

```
| x::xs -> i (i (x,x) [x]) xs
```

2. Write tail recursive versions of the following functions (without changing their types). In addition to the definition from the lecture, all functions must use constant stack space ($\mathcal{O}(1)$ in the size of its input). In particular, all the helper functions used need to be tail-recursive and use constant stack space too! If you use a library function, check that the documentation (e.g. for [List](#)) marks it as tail-recursive, or when in doubt implement a tail-recursive version yourself!

a)

```
let rec fac n =
  if n = 0 then 1
  else n * fac (n - 1)
```

a) ^{rec} let go acc π = if $x=1$ then acc
else go (acc * π) ($\pi-1$)
let rec fac n = go 1 n.

* 用 List.
init
造随机
数组

b)

```
let rec remove a = function
| [] -> []
| x::xs -> if x = a then remove a xs else x::remove a xs
```

b) ^{用 function 处理 ls 更简单} let rec remove a

= let rec remove a ls
-helper.

将对象当作
function 的
match with
acc 处理对象

* 用 let in
可以用大方法
的参数
减少一个
参数!

c)

```
let rec partition p l = match l with
| [] -> [], []
| x::xs ->
  let a,b = partition p xs in
  if p x then x::a,b else a,x::b
```

let rec remove-help a ls stor
if ls = [] then stor [终止]
else match ls with x::xs
-> if x = a then
remove-help a xs stor
else remove-help a xs stor

Note: While the tests try to tell you whether your implementation is tail-recursive, they may not be 100% accurate. Check your implementation for tail-recursion yourself.

Note: OCaml 4.14 adds an experimental "Tail Modulo Constructor" (TMC) transformation ([docs](#)) that allows some non-tail-recursive functions to become tail-recursive automatically. This needs to be activated explicitly with the annotation `@tail_mod_cons`; see the documentation for more.

You should implement these functions without TMC, as there may be problems in the future where this feature is not allowed.

int list = Cons (int * 函数)