


Two-step multi-spectral registration via key-point detector and gradient similarity. Application to agronomic scenes for proxy-sensing

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Abstract:

The potential of multi-spectral images is growing rapidly in precision agriculture, and is currently based on the use of multi-sensor cameras. However, their development usually concerns aerial applications and their parameters are optimized for high altitudes acquisition by drone (UAV \approx 50 meters) to ensure surface coverage and reduce technical problems. With the recent emergence of terrestrial robots (UGV), their use is diverted for nearby agronomic applications. Making it possible to explore new agronomic applications, maximizing specific traits extraction (spectral index, shape, texture ...) which requires high spatial resolution.

The problem with these cameras is that all sensors are not aligned and the manufacturers' methods are not suitable for close-field acquisition, resulting in offsets between spectral images and degrading the quality of extractable informations. We therefore need a solution to accurately align the different images in such condition. The objective of this article is to describe and evaluate a method that allows to define the ideal conditions for matching multi-spectral images from a multi-sensor camera at low heights in agronomic scenes.


In this study we propose a two-steps method applied to the six-bands Airphen multi-sensor camera with (i) affine correction using pre-calibrated matrix at different heights, the closest transformation can be selected via internal GPS and (ii) perspective correction to refine the previous one, using key-points matching between enhanced gradients of each spectral bands. Nine types of key-point detection algorithms (ORB, GFTT, AGAST, FAST, AKAZE, KAZE, BRISK, SURF, MSER) with three different modalities of parameters were evaluated on their speed and performances, we also defined the best reference spectra on each of them.


The results show that GFTT is the most suitable methods for key-point extraction using our enhanced gradients, and the best spectral reference was identified to be the band centered on 570 nm for this one. Without any treatment the initial error is about 62 px, with our method, the remaining residual error is less than 1 px, where the manufacturer's involves distortions and loss of information with an estimated residual error of approximately 12 px.


1 INTRODUCTION

Modern agriculture is changing towards a system that is less dependent on pesticides [1] (herbicides remain the most difficult pesticides to reduce) and digital tools are of great help in this matter. The development of imaging and image processing have made it possible to characterize

an agricultural plot [2] (crop health status or soil characteristics) using non-destructive agronomic indices [3] replacing traditional destructive and time-consuming methods. In recent years, the arrival of miniaturized multi-spectral and hyper-spectral cameras on Unmanned Aerial Vehicles (UAVs) has allowed spatio-temporal field monitoring. These vision systems have been developed for precise working conditions (flight height 50 m). Although, very practical to use, they are also used for proxy-sensing applications. However, the algorithms offered by manufactur-

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ers to co-register multiple single-band images at different spectral range, are not optimal for low heights. It thus requires a specific close-field image registration.

Image registration is the process of transforming different images of one scene into the same coordinate system. The spatial relationships between these images can be rigid (translations and rotations), affine (shears for example), homographic, or complex large deformation models (due to the difference of depth between ground and leafs) [4]. The main difficulty is that multi-spectral cameras have low spectral coverage between bands, resulting in a loss of characteristics between them. Which is caused by (i) plant leaves have different aspect depending on the spectral bands (ii) there are highly complex and self-similar structures in our images [5]. It therefore affects the process of detecting common characteristics between bands for image registration. There are two types of registration, feature based and intensity based [6]. Feature based methods works by extracting point of interest and use feature matching, in most cases a brute-force matching is used, making those techniques slow. Fortunately these features can be filtered on the spatial properties to reduce the matching cost. A GPGPU implementation can also reduce the comparisons cost. Intensity-based automatic image registration is an iterative process, and the metrics used are sensitive to determine the numbers of iteration, making such method computationally expensive for precise registration. Furthermore multi-spectral implies different metrics for each registered bands which is hard to achieve.

Different studies of images alignment using multi-sensors camera can be found for acquisition using UAV at medium (50 – 200 m) and high (200 – 1000 m) distance. Some show good performances (in term of number of key-points) of feature based [7] with strong enhancement of feature descriptor for matching performances. Other prefer to use intensity based registration [5] on better convergence metrics [8] (in term of correlation), which is slower and not necessarily robust against light variability and their optimization can also fall into a local minimum, resulting in a non-optimal registration [9].

Traditional approach to multi-spectral image registration is to designate one channel as the

target channel and register all the others on the selected one. Currently, only [7] show a method for selecting the best reference, but there is no study who as defined the best spectral reference in agronomic scene. In all cases NIR (850 nm) or middle range spectral reference are conventionally used without studying the others on precision agriculture. In addition those studies mainly propose features matching without large methods comparison [7](less than 4) of their performance (time/precision), without showing the importance of the spectral reference and the interest of normalized gradients transformation (like in Intensity-based methods).

However, despite the growing use of UGVs and multi-spectral imaging, the domain is not very well sourced, and no study has been found under agricultural and external conditions in near field of view (less than 10 meter) for multi-spectral registration.

Thus, this study propose a benchmark of popular feature extractors inside normalized gradients transformation and the best spectral reference was defined for each of them. Moreover a pre-affine registration is used to filter the feature matching, evaluated at different spatial resolutions. So this study shows the importance of the selection of the reference and the features extractor on normalized gradients in such registration.

The results of this study show that GFTT has the best overall performances in both computation time and accuracy in all modalities. Additionally the 570 nm is the best reference for GFTT and 710 nm for most of the others. At the lower height (1.6 m) we have an initial error of ≈ 62 px, the manufacturer’s methods show an error of ≈ 12 px when our methods has < 1 px of error.

2 MATERIAL AND METHOD

2.1 Material

2.1.1 Camera

The multi-spectral imagery is provided by the six-band multi-spectral camera Airphen developed by HiPhen. Airphen is a scientific multi-spectral camera developed by agronomists

for agricultural applications. It can be embedded in different types of platforms such as UAV, phenotyping robots, etc.

Airphen is highly configurable (bands, fields of view), lightweight and compact. The camera was configured using interferential filter centered at 450/570/675/710/730/850 nm with FWHM¹ of 10 nm, the position of each band is referenced on figure 1. The focal lens is 8 mm for all wavelength. The raw resolution for each spectral band is 1280×960 px with 12 bit of precision. Finally the camera also provides an internal GPS antenna that can be used to get the distance from the ground.



Figure 1: Disposition of each band on the Airphen multi-sensors camera

2.1.2 Datasets

Two datasets were taken at different heights with images of a chessboard (use for calibration) and of an agronomic scene. We used a metallic gantry for positioning the camera at different heights. The size of the gantry is $3 \times 5 \times 4$ m. Due to the size of the chessboard (57×57 cm with 14×14 square of 4 cm), the limited focus of the camera and the gantry height, we have bounded the acquisition heights from 1.6 to 5 m with 20 cm steps, which represents 18 acquisitions.

The first dataset is for the calibration. A chessboard is taken at different heights. The second one is for the alignment verification under real conditions. One shot of an agronomic scene is taken at different heights with a maximum bias set at 10 cm.

2.2 Methods

Alignment is refined in two stages, with (i) affine registration approximately estimated and (ii) perspective registration for the refinement and precision. As example the figure 2 shows each correction step, where the first line is for the (i) affine

correction (section 2.2.1), the second is for (ii) perspective correction. More precisely the second step is per-channel pre-processed where feature detectors are used to detect key-points (section 2.2.2). Each channel key-points are associated to compute the perspective correction through homography, to the chosen spectral band (section 2.2.2). These steps are explained on specific sub-sections.

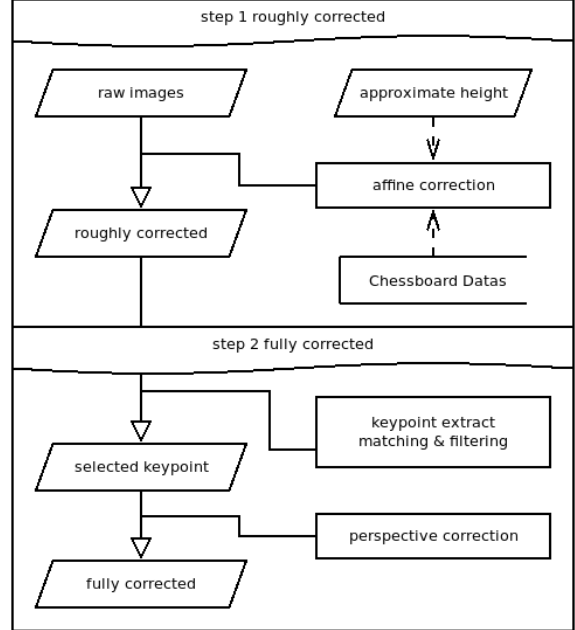


Figure 2: Each step of the alignment procedure, with (step 1) roughly corrected from affine correction and (step 2) enhancement via key-points and perspective

2.2.1 Affine Correction

We make the assumption that closer we take the snapshot, the bigger the distance between each spectral band is. On the other hand, at a distance superior or equals to 5 m, the initial affine correction become stable. A calibration is used to build a linear model based on that assumption, which will allow the affine correction to work at any height. The main purpose of this step is to reduce the offset between each spectral band, which allows the similarity between key-points to be spatially delimited within a few pixels, making feature matching more effective.

Calibration : Based on that previous assumption a calibration is run over the chessboard dataset. We detect the chessboard using the opencv calibration toolbox [10] on each spec-

¹Full Width at Half Maximum

tral image (normalized by $I = (I - \min(I)) / \max(I)$ where I is the spectral image) at different heights (from 1.6 m to 5 m). We use the function `findChessboardCorners` how attempts to determine whether the input image is a view of the chessboard pattern and locate the internal chessboard corners. The detected coordinates are roughly approximated. To determine their positions accurately we use the function `cornerSubPix` as explained in the documentation ².

Linear model : Using all the points detected for each spectral band, we calculate the centroid grid (each point average). The affine transform from each spectral band to this centroid grid is estimated. Theoretically, the rotation and the scale (A, B, C, D) do not depend on the distance to the ground, but the translation (X, Y) does. Thus a Levenberg-Marquardt curve fitting algorithm with linear least squares regression [11] can be used to fit an equation for each spectral band against X and Y independently to the centroid grid. We adjust the following curve $t = \alpha h^3 + \beta h^2 + \theta h + \gamma$ where h is the height, t is the resulted translation and factors $\alpha, \beta, \theta, \gamma$ are the model parameters.

Correction : Based on the model estimated on the chessboard dataset, we transpose them to the agronomic dataset. To make the affine matrix correction, we used the rotation and scale factors at the most accurate height (1.6 m where the spatial resolution of the chessboard is higher), because it does not theoretically depend on the height. For the translation part, the curve model is applied for each spectral band at the given height provided by the user. Each spectral band is warped using the corresponding affine transformation. Finally, all spectral bands are cropped to the minimal bounding box (minimal and maximal translation of each affine matrix). This first correction is an approximation. It provides some spatial properties that we will use on the second stage.

2.2.2 Perspective correction

Each spectral band has different properties and values by nature but we can extract the corresponding similarity by transforming each spectral

band into its absolute derivative, to find similarities in gradient break among them. As we can see in figure 3 gradients can have opposite direction depending on the spectral bands, making the absolute derivative an important step for matching between different spectral band.

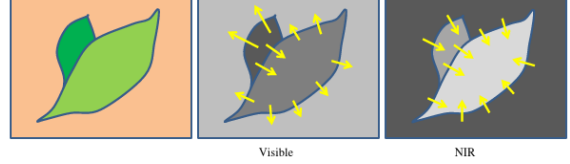


Figure 3: Gradient orientation in spectral band [12]. Orientation of the gradient is not the same depending to the spectral band.

The affine correction attempts to help the feature matching by adding properties of epipolar lines (close). Thus, the matching of extracted features can be spatially bounded, (i) we know that the maximum translation is limited to a distance of a few pixels (less than 10px thanks to affine correction), and (ii) the angle between the initial element and the matched one is limited to $[-1, 1]$ degree.

Computing the gradient : To compute the gradient of the image with a minimal impact of the light distribution (shadow, reflectance, specular, ...), each spectral band is normalized using Gaussian blur [13], the kernel size is defined by $\text{next_odd}(\text{image_width}^{0.4})$ (19 in our case) and the final normalized images are defined by $I / (G + 1) * 255$ where I is the spectral band and G is the Gaussian blur of those spectral bands. This first step minimizes the impact of the noise on the gradient and smooth the signal in case of high reflectance. Using this normalized image, the gradient $I_{grad}(x, y)$ is computed with the sum of absolute Sharr filter [14] for horizontal S_x and vertical S_y derivative, noted $I_{grad}(x, y) = \frac{1}{2}|S_x| + \frac{1}{2}|S_y|$. Finally, all gradients $I_{grad}(x, y)$ are normalized using CLAHE [15] to locally improve their intensity and increase the number of key-points detected.

Key-points Extractor : A key-point is a point of interest. It defines what is important and distinctive in an image. Different types of key-point extractors are available and the following are tested :

(ORB) Oriented FAST and Rotated BRIEF [16], (AKAZE) Fast explicit diffusion for accelerated features in nonlinear scale spaces [17],

²https://docs.opencv.org/2.4/modules/calib3d/doc/camera_calibration_and_3d_reconstruction.html

(KAZE) A novel multi-scale 2D feature detection and description algorithm in nonlinear scale spaces [18], (BRISK) Binary robust invariant scalable key-points [19], (AGAST) Adaptive and generic corner detection based on the accelerated segment test [20], (MSER) maximally stable extremal regions [21], (SURF) Speed-Up Robust Features [22], (FAST) FAST Algorithm for Corner Detection [23] and (GFTT) Good Features To Track [24].

These algorithms are largely described across multiple studies [7, 25, 26, 27], they are all available and easily usable in OpenCV. Thus we have studied them by varying the most influential parameters for each of them with three modalities, the table 1 in appendix shows all modalities and methods.

Key-point detection : We use one of the key-point extractors mentioned above between each spectral band gradients (all extractors are evaluated). For each detected key-point, we extract a descriptor using ORB features. We match all detected key-points to a reference spectral band (all bands are evaluated). All matches are filtered by distance, position and angle, to eliminate a majority of false positives along the epipolar line. Finally we use the function findHomography between the key-points detected/filtered with RANSAC [28], to determine the best subset of matches to calculate the perspective correction.

Correction : The perspective correction between each spectral band to the reference is estimated and applied. Finally, all spectral bands are cropped to the minimum bounding box, the minimum and maximum points are obtained by applying a perspective transformation to each corner of the image.

3 RESULTS AND DISCUSSION

Firstly the results will focus on affine corrections and then on the effects of the perspective correction. Figure 4 shows a closeup inside at 1.6 m (4a) raw images acquisition, (4c & 4d) registred image of each correction steps and (4b) the manufacturer results.

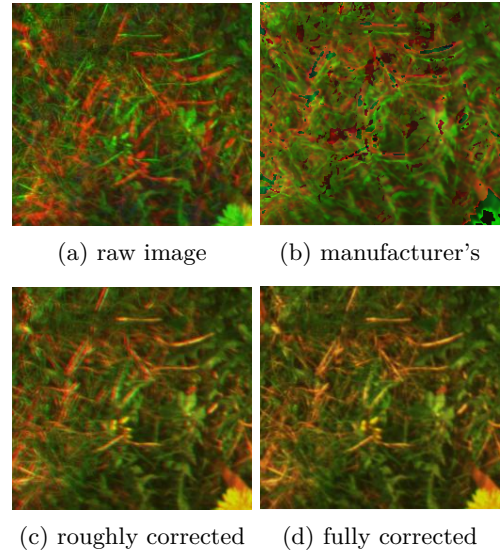


Figure 4: Example of each correction and the manufacturer's results

3.1 Affine correction

The affine correction model is based on the calibration dataset (where the chessboard are acquired). The 6 coefficients (A, B, C, D, X, Y) of the affine matrix were studied according to the height of the camera in order to see their stability. It appears that the translation part (X, Y), depends on the distance to the field (appendix figure 5) according to the initial assumption. On this part the linear model is used to estimate the affine correction from an approximated height.

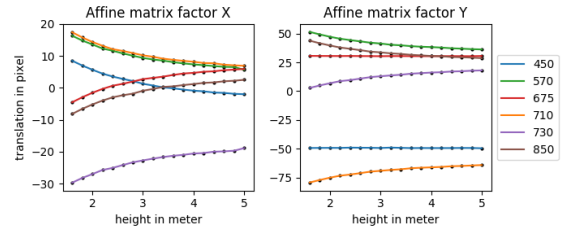


Figure 5: Affine matrix value by height

Rotation and scale do not depend on the ground distance (figure 6) according to the theory. These factors (A, B, C, D) are quite stable and close to identity, as expected (accuracy depends on the spatial resolution of the board). As result, single calibration can be used for this part of the matrix, and the most accurate are used (i.e where the chessboard has the best spatial resolution).

After the affine correction, the remaining residual distances have been extracted, it is computed using the detected, filtered and matched

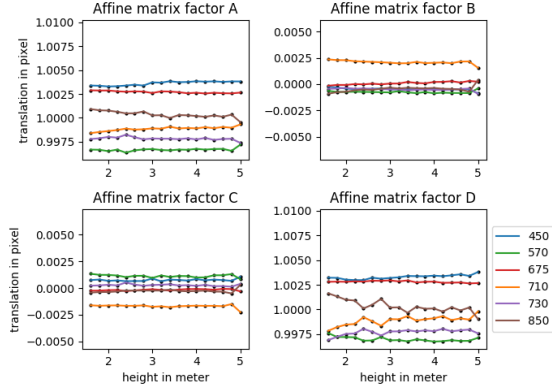


Figure 6: Affine matrix value by height

key-point to the reference spectral band, figure 9 (up) shows an example using 570 nm as reference before the perspective correction. The remaining distance between each spectral band to the reference varies according to the distance between the real height and the nearest selected (through linear model). Remember that a bias of $\pm 10\text{cm}$ was initially set to show the error in the worst case, so the difference of errors between each of them are due to the difference of sensors position in the array to the reference and the provided approximate height.

3.2 Perspective correction

The figures 7 shows the numbers of key-points after filtering and homographic association (minimum of all matches) as well as the computation time and performance ratio (matches/time) for each method. The performance ratio is used to compare methods between them, bigger he is, greater is the method (balanced between time and accuracy), making lower of them unsuitable.

All these methods offer interesting results, the choice of method depends on application needs between computation time and accuracy, three methods stand out in all of there modality:

- GFTT shows the best overall performance in both computation time and number of matches
- FAST and AGAST1 are quite suitable too, with acceptable computation time and greater matches performances.

The other ones did not show improvement in term of time or matches (especially compared to GFTT), some of them show a small number of matches which can be too small to ensure the

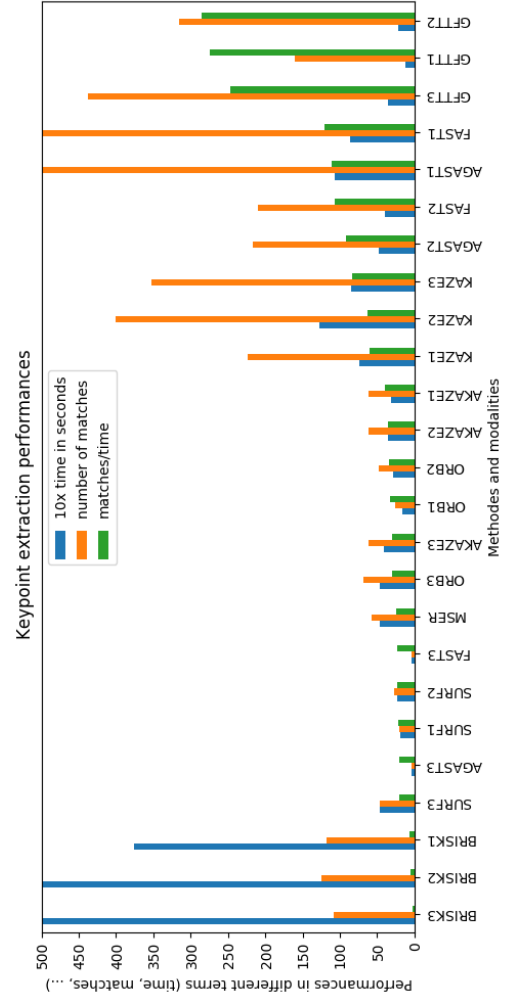


Figure 7: features extractor performances after filtering and homography association

precision. Increasing the number of key-points matched allows a slightly higher accuracy [7]. For example, switching from SURF (30 results) to FAST (130 results) reduces the final residual distances from ≈ 1.2 to ≈ 0.9 px but increases the calculation time from ≈ 5 to ≈ 8 seconds.

All methods show that the best spectral band is 710 nm (in red), with an exception for SURF and GFTT which is 570 nm. The figure 8 shows the minimum number of matches between each reference spectrum and all the others, for each relevant methods and modalities (KAZE, AGAST, FAST GFTT). Choosing the right spectral reference is important, as we can see, no correspondence is found in some cases between 675-850 nm, but correspondences are found between 675-710

nm and 710-850 nm, making the 710 nm more appropriate, the same behavior can be observed for the other bands and 570 nm as the more appropriate one. This is visible on the figure for all methods, 570 nm and 710 nm have the best minimum number of matches where all the other are quite small.

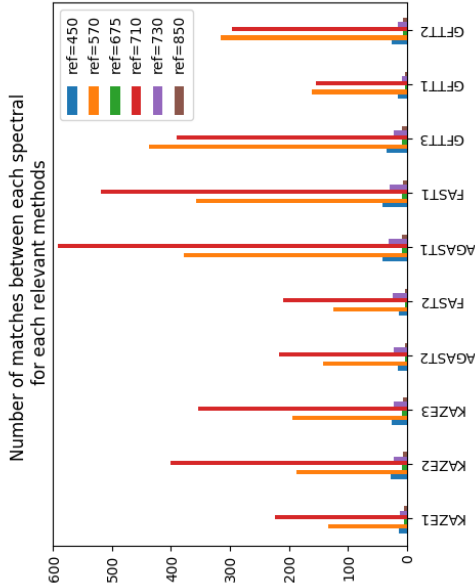


Figure 8: key-point extractor performances

Residues of the perspective correction show that we have correctly registered each spectral band, the figure 9 (down) shows the residual distance at different ground distances. In comparison the affine correction error are between $[1.0 - 4.8]$ px where the combination of affine and perspective correction the residual error are between $[0.7 - 1.0]$ px. On average the perspective correction enhance the residual error by $(3.5 - 0.9)/3.5 \approx 74\%$.

3.3 General discussion

Even if the relief of the scene is not taken into account due to the used deformation model, in our case, with flat ground, no difference arise. However, more complex deformation models [29] could be used to improve the remaining error. But could also, in some case, create large angular deformations caused by the proximity of key-points, of course, it's possible to filter these key-points, which would also reduce the overall accuracy.

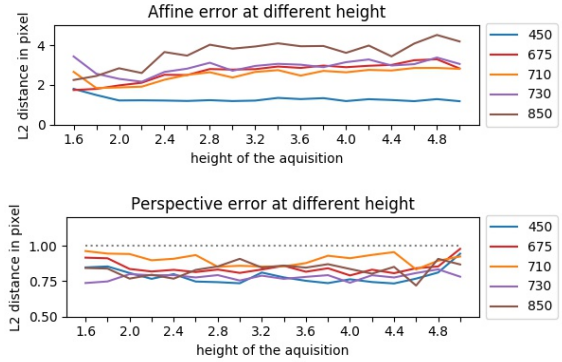


Figure 9: (up) The mean distance of detected key-point before perspective correction with 570 nm as spectral reference (down) Perspective re-projection error with GFTT using the first modality and 570 nm as reference

Further research can be performed on each parameter of the feature extractors, for those who need specific performance (time/precision), we invite anyone to download the dataset and test various combinations. Otherwise feature matching can be optimized, at this stage, we use brute-force matching with post filtering, but a different implementation that fulfill our spatial properties should greatly enhance the number of matches by reducing false positives.

4 CONCLUSION

In this work, the application of different techniques for multi-spectral image registration was explored using the Airphen camera. We have tested nine type of key-points extractor (ORB, GFTT, AGAST, FAST, AKAZE, KAZE, BRISK, SURF, MSER) at different heights and the number of control points obtained. As seen in the method, the most suitable method is the GFTT (regardless of modalities 1, 2 or 3) with a significant number of matches 150 – 450 and a reasonable calculation time 1.17 s to 3.55 s depending on the modality.

Furthermore, the best spectral reference was defined for each method, for example 570 nm for GFTT. We have observed a residual error of less than 1 px, supposedly caused by the difference of sensors nature (spectral range, lens).

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REFERENCES

- [1] Martin Lechenet, Vincent Bretagnolle, Christian Bockstaller, François Boissinot, Marie-Sophie Petit, Sandrine Petit, and Nicolas M. Munier-Jolain. Reconciling pesticide reduction with economic and environmental sustainability in arable farming. *PLOS ONE*, 9(6):1–10, 06 2014.
- [2] Sindhuja Sankaran, Lav R. Khot, Carlos Zúñiga Espinoza, Sanaz Jarolmasjed, Vidyasagar R. Sathuvalli, George J. Vandemark, Phillip N. Miklas, Arron H. Carter, Michael O. Pumphrey, N. Richard Knowles, and Mark J. Pavék. Low-altitude, high-resolution aerial imaging systems for row and field crop phenotyping: A review. *European Journal of Agronomy*, 70:112 – 123, 2015.
- [3] A. Bannari, D. Morin, F. Bonn, and A. R. Huete. A review of vegetation indices. *Remote Sensing Reviews*, 13(1-2):95–120, 1995.
- [4] Emna Kamoun. Image registration: From sift to deep learning. july 2019.
- [5] Clément Douarre, Carlos F Crispim-Junior, Anthony Gelibert, Laure Tougne, and David Rousseau. A strategy for multimodal canopy images registration. In 7th International Workshop on Image Analysis Methods in the Plant Sciences, Lyon, France, July 2019.
- [6] Barbara Zitová and Jan Flusser. Image registration methods: A survey. *Image and Vision Computing*, 21:977–1000, 10 2003.
- [7] Jocival Dantas Dias Junior, Andre Backes, and Mauricio Escarpinati. Detection of control points for uav-multispectral sensed data registration through the combining of feature descriptors. pages 444–451, 01 2019.
- [8] S. Chen, H. Shen, C. Li, and J. H. Xin. Normalized total gradient: A new measure for multispectral image registration. *IEEE Transactions on Image Processing*, 27(3):1297–1310, March 2018.
- [9] Jean-Baptiste Vioix. Conception et réalisation d’un dispositif d’imagerie multispectrale embarqué : du capteur aux traitements pour la détection d’adventices. 2004.
- [10] Jean-Yves Bouguet. Camera calibration toolbox for matlab. 2001.
- [11] Jorge J. Moré. The levenberg-marquardt algorithm: Implementation and theory. In G.A. Watson, editor, *Numerical Analysis*, volume 630 of *Lecture Notes in Mathematics*, pages 105–116. Springer Berlin Heidelberg, 1978.
- [12] G. Rabatel and S. Labbe. Registration of visible and near infrared unmanned aerialvehicle images based on Fourier-Mellin transform. *Precision Agriculture*, 17(5):564–587, 2016.
- [13] D. Sage and M. Unser. Teaching image-processing programming in java. *IEEE Signal Processing Magazine*, 20(6):43–52, November 2003. Using “Student-Friendly” ImageJ as a Pedagogical Tool.
- [14] Hanna Seitz. Contributions to the minimum linear arrangement problem, 2010.
- [15] Karel Zuiderveld. Contrast limited adaptive histogram equalization. In *Graphics gems IV*, pages 474–485. Academic Press Professional, Inc., 1994.
- [16] Ethan Rublee, Vincent Rabaud, Kurt Konolige, and Gary Bradski. Orb: An efficient alternative to sift or surf. In *Proceedings of the 2011 International Conference on Computer Vision, ICCV ’11*, pages 2564–2571, Washington, DC, USA, 2011. IEEE Computer Society.
- [17] Pablo F Alcantarilla and T Solutions. Fast explicit diffusion for accelerated features in nonlinear scale spaces. *IEEE Trans. Patt. Anal. Mach. Intell*, 34(7):1281–1298, 2011.
- [18] Alvaro Ordóñez, Francisco Arguello, and Dora B. Heras. Alignment of hyperspectral

³<https://iwmpraise.eu/>

⁴<http://challenge-rose.fr/en/projet/roseau-2/>

images using kaze features. Remote Sensing, 10(5), 2018.

[19] Stefan Leutenegger, Margarita Chli, and Roland Siegwart. Brisk: Binary robust invariant scalable keypoints. In 2011 IEEE international conference on computer vision (ICCV), pages 2548–2555. Ieee, 2011.

[20] Elmar Mair, Gregory D Hager, Darius Burschka, Michael Suppa, and Gerhard Hirzinger. Adaptive and generic corner detection based on the accelerated segment test. In European conference on Computer vision, pages 183–196. Springer, 2010.

[21] Michael Donoser and Horst Bischof. Efficient maximally stable extremal region (mser) tracking. In 2006 IEEE Computer Society Conference on Computer Vision and Pattern Recognition (CVPR’06), volume 1, pages 553–560. Ieee, 2006.

[22] Herbert Bay, Tinne Tuytelaars, and Luc Van Gool. Surf: Speeded up robust features. In European conference on computer vision, pages 404–417. Springer, 2006.

[23] Miroslav Trajković and Mark Hedley. Fast corner detection. Image and vision computing, 16(2):75–87, 1998.

[24] Jianbo Shi et al. Good features to track. In 1994 Proceedings of IEEE conference on computer vision and pattern recognition, pages 593–600. IEEE, 1994.

[25] Shaharyar Ahmed Khan Tareen and Z. Saleem. A comparative analysis of sift, surf, kaze, akaze, orb, and brisk. 2018 International Conference on Computing, Mathematics and Engineering Technologies (iCoMET), pages 1–10, 2018.

[26] Hongmou Zhang, Jürgen Wohlfeil, and Denis Griebbach. Extension and evaluation of the agast feature detector. 2016.

[27] Farman Ali, Sajid Ullah Khan, Muhammad Zarrar Mahmudi, and Rahmat Ullah. A comparison of fast, surf, eigen, harris, and mser features. International Journal of Computer Engineering and Information Technology, 8(6):100, 2016.

[28] Martin A. Fischler and Robert C. Bolles. Random sample consensus: A paradigm for model fitting with applications to image analysis and automated cartography. Commun. ACM, 24(6):381–395, June 1981.

[29] F. L. Bookstein. Principal warps: thin-plate splines and the decomposition of deformations. IEEE Transactions on Pattern Analysis and Machine Intelligence, 11(6):567–585, June 1989.

APPENDIX

| ABRV | parameters | modality 1 | modality 2 | modality 3 |
|-------|---------------------------|------------|------------|------------|
| ORB | nfeatures | 5000 | 10000 | 15000 |
| GFTT | maxCorners | 5000 | 10000 | 15000 |
| AGAST | threshold | 71 | 92 | 163 |
| FAST | threshold | 71 | 92 | 163 |
| AKAZE | (nOctaves, nOctaveLayers) | (1, 1) | (2, 1) | (2, 2) |
| KAZE | (nOctaves, nOctaveLayers) | (4, 2) | (4, 4) | (2, 4) |
| BRISK | (nOctaves, patternScale) | (0, 0.1) | (1, 0.1) | (2, 0.1) |
| SURF | (nOctaves, nOctaveLayers) | (1, 1) | (2, 1) | (2, 2) |
| MSER | None | None | None | None |

Table 1: list of algorithms with 3 modalities of their parameters