

## 1. Mathematics

### Toss Up: Multiple Choice

What is the y-intercept in the equation  $y = 4x + 3 - 2$

- W) 3
- X) 1
- Y) -2
- Z) 2

Toss Up Answer: X

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### Bonus: Multiple Choice

If  $3x - y = 12$ , what is  $(8^x) / (2^y)$

- W)  $2^{12}$
- X)  $4^4$
- Y)  $8^3$
- Z) Cannot be determined

Bonus Answer: W

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## 2. Mathematics

### Toss Up: Short Answer

What is the volume of a sphere of radius "R"?

Toss Up Answer:  $(4/3)\pi R^3$

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### Bonus: Short Answer

What is the degree of a vertex in a complete graph  $K_n$  ( $K$  sub  $n$ )?

Bonus Answer: (0,0) ; the origin

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## 3. Mathematics

### Toss Up: Short Answer

In a normal distribution, approximately what percentage of the sample, to the nearest whole number, falls within 4 standard deviations of the mean:

Toss Up Answer: 100%

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### Bonus: Multiple Choice

Which of the following properties would you use to compute the chances of rolling either a 7 or an 11 with a pair of dice:

- W) multiplicative
- X) conditional
- Y) independent
- Z) additive

Bonus Answer: Z

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## 4. Mathematics

### Toss Up: Multiple Choice

Give the range for the following six values 2, 7, 11, 19, 25, 33:

- W) 2

X) 31

Y) 33

Z) 15

**Toss Up Answer: X**

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**Bonus: Short Answer**

Convert  $6/5$  pi radians to degrees

**Bonus Answer: 216**

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## 5. Mathematics

**Toss Up: Multiple Choice**

Which of the following distances is longest?

W) Half a kilometer

X) Half a decimeter

Y) 600 meters

Z) 40 decameters

**Toss Up Answer: Y**

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**Bonus: Short Answer**

What is the name of a line that intersects two or more coplanar lines in different points?

**Bonus Answer: Transversal**

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## 6. Mathematics

**Toss Up: Short Answer**

If the log of  $n$  is 10, what is the log of  $100n$ ?

**Toss Up Answer: 12**

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**Bonus: Short Answer**

How many ways are there to seat 5 people around a circular table, if rotations are ignored?

**Bonus Answer: 24**

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## 7. Mathematics

**Toss Up: Short Answer**

How many vertices does a dodecahedron have?

**Toss Up Answer: 20**

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**Bonus: Short Answer**

In  $a+bi$  form, what is the square root of  $i$  (give the answer with positive imaginary part)?

**Bonus Answer:  $(1/(\sqrt{2})) + (1/(\sqrt{2}))i$**

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## 8. Mathematics

**Toss Up: Short Answer**

What is 11 base 5 in base 2?

**Toss Up Answer: 110**

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**Bonus: Short Answer**

If log base 10 of  $x$  is 100, what is log base 100 of  $x$ ?

**Bonus Answer: 50**

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## 9. Mathematics

**Toss Up: Short Answer**

You are trying to give 5 apples to 3 friends. You can give any number of apples to each friend, including 0. How many ways are there to share the apples?

**Toss Up Answer: 56 (its 8C3)**

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**Bonus: Multiple Choice**

If a cubic function equals 0 at exactly two points, which of the following must be true?

- W) the function passes through the origin
- X) there is a double root
- Y) the function is even
- Z) one of the roots is imaginary

**Bonus Answer: X**

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**10. Mathematics****Toss Up: Short Answer**

What is the length of the longest diagonal of a unit cube?

**Toss Up Answer: root3**

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**Bonus: Short Answer**

What is the largest integer that cant be written as the sum of 3's and 4's?

**Bonus Answer: 5**

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**11. Mathematics****Toss Up: Multiple Choice**

If  $x + (1/x) = 2$ , find  $x^{128} + (1/x)^{128}$

- W) 256
- X) 128
- Y) 64
- Z) 2

**Toss Up Answer: Z**

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**Bonus: Short Answer**

Given the quadratic  $x^2 - 20x + 9$  and its roots  $p$  and  $q$ , find  $(1/p)^2 + (1/q)^2$

**Bonus Answer: 382/81**

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**12. Mathematics****Toss Up: Multiple Choice**

If the test scores of Mr. Coco's Calculus test are assumed to have a normal distribution, and if the mean test score was 91, what can be said about the median test score of that test?

- W) The median was lower than 91
- X) The median was higher than 91
- Y) The median was 91
- Z) The median cannot be determined

**Toss Up Answer: Y**

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**Bonus: Multiple Choice**

The z-score for Shantanu's physics test grade was found to be 0.375. If he scored a 94 on the test, and the standard deviation was 8, what was the mean test score on the physics test?

- W) 91  
X) 95  
Y) 92  
Z) 98

**Bonus Answer: W**

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### 13. Mathematics

**Toss Up: Short Answer**

What shape is the graph of  $y = x^2 + 1$

**Toss Up Answer: parabola**

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**Bonus: Short Answer**

What is the name of the curve that is one possible inverse of a parabola, its shape resembling a heart, and that also appears in the Mandelbrot set?

**Bonus Answer: cardioid**

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### 14. Mathematics

**Toss Up: Short Answer**

In simplest terms, find the value of the limit as  $x$  approaches 0 of  $(4^x - 2^x) / x$

**Toss Up Answer:  $\ln(2)$  (do not accept  $\ln(4) - \ln(2)$ )**

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**Bonus: Short Answer**

How many real solutions for  $x$  does the equation  $x = \ln(x) + 2$  have?

**Bonus Answer: 2**

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### 15. Mathematics

**Toss Up: Multiple Choice**

A right triangle has a hypotenuse of length 12. The altitude to the hypotenuse has a length of 8. What is the area of this triangle?

- W) 36  
X) 48  
Y) 60  
Z) The triangle is impossible to construct

**Toss Up Answer: Z**

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**Bonus: Short Answer**

Two REAL numbers  $x$  and  $y$  satisfy the system of equations:  $x + y = 12$ ;  $x^2 + y^2 = 64$ . Find the value of the product  $xy$ .

**Bonus Answer: The system has no solutions.**

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### 16. Mathematics

**Toss Up: Short Answer**

If  $n$  is a positive integer, what is the smallest value of  $n$  such that  $n! + 1$  is a perfect square?

**Toss Up Answer: 4**

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**Bonus: Short Answer**

If  $z_1 = 3 - 4i$  and  $z_2 = 7 + i$ , find the absolute value of  $z_1 z_2$  in simplest terms.

**Bonus Answer:  $25\sqrt{2}$**

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## 17. Mathematics

### Toss Up: Short Answer

What is the inverse of the 2x2 matrix (row 1: 6 10), (row 2: 3 5)?

**Toss Up Answer: The matrix has no inverse (b.c. determinant = 0).**

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### Bonus: Short Answer

The legs of an isosceles triangle have a length of 10, and the altitudes to the legs have a length of 6. In simplified radical form, what is the length of the altitude to the base of the triangle?

**Bonus Answer:  $3 \cdot \sqrt{10}$  (Do not accept  $\sqrt{90}$ )**

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## 18. Mathematics

### Toss Up: Multiple Choice

If  $\theta$  is an angle such that  $\sin(\theta) < 0$  and  $\cos(\theta) = 0$ , where in the coordinate plane is it located?

- W) Between the 2nd and 3rd quadrants
- X) Between the 3rd and 4th quadrants
- Y) Between the 1st and 4th quadrants
- Z) Between the 1st and 2nd quadrants

**Toss Up Answer: Y**

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### Bonus: Short Answer

What is the remainder of  $x^{10} + x + 1$  divided by  $(x-1)^2$ ?

**Bonus Answer:  $11x - 8$**

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## 19. Mathematics

### Toss Up: Multiple Choice

Which of the following cannot be the root of a polynomial with rational coefficients?

- W)  $5i + 6$
- X)  $\phi - 1/2$ , where  $\phi$  is the golden ratio
- Y)  $\sqrt{3+i}$
- Z)  $6 - \pi i$

**Toss Up Answer: Z**

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### Bonus: Short Answer

What is the name given to a number that is not a root of any non-zero polynomial equation with rational coefficients?

**Bonus Answer: Transcendental number (Accept transcendental)**

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## 20. Mathematics

### Toss Up: Multiple Choice

Fermat's Last Theorem conjectures that no three positive integers  $a, b$ , and  $c$  can satisfy the equation  $a^n + b^n = c^n$  for any integer value of  $n$  greater than 2. It went unproved for more than 300 years until it was finally proved in 1994 by a mathematician who received a substantial monetary prize only this year. What is the name of this mathematician?

- W) Grigori Perelman
- X) John Nash
- Y) Andrew Wiles
- Z) Terence Tao

**Toss Up Answer: Y**

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### Bonus: Short Answer

Prime numbers of the form  $2^n(2^n) + 1$ , where  $n$  is a non-negative integer, are known as this.

Bonus Answer: Fermat Primes

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## 21. Mathematics

Toss Up: Short Answer

Completely expand  $(x-2y)^3$

Toss Up Answer:  $x^3 - 6x^2y + 12xy^2 - 8y^3$

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Bonus: Short Answer

What is the sum of all the terms in the seventh row of Pascal's triangle?

Bonus Answer: 128

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## 22. Mathematics

Toss Up: Multiple Choice

Unknown to be algebraic or transcendental

W) Rational

X) Algebraic irrational

Y) Transcendental

Z) Impossible to tell

Toss Up Answer: Y

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Bonus: Short Answer

Let  $f(x) = ax^7 + bx^3 + cx - 5$ , where  $a, b$ , and  $c$  are real numbers. What is the value of  $f(7)$  if  $f(-7) = 8$ ?

Bonus Answer: -18

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## 23. Mathematics

Toss Up: Short Answer

What is the limit as  $x$  approaches 0 of  $x^x$ ?

Toss Up Answer: Does not exist. (NOT 1)

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Bonus: Short Answer

Let  $f(x)$  be a function with no real roots. If  $f(3) = 4$ , then in what quadrants can  $f(x)$  be in?

Bonus Answer: All four quadrants (b.c. there's no specification  $f$  has to be continuous)

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## 24. Mathematics

Toss Up: Multiple Choice

Let  $f$  be an odd function over the real numbers. What is the value of  $f$  at 0?

W) -1

X) 0

Y) 1

Z) There is not enough information to determine an answer

Toss Up Answer: Z

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Bonus: Multiple Choice

Which of the following is true?

W) An irrational number raised to an irrational power must have an irrational value.

X) For all positive number  $x$  and  $y$ ,  $x^{\ln(y)}$  is equal to  $y^{\ln(x)}$

Y) For all real numbers  $a, b, c, d$  with  $b$  and  $d$  being non-zero, if  $a/b > c/d$ , then  $a*d$  must be greater than  $b*c$

Z) There are more complex numbers than there are real numbers.

Bonus Answer: X

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## 25. Mathematics

Toss Up: Multiple Choice

What is the geometric mean of the roots of the polynomial  $2x^3 - 2x^2 - 228x - 432$

W) 4

X) 6

Y) 8

Z) 10

Toss Up Answer: X

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Bonus: Short Answer

The first term of an arithmetic sequence is  $x$ , and the  $x$ th term is  $x^2$ , for  $x$  not equal to 1. If the common difference is equal to 7, what is the 12th term of the sequence?

Bonus Answer: 84

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## 26. Mathematics

Toss Up: Multiple Choice

A point with coordinates (3,5) is rotated 90 degrees clockwise about the point (2,1) and is then reflected across the  $y$ -axis. What are the coordinates of the resulting image?

W) (-5,-3)

X) (-4,0)

Y) (-6,0)

Z) (-5,-1)

Toss Up Answer: Y

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Bonus: Multiple Choice

$AC=BD=(AB)(\sqrt{2})$  [AC equals BD equals AB times the square root of 2]

W) The circumcircle of ABC is centered at the midpoint of AC

X) The midlines of ABCD are perpendicular

Y) The perpendicular bisectors of AB and CD are the same line

Z) None of the above.

Bonus Answer: Z

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## 27. Mathematics

Toss Up: Short Answer

What is the 5th non-triangular number?

Toss Up Answer: 8

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Bonus: Short Answer

Name all the following that are true:

1. An icosahedron has 18 faces.

2. A regular hexahedron has 16 edges.

3. There are only nine regular polyhedra.

4. A regular octahedron has 4 times the volume of a regular tetrahedron with the same side length.

Bonus Answer: 2,4 (an icosahedron has 20 faces; a cube has 12 edges)

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## 28. Mathematics

**Toss Up: Short Answer**

What is the sum of the infinite geometric series whose first term is 1 and fourth term is  $1/64$ ?

**Toss Up Answer:  $4/3$**

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**Bonus: Multiple Choice**

What is the value of  $e$  to the  $(\pi \text{ times } i/2)$ ?

W)  $e^{-1}$

X) 1

Y) -1

Z)  $i$

**Bonus Answer: Z**

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**29. Mathematics****Toss Up: Short Answer**

What is the integral of  $\sec x \, dx$ ?

**Toss Up Answer:  $\ln(\sec x + \tan x) + C$**

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**Bonus: Multiple Choice**

Which of these functions cannot be integrated and represented with elementary functions?

W)  $(\sin^5 x) \cos^6 x \, dx$

X)  $e^x \sin x^3 \, dx$

Y)  $e^{(x^2)} \, dx$

Z)  $\tan x \sin x \, dx$

**Bonus Answer: Y**

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**30. Mathematics****Toss Up: Short Answer**

What is the relationship between the surface area and the volume of a solid?

**Toss Up Answer: The surface area is the derivative of the volume/ the volume is the integral of the surface area when the constant is 0**

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**Bonus: Multiple Choice**

When the inner diagonal of a cube is 7 times root 3 inches, what is the surface area of the cube?

W) 216 square inches

X) 294 square inches

Y) 343 square inches

Z) 512 square inches

**Bonus Answer: X**

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**31. Mathematics****Toss Up: Multiple Choice**

Given two attempts, what is the probability in a ratio of getting a multiple choice question correct, if there are 5 choices?

W) 1:3

X) 1:4

Y) 2:3

Z) 2:4



**Toss Up Answer: Y**

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**Bonus: Multiple Choice**

What percentage of data falls within 2 standard deviations of the mean, assuming a normal distribution?

- W) 34.10%
- X) 47.70%
- Y) 68.20%
- Z) 95.40%

**Bonus Answer: Z**

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**32. Mathematics**

**Toss Up: Short Answer**

What is the 3rd mersenne prime?

**Toss Up Answer: 31**

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**Bonus: Multiple Choice**

How many terms does the 15th integral of  $\sin x \, dx$  have?

- W) 1
- X) 2
- Y) 15
- Z) 16

**Bonus Answer: Z**

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**33. Mathematics**

**Toss Up: Multiple Choice**

What is the limit as  $x$  approaches 0 of  $x \times \ln x$ ?

- W) -1
- X) 1
- Y) 0
- Z) The limit does not exist.

**Toss Up Answer: Y**

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**Bonus: Short Answer**

What is the derivative of  $\operatorname{arcsec} x$ ?

**Bonus Answer:  $1/(x(x^2-1)^{.5})$**

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**34. Mathematics**

**Toss Up: Multiple Choice**

Which of these numbers are transcendental?

- W)  $i$
- X)  $\sqrt{2}$
- Y)  $e$  to the  $\pi i$
- Z)  $\pi$

**Toss Up Answer: Z**

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**Bonus: Short Answer**

What conic section does this equation create?  $25x^2 - 150x - 16y^2 - 128y + 481 = 0$

Bonus Answer: Two intersecting lines/ a degenerate hyperbola

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### 35. Mathematics

Toss Up: Short Answer

What is  $(1000! + 999!)/(998!)$ ?

Toss Up Answer: 999,999

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Bonus: Short Answer

What is the first number with 5 distinct prime factors?

Bonus Answer: 2,310

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### 36. Mathematics

Toss Up: Short Answer

What is the value of the quantity  $((\sin^4 x) + 2(\cos^2 x)(\sin^2 x) + (\cos^4 x))^2$ ?

Toss Up Answer: 1

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Bonus: Multiple Choice

Which of the following assumptions are made in chaos theory?

W) The initial parameters are unknown and the future is deterministic

X) The initial parameters are known and the future is deterministic

Y) The initial parameters are not all known and the future is randomly determined

Z) The initial parameters are all known and the future is randomly determined

Bonus Answer: X

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### 37. Mathematics

Toss Up: Multiple Choice

Given the equation of a conic section,  $y^2/16 - x^2/25 = 1$ , what is the length of the conjugate axis?

W) 16

X) 8

Y) 10

Z) 25

Toss Up Answer: Y

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Bonus: Multiple Choice

Compute  $\log(\text{base } 2) \text{ of } 2048^2$

W) 20

X) 22

Y) 24

Z) 26

Bonus Answer: X

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### 38. Mathematics

Toss Up: Short Answer

If Bruce can do a job in 3 hours, and Clark can do the same job in 4 hours, how long, in hours, will it take them to do the job if they work together? You may leave your answer as a fraction.

Toss Up Answer: 12/7

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**Bonus: Short Answer**

What is the eccentricity of an ellipse with  $a = 5$  and  $b = 4$ ?

**Bonus Answer:  $3/5$**

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**39. Mathematics**

**Toss Up: Short Answer**

Find the perimeter of a right triangle with legs 11 and 60.

**Toss Up Answer: 132**

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**Bonus: Short Answer**

In a 15-75-90 degrees right triangle with hypotenuse 4, what are the lengths of the shorter and longer leg, respectively? Exact answers please.

**Bonus Answer:  $\text{radical } 6 - \text{radical } 2, \text{radical } 6 + \text{radical } 2$**

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**40. Mathematics**

**Toss Up: Short Answer**

If the first term in an arithmetic sequence is 2 and the third term is 6, find the 10th term.

**Toss Up Answer: 20**

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**Bonus: Short Answer**

Compute the sum of the first 100 positive integers.

**Bonus Answer: 5050**

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**41. Mathematics**

**Toss Up: Multiple Choice**

1. What statistical average is most appropriate to use when the quantities being averaged when one or more of the quantities are not necessarily bounded?

W) Geometric mean

X) median

Y) Harmonic mean

Z) Arithmetic mean

**Toss Up Answer: Y**

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**Bonus: Short Answer**

You pick two cards at random without replacement from a standard, 52 card deck. Compute the probability

exactly one is a heart.

**Bonus Answer:  $13/34$**

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**42. Mathematics**

**Toss Up: Multiple Choice**

Which of the following expressions in  $x$  grows fastest?

W)  $3^x$  [3 to the  $x$ ]

X)  $10(3/2)^x$  [10 times three halves to the  $x$ ]

Y)  $x^2$  [ $x$  squared]

Z)  $2^{(2x)}$  [2 to the  $2x$ ]

**Toss Up Answer: Z**

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**Bonus: Short Answer**

Given  $504 = 2^3 \times 3^2 \times 7$  [504 equals 2 cubed times 3 squared times 7], compute the sum of the positive divisors of

**Bonus Answer: 1560**

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### 43. Mathematics

**Toss Up: Multiple Choice**

Simplify  $(\sin 15 \cos 75 - \cos 15 \sin 75) / (\cos 15 \cos 75 + \sin 15 \sin 75)$

W) negative square root of 3

X)  $1/2$

Y)  $-1/2$

Z) square root 6 minus square root 2 all over 2

**Toss Up Answer: W**

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**Bonus: Short Answer**

Compute  $(2 + 2\sqrt{3}i)^6$ . [2+2 times the square root of 3, i to the 6th power]

**Bonus Answer: 4096**

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### 44. Mathematics

**Toss Up: Multiple Choice**

Compute  $3C1 + 4C2 + 5C3 + 6C4 + 7C5$ . [3 choose 1 + 4 choose 2 + 5 choose 3 + 6 choose 4 + 7 choose 5]

W) 55

X) 336

Y) 240

Z) 56

**Toss Up Answer: W**

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**Bonus: Short Answer**

Compute the square root of 5476

**Bonus Answer: 74**

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### 45. Mathematics

**Toss Up: Short Answer**

Compute the dot product of the following vectors:

$\langle 2, 1, 3 \rangle$  and  $\langle 10, -1, -5 \rangle$

**Toss Up Answer: 4**

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**Bonus: Multiple Choice**

$(64 + 196 + 81)(49 + 256 + 49) > (56 + 224 + 63)^2$  [Read "the quantity 64+196+81 times the quantity 49+256+49 strictly greater than the quantity 56+224+63 squared] is most directly an example of what inequality?

W) Triangle inequality

X) Power Mean Inequality

Y) Cauchy-Schwarz inequality [COW-SHEE sch-WARTS]

Z) Jensen's inequality [YEN-SIN]

**Bonus Answer: Y**

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### 46. Mathematics

**Toss Up: Short Answer**

which of the following are true about the number and nature of the roots of the polynomial

$x^3 - 29x^2 + 229x$

- I. 0 is a root
- II. There must be a real, positive root
- III. There must be three real roots

**Toss Up Answer: I**

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**Bonus: Short Answer**

Solve the following linear system of equations in 3 variables:

$$2x + y + 4z = 9$$

$$-x + 2y + 5z = -11$$

$$5x + 3y + 3z = -4$$

**Bonus Answer:  $x=4, y=-11, z=3$**

**Also accept (4,-11,3)**

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## 47. Mathematics

**Toss Up: Multiple Choice**

To test products, there is a test that identifies 95% of defective products as defective, but also labels 10% of all working products as defective. If 85% of the products made are not defective, what probability of products the test determines to be defective are actually defective?

W) 39%

X) 84%

Y) 67%

Z) 42%

**Toss Up Answer: Y**

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**Bonus: Short Answer**

Compute the surface area of a cylinder with radius 8 and height 2

**Bonus Answer:  $160\pi$**

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## 48. Mathematics

**Toss Up: Short Answer**

Tim is 5 times older than his younger brother. In 3 years Tim will be 3 times older than his younger brother. Compute the difference in the ages of Tim and his younger brother.

**Toss Up Answer: 12**

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**Bonus: Short Answer**

How many positive integers  $n$  have no solutions to the following equation where  $a$  and  $b$  are nonnegative integers?

$$3a + 7b = n$$

**Bonus Answer: 6**

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## 49. Mathematics

**Toss Up: Multiple Choice**

Which of the following is not a group?

W) the integers under multiplication

X) the integers under addition

Y) the symmetries of a regular  $n$ -gon

Z) the permutations of integers between 1 and  $n$

**Toss Up Answer: W**

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**Bonus: Short Answer**

find the smallest positive solution to the following congruences.

$x \text{ congruent to } 3 \pmod{13}$

$x \text{ congruent to } 8 \pmod{11}$

**Bonus Answer:  $x=107$**

**Also accept: 107**

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## 50. Mathematics

**Toss Up: Multiple Choice**

What mathematician proved the existence of a straight edge and compass construction of a regular 17-gon?

W) Euler

X) Euclid

Y) Gauss

Z) Galois [Gal-wah]

**Toss Up Answer: Y**

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**Bonus: Short Answer**

Given  $\sin X = 1/3$  [sine of  $x$  equals one third], compute  $\cos^2(3X)$  [co-sine squared of three  $x$ ].

**Bonus Answer:  $-23/27$**

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## 51. Mathematics

**Toss Up: Multiple Choice**

MULTIPLE CHOICE: tossup

For an infinite sequence of numbers  $a_0, a_1, \dots$ , which of the following best describes the polynomial  $P(x) = \sum_{i=0}^{\infty} a_i x^i$ .

W) Reimann-Zeta function

X) Generating function

Y) Newtonian series

Z) Tchebychev polynomial

**Toss Up Answer: X**

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**Bonus: Short Answer**

In the Pell equation  $x^2 - 3y^2 = 1$  the smallest solution is  $x=2$  and  $y=1$ . The next smallest solution is  $x=7$  and  $y=4$ . Compute the third smallest solution.

**Bonus Answer:  $x=26, y=15$**

**Also accept (26,15)**

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## 52. Mathematics

**Toss Up: Short Answer**

Which of the following statements concerning prime numbers are true?

1. If  $a$  and  $n$  are relatively prime then there are infinitely many primes that leave a remainder of  $a$  when divided by  $n$ .
2. All integers less than  $p$  are quadratic residues modulo  $p$
3. There are infinitely many prime numbers

**Toss Up Answer: 1 and 3**

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**Bonus: Short Answer**

If  $a_1+a_2+a_3+a_4+a_5=17$  for positive integers  $a_1, a_2, a_3, a_4, a_5$ , then maximize the product  $a_1a_2a_3a_4a_5$ ?

**Bonus Answer: 432**

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### 53. Mathematics

**Toss Up: Short Answer**

Which of the following transformations is a wallpaper group

1 Rotation by 90 degrees

2 Glide Reflection

3 Dilation

4 Reflection

**Toss Up Answer: 1,2, and 4**

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**Bonus: Short Answer**

In a circle O, diameter AB is drawn. Chord CD intersects AB at E.

If  $CE=3$ ,  $DE=6$ ,  $AE=x$ , and  $BE=x+4$ , compute the radius of the circle.

**Bonus Answer:  $\sqrt{22}$**

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### 54. Mathematics

**Toss Up: Short Answer**

In Triangle ABC the angle bisector of A intersects BC at D. Given  $AB=9$ ,  $AC=21$ , and  $DB=15$ , compute DC.

**Toss Up Answer: 35**

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**Bonus: Short Answer**

In triangle ABC,  $AB=14$ ,  $AC=13$ , and  $BC=15$ . Let the incenter be I. Compute CI in simplest radical form.

**Bonus Answer: square root of 65**

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