

Work in Classification

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Abstract goes here.

I. INTRODUCTION

The breakthrough ~~observation detection of the binary neutron star (BNS) merger simultaneously in gravitational and electromagnetic (EM) waves~~ the gravitational waves (GWs) generated by a binary neutron star merger (BNS) together with an electromagnetic (EM) counterpart [?] marked a new era of multi-messenger astronomy ~~including for first time gravitational waves (GWs)~~. So far, the LIGO-Virgo-KAGRA (LVK) Collaboration [?] has reported the observation of such merger, GW170817 [?] with its EM counterpart GRB170817A/AT2017gfo [?], and also GW190425 [?], but in this last case no EM counterpart was detected. The event GW170817 gave answers to open questions, such as the origin and production of gamma-ray bursts (*cite), the production of heavy elements during a merger of BNS (*cite), rule out Equations of State (EoS) (*cite) and alternative theories of gravity (*cite), +?. Such simultaneous observations are crucial for a variety of scientific fields, like astrophysics, particle physics, cosmology, and therefore the necessity to coordinate them successfully emerges. Among the challenges that this attempt brings is the early alert of the EM telescopes/facilities from the GW detectors. Some of the expected sources to produce an EM counterpart are the ~~coalescences of binary compact objects (CBCO)~~ compact binary coalescences (CBC), such as a neutron star with another neutron star (NSNS) or with a black hole (NSBH). In the case of a NSNS coalescence: GRBs, neutron star. For NSBH: accretion disk -> short GRBs. [MMT: need to develop this more.]

Numerical relativity (NR) simulations can provide accurate information about the coalescence of the binary system and its aftermath/remnant. However, these

simulations are computationally expensive and require a lot of time, making them inappropriate to alert follow-up EM searches. It is important to alert the EM ground and space telescopes quickly and accurately. (For example in the event of 2017 the EM telescopes were informed after ... *ref?)

In the previous observing runs in LIGO and Virgo there were used different matched-filtering pipelines in low latency in order to detect GWs from CBCO, such as the GstLAL-based inspiral pipeline (GstLAL) [?], the PyCBCLive [?], the MBTAOnline [?].+? During the second observing run O2 it was the first time that real-time data was made available to EM observatories to support follow-up observations. Classification of the binary systems was performed according to the following probabilities: the probability that at least one of the objects in the binary is a NS, $p(\text{HasNS})$ and the probability that there will be a matter remnant $p(\text{HasRemnant})$. For instance, in a BNS merger both probabilities will be equal to one, while in a binary black hole (BBH) merger, both probabilities will be zero. In [?] the authors approach the problem as binary classification and develop a new method based on supervised learning.

In this work, we revisit and extend the problem of classification in low-latency. First, we propose the use of a combined probability of whether there is a NS in the event and whether there is a remnant. By doing so, we exclude the unphysical situation of having a larger probability of having a remnant than having a NS (like in *ref?). In addition, we perform a thorough study of different algorithms, perform several tests and account for different EoSs. We provide a direct comparison between the methods we used, as well as the ones already implemented e.g. in Deep *ref.

Different methods of classification were considered, such as ... and were tested for the same data. Here, we present the ones that performed best, the Random Forest (RF) and KNeighborClassifier (KNN). The last one is also used in [?] and thus we provide a direct comparison.

The structure of the paper is as follows. In Section 2 there is a detailed description of the data used, as well as the labeling introduced. In Section 3, the classification methods, namely Random Forest and KNN

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are presented.

II. DATASET AND LABELING

In this section, we discuss the data conditioning process our study. The data we use for training and testing are the same injections during O2 as in [REF Deep’s paper], also aiming to predict the probability of a detected event of having a neutron star (HasNS) and/or a remnant object (HasREM) that could emit an electromagnetic counterpart. As we utilize supervised ML techniques, we first label the data accordingly.

HasNS is considered true if $m_{2ij} < 3M_{\odot}$ as in [REF]. For HasREM and following [REF] we use the Focault formula for the remnant mass and if the result is greater than 0 we label the event as true. However, this formula depends on the Equation of State (EoS) as it utilizes the compactness of the NS. The injections used in our study utilize the 2H EoS, but we relabel the data with a different one as explained later, as the EoS used for labelling the training data will affect the ability of predicting correctly a real event.

Predicting the presence of a NS and the creation of a remnant object like this requires a binary classifier for each of the two tasks. We employ a new approach that utilizes the relationship between HasNS and HasREM to train a single multilabel classifier. We relabel the data into 3 mutually exclusive categories: label 0 if there is no NS and no remnant, label 1 if there is a NS but no remnant, and label 2 if there are both. Our labelling is summarized in table ???. This labeling eliminates the possibility of an unphysical classification of the event, where $p(\text{HasREM}) > p(\text{HasNS})$, as there is no category for HasREM but no NS.

As the categories are mutually exclusive, $p(0) + p(1) + p(2) = 1$. Therefore, $p(\text{HasREM}) = p(2)$ and for the NS, $p(\text{hasNS}) = p(\text{hasNS and hasREM} \cup \text{hasNS and no hasREM}) = p(2 \cup 1) = p(2) + p(1) = 1 - p(0)$. This approach allows us to use a single classifier while avoiding any unphysical classifications without further treatment of the data or the output.

| HasNS | HasRem | Our label |
|-------|--------|-----------|
| 0 | 0 | 0 |
| 1 | 0 | 1 |
| 1 | 1 | 2 |

TABLE I. Labelling adopted for classification of having a NS and having a remnant with the same classifier

In order to avoid conditioning the results of HasREM too heavily to the equation of state (EOS) selected for training, we labeled the dataset with the 23 EOS selected by the LIGO-Virgo collaboration in [ref] for studies of neutron stars. These EOS cover a wide parameter space, making together a robust estimation for the neutron star composition.

An algorithm was trained for each of the 23 EOS and predictions were obtained. The final prediction provided is a weighted average between the results of all of them, with the weights determined by the Bayes factor of each EoS, as explained in [ref2]. This approach allows for the consideration of multiple EOS and their relative likelihoods, resulting in a more robust and accurate prediction.

III. CLASSIFICATION ALGORITHMS

A. K-Nearest Neighbors (KNN)

One of the non-parametric algorithms we have used for classification is the `KNeighborsClassifier` (KNN). This algorithm assumes that similar things are near to each other. It captures the idea of similarity by computing the distance between points in a graph. It is also a lazy learning algorithm, because it does not have a training phase, it uses all the data for training while classification -the dataset is stored and at the time of classification, it acts on the dataset.

The workflow of the KNN algorithm is the following: first, after splitting the data into training and testing sets, we need to select the number of neighbors, K , which can be any integer. Then, for each point of the testing dataset we compute the distance between the point and each row of the training data with a chosen metric (`euclidean`, `manhattan`, `chebysev`, `mahalanobis`), and we sort the points in ascending order based on the distance value. By choosing the top K neighbors from the sorted array, we assign a class to the test point, which is the most frequent class of the chosen neighbors.

B. Random Forest (RF)

A RF is an ensemble of decision trees. One of its major strengths is that every train trains and classifies independently from the rest, while the RF classification joints all the results and assign as category the mode from the trees. The probability of belonging to a category is therefore straightforward, being the number of trees that chose it divided by the total number of trees. Notice that the training and evaluation of a RF can be accelerated by parallelization, as computations inside each tree are independent from the rest.

The training of a RF is usually done with bootstrap, a technique that assigns a random subset of the training dataset to each tree. This prevents overfitting as every individual classifier is not exposed to the same data, and encourages pattern recognition by studying the same data from different subsets. Every decision tree is composed by nodes, where data is splitted until the different categories are separated. At each node, a subset of the features of the data is selected along threshold values that maximize the information gain at the separation. The binary splitting

at each node gives the tree its name, as it can be visualized as roots going deeper at separations.

We use the RK implementation in scikitlearn [?]. The main hyperparameters to tune in this module are the number of trees, the maximum depth allowed and the information gain criteria used at splitting (two are offered). We have observed that the maximum number of features to be considered in a node can be kept fix as the square root of the total number of features. Given that the aiming of this work is to improve the current low latency classification, the model once trained can occupy a restricted amount of memory. Therefore before searching the optimum hyperparameters for our dataset, we restrict those which make heavier models: the number of trees and their depth. We set to 300 the maximum number of trees the forest may have, and 45 their possible maximum depth.

For the RF we use events with 5 features: the two masses, their corresponding spins and the SNR of the detection. In the tuning of the hyperparameters we measure the performance by its score: the number of events correctly classified against the total number of events in the testing dataset, if threshold is taken as 0.5. As all categories are balanced, this approach is enough to roughly compare models. The best model found achieves a score of *whatever* using *number* of trees, *number* maximum depth and *name* criteria for the information gain.

IV. RESULTS

In order to decide which method gives a better performance in classifying this kind of events, we can apply them over testing data and finally do a comparison between both. A way to see how data is classified we can construct histograms where the number of events that are classified with a label (`HasNS/HasRemnant`) `True` or `False` will change with a given threshold of the probability. For an algorithm with perfect performance, all the events with label `True` (`False`) should be at $p(\text{label}) = 1$ ($p(\text{label}) = 0$).

Another way to check the algorithm's performance is by building the so-called *Receiver Operating Characteristic (ROC) Curve*. They show the variation of the true-positive rate (or efficiency) with the false-positive rate given a certain threshold for the probability. An algorithm with a proper performance will give a steeper ROC curve, or in other words, will have a higher efficiency with a lower false-positive rate.

In the ROC curves that we will present in the following subsections, we highlight three reference EoS in color, from which we show results in more detail. We select BHF_BBB2 because is the model that give the lowest maximum mass, MS1_PP as the model with the bigger maximum mass, and we also include SLy because is the most accepted EoS for NS modeling (reference), and is the one that was used in the injections that are our dataset.

| EOS | Score | $K_{\text{neighbors}}$ | Bayes Factor |
|----------|-------|------------------------|--------------|
| APR4 EPP | 0.953 | 10 | 1.526 |
| BHF BBB2 | 0.951 | 8 | 1.555 |
| H4 | 0.941 | 10 | 0.056 |
| HQC18 | 0.950 | 10 | 1.422 |
| KDE0V | 0.951 | 8 | 1.177 |
| KDE0V1 | 0.949 | 10 | 1.283 |
| MPA1 | 0.951 | 14 | 0.276 |
| MS1 PP | 0.948 | 12 | 0.001 |
| MS1B PP | 0.947 | 11 | 0.009 |
| RS | 0.945 | 10 | 0.176 |
| SK255 | 0.946 | 10 | 0.179 |
| SK272 | 0.945 | 10 | 0.156 |
| SKI2 | 0.943 | 12 | 0.108 |
| SKI3 | 0.943 | 12 | 0.107 |
| SKI4 | 0.949 | 10 | 0.330 |
| SKI5 | 0.945 | 9 | 0.025 |
| SKI6 | 0.949 | 10 | 0.288 |
| SKMP | 0.948 | 10 | 0.290 |
| SKOP | 0.948 | 10 | 0.618 |
| SLy | 0.950 | 10 | 1.000 |
| SLY2 | 0.950 | 10 | 1.028 |
| SLY9 | 0.949 | 10 | 0.370 |
| SLY230A | 0.950 | 10 | 0.932 |

TABLE II.

Here are the results for both methods:

A. KNN Results

We apply cross validation in order to fix the different hyperparameters of the algorithm. To do so, we compute the score over a range of different parameters. We consider a number of neighbors between 1 and 20; the different metrics we test are the `euclidean`, `manhattan` and `cityblock`; the algorithms to compute the nearest neighbors can be `BallTree`, `KDTree` and the brute-force search, and the possible weight functions are the uniform weights (all points are weighted equally) and the `distance` weights (points are weighted by the inverse of their distance).

Considering all these possibilities, we apply the `cross_val score` function from `scikit-learn` using a 10-fold cross validation to all the 23 datasets with different EOS. We find that the optimal metric, algorithm and weights are the same for all the EOS, being the `manhattan` metric, the `BallTree` algorithm (with a leaf size of 30) and the `distance` weights. The only parameter that differs is the number of neighbors, that goes from 8 to 12. One can find the optimal hyperparameters and the corresponding score for each EOS in Table ???. Doing an average weighting by the Bayes factor of each EOS, we finally get an optimal number of neighbors of 10. The mean score from the cross validation goes from 0.941 (for H4 EOS) to 0.953 (for APR4 EPP), as one can see in Table ??.

Considering now the SLy EOS, the model with these parameters gives a confusion matrix that is shown in

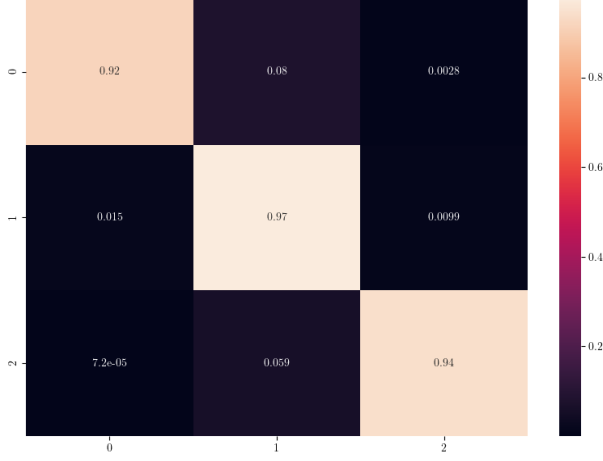


FIG. 1. Confusion matrix SLy KNN

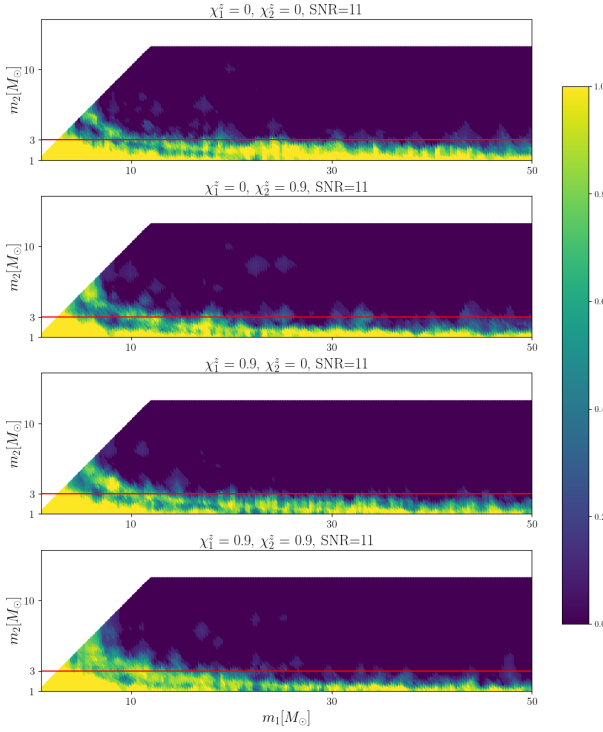


FIG. 2. Parameter sweep NS SLy KNN

Fig. ???. The probability of having a NS as a function of m_1 and m_2 is shown in Fig. ??. There are no big differences with different values of the spins, but the most remarkable one is that the model classifies better for 0-spin values, especially when m_1 is large. There is also a dependence of the probability of having a remnant on the value of the spin that can be seen in Fig. ??. This dependence is correct, since the probability of having a remnant increases for large values of m_1 at larger spin, but this dependence is given by the EOS.

In Figs. ??, ?? and ?? we depict the histograms of the probabilities $p(\text{HasNS})$ ($p(\text{HasRemnant})$) for injections

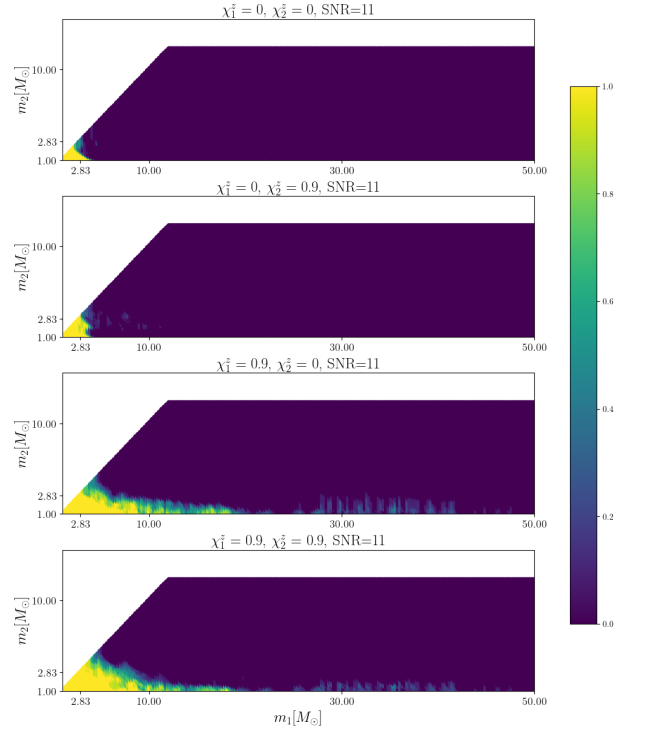


FIG. 3. Parameter sweep REM SLy KNN

of binaries that had a NS (EM counterpart) and for those that not, for the EOS BHF BB2, MS1 PP and SLy, respectively.

We show in Fig. ?? the ROC curves of the classifier for the two different probabilities we consider. All the EOS are depicted in this figure, but we highlight three cases: BHF BBB2, MS1 PP and SLy.

B. RF Results

We apply crossvalidation in the number of trees and depth of the forests for the 23 EoS, fixing the information gain criteria to **entropy**. We also save the second best option for comparison, and save both forests for each EoS in order to compare the file size. As the goal is to provide a model that can run in a low latency pipeline the amount of memory it can take is limited, even more when there will be 23 different model for the EoS generalization.

In table ?? we present a summary of best and second best hyperparameters found in the crossvalidation for each EoS, along the memory the model occupies and the difference in the score. As we can see, usually a forest with many trees has a second best option with far less that is lighter in memory and achieves a similar performance. The optimum maximum depth is always 15. Also the score achieved for every EoS is similar, and so we check that our accuracy is not NS model dependent.

To simplify the model and according to the results of crossvalidation, we train the final forests for all EoS

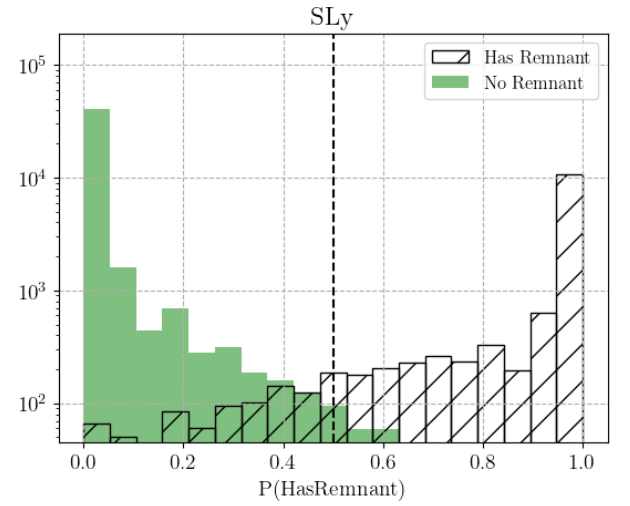
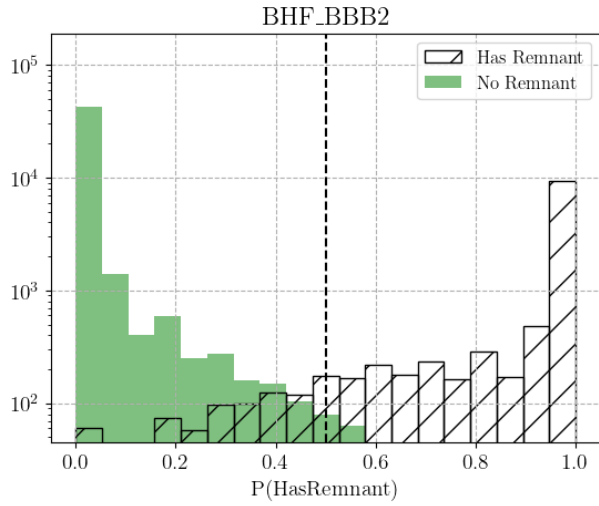
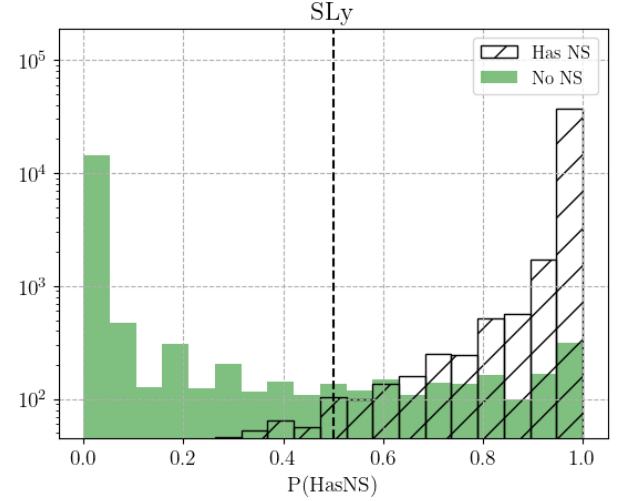
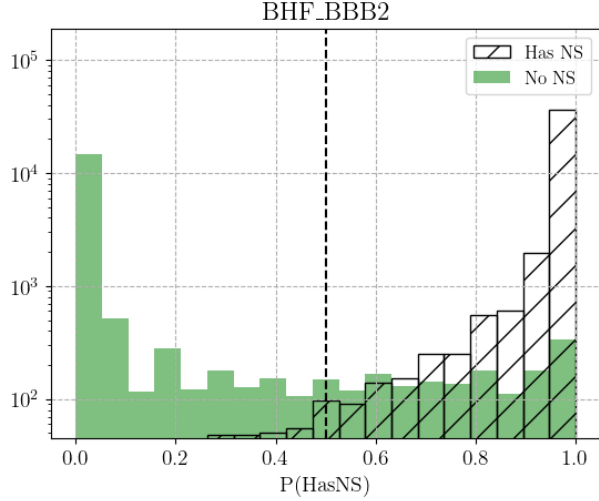


FIG. 4. Histograms BHF BBB2 KNN

FIG. 5. Histograms SLy KNN

with 50 trees and 15 maximum depth. In figure ?? we show the ROC curves for all models to give an idea of the performance. Notice that HasREM performs better than HasNS. The ourperformance of HasREM against HasNS in RF is even more noticeable in the histograms in figures ??, ?? and ?? for the highlighted EoS, where the bars of assigned probabilities do not intersect each other and therefore there exists a threshold value for perfect classification in the testing dataset.

C. Algorithm comparison

To compare quantitatively the results from RF and KNN we compute the true positive and false positive rate for several threshold values, for both HasNS and HasREM, for the three selected EoS. These are tables ??, ?? and ?. For HasNS the two algorithms perform similarly, with almost the same TP for all threshold values and accross EoSs, although the false positive is smaller always in the

RF. For HasREM we obtain that RF performs better than KNN in every case, with not only a smaller false positive rate, but a greater true positive rate.

V. CONCLUSIONS

Reiterate why what we did is important and how it improves current knowledge.

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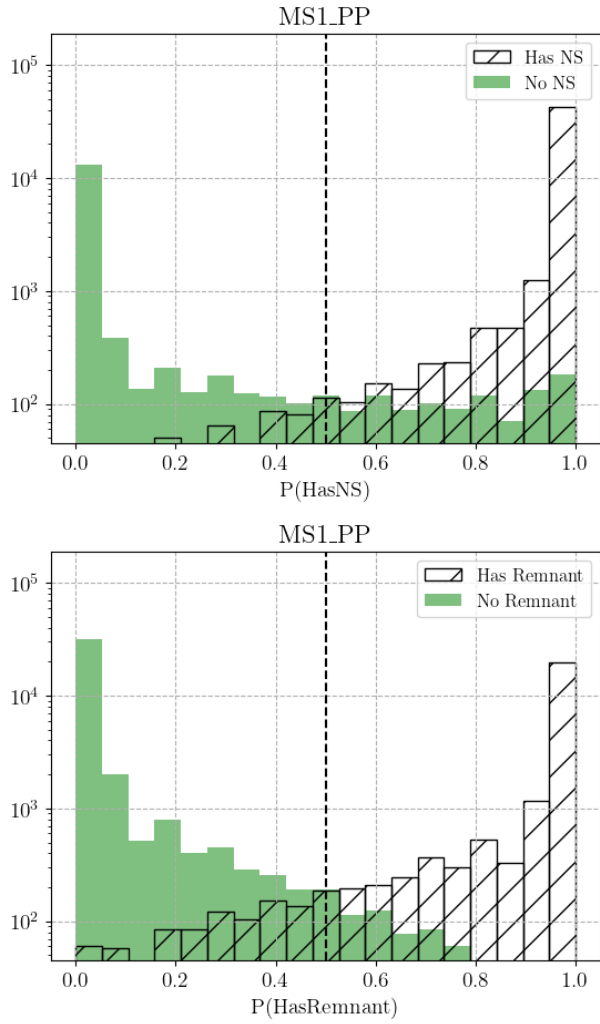


FIG. 6. Histograms MS1 PP KNN

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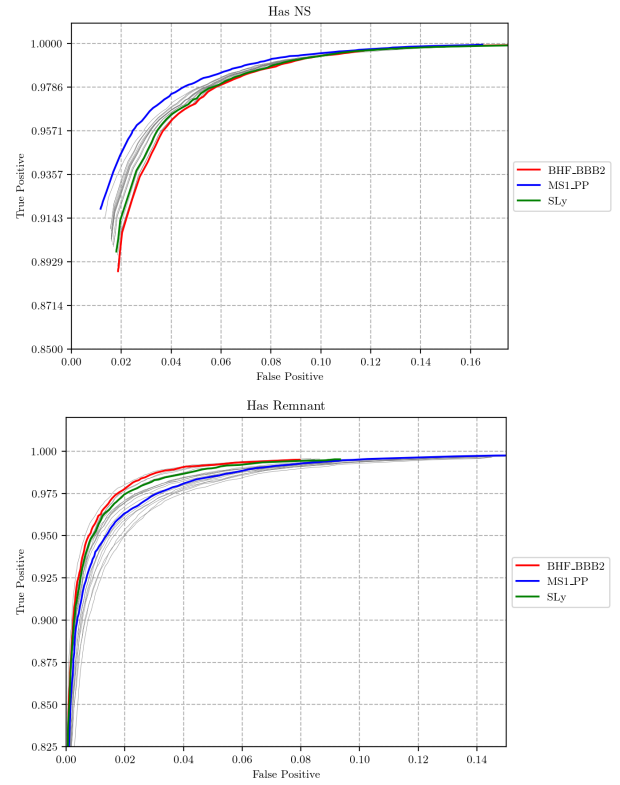


FIG. 7. ROC curves KNN

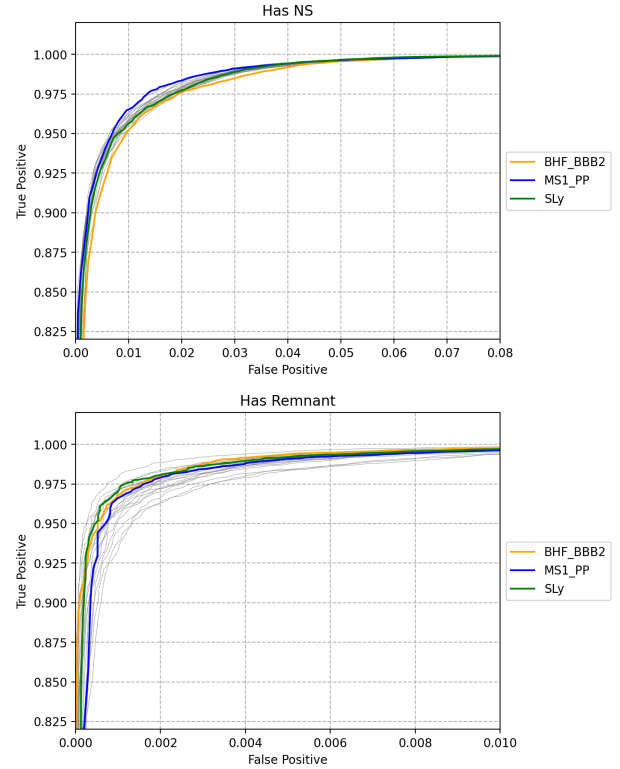


FIG. 8. ROC curves

| Best | | | | | Second | | |
|----------|-------|-------|----------|------------|--------|-------|------|
| EOS | Trees | Depth | Size(MB) | Score | Trees | Depth | Size |
| APR4_BB | 300 | 15 | 94.7 | 0.9683018 | 50 | 15 | 1 |
| BHF_BBB2 | 80 | 15 | 24.4 | 0.9685127 | 300 | 15 | 9 |
| H4 | 80 | 15 | 29.6 | 0.9618587 | 300 | 15 | 1 |
| HQC18 | 300 | 15 | 93.7 | 0.9673755 | 100 | 15 | 3 |
| KDE0V | 300 | 15 | 92.0 | 0.9673295 | 80 | 15 | 2 |
| KDE0V1 | 100 | 15 | 30.9 | 0.96704954 | 80 | 15 | 2 |
| MPA1 | 80 | 15 | 27.2 | 0.96601225 | 300 | 15 | 10 |
| MS1_PP | 300 | 15 | 113.5 | 0.96563534 | 80 | 15 | 3 |
| MS1B_PP | 300 | 15 | 114.2 | 0.96555340 | 100 | 15 | 3 |
| RS | 300 | 15 | 103.8 | 0.96447350 | 80 | 15 | 2 |
| SK255 | 300 | 15 | 105.8 | 0.96472405 | 100 | 15 | 3 |
| SK272 | 300 | 15 | 109.0 | 0.96401816 | 100 | 15 | 3 |
| SKI2 | 50 | 15 | 18.8 | 0.96242338 | 300 | 15 | 1 |
| SKI3 | 50 | 15 | 19.0 | 0.96174537 | 100 | 15 | 3 |
| SKI4 | 300 | 15 | 100.6 | 0.96598969 | 30 | 15 | 1 |
| SKI5 | 100 | 15 | 38.2 | 0.96343381 | 80 | 15 | 3 |
| SKI6 | 300 | 15 | 101.7 | 0.96586928 | 30 | 15 | 1 |
| SKMP | 300 | 15 | 100.2 | 0.96544567 | 80 | 15 | 2 |
| SKOP | 100 | 15 | 32.3 | 0.96610459 | 300 | 15 | 9 |
| SLy | 80 | 15 | 25.3 | 0.96728884 | 300 | 15 | 9 |
| SLY2 | 100 | 15 | 31.8 | 0.96745868 | 80 | 15 | 2 |
| SLY9 | 300 | 15 | 101.6 | 0.96605993 | 100 | 15 | 3 |
| SLY230A | 300 | 15 | 95.5 | 0.96714915 | 100 | 15 | 3 |

TABLE III. Comparison of the best and second best RF models obtained during crossvalidation for all EoS. We show the file size in MB of the forest, and the difference in score between the two options.

| Threshold | Has NS | | | | Has REM | | | |
|-----------|--------|-------|-------|-------|---------|-------|-------|-------|
| | RF | | KNN | | RF | | KNN | |
| | TP | FP | TP | FP | TP | FP | TP | FP |
| 0.1 | 0.999 | 0.107 | 0.999 | 0.156 | 0.998 | 0.011 | 0.992 | 0.051 |
| 0.3 | 0.998 | 0.068 | 0.996 | 0.117 | 0.993 | 0.005 | 0.974 | 0.017 |
| 0.5 | 0.994 | 0.042 | 0.991 | 0.088 | 0.985 | 0.003 | 0.937 | 0.006 |
| 0.8 | 0.967 | 0.014 | 0.966 | 0.043 | 0.957 | 0.001 | 0.845 | 0.001 |

TABLE IV. BHF_BB2

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All plots were made using the python package `matplotlib` [?].

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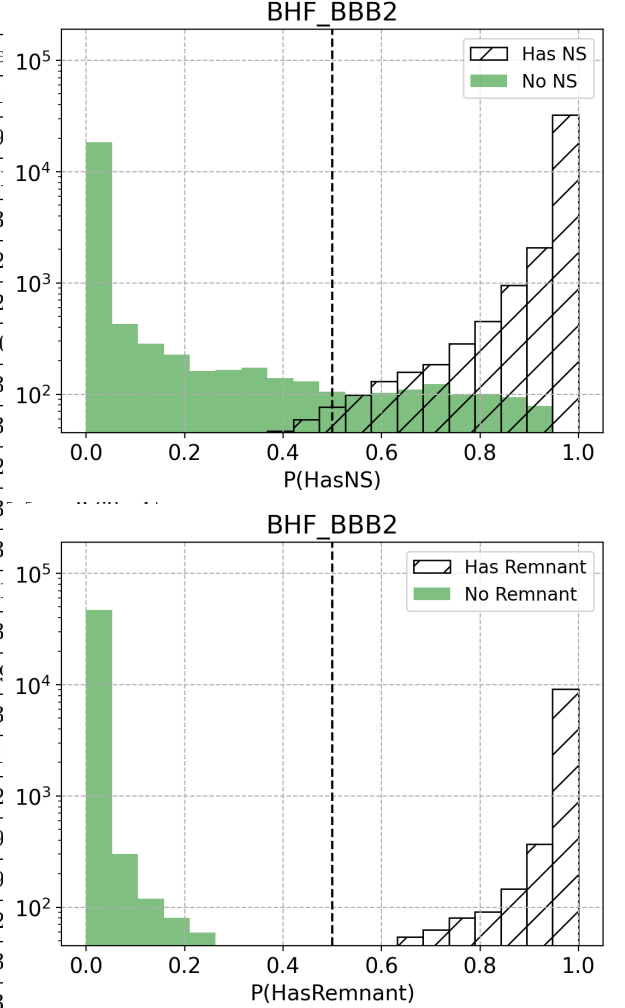


FIG. 9. Histograms BHF BBB2

| Threshold | Has NS | | | | Has REM | | | |
|-----------|--------|-------|-------|-------|---------|-------|-------|-------|
| | RF | | KNN | | RF | | KNN | |
| | TP | FP | TP | FP | TP | FP | TP | FP |
| 0.1 | 1.000 | 0.114 | 0.999 | 0.138 | 0.999 | 0.023 | 0.995 | 0.103 |
| 0.3 | 0.998 | 0.065 | 0.995 | 0.097 | 0.996 | 0.010 | 0.983 | 0.044 |
| 0.5 | 0.994 | 0.036 | 0.989 | 0.068 | 0.990 | 0.004 | 0.961 | 0.019 |
| 0.8 | 0.968 | 0.011 | 0.967 | 0.031 | 0.967 | 0.001 | 0.899 | 0.004 |

TABLE V. MS1_PP

| Threshold | Has NS | | | | Has REM | | | |
|-----------|--------|-------|-------|-------|---------|-------|-------|-------|
| | RF | | KNN | | RF | | KNN | |
| | TP | FP | TP | FP | TP | FP | TP | FP |
| 0.1 | 1.000 | 0.107 | 0.999 | 0.155 | 0.998 | 0.013 | 0.992 | 0.059 |
| 0.3 | 0.999 | 0.064 | 0.996 | 0.112 | 0.993 | 0.005 | 0.974 | 0.020 |
| 0.5 | 0.994 | 0.038 | 0.990 | 0.084 | 0.986 | 0.003 | 0.940 | 0.007 |
| 0.8 | 0.965 | 0.012 | 0.965 | 0.040 | 0.958 | 0.001 | 0.848 | 0.001 |

TABLE VI. SLy

Control Center number LIGO-P22XXXXX.

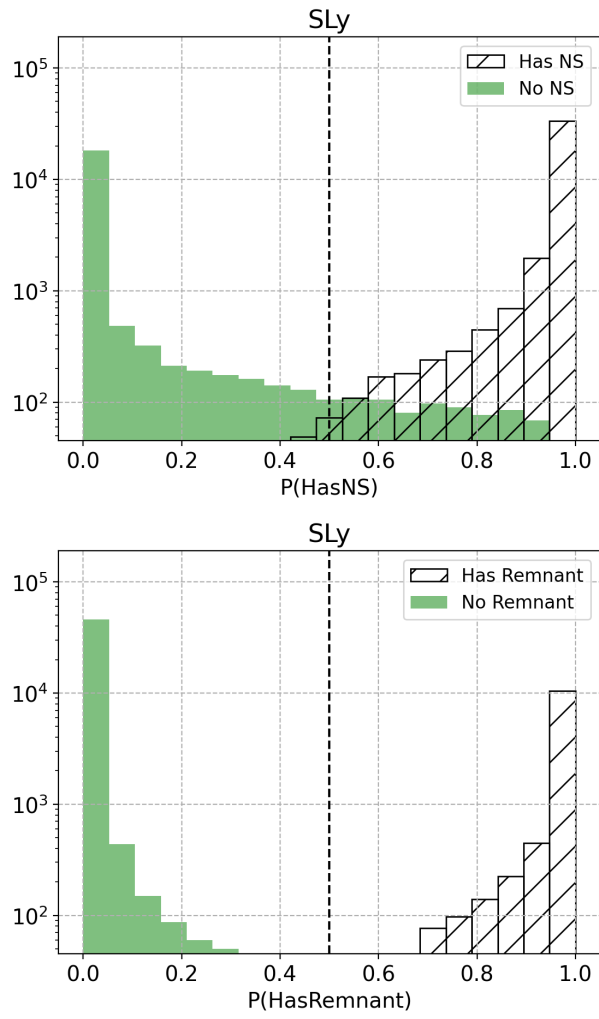


FIG. 10. Histograms SLy

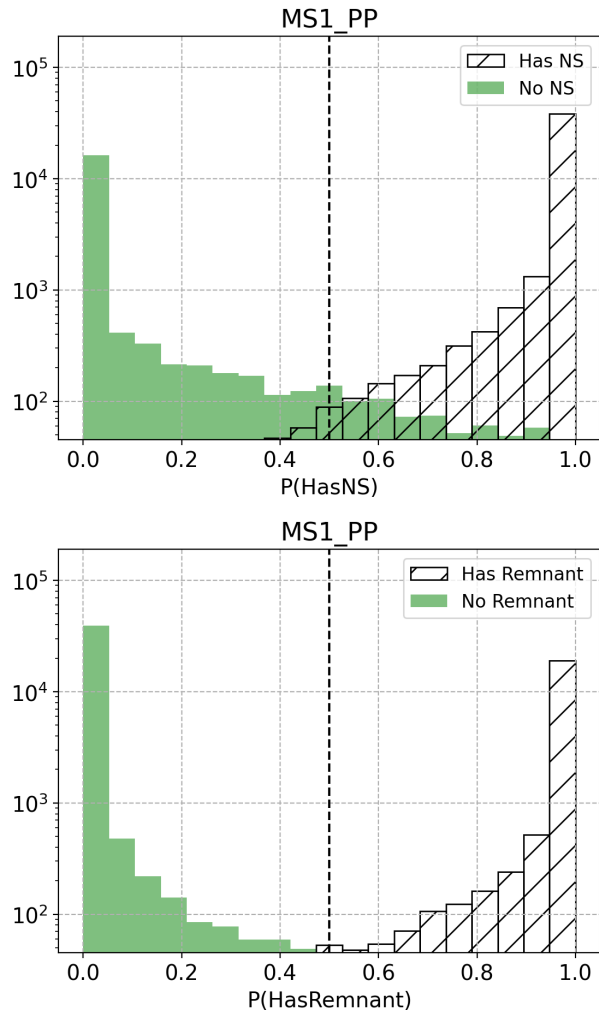


FIG. 11. Histograms MS1 PP