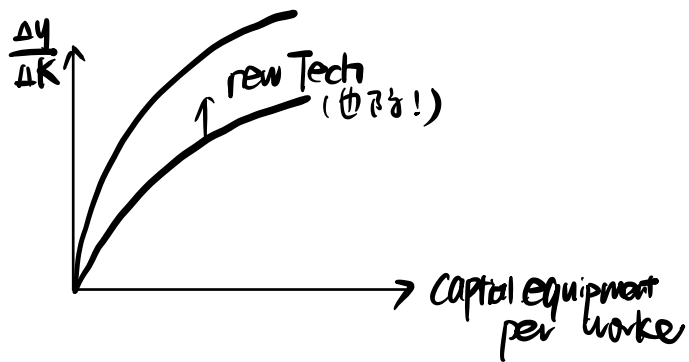


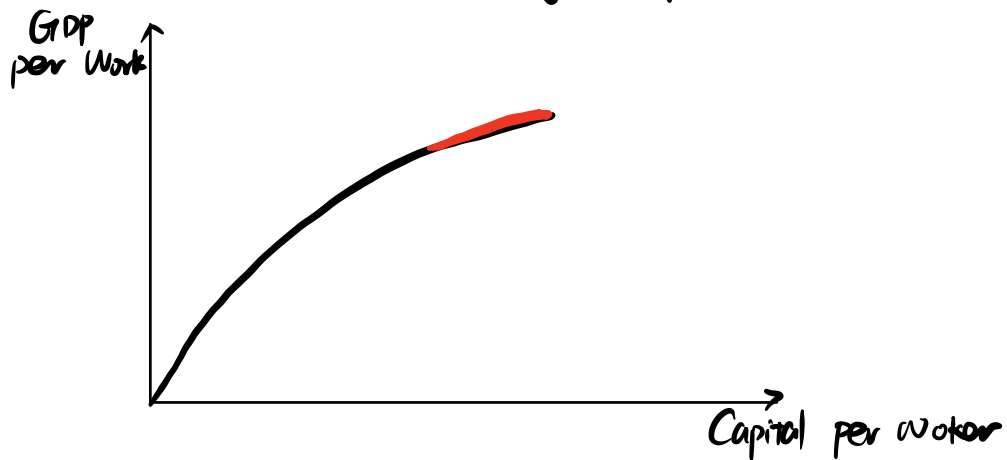
innovation rent  $\sim$

creative destruction  $\sim$

Capital-intensive



accumulation of capital process proceed in the absence of technological progress



随 Capital intensive  $\uparrow$  按理说 Capital productivity 应该  $\downarrow$ . 但从长远来看, 技术的进步抵消了边际递减

Solow Model explains

1. catching up of developing countries over time (with little accumulated Capital per worker)
2. Long run only: tech  $\uparrow \Rightarrow$  econo growth  $\uparrow$

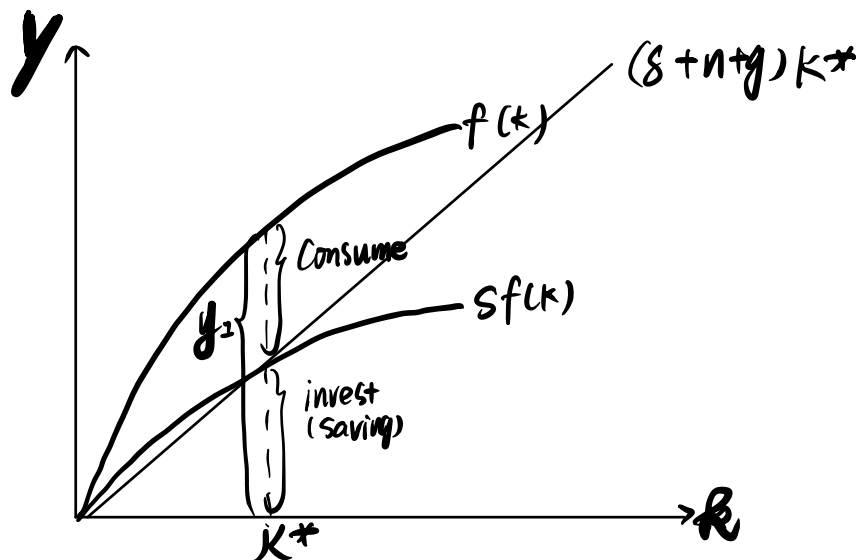
$K$ : Capital (资本)     $L$ : 劳动力     $E$ : 效率.

$$y = Y/L \quad k = K/L$$

$$y = Y/LE = f(k) \quad K = K/LE \text{ (Capital per Unit of effective Labour)}$$

Saving:  $S * y = S * f(k)$

Consume:  $C = y - i = f(k) - S y$

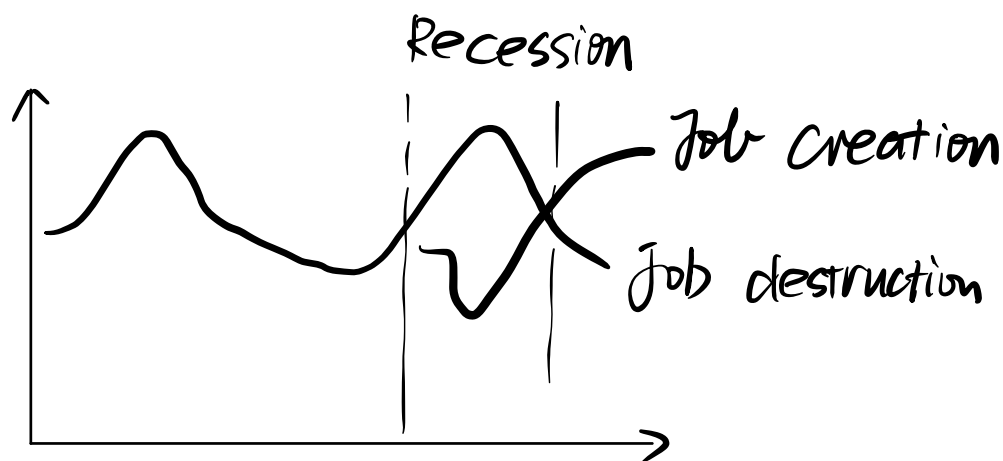


$$\Delta k = sf(k) - (\delta + n + g)k$$

$$\Delta k = 0 \text{ (K, L grow with same rate)}$$

则

1.  $\delta f(k^*) = (\delta + n + g)k^*$
2. golden rule level of capital
3.  $f'(k^*) = \delta + n + g$
4. GDE per person grow with same rate as tech progress



Labour market matching

1. 能力不符 2. 地区不同 3. 互不相识

\* Long run Labour Market Model

## 7. Technological progress, unemployment and living standards in the long run

### I. Exercise Questions

#### Readings

Lecture slide set: #9

Macroeconomics ed.9 (Mankiw): *Steady state (8.1), technological progress (9.1), golden rule (8.2)*

#### Problem 1 (*Solow model*)

Consider an economy with the following Cobb-Douglas-production function:

$$Y = K^{0,5}(LE)^{0,5}$$

where  $K$  is the capital stock,  $L$  is the employed labour force and  $E$  is the efficiency of the economy.

Assume a savings rate of  $s = 0,25$ , a population growth rate of  $n = 0,1$ , a depreciation rate of  $\delta = 0,3$  and a rate of  $g = 0,1$  for the technological progress.

- (a) What is the production function per unit of effective labour of the economy?
- (b) What is the break-even investment in this economy (the investment needed to keep the capital stock per unit of effective labour constant)?
- (c) Calculate the capital stock per unit of effective labour of the economy in the steady state.
- (d) Calculate the income stock per unit of effective labour of the economy in the steady state.
- (e) Calculate the consumption per unit of effective labour of the economy in the steady state.
- (f) Calculate the savings rate that maximises the per unit of effective labour consumption of the economy in the steady state.
- (g) Sketch the results of (a)–(f) in an appropriate Solow diagramme.
- (h) Determine the growth rates of output per capita, the capital stock per capita, and consumption per capita in the steady state.

## II. Multiple Choice

Select one answer.

### 1. Technological progress and unemployment

The diagram plots GDP per worker vs capital per worker, both across countries in 1990 (the scatter plots) and the trajectories since 1760 for a few representative countries (the paths).

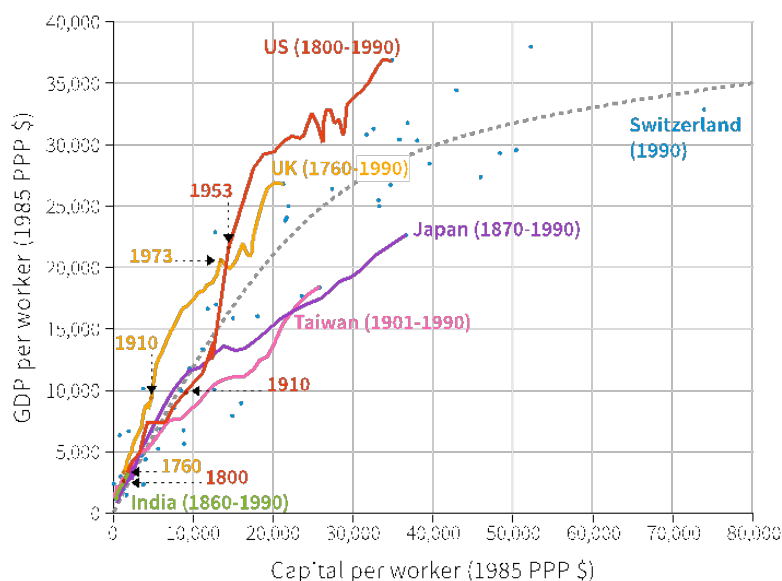


Figure 1

Which of the following statements is correct?

- (A) There is no clear evidence of technological progress in the US GDP per worker.
- (B) Switzerland has been the most successful country in attaining high GDP per worker by use of its capital.
- (C) Taiwan is more capital intensive than the UK in 1990.
- (D) The average product of capital has been higher in Japan than in the UK over the years shown.

## 2. Okun's Law

Figure 2 depicts the relationship between changes in real GDP (in percent) and unemployment rate (in percentage points) in Germany from 1993 to 2016. Each point represents one year.

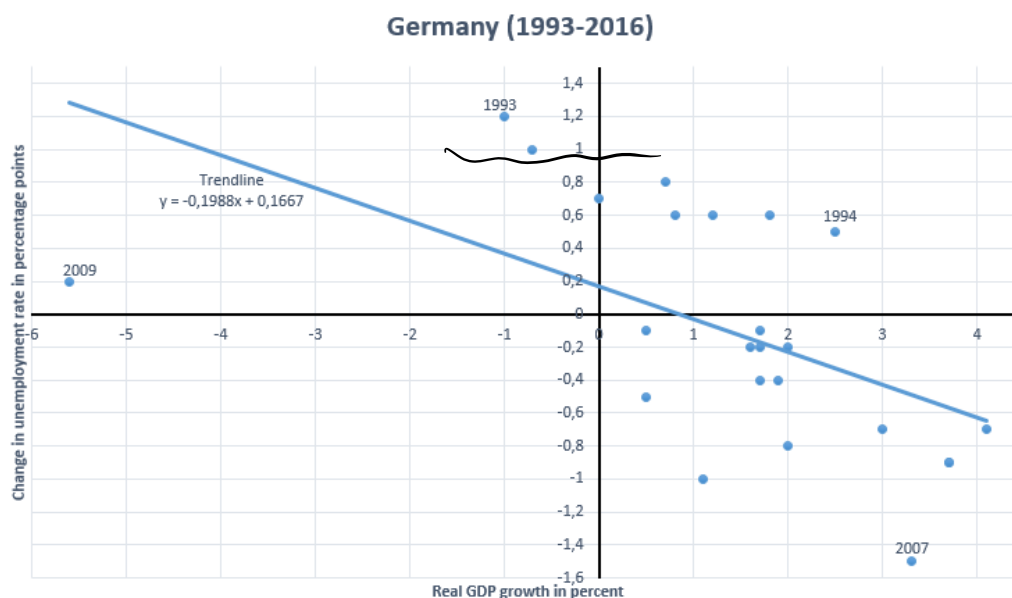


Figure 2

Which of the following statements is true?

- (A) A growth in real GDP always results in a decline of the unemployment rate.
- (B) A growth in real GDP above 0.9% on average is accompanied by a decline of the unemployment rate.
- (C) In 1994 a growth in real GDP of approximately 2.5% led to a decrease of unemployment by approximately 0.5 percentage points.
- (D) An increase of the unemployment rate of 0.1 percentage points on average leads to an increase of real GDP of 0.5%.