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CRYPTOGRAPHY AND DATA SECURITY
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KZG XBWOZIXPG IVLLIB IAMKCZQBG
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IXE VZUMXGVN EGTJJGZ GYKIAOXE

Cryptography and Data Security

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In memory of my Father,

Cornelius Lowell Robling

1910-1965

Preface

Electronic computers have evolved from exiguous experimental enterprises in the 1940s to prolific practical data processing systems in the 1980s. As we have come to rely on these systems to process and store data, we have also come to wonder about their ability to protect valuable data.

Data security is the science and study of methods of protecting data in computer and communication systems from unauthorized disclosure and modification. The goal of this book is to introduce the mathematical principles of data security and to show how these principles apply to operating systems, database systems, and computer networks. The book is for students and professionals seeking an introduction to these principles. There are many references for those who would like to study specific topics further.

Data security has evolved rapidly since 1975. We have seen exciting developments in cryptography: public-key encryption, digital signatures, the Data Encryption Standard (DES), key safeguarding schemes, and key distribution protocols. We have developed techniques for verifying that programs do not leak confidential data, or transmit classified data to users with lower security clearances. We have found new controls for protecting data in statistical databases and new methods of attacking these databases. We have come to a better understanding of the theoretical and practical limitations to security.

Because the field is evolving so rapidly, it has been difficult to write a book that is both coherent and current. Even as the manuscript was in production, there were new developments in the field. Although I was able to incorporate a few of these developments, they are not as well integrated into the book as I would like. In many cases, I was only able to include references.

Some areas are still unsettled, and I was unable to treat them to my satisfaction. One such area is operating system verification; another is the integration of

cryptographic controls into operating systems and database systems. I hope to cover these topics better in later editions of the book.

Data security draws heavily from mathematics and computer science. I have assumed my audience has some background in programming, data structures, operating systems, database systems, computer architecture, probability theory, and linear algebra. Because I have found most computer science students have little background in information theory and number theory, I have included self-contained tutorials on these subjects. Because complexity theory is a relatively new area, I have also summarized it.

This book is used in a one-semester graduate computer science course at Purdue University. The students are assigned exercises, programming projects, and a term project. The book is suitable for a graduate or advanced undergraduate course and for independent study. There are a few exercises at the end of each chapter, most of which are designed so the reader can recognize the right answer. I have purposely not included solutions. There is also a puzzle.

Here is a brief summary of the chapters:

- Chapter 1, Introduction, introduces the basic concepts of cryptography, data security, information theory, complexity theory, and number theory.
- Chapter 2, Encryption Algorithms, describes both classical and modern encryption algorithms, including the Data Encryption Standard (DES) and public-key algorithms.
- Chapter 3, Cryptographic Techniques, studies various techniques related to integrating cryptographic controls into computer systems, including key management.
- Chapter 4, Access Controls, describes the basic principles of mechanisms that control access by subjects (e.g., users or programs) to objects (e.g., files and records). These mechanisms regulate direct access to objects, but not what happens to the information contained in these objects.
- Chapter 5, Information Flow Controls, describes controls that regulate the dissemination of information. These controls are needed to prevent programs from leaking confidential data, or from disseminating classified data to users with lower security clearances.
- Chapter 6, Inference Controls, describes controls that protect confidential data released as statistics about subgroups of individuals.

I am deeply grateful to Jim Anderson, Bob Blakley, Peter Denning, Whit Diffie, Peter Neumann, and Rich Reitman, whose penetrating criticisms and suggestions guided me to important results and helped me focus my ideas. I am also grateful to Greg Andrews, Leland Beck, Garrett Birkhoff, Manuel Blum, David Chaum, Francis Chin, Larry Cox, Töre Dalenius, George Davida, Dave Gifford, Carl Hammer, Mike Harrison, Chris Hoffmann, Stephen Matyas, Jon Millen, Bob Morris, Glen Myers, Steve Reiss, Ron Rivest, Brian Schanning, Jan Schlörer, Gus Simmons, and Larry Snyder. These people gave generously of their time to help make this a better book.

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