

CANDIDATE  
NAME

--

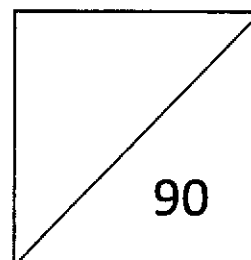
CLASS

--

INDEX  
NUMBER

--	--	--	--

# Anglo-Chinese School (Independent)



## PRELIMINARY EXAMINATION 2024 YEAR FOUR EXPRESS MATHEMATICS PAPER 1

4052/01

Thursday

1 August 2024

2 hours 15 minutes

Candidates answer on the Question Paper.

### READ THESE INSTRUCTIONS FIRST

Write your index number, name and class in the spaces on top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **all** questions.

If working is needed for any question, it must be shown with the answer.

Omission of essential working will result in loss of marks.

The use of an approved scientific calculator is expected, where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142, unless the question requires the answer in terms of  $\pi$ .

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 90.

**Mathematical Formulae***Compound Interest*

$$\text{Total amount} = P \left( 1 + \frac{r}{100} \right)^n$$

*Mensuration*

$$\text{Curved surface area of a cone} = \pi r l$$

$$\text{Surface area of a sphere} = 4 \pi r^2$$

$$\text{Volume of a cone} = \frac{1}{3} \pi r^2 h$$

$$\text{Volume of a sphere} = \frac{4}{3} \pi r^3$$

$$\text{Area of a triangle} = \frac{1}{2} ab \sin C$$

$$\text{Arc length} = r\theta, \text{ where } \theta \text{ is in radians}$$

$$\text{Sector area} = \frac{1}{2} r^2 \theta, \text{ where } \theta \text{ is in radians}$$

*Trigonometry*

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

*Statistics*

$$\text{Mean} = \frac{\sum fx}{\sum f}$$

$$\text{Standard deviation} = \sqrt{\frac{\sum fx^2}{\sum f} - \left( \frac{\sum fx}{\sum f} \right)^2}$$

Answer **all** the questions.

- 1 The point  $C$  lies on the line  $AB$  such  $AC:AB = 2:7$ .

(a) Write  $AC$  as a fraction of  $BC$ .

Answer ..... [1]

(b) Given that  $AC$  is 24 cm, calculate the length of  $BC$ .

Answer ..... cm [1]

---

- 2 (a)  $\sin x^\circ = 0.66913$   
Given that  $x$  is an obtuse angle, find  $x$ .

Answer  $x =$  ..... [1]

- (b)  $\cos y^\circ = -\cos 121^\circ$   
Given that  $y$  is an acute angle, find the value of  $y$ .

Answer  $y =$  ..... [1]

- 3 During a game, Lee rolled two fair six-sided die. To obtain the score, he subtracted the lower number from the higher number. If the numbers shown on the dice were the same, his score is zero.

(a) Construct a possibility diagram to show all possible outcomes. [1]

*Answer*

(b) Find the probability that Lee's score is 5.

*Answer* ..... [1]

---

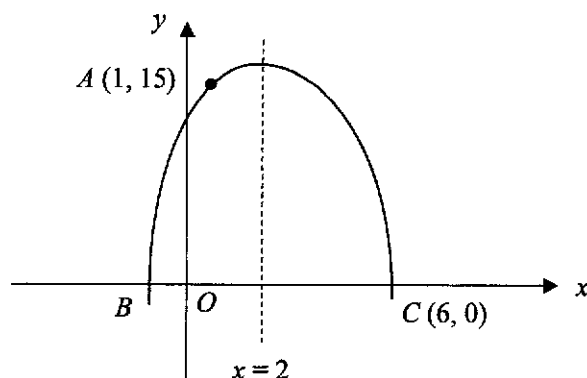
- 4 A shopkeeper bought a pair of shorts for \$24. He made a percentage profit of 45% despite selling it at a discount of 20% off the listed price. Calculate the listed price for this pair of shorts.

*Answer* \$..... [2]

---

5

- 5 Part of the graph of a quadratic function is shown below.



The graph passes through the point  $A(1, 15)$  and it cuts the  $x$ -axis at the points  $B$  and  $C$ .  
Given that  $C$  is  $(6, 0)$  and  $x = 2$  is the line of symmetry of the graph,

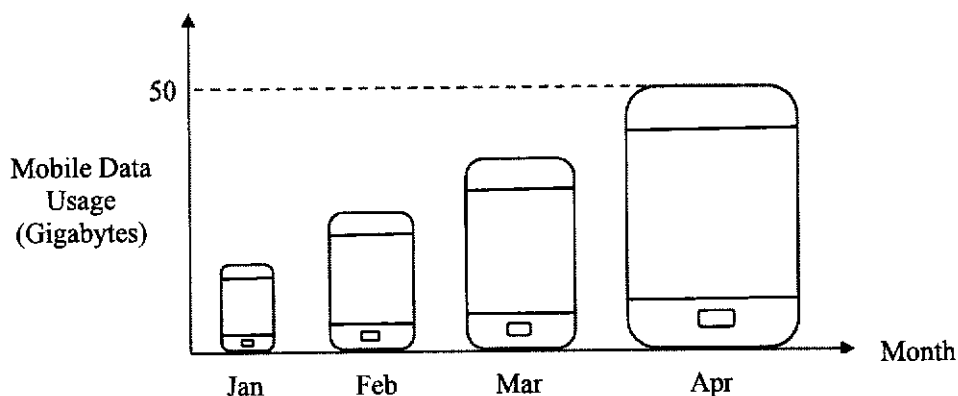
- (a) write down the equation of the quadratic curve in the form  $y = a(x - h)^2 + k$ .

Answer ..... [2]

- (b) find the positive value of  $x$  when  $y = 4$ , leaving your answer in exact form.

Answer  $x =$  ..... [1]

- 6 Justin drew this graph to show his mobile data usage for each of the following four months.



State one aspect of the graph that may be misleading and explain how this may lead to a misinterpretation of the graph.

Answer .....

.....

.....

..... [2]

- 7 Simplify  $\left(\frac{1}{2}x^2\right)^3 \div \left(4\sqrt[3]{x^5}\right)$  giving your answer in the form of  $ax^n$ , where  $a$  and  $n$  are rational numbers.

Answer ..... [2]

- 8 (a) Express 13 824 as a product of its prime factors.

*Answer* ..... [1]

- (b) Explain why 13 824 is a perfect cube.

*Answer* .....  
 .....  
 .....  
 ..... [1]

- (c) Given that  $a$  is a prime number, find the value of  $a$  such that  $\frac{1}{8a} \times 13824$  is a perfect square.

*Answer*  $a =$  ..... [1]

- 9 In the diagram,  $ABCD$  is a rectangle and  $E$  and  $F$  are points on  $AD$  and  $BC$  respectively.

The ratio of the area of triangle  $ABF$  to the area of rectangle  $ABCD$  is 1: 9.

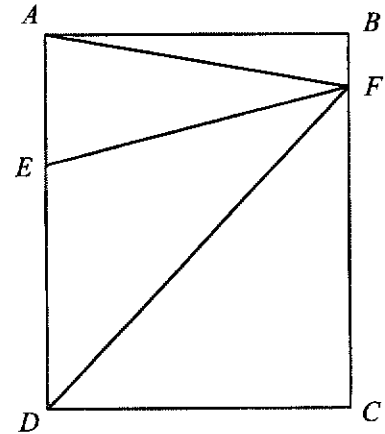
The ratio of the area of triangle  $AFE$  to the area of rectangle  $ABCD$  is 1: 6.

Explain with clear workings, if the following statements are true/ false.

- A: The ratio of the area of triangle  $ABF$  to that of triangle  $AFE$  is 2: 3.
- B: The ratio of the area of triangle  $DFC$  to that of rectangle  $ABCD$  is 2: 5.
- C: The sum of the area of triangles  $ABF$  and triangle  $DFC$  is equal to the sum of the area of triangles  $AFE$  and  $EFD$ .

- B:** The ratio of the area of triangle  $DFC$  to that of rectangle  $ABCD$  is 2: 5.

- C: The sum of the area of triangles  $ABF$  and triangle  $DFC$  is equal to the sum of the area of triangles  $AFE$  and  $EFD$ .



Answer .....

.....

\*\*\*\*\*

.....

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 162 163 164 165 166 167 168 169 170 171 172 173 174 175 176 177 178 179 180 181 182 183 184 185 186 187 188 189 190 191 192 193 194 195 196 197 198 199 200 201 202 203 204 205 206 207 208 209 210 211 212 213 214 215 216 217 218 219 220 221 222 223 224 225 226 227 228 229 230 231 232 233 234 235 236 237 238 239 240 241 242 243 244 245 246 247 248 249 250 251 252 253 254 255 256 257 258 259 260 261 262 263 264 265 266 267 268 269 270 271 272 273 274 275 276 277 278 279 280 281 282 283 284 285 286 287 288 289 290 291 292 293 294 295 296 297 298 299 300 301 302 303 304 305 306 307 308 309 310 311 312 313 314 315 316 317 318 319 320 321 322 323 324 325 326 327 328 329 330 331 332 333 334 335 336 337 338 339 340 341 342 343 344 345 346 347 348 349 350 351 352 353 354 355 356 357 358 359 360 361 362 363 364 365 366 367 368 369 370 371 372 373 374 375 376 377 378 379 380 381 382 383 384 385 386 387 388 389 390 391 392 393 394 395 396 397 398 399 400 401 402 403 404 405 406 407 408 409 410 411 412 413 414 415 416 417 418 419 420 421 422 423 424 425 426 427 428 429 430 431 432 433 434 435 436 437 438 439 440 441 442 443 444 445 446 447 448 449 450 451 452 453 454 455 456 457 458 459 460 461 462 463 464 465 466 467 468 469 470 471 472 473 474 475 476 477 478 479 480 481 482 483 484 485 486 487 488 489 490 491 492 493 494 495 496 497 498 499 500 501 502 503 504 505 506 507 508 509 510 511 512 513 514 515 516 517 518 519 520 521 522 523 524 525 526 527 528 529 530 531 532 533 534 535 536 537 538 539 540 541 542 543 544 545 546 547 548 549 550 551 552 553 554 555 556 557 558 559 560 561 562 563 564 565 566 567 568 569 570 571 572 573 574 575 576 577 578 579 580 581 582 583 584 585 586 587 588 589 590 591 592 593 594 595 596 597 598 599 600 601 602 603 604 605 606 607 608 609 610 611 612 613 614 615 616 617 618 619 620 621 622 623 624 625 626 627 628 629 630 631 632 633 634 635 636 637 638 639 640 641 642 643 644 645 646 647 648 649 650 651 652 653 654 655 656 657 658 659 660 661 662 663 664 665 666 667 668 669 670 671 672 673 674 675 676 677 678 679 680 681 682 683 684 685 686 687 688 689 690 691 692 693 694 695 696 697 698 699 700 701 702 703 704 705 706 707 708 709 710 711 712 713 714 715 716 717 718 719 720 721 722 723 724 725 726 727 728 729 730 731 732 733 734 735 736 737 738 739 740 741 742 743 744 745 746 747 748 749 750 751 752 753 754 755 756 757 758 759 760 761 762 763 764 765 766 767 768 769 770 771 772 773 774 775 776 777 778 779 780 781 782 783 784 785 786 787 788 789 790 791 792 793 794 795 796 797 798 799 800 801 802 803 804 805 806 807 808 809 810 811 812 813 814 815 816 817 818 819 820 821 822 823 824 825 826 827 828 829 830 831 832 833 834 835 836 837 838 839 840 841 842 843 844 845 846 847 848 849 850 851 852 853 854 855 856 857 858 859 860 861 862 863 864 865 866 867 868 869 870 871 872 873 874 875 876 877 878 879 880 881 882 883 884 885 886 887 888 889 890 891 892 893 894 895 896 897 898 899 900 901 902 903 904 905 906 907 908 909 910 911 912 913 914 915 916 917 918 919 920 921 922 923 924 925 926 927 928 929 930 931 932 933 934 935 936 937 938 939 940 941 942 943 944 945 946 947 948 949 950 951 952 953 954 955 956 957 958 959 960 961 962 963 964 965 966 967 968 969 970 971 972 973 974 975 976 977 978 979 980 981 982 983 984 985 986 987 988 989 990 991 992 993 994 995 996 997 998 999 1000 1001 1002 1003 1004 1005 1006 1007 1008 1009 1010 1011 1012 1013 1014 1015 1016 1017 1018 1019 1020 1021 1022 1023 1024 1025 1026 1027 1028 1029 1030 1031 1032 1033 1034 1035 1036 1037 1038 1039 1040 1

.....

.....

.....

.....

.....



- 10 The ratio of the number of soccer balls and volleyballs in a sports shop was 11: 7. After 126 soccer balls were added and 233 volleyballs were sold, the ratio became 14: 3. How many volleyballs were there in the shop at first?

*Answer* .....volleyballs [3]

- 
- 11 Explain why  $(5n+2)^2 - (5n-2)^2$  is a multiple of 8 for all integer values of  $n$ .

*Answer*

.....

..... [2]

10

12 Factorise the following completely.

(a)  $45b - 18ab - 2a^2 + 5a,$

*Answer* ..... [2]

(b)  $2p^2 - \frac{2}{3}p - \frac{1}{6}.$

*Answer* ..... [2]

13 Simplify  $\frac{x^2 - 9y^2}{3x^2 + 7xy - 6y^2}.$

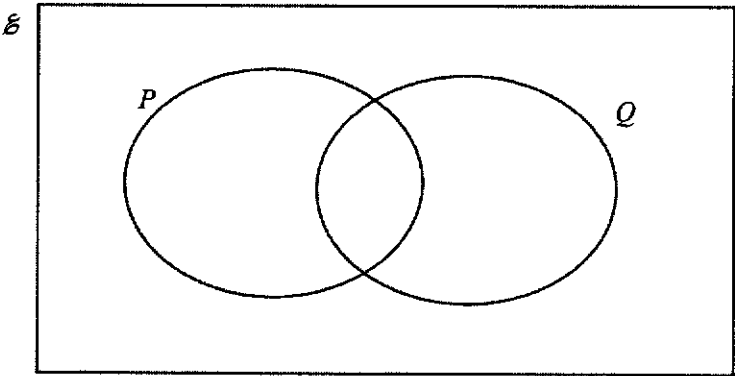
*Answer* ..... [3]

- 14 The sets  $P$  and  $Q$  consists of the points whose coordinates  $(x, y)$  are given by  $P = \{(x, y) : y = 2x + 3\}$  and  $Q = \{(0, 0), (0, 3), (1, 5), (2, 5), (3, 9)\}$  respectively.

(a) List the elements in  $P \cap Q$ .

Answer ..... [2]

(b) Shade the region which represents  $(P \cup Q)'$ .



[1]

- 15 The distance between the points  $M(k, 7)$  and  $N(9, k)$  is  $\sqrt{20}$  units.  
Given that  $k > 10$ , find the value of  $k$ .

Answer  $k =$  ..... [3]

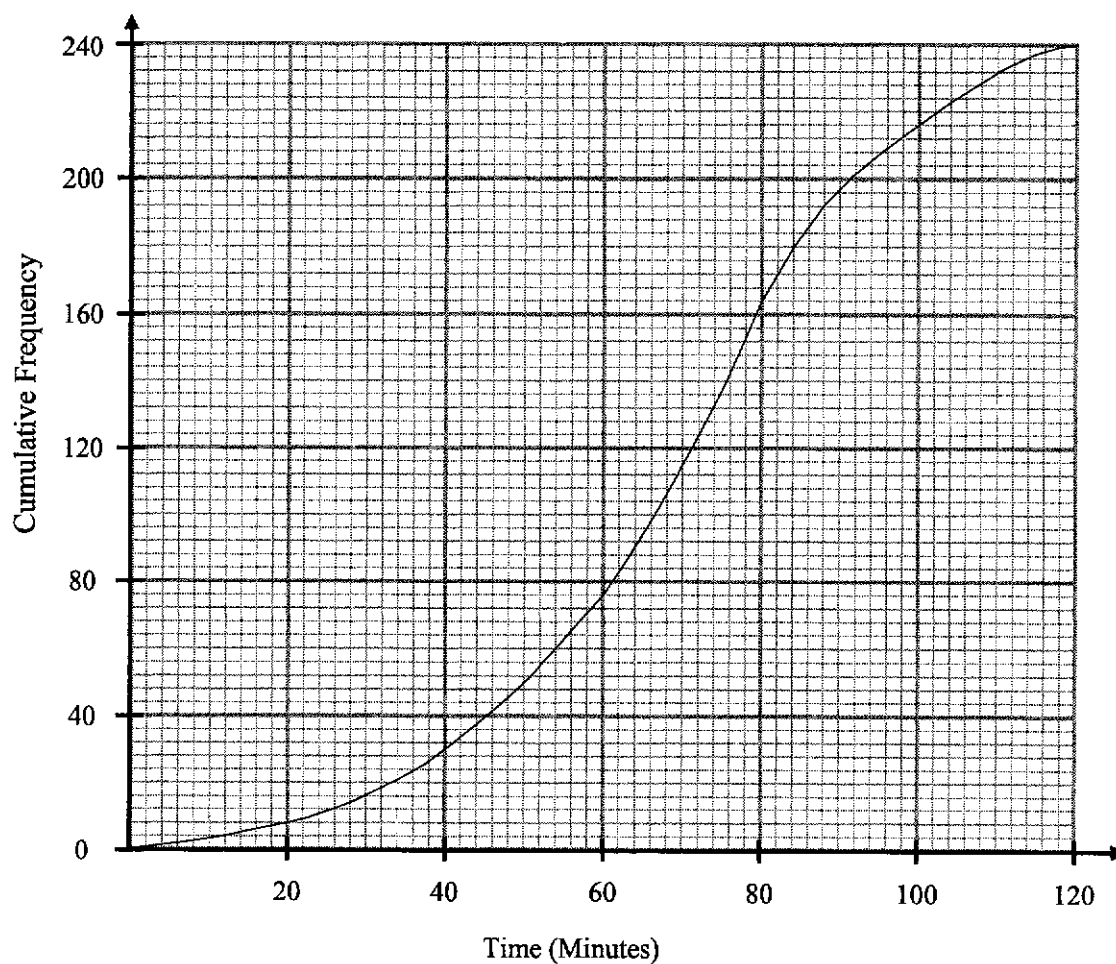
- 16 Mr Tan took 4 hours to travel from Town A to Town B. Mr Lim took 8 hours to travel in the opposite direction from Town B to Town A using the same route. They both started at 11am. What time did they pass each other?

Answer ..... pm [2]

- 
- 17 Sam and Wilson can paint a house together in 6 days. They painted the house together for 5 days and then Sam completed the painting of the remaining house alone in 3 days. How many days would it take for Wilson to paint the entire house by himself?

Answer ..... days [3]

- 18 The cumulative frequency curve below illustrates the wait time of 240 customers who visited a bank.



Use the graph to estimate

- (a) the 60th percentile,

Answer ..... minutes [1]

- (b) the interquartile range of the wait time.

Answer ..... minutes [2]

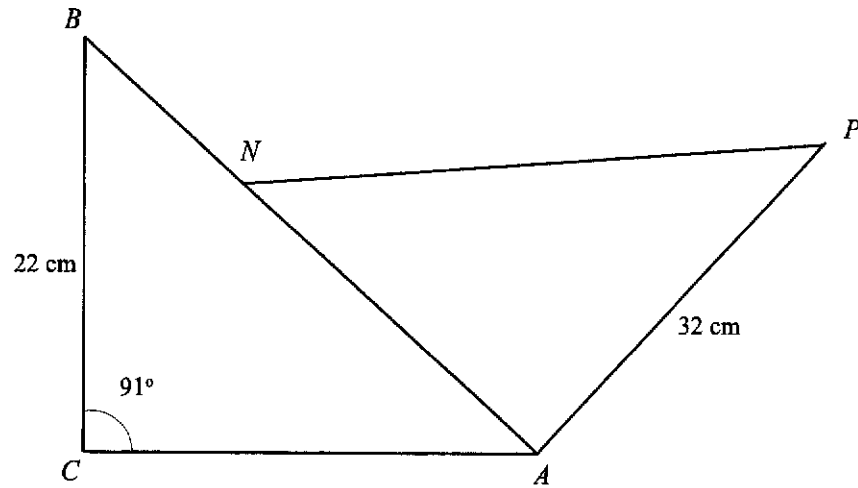
- (c) Only 10% of the customers complained about the long wait time they experienced. What was the minimum wait time for these customers?

*Answer* ..... minutes [2]

- (d) Two customers are chosen at random. Find the probability that one customer waited for less than or equal to 60 minutes and the other waited for more than 100 minutes.

*Answer* ..... [2]

- 19 In the diagram below, triangle  $ABC$  is congruent to triangle  $PNA$ .



Given that  $BC = 22$  cm,  $AP = 32$  cm and angle  $ACB = 91^\circ$ , calculate

- (a) the length of  $BN$ ,

Answer ..... cm [3]

- (b) angle  $APN$ .

Answer Angle  $APN =$  ..... [2]

20 The mean of ten different numbers is 11.8.

- (a) Write down a number which will generate a mean of 12, when added to these ten numbers.

Answer..... [1]

- (b) Each value within the ten numbers is adjusted as follows:

If the number is less than the mean, the number is decreased by 2,  
if the number is greater than the mean, the number is increased by 2 and  
if the number is equal to the mean, it remains unchanged.

Explain clearly how these adjustments would affect the standard deviation.

Answer .....

.....

.....

.....

..... [2]



- 21 A tour agency sells cruise packages to Vietnam, Maldives and Taiwan at \$1299, \$1398 and \$2538 respectively. The table below shows the number of customers who have signed up for the respective cruise packages via the tour agency from January to June and from July to December.

	First Period	Second Period
	From January to June	From July to December
Vietnam	27	24
Maldives	23	29
Taiwan	19	22

The number of people who signed up for cruise packages to Vietnam, Maldives and Taiwan can be

represented by the matrix  $P = \begin{pmatrix} 27 & 24 \\ 23 & 29 \\ 19 & 22 \end{pmatrix}$ .

- (a) The elements of matrix  $C$ , where  $C = AP$ , represents the total earnings for each period. Write down the matrix  $A$ .

Answer A =

[1]

- (b) Hence, by using matrix multiplication, determine the total earnings,  $C$  by the tour agency for each of the period respectively.

Answer C =

[2]

18

- (c) Given  $\mathbf{M} = \mathbf{C}\mathbf{R}$ , where  $\mathbf{R} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$ , find the matrix  $\mathbf{M}$ .

*Answer*  $\mathbf{M} =$

[2]

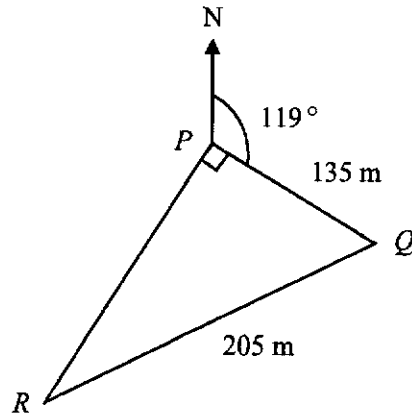
- (d) Describe what is represented by the element(s) of  $\mathbf{M}$ .

*Answer* .....

.....

..... [1]

- 22  $P$ ,  $Q$  and  $R$  are three points on level ground such that  $RPQ$  forms a right-angled triangle with  $PQ$  and  $RQ$  measuring 135 m and 205 m respectively. It is given that a building of height 50 m is situated at  $P$  and that the bearing of  $Q$  from  $P$  is  $119^\circ$ .



- (a) Calculate the bearing of  $R$  from  $Q$ .

Answer ..... [2]

- (b) Calculate the largest possible angle of depression from the top of the building to any point on the path  $RQ$ .

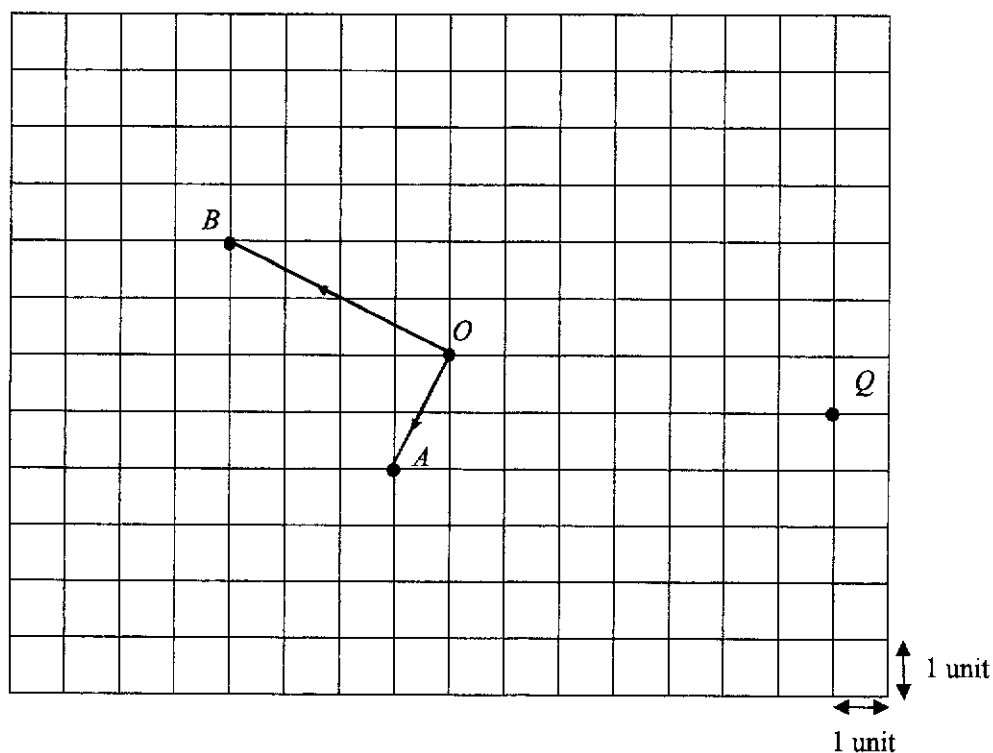
Answer ..... [3]

- 23 Jefferson and Victor were sent by their company to work in Washington D.C. and Beijing respectively. Jefferson rented a 696 sq ft apartment in Washington D.C. for 1800 USD while Victor rented a 60 m<sup>2</sup> apartment in Beijing for 8000 CNY. Given that the currency exchange rate for both cities is 1 USD = 7.25 CNY and that 1 m<sup>2</sup> = 10.7639 sq ft, illustrate with clear working, which apartment has a higher rental cost.

*Answer*

.....  
..... [3]

- 24 In the grid,  $\overrightarrow{OA} = \mathbf{a}$  and  $\overrightarrow{OB} = \mathbf{b}$ .  $Q$  is a point on the grid.



- (a) Mark and label the point  $P$  such that  $\overrightarrow{OP} = -\mathbf{b} - 2\mathbf{a}$ . [1]
- (b) Express  $\overrightarrow{OQ}$  in the form  $m\mathbf{a} + n\mathbf{b}$ , where  $m, n$  are real numbers.

Answer  $\overrightarrow{OQ} = \dots\dots\dots$  [1]

- (c) Given that  $\overrightarrow{OC} = \begin{pmatrix} 6 \\ x \end{pmatrix}$  and  $\overrightarrow{OC}$  is parallel to  $\overrightarrow{AB}$ , find the value of  $x$ .

Answer  $x = \dots\dots\dots$  [2]

- 25 Edwin deposited  $\$P$  each into Bank  $A$  and Bank  $B$ . Bank  $A$  offered a simple interest of 4% per annum while Bank  $B$  offered an interest rate of 2% per half-year, compounded every six months. The difference in the amount Edwin received from both banks after a period of 7 years is \$513. Find  $P$ , correct your answer to the nearest hundred.

*Answer* ..... [4]

- 26  $X$ ,  $Y$ , and  $Z$  are three points on a horizontal sea level map as shown below.  
 $X$  is due North of  $Y$  and  $Z$  is due east of  $Y$ .  
 Ship  $A$  is on a bearing of  $070^\circ$  from  $X$  and on a bearing of  $350^\circ$  from  $Z$ .  
 It is given that 1 cm represents 2 km on the sea level.

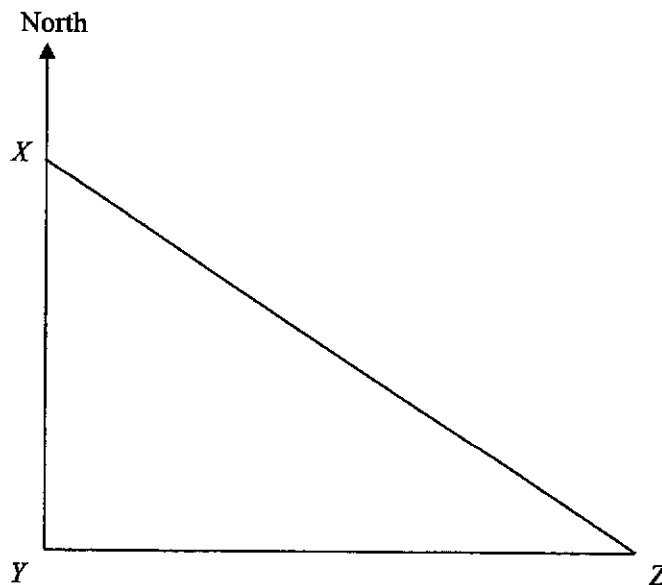
- (a) Label the position of Ship  $A$  and write down the actual distance  $AX$ .

Answer  $AX = \dots\dots\dots$  km [2]

- (b) A boat,  $B$  stationed along path  $XZ$  is equidistant from  $Y$  and  $Z$ . Label the position of  $B$ . [2]

- (c) Showing your constructions clearly, draw a circle with centre  $O$ , on the map such that the lines  $XY$ ,  $YZ$  and  $XZ$  are tangents to the circle. Hence write down the radius of the circle on the map.

Answer  $\dots\dots\dots$  cm [2]







CANDIDATE  
NAME

--

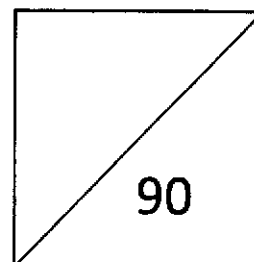
CLASS

--

INDEX  
NUMBER

--	--	--	--

# Anglo-Chinese School (Independent)



## PRELIMINARY EXAMINATION 2024 YEAR FOUR EXPRESS MATHEMATICS PAPER 2

4052/02

Wednesday

7 August 2024

2 hours 15 minutes

Candidates answer on the Question Paper.

### READ THESE INSTRUCTIONS FIRST

Write your index number, name and class in the spaces on top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **all** questions.

The number of marks is given in brackets [ ] at the end of each question or part question.

If working is needed for any question it must be shown with the answer.

Omission of essential working will result in loss of marks.

The total of the marks for this paper is 90.

The use of an approved scientific calculator is expected, where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142.

***Mathematical Formulae******Compound Interest***

$$\text{Total amount} = P \left( 1 + \frac{r}{100} \right)^n$$

***Mensuration***

$$\text{Curved surface area of a cone} = \pi r l$$

$$\text{Surface area of a sphere} = 4 \pi r^2$$

$$\text{Volume of a cone} = \frac{1}{3} \pi r^2 h$$

$$\text{Volume of a sphere} = \frac{4}{3} \pi r^3$$

$$\text{Area of a triangle} = \frac{1}{2} ab \sin C$$

$$\text{Arc length} = r\theta, \text{ where } \theta \text{ is in radians}$$

$$\text{Sector area} = \frac{1}{2} r^2 \theta, \text{ where } \theta \text{ is in radians}$$

***Trigonometry***

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

***Statistics***

$$\text{Mean} = \frac{\sum fx}{\sum f}$$

$$\text{Standard deviation} = \sqrt{\frac{\sum fx^2}{\sum f} - \left( \frac{\sum fx}{\sum f} \right)^2}$$

3

Answer **all** the questions.

- 1 (a) Solve the equation  $2(x-5) = 3x-1$ .

Answer  $x = \dots\dots\dots$  [2]

- (b) Solve the inequality  $7-4y > 3(y+2)$ .

Answer  $\dots\dots\dots$  [2]

- (c) Given that  $\frac{1}{p} - \frac{1}{2q} = \frac{1}{3r}$ ,

- (i) find  $p$  when  $q = -1$  and  $r = 2$ ,

Answer  $p = \dots\dots\dots$  [2]

- (ii) rearrange the formula to make  $q$  the subject.

Answer  $q = \dots\dots\dots$  [3]

4

- (d) Solve the equation  $\frac{5}{x+2} - \frac{3x}{2x-1} = 3$ .

Give your solutions correct to 2 decimal places.

Answer  $x = \dots\dots\dots$  or  $\dots\dots\dots$  [5]

- 2 (a) A manufacturing company produces electronic components for various devices. They are analyzing the production data for the past 3 months, which includes quantities of components produced and the corresponding costs.

The data is presented in the table below:

Month	Quantity Produced (in units)	Cost per unit (in dollars)
May	$5.8 \times 10^5$	0.0211
June	$4.3 \times 10^6$	0.0183
July	$7.6 \times 10^5$	0.0203

- (i) Express the total quantity produced from May to July in standard form correct to 3 significant figures.

Answer  $\dots\dots\dots$  [1]

- (ii) Calculate the average cost per unit for these 3 months.  
Express your answer in cents.

*Answer* ..... cents [2]

- (iii) Given that the percentage increase in the quantity produced from July to August is 11.8%, calculate the quantity produced in August.  
Leave your answer in standard form correct to 3 significant figures.

*Answer* ..... units [2]

- (b) The company wants to build a prototype of a particular electronic component they are manufacturing.  
The radius of the actual electronic component is  $3.8 \times 10^{-5}$  m.  
In a scale drawing, the radius of the prototype of the electronic component is 1.9 cm.

- (i) Find the scale used for the drawing.  
Give your answer in the form  $n : 1$ .

*Answer* ..... : 1 [2]

- (ii) Given that the prototype has a total surface area of  $1.81 \times 10^{-8}$  m<sup>2</sup>, find, in cm<sup>2</sup>, the actual total surface area of the electronic component. Give your answer in standard form.

*Answer* ..... cm<sup>2</sup> [2]

- 3 In Diagram I below,  $ABCDE$  is a regular pentagon, centre  $O$ .  $OA = OB = 4$  cm.

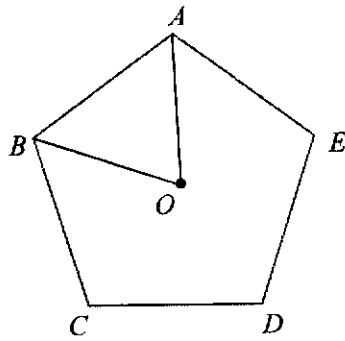


Diagram I

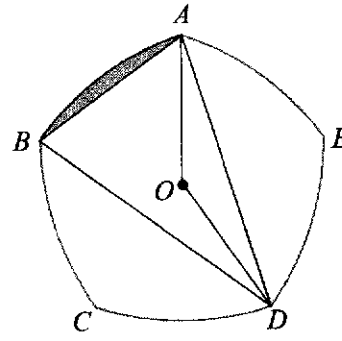


Diagram II

- (a) State the value of angle  $AOB$ .

Answer Angle  $AOB = \dots\dots\dots^\circ$  [1]

- (b) Calculate the area of the pentagon  $ABCDE$ .

Answer  $\dots\dots\dots \text{cm}^2$  [2]

- (c) Diagram II shows a design for a new badge.

The vertices of the regular pentagon  $ABCDE$  are joined by circular arcs whose centres are the opposite vertices.

For example, the arc  $AB$  has centre  $D$  and radius  $AD$ .

- (i) Find angle  $ABD$ .  
Give reasons for each step of your working.

Answer Angle  $ABD = \dots\dots\dots^\circ$  [2]

(ii) Show that the length of  $BD$  is approximately 7.61 cm.

*Answer*

[2]

(iii) Calculate the area of the shaded segment in Diagram II.

*Answer* .....  $\text{cm}^2$  [3]

(iv) Calculate the area of the face  $ABCDE$  of the badge.

*Answer* .....  $\text{cm}^2$  [2]

- 4 Here are the first four terms of a sequence.

$$2 \quad \frac{5}{3} \quad \frac{10}{5} \quad \frac{17}{7}$$

- (a) Find the fifth term of the sequence.

Answer ..... [1]

- (b)  $T_n$  is the  $n$ th term of the sequence.

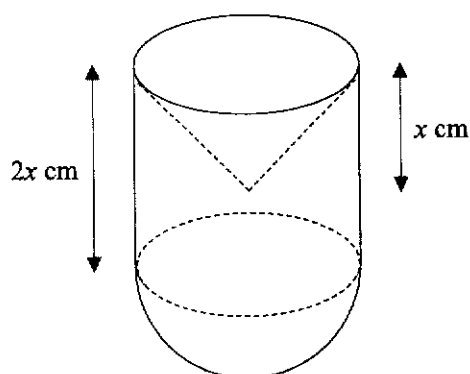
Find an expression, in terms of  $n$ , for  $T_n$ .

Answer  $T_n =$  ..... [2]

- (c) Find the value of  $T_{25} - T_{24}$ .

Answer  $T_{25} - T_{24} =$  ..... [1]

- 5 The diagram shows a solid ornament in the shape of a cylinder with an upright cone cut out at one end and a hemisphere attached to the other end.



The vertical heights of the cone and cylinder are  $x$  cm and  $2x$  cm respectively.

- (a) Find the ratio of the volume of the cone to that of the cylinder, expressing your answer as a fraction in the simplest form.

Answer ..... [1]



(b) If the volume of the cylinder is  $345\text{ cm}^3$  and its height is  $8\text{ cm}$ , calculate

(i) the radius of the cylinder,

*Answer* .....  $\text{cm}$  [2]

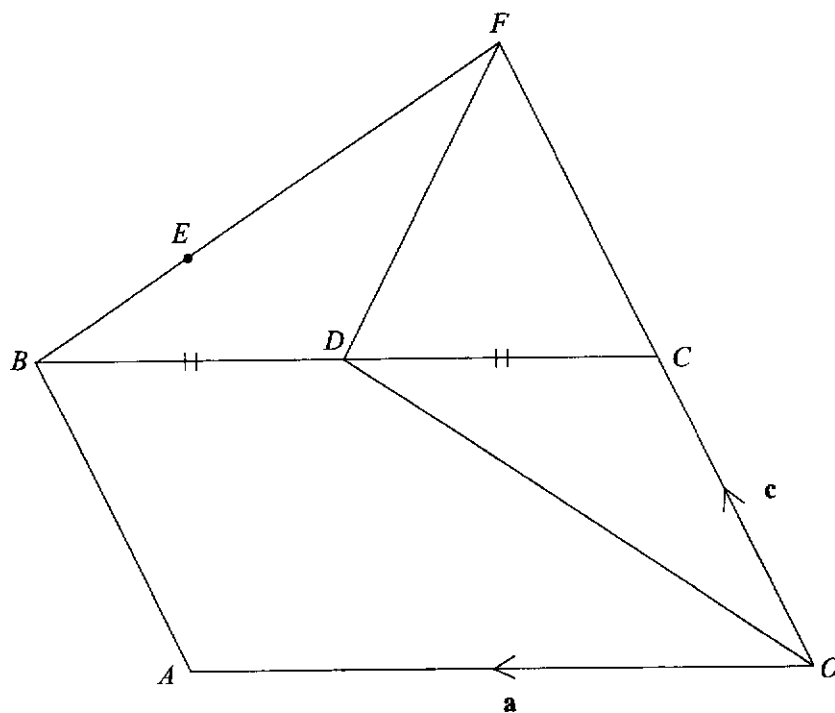
(ii) the curved surface area of the cone,

*Answer* .....  $\text{cm}^2$  [3]

(iii) the quantity of paint needed to paint the exterior of the ornament with a  $0.2\text{ mm}$  thick coat of paint.

*Answer* .....  $\text{cm}^3$  [3]

- 6 In the diagram,  $OABC$  is a parallelogram and  $D$  is the midpoint of  $BC$ .  $BE$  and  $OC$  produced intersect at point  $F$ . It is given that  $BE : BF = 1 : 3$ ,  $OC : OF = 1 : 2$ ,  $\overrightarrow{OA} = \mathbf{a}$  and  $\overrightarrow{OC} = \mathbf{c}$ .



- (a) Express and simplify the following vectors in terms of  $\mathbf{a}$  and  $\mathbf{c}$ ,

(i)  $\overrightarrow{BF}$ ,

Answer  $\overrightarrow{BF} = \dots\dots\dots [1]$

(ii)  $\overrightarrow{AE}$ ,

Answer  $\overrightarrow{AE} = \dots\dots\dots [2]$

(iii)  $\overline{OD}$ .

Answer  $\overline{OD}$  = ..... [1]

(b) Determine, with clear working shown, whether points  $O$ ,  $D$  and  $E$  lie on a straight line.

Answer

.....  
.....  
.....  
.....[3]

(c) Find the value of  $\frac{\text{area of triangle } CDE}{\text{area of parallelogram } OABC}$ .

Answer ..... [2]

- 7 (a) Complete the table of values for  $y = 2x + \frac{1}{x^2} - 4$ .

Values are given to two decimal places where appropriate.

$x$	-2	-1	-0.5	-0.3	0.3	0.5	1	2	3
$y$	-7.75	-5	-1	6.51	7.71		-1	0.25	2.1

[1]

- (b) On the grid opposite, draw the graph of  $y = 2x + \frac{1}{x^2} - 4$  for  $-2 \leq x \leq 3$ . [3]

- (c) (i)  $y = b$  cuts the graph of  $y = 2x + \frac{1}{x^2} - 4$  at one point for  $-2 \leq x \leq 3$ , state the range of values of  $b$ .

Answer ..... [1]

- (ii) On the same grid, draw the graph of  $3y - 5x = 4$  for  $-2 \leq x \leq 3$ . [2]

- (iii) Write down the  $x$ -coordinates of the points where the graph of  $3y - 5x = 4$  intersects the curve for  $-2 \leq x \leq 3$ .

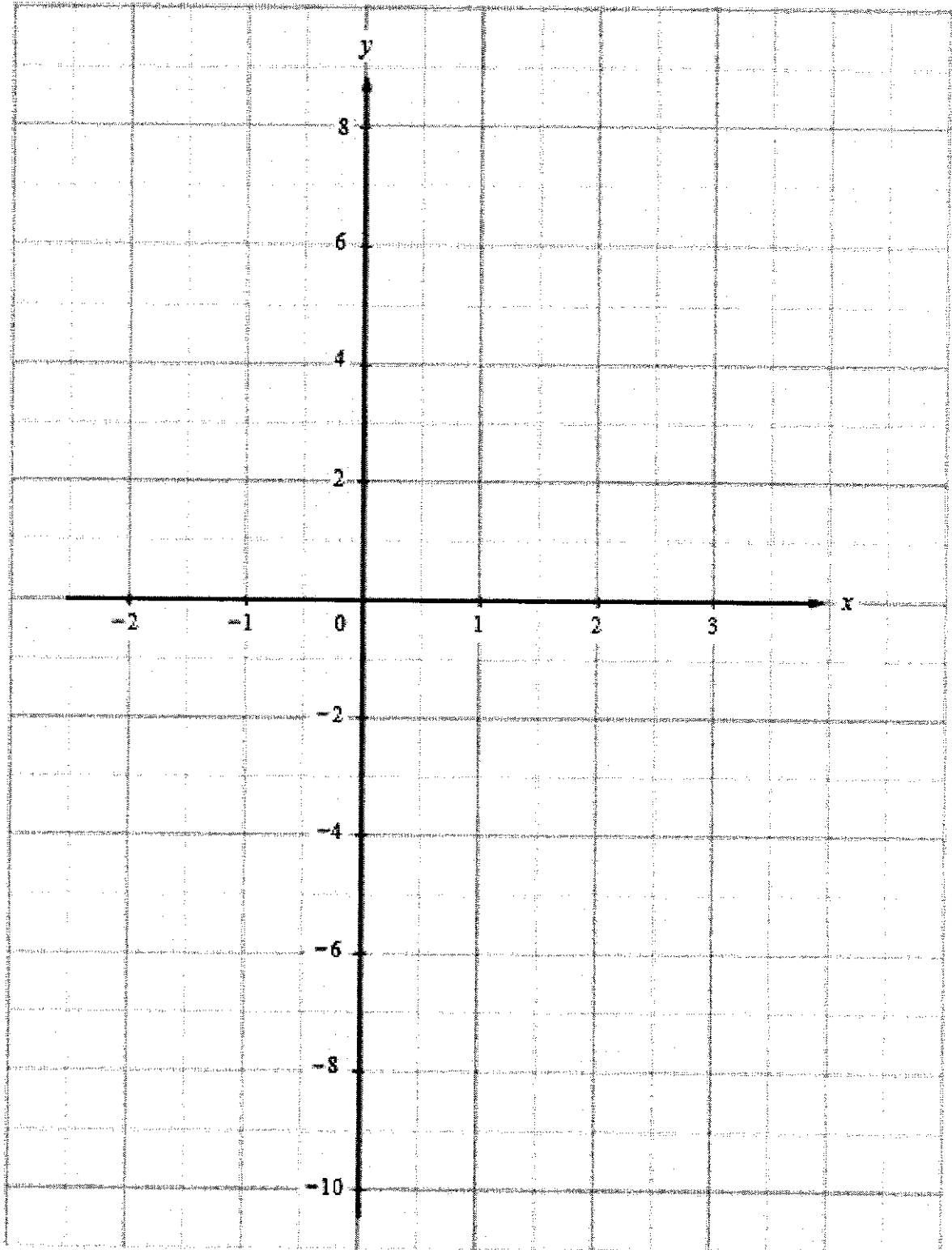
Answer  $x = \dots\dots\dots$  and  $\dots\dots\dots$  [2]

- (iv) These values of  $x$  are solutions of the equation  $x^3 + Ax^2 + B = 0$ .  
Find the value of  $A$  and the value of  $B$ .

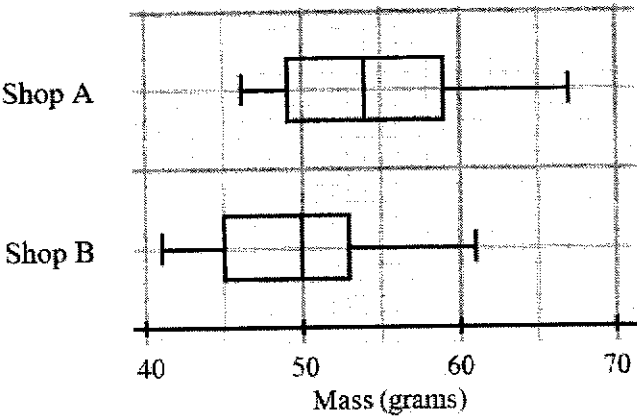
Answer  $A = \dots\dots\dots$

$B = \dots\dots\dots$

[3]



- 8 (a) The box-and-whisker plots show the distribution of the masses (in grams) of eggs sold in Shop A and Shop B.



- (i) There are 25 eggs with masses of more than 59 g sold in Shop A.  
Find the total number of eggs sold in Shop A.

Answer ..... eggs [1]

- (ii) Make a comment comparing the averages and a comment comparing the distribution of the masses of the eggs sold in Shop A and Shop B.

Use figures to support your answers.

1. ....  
.....  
.....  
.....  
.....

2. ....  
.....  
.....  
.....  
.....[3]

15

(b) In a sample of 80 eggs, 4 are cracked.

(i) One egg is selected from the sample at random.

Find the probability that the egg is cracked.

*Answer* ..... [1]

(ii) Two eggs are selected from the sample at random.

Find the probability that both eggs are cracked.

*Answer* ..... [2]

(iii) Three eggs are selected from the sample at random.

Find the probability that at least one egg is cracked.

*Answer* ..... [2]

- 9 Emily is considering signing up for a new credit card and has shortlisted three options: Card A, Card B and Card C. Each card offers distinct benefits, rewards, and imposes different annual fees.

The table below presents the essential features of each card:

Card Features	Credit Card		
	Card A	Card B	Card C
Annual Fee <sup>1</sup> (in SGD) payable at the end of 12 months	\$110	\$90	Waived off for the first year; \$250 for 2nd year onwards
Cashback <sup>2</sup> Rate per month	1.5% of expenditure	1.3% of expenditure	1.2% of expenditure
Sign-up Bonus (in SGD) to be used to offset the first bill payment	\$50	\$60	\$70
Number of Free Airport Lounge Access Passes per year	2	4	Unlimited

<sup>1</sup> Cardholder does not enjoy cashback on the annual fee.

<sup>2</sup> Cashback amount is the amount of money received by the cardholder based on his/her expenditure. The cashback amount will be credited to the card account and used to offset the credit card bill for that month.



- (a) Calculate the net rewards (which consist of cashback and sign-up bonus) for each credit card for an expenditure of SGD 2000 within the first month of card usage.

*Answer* Card A: \$.....

Card B: \$.....

Card C: \$.....

[3]

- (b) Emily's monthly card expenditure is SGD 2000.

Assuming Emily has signed up for credit card A, by considering only the annual fee and the net rewards, calculate the total amount she has to pay for her credit card bill after the first year of usage.

*Answer* \$..... [2]

- (c) Emily enjoys travelling. As such, travel perks are important to her.

The following table provides a summary of Emily's monthly expenditure and travel needs.

Additional information

- Monthly Card Expenditure (excluding annual fee and purchases made for airport lounge access passes): SGD 2000
- Airport Lounge Access Passes<sup>3</sup> required per year: 5

<sup>3</sup> Credit card must be presented at the Airport Lounge. Any Airport Lounge access pass bought, costing \$50 each, must be charged to the same credit card. Cardholder will not be able to enjoy cashback on the amount spent on Airport Lounge access passes.

Determine which credit card might be the best choice for Emily if she signs up for the card and uses it for two consecutive years.

Justify any decisions you make and show your calculations clearly.

Continuation of working space for question 9(c).

.....

.....

.....[7]

**BLANK PAGE**