoherence, and the Restricted Isometry Property

2.5.3 Inversion

2.5.3.1 L0 and L1 Norm Minimization

2.5.3.2 LASSO and sparsity regularization

Acronyms

- ADC** analog-to-digital converter. 8, 11
- AFSSI-C** Adaptive Feature Specific Spectral Imaging-Classifier. 4, 5, 22
- CCD** Charge-Coupled Device. 20
- CMOS** Complementary Metal–Oxide–Semiconductor. 20
- CT** Computed Tomography. 19
- DISP** Duke Imaging and Spectroscopy Program. 5
- FPA** focal-plane array. 13, 15–18, 20
- LCOS** Liquid Crystal on Silicon. 5
- LENS** Laboratory for Engineering Non-Traditional Sensors. 4, 5
- MRI** Magnetic Resonance Imaging. 19
- PET** Positron Emission Tomography. 19
- PSF** point spread function. 13, 15
- SAR** Synthetic Aperture Radar. 19
- SCOUT** Static Computational Optical Undersampled Tracker. 5
- SLM** Spatial Light Modulator. 5
- SNR** Signal-To-Noise Ratio. 15, 16, 18
- SPECT** Single-Photon Emission Computed Tomography. 19
- SWAP-C** Size, Weight and Power-Cost. 15

Symbols

$\delta\lambda$ Spectral Resolution. 15, 16

\mathbf{g} The Measurement Vector. 22

N_λ The Number of Spectral Channels. 17

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