

Name: Krishna Biswakarma  
Roll: 24CS60871  
Subject - ADA.

① Let the input be as following:

A complete weighted graph  $G = (V, E)$  where,

$V$  = set of cities.  $|V| = n$

$E$  = set of edges with weights  $w(u, v)$  representing the distance between cities  $u$  and  $v$ .

A value ' $K$ ' which denotes the maximum allowed distance between any two consecutive cities in the tour.

State space definition for CTSP:

• It is defined as the tuple  $(s, c)$  where,  $s \subseteq V$  is the set of cities visited so far, excluding the starting city.

NOTE -  $s$  = start city (initially).

•  $c \in V$  is the current city in the tour (starting at the given initial city),

• Given remaining cities to be visited are  $V - s$ .

Here, the state represents the partial tour with a specific set of cities visited with the current position in the tour.

Also, a constraint of ' $K$ ' should be enforced between city ' $c$ ' and the next city to visit must not exceed ' $K$ '.

Heuristic Estimate (Lower Bound):

Let  $h(s, c)$  be a heuristic function for CTSP.

We can use the MST as a guaranteed lower bound heuristic.

To create the heuristic we can follow the below steps:

i)  $V - s$  be the remaining cities. Compute MST over the subgraph.

NOTE - Only edges with weight  $\leq K$  will be considered.

$\therefore h(s, c) = \text{Weight of MST} \rightarrow$  This gives the LB on the cost of completing the tour starting from the current state.

② The statement is "partially true".

Comparision -

A\*: Expands nodes with lowest cost i.e.,  $f(n) = g(n) + h(n)$

$g(n)$  = Actual distance

$h(n)$  = Heuristic cost

It is proven the A\* gives optimal result with fewest nodes possible given an admissible i.e., non-overestimating heuristic.

DFBB: It explores the depth first until it either finds a sol<sup>n</sup> or the path cost becomes too high. If the meanwhile we keep on updating the bound whenever it has the lowest cost.

Heuristic Estimate and Node Expansion:

If both uses same admissible heuristic then both should agree on the potential quality of solution in terms of cost. However DFBB may expand nodes that A\* won't expand; because it don't prioritize node based on  $f(n)$  but goes on expanding the depth.

Cases where DFBB expands extra nodes:

DFBB may expand more nodes because it explores each path or prune it without choosing the lowest cost node first. This means it will also expand the path that A\* won't.

∴ DFBB may expand nodes in the path with relatively high  $g(x)$  even if better paths are there.

Hence, It is partially true because DFBB could indeed expand every node that A\* expands if both algorithm are running on the same problem with similar heuristic.

However, DFBB may additionally expand some nodes that A\* won't due to its DFS behaviour and lack of storing global  $f(x)$ .

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③ The statement is <sup>Partially</sup> true.

A\* we saw previously how it expands the nodes based on global value of  $f(n)$  where,  $f(n) = g(n) + h(n)$

$\downarrow \quad \downarrow$   
Actual cost Heuristic cost.

- IDA expands all nodes that A\* will -

since IDA is performing DFS with increasing cut-off based on  $f(n)$  it will eventually expand all nodes that A\* will expand provided the search reaches the same state.

- IDA may expand ~~and~~ some nodes that A\* won't -

since IDA uses DFS with thresholding mechanism, it may explore nodes in different order and may explore nodes that A\* doesn't particularly if the nodes have  $f(n)$  value above the current threshold but still leads to other potentially optimal path. Specifically IDA\* might expand nodes early in search that A\* would have expanded later due to its greedy priority queue. This happens because IDA\* explores all possibility in DFS manner without the guarantee of always expanding the least  $f(n)$  value node at each step.

- The statement is ~~not~~ partially true because IDA\* will indeed expand what A\* will but will also expand what A\* won't because of its higher threshold at each iteration.

- ② ④ Genetic algorithm for CTSP -  
 C Each we represent each solution as a sequence of cities.  
 A Chromosome Representation:  
 Each chromosome represents a tour of cities, i.e. ordered list  
 of integers.  
 Eg: 1, 3, 5, 2, 4 → cities.  
 I Fitness Function:  

$$\text{Fitness} = -(\text{Total Distance} + \text{Constraint Penalty})$$
 U Actual distance + penalty added due to  
 H constraint violation  
 I Population:  
 Permutation of cities.  
 Ensure cities does not repeat.  
 L Selection:  
 Tours with higher fitness value for reproduction. We may use  
 Roulette / Tournament Selection method.  
 P Crossover:  
 Combining two parent chromosomes to create new offspring.  
 We may either use, Ordered Crossover / Partially Mapped  
 crossover for this.  
 M Mutation:  
 H Introducing small random changes to maintain diversity  
 in the population and avoid premature convergence.  
 Swap mutation - Randomly swap two cities.  
 Inversion mutation - Select two cities and reverse the order.  
 Insert mutation - Remove the city and reinsert it.

- Constraint Handling -  
 Using penalty based approach - As we saw above adding  
 penalty to fitness function.
- Terminating Condition -  
 i) Max. no. of generations reached,  
 ii) No. improvement in best sol", iii) High fitness value is found.