

Activation function

Reference

<https://www.zhihu.com/question/22334626>

https://en.wikipedia.org/wiki/Activation_function

Definition

The activation function of a node defines the output of that node given an input or set of inputs.

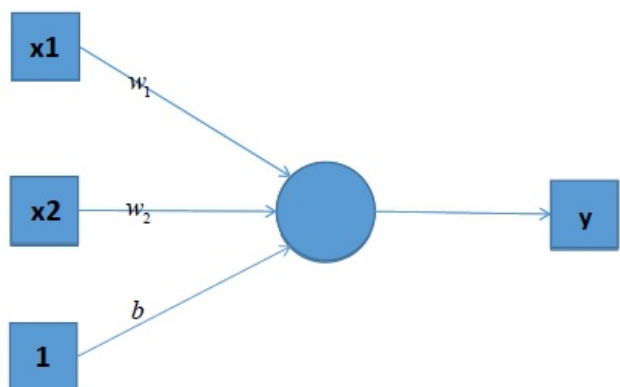
Why do we need it?

为什么说activation function能实现非线性的分类？

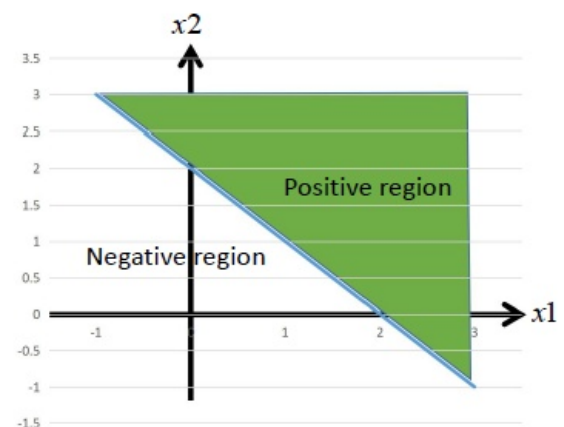
没有hidden layer的神经网络 --- 线性划分

这是一个单层的感知机, 也是我们最常用的神经网络组成单元啦. 用它可以划出一条线, 把平面分割开。

Perceptron



$$y = w_1x_1 + w_2x_2 + b$$



$$w_1 = 1, w_2 = 1, b = -2$$

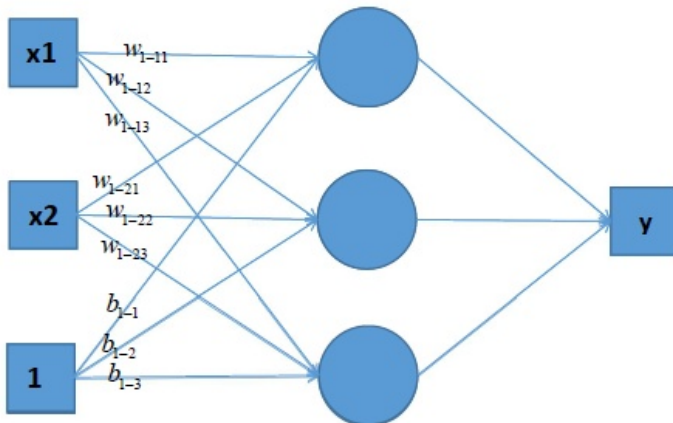
single layer perceptron is a linear classifier

推广到全连接

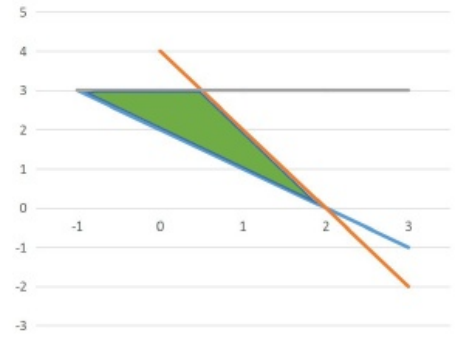
那么很容易地我们会想用多个感知机来进行组合, 获得更强的分类能力:

Perceptron

single layer perceptron is a linear classifier



linear combination of three decision lines



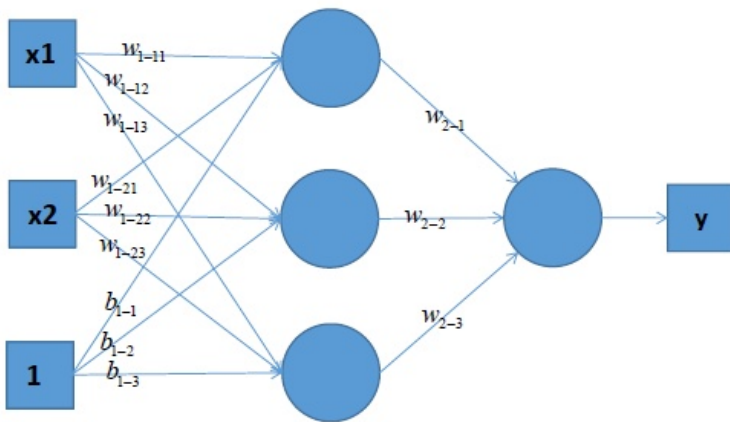
$$w_{1-11} = 1, w_{1-12} = 1, b_{1-1} = -2$$

$$w_{1-21} = 2, w_{1-22} = 1, b_{1-2} = 4$$

$$w_{1-31} = 0, w_{1-32} = 1, b_{1-3} = 3$$

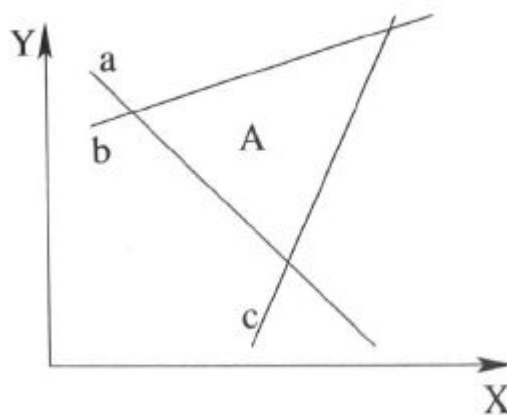
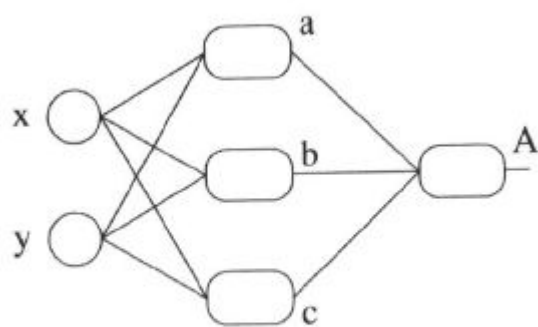
如果加上隐藏层(不管加上多少层), 分类器还是线性的

Perceptron with one hidden layer



$$y = w_{2-1}(w_{1-11}x_1 + w_{1-21}x_2 + b_{1-1}) + w_{2-2}(w_{1-12}x_1 + w_{1-22}x_2 + b_{1-2}) + w_{2-3}(w_{1-13}x_1 + w_{1-23}x_2 + b_{1-3})$$

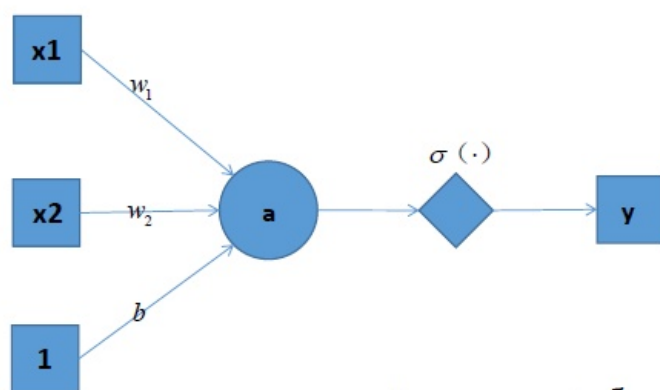
当然你可以说我们可以用无限条直线去逼近一条曲线啊! 额,当然可以,不过比起用non-linear的activation function来说就太萌了!



with step activation function

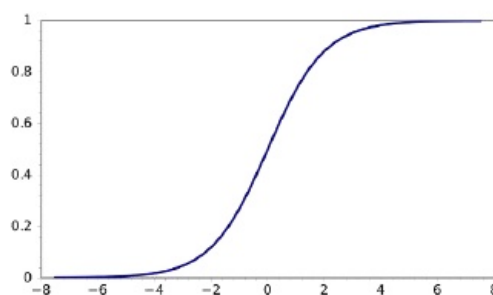
每一层叠加完了以后, 加一个激活函数

Perceptron with non-linear activation function



$$a = w_1 x_1 + w_2 x_2 + b$$

$$y = \sigma(a)$$

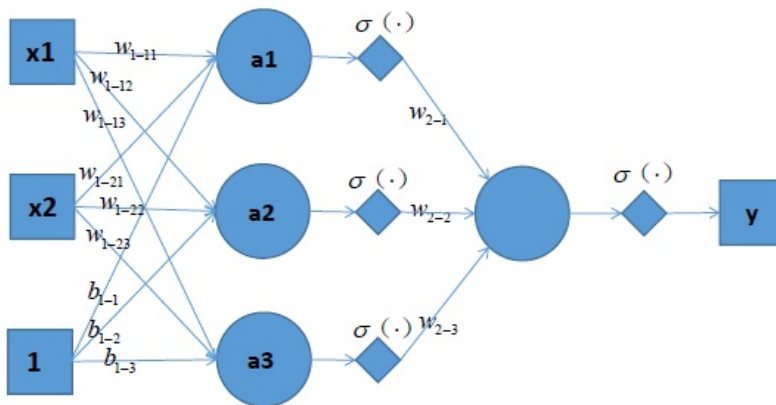


$\sigma(\cdot)$ is a non-linear activation function, sigmoid was the most popular one,

$$\sigma(y) = \frac{1}{1 + e^{-y}}$$

复杂一点

Perceptron with non-linear activation function



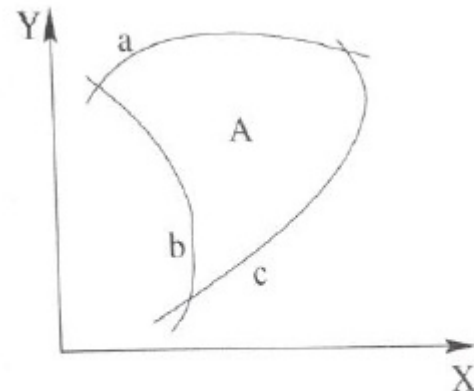
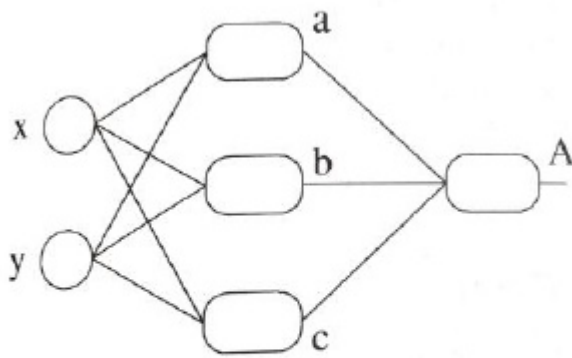
$$a1 = w_{1-11}x_1 + w_{1-21}x_2 + b_{1-1}$$

$$a2 = w_{1-12}x_1 + w_{1-22}x_2 + b_{1-2}$$

$$a3 = w_{1-13}x_1 + w_{1-23}x_2 + b_{1-3}$$

$$y = \sigma(w_{2-1}\sigma(a1) + w_{2-2}\sigma(a2) + w_{2-3}\sigma(a3))$$

加上非线性激活函数之后, 我们就有可能学习到这样的平滑分类平面。



with sigmoid activation function

Most common use activation functions

sigmoid

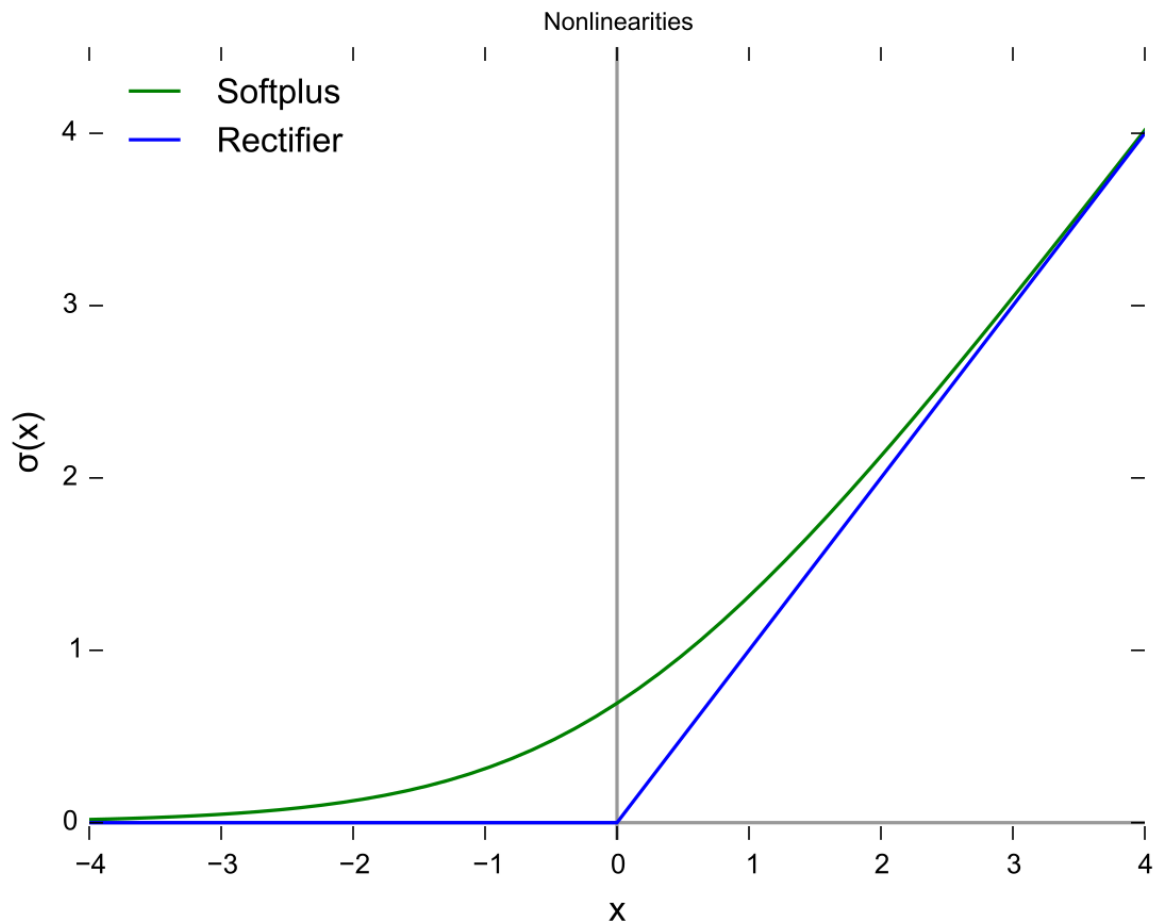
See in 02-Classification.md Sigmoid Function.

ReLU 整流线性单位函数 (Rectified Linear Unit, ReLU)

The rectifier is an activation function defined as the positive part of its argument:

$$f(x) = \max(0, x)$$

where x is the input to a neuron.



When $x=0$, $f(x)$ is not differentiable.

Thus, we have this **softplus or SmoothReLU function**.

$$f(x) = \ln(1 + e^x)$$

The Derivative is $f'(x) = \frac{1}{1 + e^{-x}}$, logistic function.

TanH (hyperbolic tangent)

$$\tanh(x) = \sinh(x)/\cosh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

