

AN INVESTIGATION INTO THE PERFORMANCE OF INTEGRATION METHODOLOGIES FOR REAL TIME MASS-SPRING CLOTH SIMULATIONS

by

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I declare that this dissertation is my own work and that the work of others is acknowledged and indicated by explicit references.

Christopher Phillips
September 2016

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Abstract

There has been much research into teaching computers to play games effectively, resulting in programs which are capable of beating the best human players at chess and other board games. These programs typically make use of strongly defined rules to provide their intelligence. This project suggests a different technique; applying stochastic optimisation techniques to effectively learn the strategic rules for playing Connect 4.

Three popular algorithms, a genetic algorithm, evolution strategies and particle swarm optimisation, were implemented to play Connect 4 in The Arena, a Java based framework providing the implementation of the game. Following a training period to learn the rules of the game, the playing performance of these algorithms was tested. The test results showed limited success, with only one of the algorithms able to play relatively successfully. The time constraints for the development of this project may be the reason for the poor performance of the algorithms, therefore more research and testing should be considered.

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Contents

| | |
|---|-----------|
| List of Figures | 8 |
| List of Tables | 9 |
| 1 Introduction | 10 |
| 1.1 Project Aims | 11 |
| 1.2 Hypotheses | 11 |
| 1.2.1 Null Hypothesis | 11 |
| 1.2.2 Alternative Hypothesis | 11 |
| 1.3 Report Structure | 12 |
| 2 Literature Review | 13 |
| 2.1 Cloth Simulation | 13 |
| 2.1.1 Cloth Properties | 13 |
| 2.1.1.1 Mechanical Properties | 14 |
| 2.1.1.2 Visual Properties | 14 |
| 2.1.2 Cloth Models | 14 |
| 2.1.2.1 Geometric Models | 15 |
| 2.1.2.2 Physically-based Models | 15 |
| 2.1.2.2.1 Continuum Models | 16 |
| 2.1.2.2.2 Discrete Models | 16 |

| | | |
|-----------|--|-----------|
| 2.1.3 | Mass-Spring Models | 17 |
| 2.1.3.1 | Provot Model | 17 |
| 2.1.3.2 | Choi Ko Model | 20 |
| 2.1.3.3 | Justification of Choice | 21 |
| 2.1.3.4 | Mass-Spring Models for Video Games | 22 |
| 2.1.4 | Numerical Integration for Mass-Spring Models | 25 |
| 2.1.4.1 | Explicit Integrators | 25 |
| 2.1.4.1.1 | Euler | 25 |
| 2.1.4.1.2 | Midpoint | 26 |
| 2.1.4.1.3 | Fourth order Runge-Kutta | 26 |
| 2.1.4.1.4 | Verlet | 27 |
| 2.1.4.2 | Implicit Integrators | 28 |
| 2.1.4.2.1 | Euler | 28 |
| 2.1.4.3 | Chosen Integration Methods | 29 |
| 3 | Design and Implementation | 31 |
| 3.1 | Development Methodology | 31 |
| 3.1.1 | Sequential | 31 |
| 3.1.2 | Cyclical | 32 |
| 3.1.3 | Chosen Methodology | 33 |
| 3.2 | Development | 33 |
| 3.2.1 | First Cycle | 33 |
| 3.2.2 | Second Cycle | 35 |
| 3.2.3 | Third Cycle | 36 |
| 3.3 | Profiling and Optimisation | 36 |
| 3.3.1 | First Cycle | 36 |

| | | |
|----------|---|-----------|
| 3.3.1.1 | Second Cycle | 38 |
| 4 | Test Plan | 39 |
| 4.1 | Test Data | 39 |
| 4.2 | Test Parameters | 40 |
| 4.2.1 | Mesh Size | 40 |
| 4.2.2 | Integrator Time Step | 40 |
| 4.2.3 | Spring and Damping Coefficients | 41 |
| 4.2.4 | Particle Mass | 41 |
| 4.3 | Test Process | 42 |
| A | Class Diagrams | 43 |
| A.1 | First Cycle Design | 43 |
| A.2 | Second Cycle Design | 45 |
| B | Profiling Results | 47 |
| B.1 | First Cycle | 47 |

List of Figures

| | | |
|-----|--|----|
| 2.1 | Mechanical properties of cloth | 14 |
| 2.2 | Visual Properties of cloth | 15 |
| 2.3 | Cloth with structural springs only | 18 |
| 2.4 | Cloth with structural and shear springs | 18 |
| 2.5 | Provot cloth model | 19 |
| 2.6 | Choi Ko cloth model | 21 |
| 2.7 | Super-elasticity problems | 22 |
| 2.8 | Constraint relaxation | 24 |
| 2.9 | Explicit integrator stability regions | 27 |
| 3.1 | Waterfall development methodology | 32 |
| A.1 | Initial design for the first development cycle | 43 |
| A.2 | Final design for the first development cycle | 44 |
| A.3 | Initial design for the second development cycle | 45 |
| A.4 | Final design for the second development cycle | 46 |
| B.1 | Profiling results using an <code>std::vector</code> to store springs | 47 |
| B.2 | Profiling results using dynamic arrays to store springs | 48 |
| B.3 | Profiling results for unoptimised <code>calcSpringForce</code> | 48 |
| B.4 | Profiling results for optimised <code>calcSpringForce</code> | 49 |

List of Tables

| | | |
|-----|-------------------------------------|----|
| 3.1 | First cycle requirements | 33 |
| 3.2 | Second cycle requirements | 35 |

Chapter 1

Introduction

The visual fidelity of video games has increased dramatically in recent years largely due to developments in discrete graphics hardware, or graphics processing units (GPUs). As a result, there is a need for realistic cloth in order to sell the appearance of video game characters and scenes. It is essential that the cloth should react to dynamic behaviour, such as a character moving or the wind blowing, and it must be animated in real time, i.e. at a minimum of 30 frames per second (FPS). These requirements render many cloth simulation techniques inappropriate, as they are too computationally expensive to be run in real time. The Mass-Spring model is one technique that is appropriate for use in video games, and is the most popular method for handling cloth for games. Whilst not necessarily providing 100% accuracy, Mass-Spring models result in visually pleasing animations, good enough for games, at, most importantly, real time frame rates.

Mass-Spring models use forces, calculated using Newtonian mechanics, to animate the cloth. This results in a series of differential equations that must be approximated by a numerical integrator at discrete time intervals. There are many different integrators that can be used and the choice of integrator can directly affect the performance of the simulation. Some integrators must necessarily use small time intervals in order to maintain the stability of the cloth, and this increases the frequency of the integration calculations thus reducing performance.

This project will investigate the effect different integration methods have on a real time cloth simulation using the Mass-Spring model.

1.1 Project Aims

The aim of this project is to investigate the performance effects of different integration methods on real time cloth simulation using the Mass-Spring model.

Based on this aim, the objectives of the proposed project are as follows:

- To research cloth simulation and numerical integration techniques
- To implement the Mass-Spring model for cloth simulation and several integrators, including explicit Euler
- To investigate the performance effects of the implemented integration methods on the simulation

1.2 Hypotheses

Volino and Magnenat-Thalmann (2001) were the first to investigate the performance impact of different integrators on cloth simulation. Their results, however, are extremely outdated, due to the vast increase in CPU power since 2001; from a 200MHz workstation CPU to the 3GHz+ CPUs available in modern desktops and laptops. Later work by Wang, Hu, and Zhuang (2009) also investigated the impact of different integrators, and found that integrator choice still has an impact on simulation performance. However they make no reference to the hardware their experiments were run on.

As a result, two hypotheses are proposed for this project, a null and an alternative.

1.2.1 Null Hypothesis

The null hypothesis is that all integration methods result in a real time cloth simulation when running on modern hardware.

This was chosen because Wang, Hu, and Zhuang (ibid.) make no reference to the hardware used, and the simulation developed will be run on an Intel I7 4770K at 4.2GHz, so it may be the case that there are no performance concerns with this modern hardware.

1.2.2 Alternative Hypothesis

The alternate hypothesis is that some integration methods are prohibitively expensive for real time cloth simulation and other methods provide better performance.

Recently, some researchers, such as Zeller (2005) and Tang et al. (2013), have proposed GPU accelerated approaches to Mass-Spring models which suggests that performance is still a consideration. Third party physics engines, such as PhysX[®] also use GPU accelerated models (Kim 2011) again suggesting performance of Mass-Spring models are still a concern.

1.3 Report Structure

This remainder of this report will be structured as follows:

- Chapter 2: literature review. An overview of cloth simulation techniques will be given and the Mass-Spring models and some numerical integrators described in detail
- Chapter 3: design and implementation. This chapter will describe the development methodology, design and some of the implementation details of the project
- Chapter 4: test plan. Details on how the hypotheses will be tested given

Chapter 2

Literature Review

2.1 Cloth Simulation

The simulation of cloth is a relatively old and well studied field with applications in many different areas, including, but not limited to:

- Virtual Garment Design
- Virtual Fitting Rooms
- Films
- Video Games

Different use cases require different things from the cloth simulation. For example, in virtual garment design, the physical accuracy of the simulation is paramount whereas cloth simulation for video games prioritises real-time simulation, sacrificing accuracy. Hence, many different models for cloth simulation have been proposed.

Since this project is concerned with the real-time simulation of cloth, only those models appropriate for real-time simulations have been studied in detail. However, a brief overview of other techniques will be provided. For a more detailed overview of cloth simulation techniques, see Ng and Grimsdale (1996).

2.1.1 Cloth Properties

Cloth has several properties that should be considered for modelling.

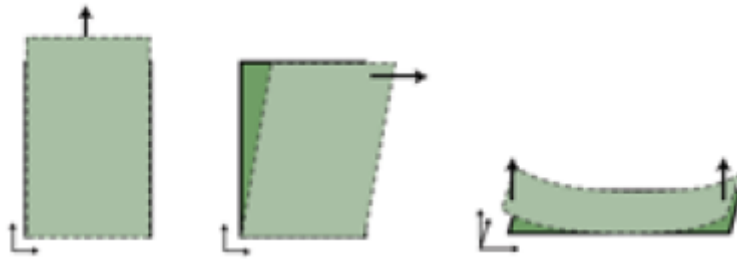


Figure 2.1: Mechanical properties of cloth (*Techniques for Animating Cloth*, p. 1)

2.1.1.1 Mechanical Properties

Cloth has three mechanical properties that control its behaviour; stretching, shearing and bending, Fig 2.1 shows how each property affects the cloth.

Stretching is the displacement of the cloth in either the horizontal or vertical direction. Most cloth has a high resistance to stretching and can typically only be stretched by 10% (*Techniques for Animating Cloth*, p. 1; Provot 1995, p. 4).

Shearing is the displacement of the cloth in a diagonal direction. Again, most cloths have high shearing resistance and this, coupled with high stretch resistance, makes cloth incompressible.

Finally, bending is the overall curvature of the cloth surface. Typically, cloth has low bending resistance and so is easily folded.

2.1.1.2 Visual Properties

The mechanical properties of cloth, discussed above, cause cloth to exhibit two visual properties. These properties arise from the fact that cloth is typically non-elastic, due to stretch and shear resistances, but highly flexible, due to low bend resistance.

Firstly, cloth will drape over objects and secondly the cloth will form many folds and wrinkles. Fig 2.2 demonstrates the visual properties of cloth.

2.1.2 Cloth Models

Techniques for modelling cloth are usually classified as either Geometric or Physically-based, and the choice of which modelling method to use depends on the use-case for the simulation.

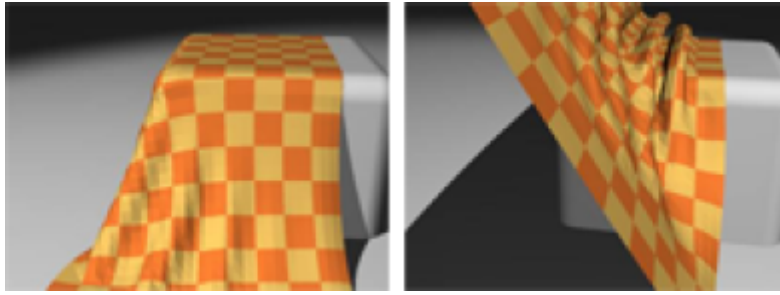


Figure 2.2: Visual properties of cloth (*Techniques for Animating Cloth*, p. 1)

2.1.2.1 Geometric Models

This family of techniques were the first models used to simulate cloth. They model the cloth using geometric equations and are especially good at modelling folds and wrinkles.

Weil was the first to propose a geometric model in 1986 and uses catenary curves to model the drape and folds of a hanging cloth. Following on from Weil, a number of other geometric models were proposed (see Ng and Grimsdale (1996) for more information).

All geometric techniques focus on simulating the appearance of cloth, rather than the physical properties. As such, geometric models are typically more computationally efficient than physically-based models, as there is no need to solve a series of complex equations. However, geometric techniques are unable to accurately simulate the motion of cloth, (Mongus et al. 2012, p. 1; Zhang and Yuen 2001, p. 2; Xinrong et al. 2009, pp. 1-2), and so are mostly useful for static cloth simulations.

As such, geometric models have not been considered for this project.

2.1.2.2 Physically-based Models

By contrast, physically-based models are concerned with the accurate modelling of the physical properties of the cloth and can therefore be used to produce realistic animations.

These models typically use a system of partial differential equations (PDE), or other differential equations, to model the cloth. These equations cannot be solved analytically and therefore the system requires discretisation to solve the equations at specific points in space and time. Following discretisation, a physically-based model typically requires the solving of an ordinary differential equation (ODE) of

the form (Baraff and Witkin 1998, p. 1):

$$\ddot{x} = M^{-1} \left(-\frac{\delta E}{\delta x} + F \right)$$

where:

x is a vector representing the geometric state of the system (2.1)

M is a diagonal matrix representing the mass distribution of the system

E is a function of x which yields the internal cloth energy

F is a function of x and \dot{x} which describes other forces

Physically-based models can be classified as either Continuum or Discrete.

2.1.2.2.1 Continuum Models

Continuum models were the first physical models to be proposed. Techniques in this family model cloth as a continuous surface and utilise continuum mechanics to calculate its behaviour; the Lagrange equations are most commonly used.

To discretise the continuous model, a numerical technique, such as a finite element method, is used. This is one of the advantages of continuum methods; they allow the use of a low resolution discretisation without sacrificing the accuracy of the simulation (Wacker, Thomaszewski, and Keckeisen 2005, pp. 4-5).

Another advantage of continuum models are that they are accurate; "they provide accurate models of the material derived directly from mechanical laws and models of material properties" (Magenat-Thalmann and Thalmann 2004, p. 200).

This accuracy comes at the cost of computational performance, the main disadvantage of these techniques. The accuracy also renders these models inappropriate for use in dynamic simulations; "the formal and analytical description they require for the mechanical behavior of the material cannot easily be altered to represent transitory and non-linear events. Hence, phenomena such as frequent collisions or other highly variable geometrical constraints cannot be conveniently taken into account" (ibid., p. 200). Hence, continuum models are typically only considered appropriate for static simulations, or simulations where accuracy is paramount. As a result, continuum models have not been considered.

2.1.2.2.2 Discrete Models

According to Choi and Ko (2002, p. 2), "Cloth is not a homogeneous continuum. Therefore modeling

fabrics as a continuum and employing FEM or FDM has several potential drawbacks". As a result several discrete, or particle, models have been proposed.

With these techniques the discretisation in space is carried out by modelling the cloth as a discrete mesh, either regular or triangular, of point masses, called particles. This sacrifices some of the accuracy of continuum models, as the accuracy will depend on the number of particles used. However, this loss in accuracy is traded off against better computational performance; physical models are the only models that can be used for dynamic, real-time simulations. The discretisation of the cloth has a direct affect on the performance of the simulation; Volino and Magnenat-Thalmann (2001, p. 5) have shown that simulation time varies cubically with mesh size. Hence, there is a trade off to be made between accuracy and performance when using discrete models, depending on the use-case.

By far the most popular technique is the mass-spring model. This model is popular as it is simple, easy to implement and offers a good balance between accuracy and efficiency. This model is the most common model used for dynamic, real-time simulations and as such, it has been chosen for this project and will now be described in more detail.

2.1.3 Mass-Spring Models

Mass-spring models were first proposed for use in cloth simulation in Provot (1995). Using these models, the cloth is discretised as a 2-dimensional mesh of point masses, either regular or triangular, connected by linear springs.

2.1.3.1 Provot Model

Using the mass-spring model proposed in Provot (ibid.) the cloth is modelled as a regular mesh of point masses. The points are connected together using three different types of springs:

- Structural springs, connecting particle $[i, j]$ to particles $[i + 1, j]$ and $[i, j + 1]$. These springs resist structural deformations of the cloth, and provide the overall cloth structure. Structural springs are not enough to provide a realistic cloth model. Fig 2.3 shows the results of running a cloth simulation with structural springs only. As can be seen, this does not produce a realistic image
- Shear springs, connecting particle $[i, j]$ to particle $[i + 1, j + 1]$ and particle $[i + 1, j]$ to particle $[i, j + 1]$. These springs provide shearing resistance for the cloth. By adding shear springs, the realism of the model is improved; Fig 2.4 shows the improved fidelity afforded by shear springs

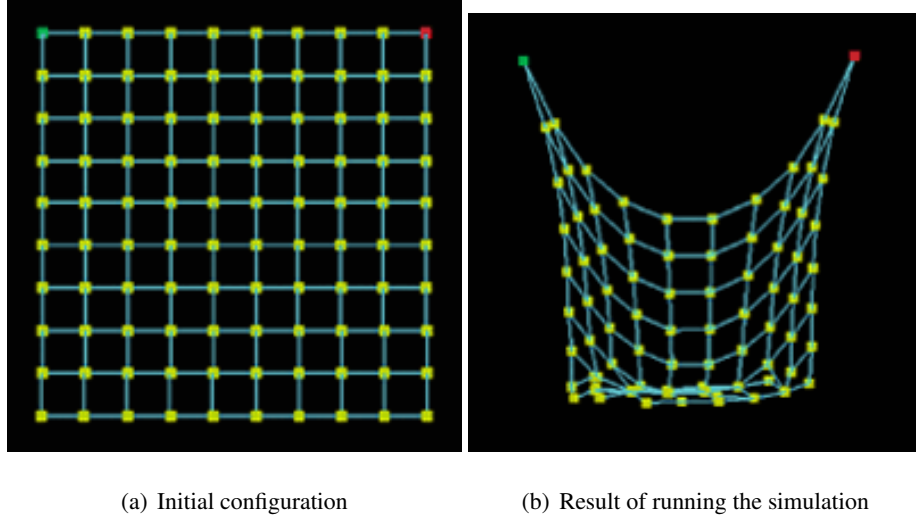


Figure 2.3: Cloth with structural springs only (Lander 2000b, p. 2)

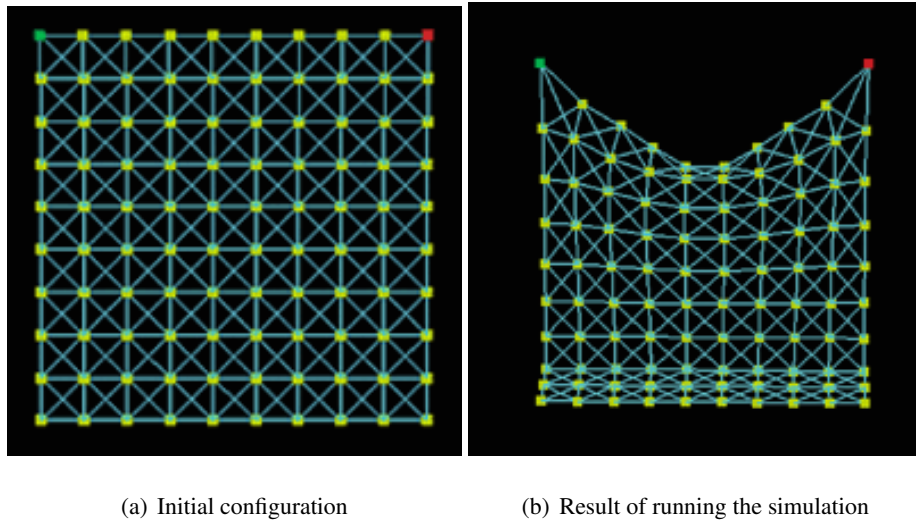


Figure 2.4: Cloth with structural and shear springs (Lander 2000b, p. 2)

- Bend springs, connecting particle $[i, j]$ to particles $[i + 2, j]$ and $[i, j + 2]$. These springs model bend resistance

Fig 2.5 shows the arrangement of these springs for a small cloth model.

The total number of each type of spring can be calculated with:

$$\begin{aligned}
 Num_{structural} &= 2((m-1)(n-1)) + (m-1) + (n-1) \\
 Num_{shear} &= 2((m-1)(n-1)) \\
 Num_{flexion} &= 2((m-2)(n-2)) + 2((m-2) + (n-2))
 \end{aligned} \tag{2.2}$$

where:

m and n are the vertical and horizontal dimensions of the mesh respectively

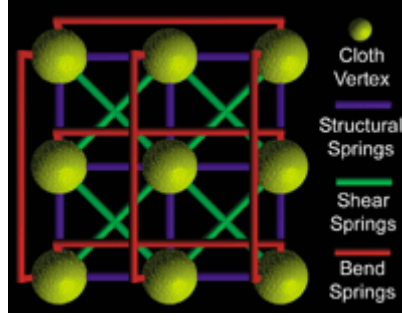


Figure 2.5: Provot cloth model (Lander 2000b, p. 2)

To animate the mesh, forces are applied to the particles and are calculated using Newton's second law:

$$F_{ij} = m_{ij}a_{ij}$$

where:

F_{ij} is the total sum of forces acting on particle ij (2.3)

m_{ij} is the mass of particle ij

a_{ij} is the acceleration of particle ij

The total force acting on a particle is defined as:

$$F_{total} = \Sigma F_{external} + \Sigma F_{internal} \quad (2.4)$$

$F_{external}$ are external forces acting on the mesh, such as gravity and wind.

Gravity is calculated by:

$$F_g = m_{ij}G$$

where: (2.5)

G is the gravitational constant

Wind is calculated by:

$$F_{wind} = w(n_{ij} \bullet \vec{W})$$

where:

n_{ij} is the surface normal of particle ij (2.6)

\vec{W} is the wind direction vector

w is the wind constant

$F_{internal}$ are the resultant forces of the springs connecting the mesh.

The spring force is calculated using the Hooke equation (Parent 2012, p. 201):

$$F_{spring} = -k_s(L_c - L_r) \frac{p_2 - p_1}{\|p_2 - p_1\|}$$

where:

k_s is the spring stiffness coefficient (2.7)

L_c is the current length of the spring

L_r is the initial, or rest, length of the spring

p_1 & p_2 are the positions of the two connected particles

Using this equation, the cloth will be modelled with pure elastic springs and will oscillate indefinitely.

However, as mentioned in 2.1.1.2 and Provot (1995, p. 1), cloth is a non-elastic medium and therefore the model needs to account for the energy lost due to internal friction in the cloth.

This is typically modelled as an extra internal damping force, calculated using (Parent 2012, p. 201):

$$F_{damping} = -k_d(\dot{p}_2 - \dot{p}_1) \bullet \left(\frac{p_2 - p_1}{\|p_2 - p_1\|} \right) \left(\frac{p_2 - p_1}{\|p_2 - p_1\|} \right)$$

where:

(2.8)

k_d is the spring damping coefficient

\dot{p}_1 & \dot{p}_2 are the velocities of the two connected particles

2.1.3.2 Choi Ko Model

A different mass-spring model was proposed in Choi and Ko (2002) and aims to improve the buckling behaviour of the cloth, resulting in more realistic draping and wrinkling behaviour.

The cloth is modelled in a similar way to the Provot method, but additional bend springs are added, connecting particle $[i, j]$ to particle $[i + 2, j + 2]$ and particle $[i + 2, j]$ to particle $[i, j + 2]$; fig 2.6 shows the arrangement of springs.

This model uses an energy-based approach, of the general formula 2.9(Bartels 2014, p. 3), to calculate the forces acting on individual particles.

$$F = \left(\frac{\delta E(S)}{\delta x}, \frac{\delta E(S)}{\delta y}, \frac{\delta E(S)}{\delta z} \right)$$

where:

(2.9)

$E(S)$ is an energy function of S , a representation of the cloth's state

Two types of interactions are defined, type 1 and type 2. Type 1 interactions model stretch and shear resistances, the red lines in 2.6, and are represented by a linear spring model. Type 2 interactions model

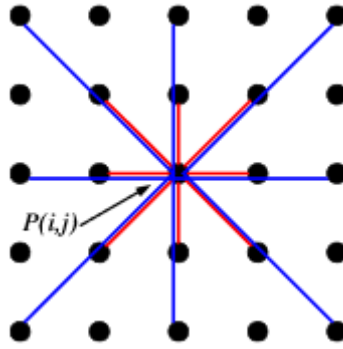


Figure 2.6: Choi Ko cloth model (Choi and Ko 2002, p. 2)

bend forces, the blue lines in 2.6, and helps prevent the so called post-buckling instability problem. The interested reader should see Choi and Ko (2002) for more information on the energy functions for each interaction type.

2.1.3.3 Justification of Choice

Mass-spring models are suitable for use in this project as they are efficient and simple to implement; "Mass-spring models are the most efficient as well as the simplest of the cloth models. This method is one of the most popular techniques for simulating cloth, especially when interactive frame rates are required" (Zink and Hardy 2007, p. 2). As this project is concerned with the real time animation of cloth, mass-spring models are therefore the obvious choice.

Mass-spring models are also the most common method of modelling cloth in video games, used in games such as Alan Wake, (Enqvist 2010, p. 2), and Hitman: Codename 47, (Jakobsen 2005, p. 1), as well as commercial physics engines for games, such as PhysX[®]. Again, since this project is concerned with the simulation of cloth for use in a video game, mass-spring models are the logical choice.

In particular, the Provot model was used for this project as the force-based approach requires the solving of a much simpler series of equations than the energy-based approach of the Choi Ko model, and is therefore likely to be more computationally efficient.

One disadvantage of the mass-spring model is that it does not achieve realistic animation of cloth as "mass-spring systems do not model any specific material and are not related to measured properties of real clothes" (Wacker, Thomaszewski, and Keckeisen 2005, p. 3). However, by careful tuning of the spring stiffness coefficients pleasing results can be achieved; Mongus et al. (2012) have shown that, with tuning, mass-spring models can reproduce the drape of a cloth with an accuracy of 97%.

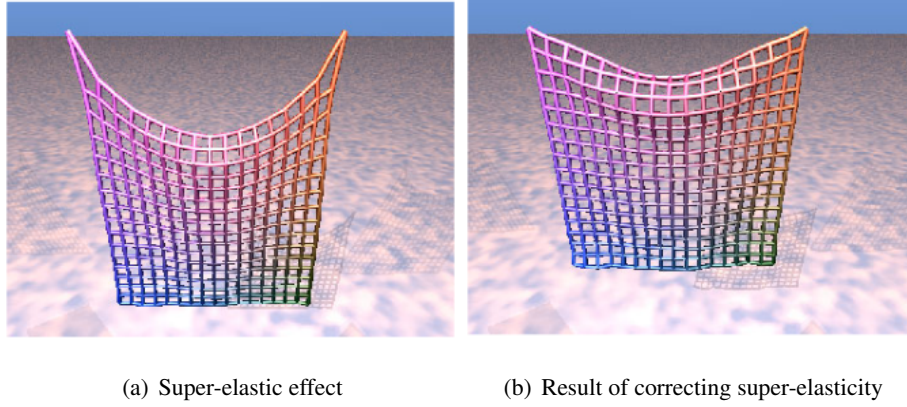


Figure 2.7: Super-elasticity problems (Provot 1995, pp. 4,6)

Another disadvantage of mass-spring models is what Provot calls 'super-elasticity'; springs are allowed to deform too much, leading to unrealistic looking cloth. This is caused because "the springs are "ideal" and they have unlimited linear deformation rate" (Vassilev, Spanlang, and Chrysanthou 2001, p. 3). To counter this effect, Provot suggests enforcing length constraints on structural and shear springs. First the position of the particles are updated, then the deformation of the springs are calculated. If this deformation value is greater than some threshold, τ_c , then the position of the connected particles are adjusted so the deformation rate equals τ_c . Fig 2.7 shows the super-elasticity problem and the results of employing Provot's corrective method. As can be seen, correcting the super-elasticity results in a much more realistic model.

2.1.3.4 Mass-Spring Models for Video Games

Both the Provot and Choi Ko Mass-Spring models can be separated into two component, the modelling component and the animation component. The modelling component describes how the cloth will be represented internally, i.e. the discretisation by point masses and the interconnectivity of the springs, and the animation component details how the cloth will be animated over time; for the Provot model, using the forces detailed in the previous sections.

For video games, where performance is a key factor, using the force based animation methods in the Provot and Choi Ko models may be prohibitively expensive over a certain mesh size. This results from the fact that the number of springs grows rapidly as the number of particles increases, leading to more internal force calculations per frame. For example, for a cloth represented by a 50 by 50 mesh of particles connected as in the Provot model, there are 14502 springs, and therefore Equations 2.7 and 2.8 must be calculated 14502 times every frame. For the Choi Ko model, the internal force cost would only

rise, as not only are there more springs in their model, but also their force calculations are more expensive. Thus, another approach to animating Mass-Spring models is usually taken for video games, called Position Based Dynamics (PBD).

PBD were first used by Jakobsen (2005) to implement cloth in *Hitman: Codename 47* and have since gone on to become the standard for cloth animation in games (Enqvist 2010, p. 2) and commercial physics engines (Kim 2011).

When using PBD, the cloth is modelled either using the Provot method (Enqvist 2010, p. 2) or using a simplified version of the Provot model, where the flexion springs are omitted (Zeller 2005, p. 7; Kim 2011, p. 25). Instead of being modelled as Hooke springs, the spring connections are instead treated as distance constraints of the form

$$\|x_2 - x_1\| = d$$

where:

(2.10)

x_2 and x_1 are the positions of the particles connected by the constraint

d is the length of the constraint

The work of Jakobsen (2005) was developed in Müller et al. (2006) resulting in a more general PBD model that supports both equality and inequality constraints. For games however, modelling cloth as a mesh of particles connected by simple distance constraints is enough.

To animate the cloth using PBD, external forces are first applied to the cloth, integrated using Verlet integration and the particle positions updated. Since the particles have moved, it is possible that one or more of the spring constraints are violated so they are checked and the positions of the particles corrected so none are violated; this is called constraint relaxation and is shown in Fig 2.8 . The constraints are correct using Equation 2.11 (ibid., p. 4); stiffness and damping can also be added to control the appearance of the cloth.

$$\begin{aligned}\Delta x_1 &= -\frac{w_1}{w_1 + w_2}(\|x_2 - x_1\| - d)\frac{x_2 - x_1}{\|x_2 - x_1\|} \\ \Delta x_2 &= \frac{w_2}{w_1 + w_2}(\|x_2 - x_1\| - d)\frac{x_2 - x_1}{\|x_2 - x_1\|}\end{aligned}\tag{2.11}$$

where:

w_1 and w_2 are the weights of the respective particles

This method of iteratively checking constraints and relaxing them immediately is called the Gauss-Seidel method and has one main problem; relaxing one constraint may violate other, already examined, constraints and therefore multiple relaxation passes may be needed. According to Jakobsen (2005, p. 1)

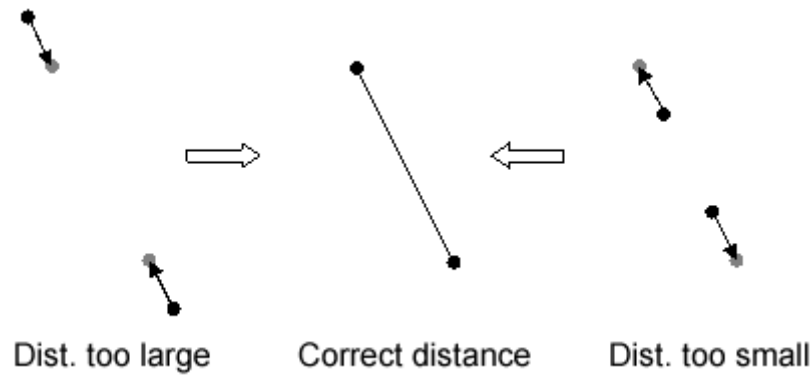


Figure 2.8: Constraint relaxation (Jakobsen 2005, p. 1)

however, for most cloth only one relaxation pass is necessary for visually pleasing animation, although this is contradicted by (Kim 2011), who suggests that multiple passes are needed when using a Gauss-Seidel approach.

A PBD approach is unconditionally stable, as any instability will be corrected by the relaxation process, and can therefore use a large time step to reduce the performance cost of the simulation. Whilst implicit integrators, discussed below, offer unconditional stability for the traditional Mass-Spring models they are much more difficult to implement and understand, so the fact that PBD are stable and simple explains their popularity for use in video games. The need for multiple Gauss-Seidel passes can be used to control the performance hit of the cloth as well; the amount of frame time available for cloth simulation could be used to adjust the number of relaxation passes, so that if more time is available, more accurate cloth is produced.

Despite its advantages, PBD was not chosen for this project as they are a closed problem for cloth simulation in video games. PBDs are the standard method of animating cloth for games, and have been implemented efficiently in commercial physics engines. By contrast, the Provot Mass-Spring model is not conventionally used, as it may be too expensive for certain mesh sizes. However, the research into the performance of the Provot model is either old, or makes no reference to the hardware used, and therefore there is scope for further work to investigate whether performance is still a concern with modern hardware.

2.1.4 Numerical Integration for Mass-Spring Models

As mentioned above, physically-based models for cloth simulation require solving a series of differential equations, discretised in space and time. According to Wacker, Thomaszewski, and Keckeisen (2005, p. 5), "since particle systems already represent a discretisation in space, only a system of ordinary differential equations has to be solved". For the Mass-Spring model using Newtonian mechanics a series of second order ODEs, of the form 2.12, must be solved (Zink and Hardy 2007, p. 5).

$$\frac{\delta^2 x}{\delta t^2} = M^{-1}F(x, v) \quad (2.12)$$

This can be converted into a coupled series of first order ODEs by separating the position and velocity (ibid., p. 5):

$$\frac{\delta}{\delta t} \begin{pmatrix} x \\ v \end{pmatrix} = \begin{pmatrix} v \\ M^{-1}F(x, v) \end{pmatrix} \quad (2.13)$$

Equations 2.12 and 2.13 cannot be solved analytically, and therefore it is necessary to use a numerical method, or integrator, to approximate them at discrete time intervals. There are many integration methods that could be chosen, typically classified as either explicit or implicit, and the most popular choices will be described now.

2.1.4.1 Explicit Integrators

Most of the early work on physically-based cloth simulation used explicit integrators as they are simple and easy to implement; they only require information about the state of the system at the previous interval to calculate the current state.

The most commonly used explicit integrators are the Runge-Kutta family of integrators.

2.1.4.1.1 Euler

The first order Runge-Kutta integrator, or explicit Euler, was used in Provot (1995) to approximate a Mass-Spring system.

Equation 2.13 is approximated by (Wang, Hu, and Zhuang 2009, p. 3):

$$v_{i+\Delta t} = v_i + \Delta t F(t_i, v_i)$$

where:

v_i is the velocity of a particle at time interval i

Δt is the time step

(2.14)

When applied to the Provot Mass-Spring model, this gives (Provot 1995, p. 3):

$$\begin{aligned} a_{i,j}(t + \Delta t) &= \frac{1}{m_{i,j}} F_{i,j}(t) \\ v_{i,j}(t + \Delta t) &= v_{i,j}(t) + \Delta t a_{i,j}(t + \Delta t) \\ x_{i,j}(t + \Delta t) &= x_{i,j}(t) + \Delta t v_{i,j}(t + \Delta t) \end{aligned}$$

where:

$$a_{i,j}, m_{i,j}, v_{i,j} \text{ and } x_{i,j} \text{ are the acceleration, mass, velocity and position of particle } i, j \text{ respectively} \quad (2.15)$$

The explicit Euler method is computationally cheap but can result in numerical instability if too large a time step is used. Mathematically, the explicit Euler method is stable only if the time step is less than the natural period of the system, approximated as $\pi\sqrt{\frac{m}{K}}$, where K is the maximum stiffness in the system. Vassilev, Spanlang, and Chrysanthou (2001, p. 2) found that in fact explicit Euler is only stable for Δt values less than $0.4\pi\sqrt{\frac{m}{K}}$.

As cloth generally does not stretch easily, this results in high stiffness in the structural and shear springs, which necessitates the use of a small time step if the explicit Euler integrator is chosen. This can impact the overall performance of the simulation, as while this integrator is cheap, the frequency of calculations is high as a result of the time step limitations.

2.1.4.1.2 Midpoint

The explicit Midpoint integrator is a second order Runge-Kutta method and modifies the Euler integrator to give greater stability.

Equation 2.14 is modified to give the following (Wang, Hu, and Zhuang 2009, p. 3):

$$v_{i+\Delta t} = v_i + \Delta t F\left(t_i + \frac{\Delta t}{2}, v_i + \frac{\Delta t}{2} F(t_i, v_i)\right) \quad (2.16)$$

Since this method requires two derivatives, the computational cost is greater than Euler. However, because the midpoint method affords greater numerical stability (see fig 2.9), a larger time step can be used which increases the overall simulation performance; Wang, Hu, and Zhuang (ibid.) have shown that the midpoint integrator offers close to twice the simulation performance over explicit Euler.

2.1.4.1.3 Fourth order Runge-Kutta

The Fourth order Runge-Kutta integrator offers greater stability using larger time steps over the midpoint

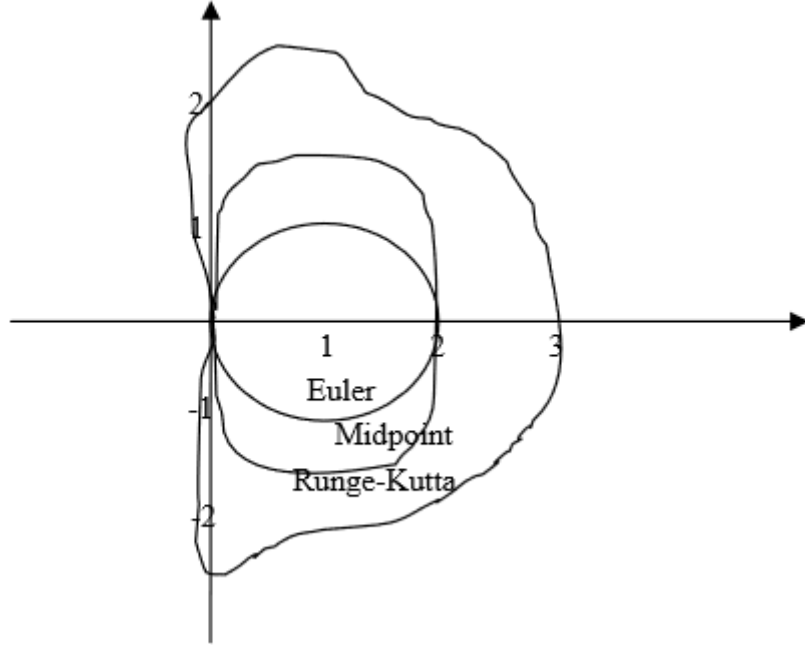


Figure 2.9: Explicit integrator stability regions (Wang, Hu, and Zhuang 2009, p. 4)

method and is formulated as (Wang, Hu, and Zhuang 2009, p. 3):

$$\begin{aligned}
 v_{i+\Delta t} &= v_i + \frac{\Delta t}{6}(k_1 + 2k_2 + 2k_3 + k_4) \\
 k_1 &= F(t_i + v_i) \\
 k_2 &= F\left(t_i + \frac{\Delta t}{2}, v_i + \frac{\Delta t}{2}k_1\right) \\
 k_3 &= F\left(t_i + \frac{\Delta t}{2}, v_i + \frac{\Delta t}{2}k_2\right) \\
 k_4 &= F\left(t_i + \Delta t, v_i + \frac{\Delta t}{2}k_3\right)
 \end{aligned} \tag{2.17}$$

This integrator has a significantly higher computational cost than the other methods discussed, however Volino and Magnenat-Thalmann (2001, p. 4) have shown that the Runge-Kutta integrator supports time steps almost six times larger than the midpoint method. Therefore, given that Runge-Kutta is three times as computationally expensive as midpoint, this suggests that this integrator can lead to twice the overall simulation performance. Wang, Hu, and Zhuang (2009, p. 4) have also shown that the fourth order Runge-Kutta integrator offers simulation performance over midpoint and explicit Euler.

2.1.4.1.4 Verlet

Verlet integration is an alternative to the Runge-Kutta family of integrators. It avoids velocity calculations by approximating the velocity of a particle using its previous positions.

A particle's new position is approximated by (Mongus et al. 2012, p. 2):

$$x_{i+\Delta t} = 2x_i - x_{i-\Delta t} + a_{i+\Delta t}\Delta t^2 \quad (2.18)$$

This method is computationally fast and reasonably stable, as "velocity is implicitly given and consequently it is harder for velocity and position to come out of sync" (Jakobsen 2005, p. 1). However it does still suffer from time step issues; figures 11 and 13 in Wacker, Thomaszewski, and Keckeisen (2005, pp. 14-15) show that below a certain threshold Verlet integration is less stable than explicit Euler, but more stable over that threshold.

2.1.4.2 Implicit Integrators

According to Baraff and Witkin (1998, p. 1), "Explicit methods are ill-suited to solving stiff equations because they require many small steps to stably advance the simulation forward in time". Therefore they propose an implicit integrator for use in cloth simulation since implicit integrators are unconditionally stable regardless of step size.

However implicit integrators are computationally more expensive than their explicit equivalents, as "they involve the resolution of a large and sparse linear equation system for each iteration" (Volino, Cordier, and Magnenat-Thalmann 2005, p. 4). Since they are unconditionally stable however, this can be countered by simply using a larger time step. The guaranteed stability of these methods also reduces the accuracy of the simulation, as they introduce inherent numerical damping, which increases as the time step increases (see Volino and Magnenat-Thalmann (2001, p. 4)). As such, there is a balance to be found between performance and accuracy of the simulation with implicit integrators.

The most common implicit integrator is the implicit, or backward, Euler method which will be described now. It should be noted that there are many other implicit integrators available.

2.1.4.2.1 Euler

First proposed for use in cloth simulation in Baraff and Witkin (1998), the implicit, or backward, Euler method is an adaptation of the explicit Euler method.

Equation 2.15 is modified to give (Kang, Choi, and Cho 2000, p. 3):

$$v_i^{t+\Delta t} = v_i^t + F_i^{t+\Delta t} \frac{\Delta t}{m_i} \quad (2.19)$$

$F_i^{t+\Delta t}$ cannot be calculated at the current time step, and so must be approximated as (ibid., p. 3):

$$F^{t+\Delta t} = F^t + \frac{\delta F}{\delta x} \Delta x^{t+\Delta t} \quad (2.20)$$

$\Delta x^{t+\Delta t}$ can be written as $\Delta t(v^t + \Delta v^{t+\Delta t})$ and so eq. 2.20 can be rewritten, giving the series of linear equations (Kang, Choi, and Cho 2000, p. 3):

$$\left(I - \frac{\Delta t^2}{m} \frac{\delta F}{\delta x}\right) \Delta v^{t+\Delta t} = F^t \frac{\Delta t}{m} \quad (2.21)$$

where:

I is the identity matrix

Thus, implicit Euler involves calculating $\Delta v^{t+\Delta t}$ every iteration using:

$$\Delta v^{t+\Delta t} = \left(I - \frac{\Delta t^2}{m} \frac{\delta F}{\delta x}\right)^{-1} F^t \frac{\Delta t}{m} \quad (2.22)$$

$\frac{\delta F}{\delta x}$ is the negated Hessian matrix, denoted as H, and can be approximated as (ibid., p. 3):

$$H_{ij} = \begin{cases} k_{ij} & \text{if } i \neq j \\ -\sum_{i \neq j} k_{ij} & \text{if } i = j \end{cases} \quad (2.23)$$

where:

k_{ij} is the spring stiffness

As a result, the implicit Euler method requires the computation of an n x n matrix each iteration, and thus increasing the size of the mesh greatly impacts the performance of this method.

However, if the stiffness of the springs and mass of the particles are constant throughout the simulation then $\left(I - \frac{\Delta t^2}{m} H\right)^{-1}$ can be precomputed, giving performance gains.

This method has been shown by Volino and Magnenat-Thalmann (2001) to be stable for any time step value, however as the time step increases, the accuracy decreases rapidly over a certain threshold. Using the method described above, it is also not possible to use an adaptive time step or to vary the mass or stiffness of the model as the cost of computing H every iteration is high. As such, many researchers, such as Mesit, Guha, and Chaudhry (2007) and Kang, Choi, and Cho (2000), have presented faster approximation methods for the implicit Euler integrator.

2.1.4.3 Chosen Integration Methods

Four integrations methods were chosen for investigation by this project.

- Explicit Euler. This is the simplest integrator and one of the most popular in the literature but it is also most likely to impact simulation performance due to its reliance on small time steps

- Fourth order Runge-Kutta. Computationally more expensive than explicit Euler, but stable with larger time steps, therefore offering an interesting comparison between computational cost and simulation performance
- Verlet. Chosen as it is an explicit integrator that is not part of the Runge-Kutta family
- Implicit Euler. Unconditionally stable regardless of time step, Chosen to provide a contrast between explicit and implicit integrators

Chapter 3

Design and Implementation

3.1 Development Methodology

Software development methodologies break the development of a piece of software down into a number of phases with the aim of improving design and code quality as well as aiding in project management. There are a large number of different development methodologies, although they can typically be classified as either sequential, also called waterfall, or cyclical, also called spiral. The choice of which method to use will depend on the specifics of the software project as well as developer preference and team size.

3.1.1 Sequential

The sequential, or waterfall, approach uses a number of strict, sequential phases for developing software; each phase must be completed before the next phase can begin. Fig. 3.1 shows the typical structure of this methodology.

This approach works well for projects where the requirements are strictly defined, the project's subject area well known and the technologies involved well understood by the developers. In this case, the software can be designed well from the start, so there is little need for iterative development. If the project's requirements are likely to change, or the subject area and technologies are ill-understood or new then a waterfall approach is inappropriate. The rigid structure of the waterfall method does not allow requirements to be easily changed, or poor design choices corrected; in order to change requirements or correct poor design the whole development process must be started again, as there is no method of feedback between development phases.

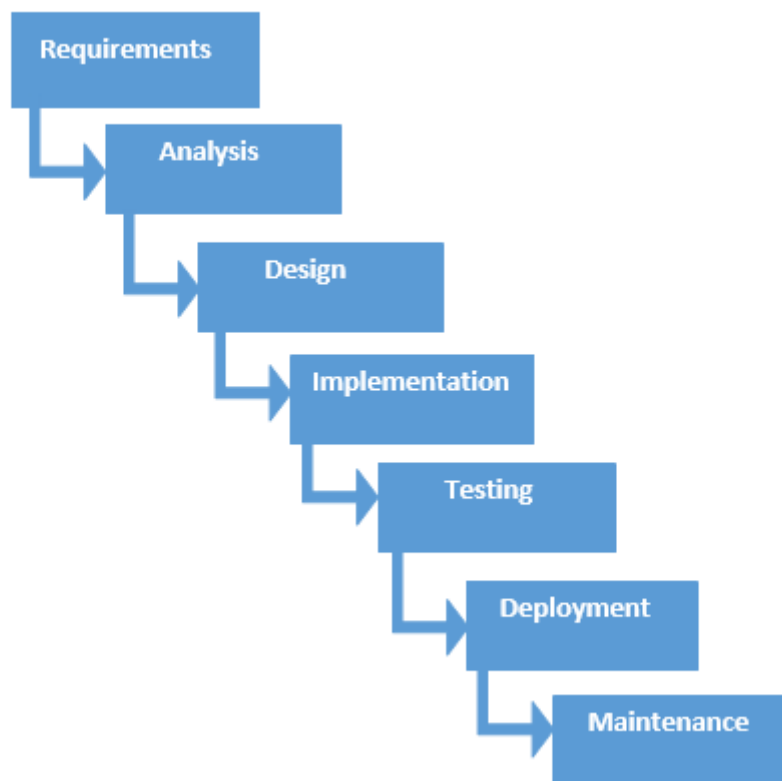


Figure 3.1: Waterfall development methodology (*What is Waterfall Model in software testing and what are advantages and disadvantages of Waterfall Model*)

3.1.2 Cyclical

Cyclical approaches, as the name suggests, develop software using iterative cycles. At the start of each cycle requirements and design are set and at the end, a working software prototype is produced. This prototype is used as feedback for the next cycle, adjusting the requirements and correcting design mistakes and issues as necessary. These methods counteract the disadvantages of the waterfall approach; by using an iterative approach it is easy to add or change requirements or redesign areas of the project.

There are many development methods which are derived from a cyclic approach, including Rapid Application Development (RAD) and Scrum.

RAD is a development method which favours rapid prototyping with minimal planning. Since there is less focus on planning at each iteration it is extremely easy to incorporate design and requirement changes. Prototype development will start earlier than other methods and this enables issues to be caught early, and the design to be altered appropriately. There is a requirement when using RAD of skilled and experience developers and designers, as the prototypes developed must be reusable so as to

| Requirement | Type |
|--|----------------|
| Must model cloth using the Provot Mass-Spring model | Functional |
| Must be able to render cloth to the screen | Functional |
| Must be able to pin particles so they are unaffected by forces | Functional |
| Must perform in real time | Non-functional |

Table 3.1: First cycle requirements

avoid wasting time.

Using Scrum, a project is broken down into sprints and each sprint is timeboxed with a duration, i.e. 24 hours, 4 weeks. At the end of each sprint a working prototype is produced and as the sprints are completed the project is designed and developed over time.

3.1.3 Chosen Methodology

For this project, cyclical methods were preferred over waterfall. This was partly due to the author's preference for cyclical methods and partly because there were some unknowns, particularly related to rendering, that made rigidly designing the system difficult. Using the more agile cyclical methods allowed for some investigative work before finalising the system design.

In particular, RAD was chosen as the development methodology.

3.2 Development

Since RAD was the chosen development methodology, the artefact was developed over several cycles.

3.2.1 First Cycle

In the first cycle the Mass-Spring model was implemented. Springs were implemented using the Hooke equation (Equation 2.7) to calculate the internal spring force with linear damping as an additional internal force using Equation 2.8. Gravity, implemented as Equation 2.5, was the only external force. Rendering of the cloth was also implemented.

Table 3.1 shows the initial requirements of the first development cycle.

Before designing this cycle, an initial investigation into the rendering component was carried out, as the choice between DirectX11 or OpenGL would affect the design of the system.

As this project is not concerned with rendering cloth, but simulating it, it was decided that the cloth would be rendered as a mesh of lines, representing the structural and shear springs (as in Figs 2.4 and 2.7). Since the positions of the particles, and therefore vertices, will change over time, a DirectX11 implementation would have to use a dynamic vertex buffer and remap the vertex data every frame. This is not an issue in OpenGL, since it is possible to draw vertices directly with the `glVertex3f` function. It was unknown by the author what the cost of this remapping would be so simple OpenGL and DirectX11 implementations were created and their performance compared. For a 500 by 500 mesh, with a debug build, the OpenGL implementation rendered the structural and shear springs at 80FPS and the DirectX11 version at 450FPS. Hence, DirectX11 was chosen as the rendering language. It should be noted that the OpenGL implementation was very naive, due to the author's inexperience, and this is most likely the reason for the poor performance. It is probable that a more robust implementation, using more advanced features, would perform much more closely to the DirectX11 implementation.

The initial design can be seen in Fig A.1; the rendering component, constructors, accessors and mutators have been excluded for brevity.

Since DirectX11 was the rendering language, DirectXMath types were used for the key variables in the Particle class. This gives performance gains over manually implementing a 3-dimensional vector and functions, as the functions that operate on DirectXMath types are compiled into SIMD instructions, allowing the calculations to be completed in fewer CPU cycles.

An `std::vector` was initially used to store the springs as it is not necessary to separate the springs into types, since the internal forces are calculated the same for every spring type. Also, the equations for calculating the amount of each spring (see Equation 2.2) were unknown during the initial design process, so an `std::vector` was chosen as it would allow an any number of springs to be stored, thanks to its expandable storage.

During implementation, the initial design had to be adapted as a result of performance concerns; these optimisations will be discussed in the section 3.3.

Fig A.2 shows the final design of this cycle with the optimisation changes. Timing code was also added to allow performance data necessary for testing the hypotheses to be extracted from the cloth. The test plan for this project will be detailed in the next chapter. Code for automating the testing process using an XML file was also added, again, details of this will be discussed in the next chapter.

| Requirement | Type |
|--|------------|
| Must implement the Explicit Euler and Verlet integrators | Functional |
| Must be able to dynamically switch integrators | Functional |

Table 3.2: Second cycle requirements

3.2.2 Second Cycle

During the second development cycle the model developed in the first cycle was adapted to use different integration methods. The explicit Euler and Verlet integrators were implemented as described in 2.1.4.1. Wind was also added as an additional external force.

The requirement for this development cycle are shown in Table 3.2.

The initial design of this development cycle can be seen in Fig A.3. For brevity, only the changes introduced for this cycle are shown for the classes developed previously; it can be assumed that the Particle and Cloth classes are unchanged other than the documented additions.

Two separate designs were initially proposed, one using static classes and storing a function pointer for the appropriate integrator, and the second using an interface and virtual functions. For the interface design, the inheriting classes were designed using the Singleton design pattern. Since particles are passed as parameters to the integrate function, there is no need for each particle to have their own instance of a particular integrator. Therefore it makes sense for integrators to be Singletons, and this helps to reduce the memory footprint of the application as well as the cost of dynamically switching integrators; as each integrator only needs to be dynamically allocated once, rather than for every particle.

The two different designs were suggested as the aim was to use the most efficient implementation possible and it was unknown during the design process which would be more efficient. As such, both designs were implemented and then some tests run using the explicit Euler integrator to determine which was most efficient. Compared with implementing explicit Euler directly in Particle, both implementations increased total update time by approximately 0.4ms for a 50 by 50 mesh on a debug build. This translated to an approximate drop of 4-5 FPS, and was expected due to the fact that both designs must call accessors to access Particle's data.

Compared with each other, the results were more variable. For some runs the static class design was more efficient and for others the interface design more so. Ultimately, the efficiency difference was

small, at most a 0.1ms difference between them, so the conclusion was reached that both designs were equally efficient. However, the explicit Euler integrator is the cheapest integrator, so for more expensive integrators, such as fourth order Runge-Kutta, a wider performance gap may be found. Therefore these experiments will be run again during the third development cycle using fourth order Runge-Kutta and the design retroactively changed if a significant efficiency gulf is found.

Since both design were equally efficient, the interface design was chosen as the author felt that it was, ostensibly, a better quality approach than using static classes. One minor optimisation was made to the initial design and is documented in the next section. As a result of this optimisation, the chosen design now performs almost as well as coding the integrator directly in Particle and means Particle conforms much more to the Open/Closed SOLID principle. Since Particle stores a pointer to the interface, and only calls virtual functions, new integrators can easily be added and used without any changes needed in Particle. The final design can be seen in Fig A.4.

3.2.3 Third Cycle

In the final development cycle the fourth order Runge-Kutta and implicit Euler integrators were implemented.

3.3 Profiling and Optimisation

3.3.1 First Cycle

Several optimisations were made to the design of the first development cycle as a result of profiling the application.

Firstly the `std::vector` was replaced with dynamically allocated arrays in the Cloth class. Iterating though the vector to calculate the spring forces proved prohibitively expensive for meshes over a certain size, even when `calcSpringForce` was an empty function; a 100 by 100 mesh was the largest mesh that supported real time frame rates, running at 40FPS on a debug build. Profiling showed that `std::vector` iterator functions were the most expensive execution path, as a range-based for loop was used to iterate over every spring. This can be seen in Fig B.1 in the appendices. Hence, the vector was replaced with dynamically allocated arrays and the equations listed in 2.2 identified. Fig B.2 shows the profiling results

using dynamic arrays. As can be seen, the high cost execution paths have moved away from iterating over the springs and into calculating the spring forces themselves.

Switching to arrays gave a 4x FPS increase, for the same mesh size, and a 2x increase in the maximum real time mesh size.

Secondly, profiling showed there were optimisations to be made in `calcSpringForce`.

The profile in Fig B.3 shows that `calcSpringForce` was the most expensive code path, and within it, `addForce` and `XMLoadFloat3` were the most expensive functions. This results from the fact that `XMVECTOR`s are used in `Particle` for variables such as position. `XMVECTOR`s must be converted into `XMVECTOR`s using `XMLoadFloat3` in order to be able to use the `DirectXMath` vector functions. Therefore, the position and velocity of every particle had to be converted every frame in order to implement Equations 2.7 and 2.8. Similarly, `addForce` must call `XMLoadFloat3` and `XMStoreFloat3` to first convert `totalForce` into an `XMVECTOR` for use in addition, and then convert the resultant `XMVECTOR` back into an `XMVECTOR`. Again, this had to be done every frame, hence why Fig B.3 shows that `XMLoadFloat3` and `XMStoreFloat3` are the two most expensive functions in the entire system. As a result, `XMVECTOR`s were used instead of `XMVECTOR`s, removing the need for conversions, and giving reasonable performance gains.

Fig B.3 also shows that calls to the overloaded subtraction and multiplication operators were other expensive code paths. These simply call the appropriate `DirectXMath` function, and so calls to operators were replaced with direct calls to the `DirectXMath` function. For example,

```
XMVECTOR length = p1->getPosition() - p2->getPosition();
```

became

```
XMVECTOR length = XMVectorSubtract(p1->getPosition(), p2->getPosition());
```

Fig B.4 shows the the profiling results after these changes were added. The most expensive code paths now are all `DirectXMath` functions directly involved in calculating Equations 2.7 and 2.8.

Implementing both of these changes awarded performance gains of 40FPS for a debug build with a 50 by 50 mesh.

A final optimisation step was changing the accessors and mutators in `Particle` to return and pass by reference. This improved performance slightly, giving gains of roughly 5FPS.

3.3.1.1 Second Cycle

One optimisation was made to the initial design of cycle two.

The VerletIntegrator and ExplicitEulerIntegrator classes were made friend classes of Particle. This allows the integrators to access Particle's private member variables directly, removing the overhead of having to call accessors. This change resulted in small performance increases for both integrators, reducing overall update time by approximately 0.3ms, for a 50 by 50 mesh on a debug build, which translated to an increase of 3-4FPS. This increase was also enough to move from unstable to stable cloth when using Verlet integration.

Chapter 4

Test Plan

4.1 Test Data

To evaluate the hypotheses, a number of data fields will be captured from the simulation

- Simulation frame rate. This will be affected by the cost and frequency of the integration calculations and is essential to capture to determine if the simulation is running in real time
- Average time spent on integration calculations. Extracting this allows investigations into the affect of more expensive, but less frequent, integrators
- Time taken to reach the equilibrium point. The equilibrium point is defined as the point at which there is close to zero total force for all particles, i.e. the external and internal forces are balanced. Wang, Hu, and Zhuang (2009) have shown that using higher order Runge-Kutta integrators reduces the time taken to reach equilibrium and thus, extracting this data will allow comparisons with their results

In addition, the average time spent updating and rendering the cloth will also be extracted, in order to gain a better understanding of where the time each frame is spent.

The data mentioned above will be extracted by simulating the cloth in two different scenarios.

The first, or sheet, scenario will simulate a sheet hanging from a washing line. The top left and right particles of the cloth will be pinned, so as to be unaffected by any forces, and gravity applied as the sole external force. As a result, the simulation will evolve to an equilibrium, such as those show in Figures

2.4 and 2.7, so this scenarios can be used for measuring the time taken to reach the equilibrium point.

The second scenario will simulate a flag on a flag pole flapping in the wind. Particles on the left edge of the cloth will be pinned with gravity and a wind force, applied at pre-determined intervals, acting as external forces. Because of the wind, this scenario will not evolve to an equilibrium and so cannot be used to extract data about the time taken to reach equilibrium. However, the addition of wind will result in much more movement in the cloth so this scenario provides data on performance of a more active simulation.

4.2 Test Parameters

Mass-Spring models for cloth simulation have a number of different parameters which affect realism and performance, and are notoriously difficult to tune.

4.2.1 Mesh Size

This is the discretisation of the cloth, i.e. the number of particles used to represent the cloth, and is represented by two integers representing the number of rows and columns; the total number of particles in the cloth is therefore $rows \times columns$.

Increasing mesh size will result in a more realistic simulation but there will be direct impacts on performance as a result. Adding more particles adds more springs, and therefore more calculations are needed every frame to calculate the internal forces. Adding more particles also increases the number of integration calculations needed every time step and both of these factors combined will result in a performance hit for the simulation.

Several different mesh sizes will be used when evaluating the project hypotheses. Data will be extracted for each integrator at each mesh size. This will allow a comparison of the performance impact of the integrators when mesh size is varied.

4.2.2 Integrator Time Step

The time step will vary from integrator to integrator and must be set carefully in order to maintain the stability of the cloth.

Varying the time step will affect the performance of the simulation as it will vary the frequency with which the integration calculations must be performed.

For each integrator the maximum stable time step will be used along with a number of smaller time steps. This will allow a direct comparison of performance impact as time step decreases. For the explicit Euler method, the maximum stable time step is known; Vassilev, Spanlang, and Chrysanthou (2001, p. 2) found that explicit Euler is stable for time steps less than $0.4\pi\sqrt{\frac{m}{K}}$, where K is the maximum spring stiffness. For the other explicit integrators, the maximum time step value will be found by investigating the point at which they become unstable. For implicit Euler it is more difficult to define a maximum stable time step, as it is unconditionally stable regardless of time step. However, Volino and Magnenat-Thalmann (2001) have shown that as the time step increases the accuracy decreases and so an investigation will be carried out to find the maximum time step at which the simulation is still, subjectively, accurate.

4.2.3 Spring and Damping Coefficients

Varying the spring and damping coefficients of the springs will affect the realism of the simulation. If the stiffness is set too low, then the particle displacement will increase and may result in unrealistic deformations of the cloth. On the other hand, if the stiffness is set too high then this can lead to no displacement in the cloth at all. For damping, if it is set too low then the cloth will oscillate too much and appear too elastic, if set too high then the cloth will appear as if moving through a viscous fluid, such as oil.

Varying stiffness may also have an impact on the simulation's performance; increasing the stiffness may require the use of smaller time steps in order to maintain stability, depending on the chosen integrator.

4.2.4 Particle Mass

Since this project is not concerned with truly accurate cloth modelling, the particles' mass will be defined uniformly; that is, a total mass will be defined for the cloth and then divided by the number of particles to give the mass of an individual particle.

Varying the mass of the particles may have an impact on simulation performance. As a result of Equation 2.5, increasing the mass of a particle will increase its displacement due to gravity and therefore, the stiffness of the springs may need to be increased in order to maintain the realism of the simulation.

For both particle mass and spring and damping coefficients, investigations will be carried out for each mesh size to determine what values result in a, subjectively, realistic looking cloth.

4.3 Test Process

As the previous section details, the first stage of the testing process will be investigations into suitable values for the various test parameters. Following this, the test data detailed above will be extracted for each integrator with all combinations of test parameters in both the flag and sheet scenarios.

This, second, testing phase will be automated, using an XML file to detail the specific integrator and test parameters to use. The XML file will take the following form:

```
<test_list>
  <test>
    <integrator type=''...'' time_step=''...''/>
    <cloth_params height=''...'' width=''...'' mass=''...''>
      <top_left_position x=''...'' y=''...'' z=''...'' />
      <mesh_size rows=''...'' columns=''...'' />
      <structural spring_coefficient=''...'' damping_coefficient=''...'' />
      <shear spring_coefficient=''...'' damping_coefficient=''...'' />
      <flexion spring_coefficient=''...'' damping_coefficient=''...'' />
    </cloth_params>
  </test>
</test_list>
```

Each test element extracted from the test_list will be run in both the flag and sheet scenario.

Scenarios will be run for a maximum of one minute, and when the run is completed, the appropriate test data will be extracted and stored in a CSV file.

For the sheet scenario, a test run will end as soon as the equilibrium is reached, or after one minute, whichever occurs first. Whether or not the equilibrium was reached will be stored in the CSV. Some integrators, particularly lower order Runge-Kutta, may be unstable for certain mesh sizes and therefore will never arrive at an equilibrium. Extracting whether or not an integrator is stable with a particular time step and mesh size is essential as it can be used to contradict any performance justification for that integrator with those parameters.

Appendix A

Class Diagrams

A.1 First Cycle Design

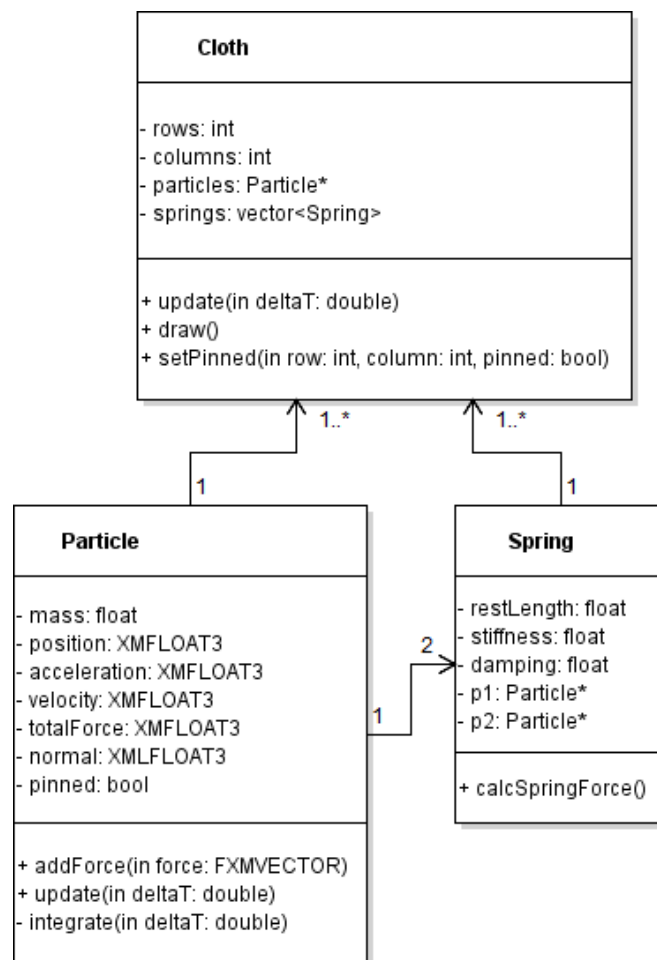


Figure A.1: Initial design for the first development cycle

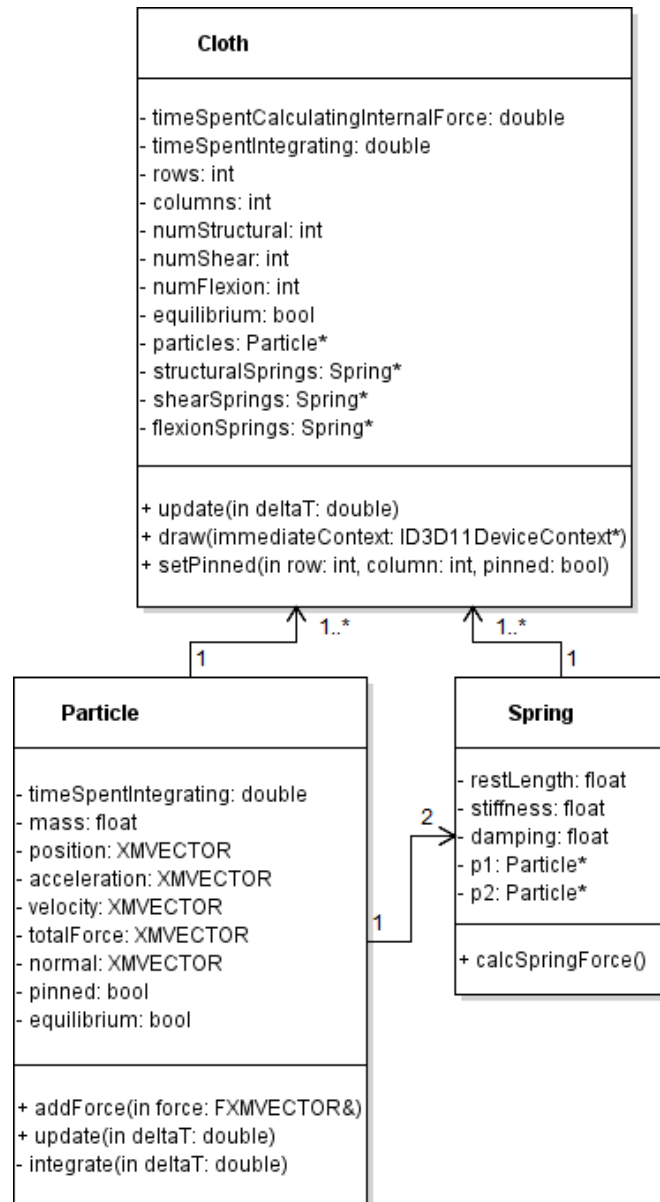


Figure A.2: Final design for the first development cycle

A.2 Second Cycle Design

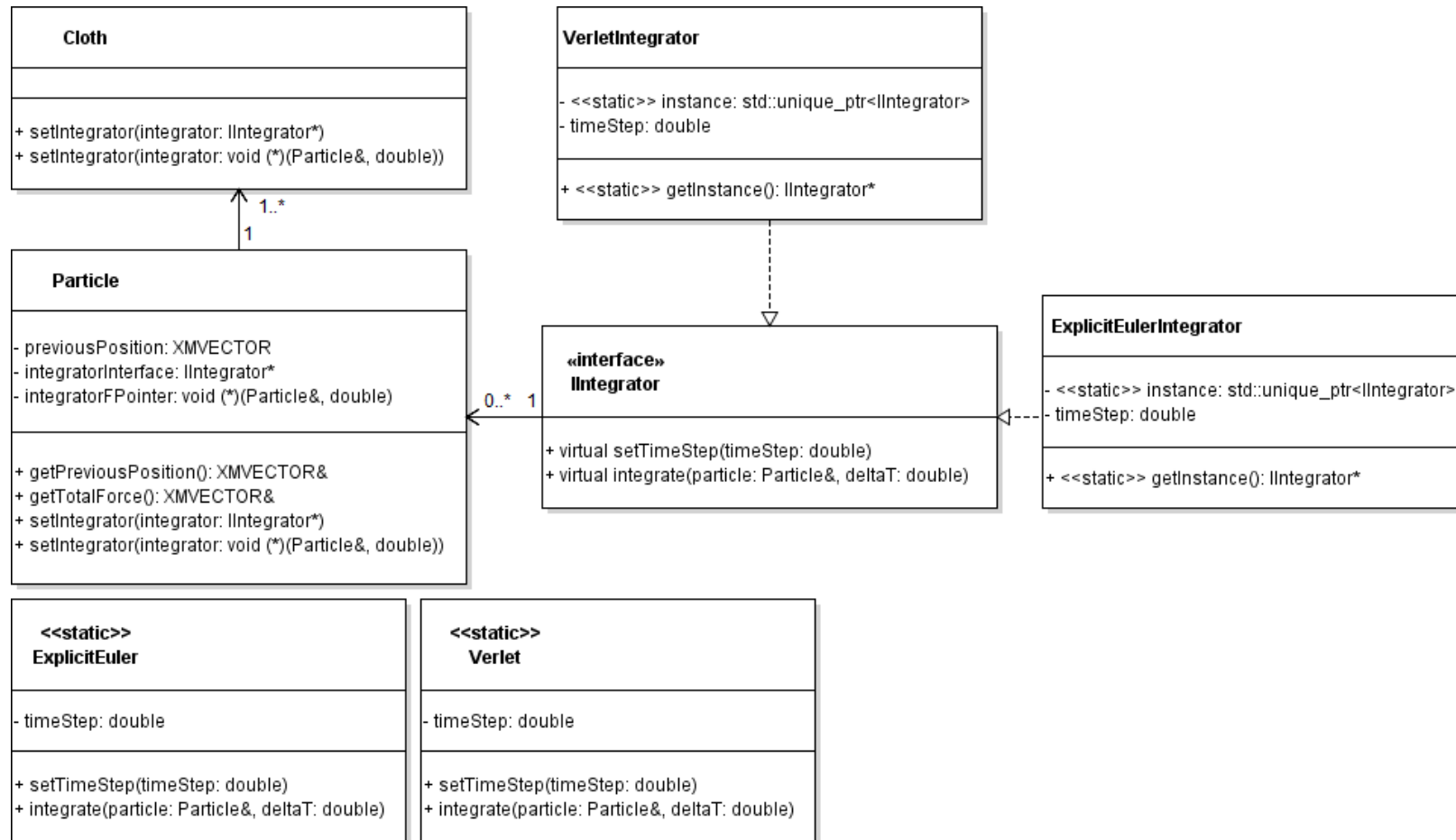


Figure A.3: Initial design for the second development cycle

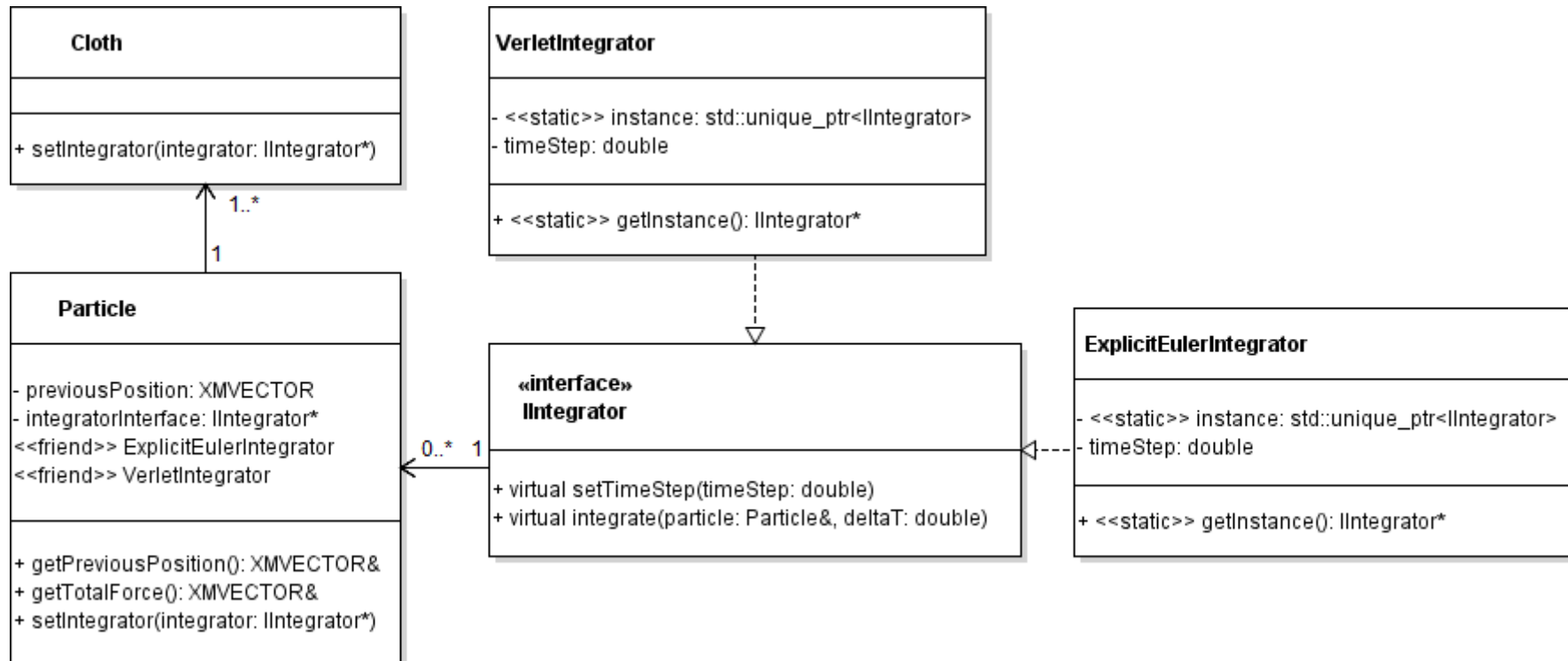


Figure A.4: Final design for the second development cycle

Appendix B

Profiling Results

B.1 First Cycle

Hot Path


| Function Name | Inclusive Samples % | Exclusive Samples % |
|---|---------------------|---------------------|
|  Cloth::update | 93.00 | 1.11 |
|  std::_Vector_const_iterator<std::_Vector_val<std::_Simple_types<Spring> > >::operator!= | 25.13 | 3.47 |
|  std::_Vector_iterator<std::_Vector_val<std::_Simple_types<Spring> > >::operator* | 22.37 | 3.92 |
|  std::_Vector_iterator<std::_Vector_val<std::_Simple_types<Spring> > >::operator++ | 17.06 | 3.65 |
|  Spring::calcSpringForce | 9.74 | 4.57 |

Figure B.1: Profiling results using an std::vector to store springs

Hot Path

| Function Name | Inclusive Samples % | Exclusive Samples % |
|---------------------------|---------------------|---------------------|
| ⚡ wWinMain | 99.12 | 0.00 |
| ⚡ Application::update | 96.81 | 1.91 |
| ⚡ Cloth::update | 77.81 | 2.23 |
| 🔥 Spring::calcSpringForce | 41.99 | 20.32 |
| 🔥 Particle::addForce | 17.71 | 3.88 |

Figure B.2: Profiling results using dynamic arrays to store springs

Hot Path

| Function Name | Inclusive Samples % | Exclusive Samples % |
|---------------------------|---------------------|---------------------|
| ⚡ Spring::calcSpringForce | 89.51 | 5.09 |
| 🔥 Particle::addForce | 23.05 | 5.12 |
| 🔥 DirectX::XMLoadFloat3 | 12.17 | 12.17 |
| 🔥 DirectX::operator- | 9.13 | 4.39 |
| 🔥 DirectX::operator* | 8.63 | 4.26 |


Related Views: [Call Tree](#) [Functions](#)

Functions Doing Most Individual Work

| Name | Exclusive Samples % |
|-------------------------|---------------------|
| DirectX::XMLoadFloat3 | 18.00 |
| DirectX::XMStoreFloat3 | 8.45 |
| Particle::addForce | 5.86 |
| DirectX::XMVectorAdd | 5.75 |
| Spring::calcSpringForce | 5.19 |

Figure B.3: Profiling results for unoptimised calcSpringForce

Hot Path

| Function Name | Inclusive Samples % | Exclusive Samples % |
|---|---------------------|---------------------|
|  DirectX::XMVectorScale | 8.88 | 8.88 |
|  DirectX::XMVectorSubtract | 7.28 | 7.28 |
|  DirectX::XMVector3Length | 6.53 | 6.53 |
|  DirectX::XMVector3Dot | 4.80 | 4.80 |
|  Particle::getPosition | 4.77 | 4.77 |

Related Views: [Call Tree](#) [Functions](#)

Functions Doing Most Individual Work

| Name | Exclusive Samples % |
|---|---------------------|
| DirectX::XMVectorScale | 11.54 |
| DirectX::XMVectorAdd | 9.86 |
| Spring::calcSpringForce | 9.74 |
| DirectX::XMVectorSubtract | 7.64 |
| Particle::addForce | 6.87 |

Figure B.4: Profiling results for optimised calcSpringForce

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