

Example: Attribute Selection with Information Gain

□ Class P: buys_computer = “yes”

□ Class N: buys_computer = “no”

$$Info(D) = I(9,5) = -\frac{9}{14} \log_2\left(\frac{9}{14}\right) - \frac{5}{14} \log_2\left(\frac{5}{14}\right) = 0.940$$

age	p_i	n_i	$I(p_i, n_i)$
≤ 30	2	3	0.971
31...40	4	0	0
> 40	3	2	0.971

age	income	student	credit_rating	buys_computer
≤ 30	high	no	fair	no
≤ 30	high	no	excellent	no
31...40	high	no	fair	yes
> 40	medium	no	fair	yes
> 40	low	yes	fair	yes
> 40	low	yes	excellent	no
31...40	low	yes	excellent	yes
≤ 30	medium	no	fair	no
≤ 30	low	yes	fair	yes
> 40	medium	yes	fair	yes
≤ 30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
> 40	medium	no	excellent	no

$$Info_{age}(D) = \frac{5}{14} I(2,3) + \frac{4}{14} I(4,0) + \frac{5}{14} I(3,2) = 0.694$$

$\frac{5}{14} I(2,3)$ means “age ≤ 30 ” has 5 out of 14 samples, with 2 yes’es and 3 no’s.

Hence **4/14**

$$Gain(age) = Info(D) - Info_{age}(D) = 0.246$$

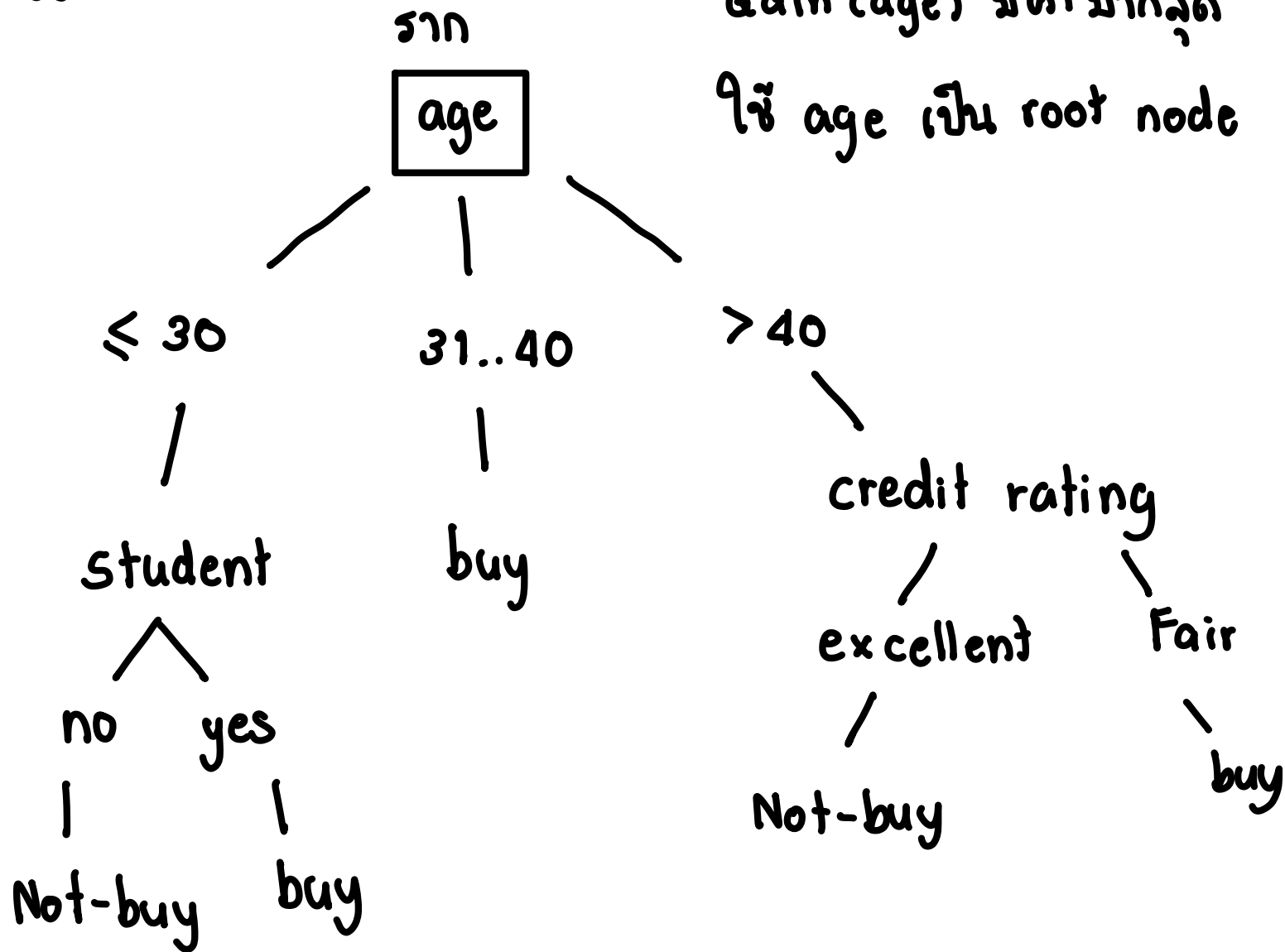
Similarly, we can get

$$Gain(income) = 0.029$$

$$Gain(student) = 0.151$$

$$Gain(credit_rating) = 0.048$$

Resulting tree :



$$I(3,2) = - \left(\frac{3}{5} \log_2 \frac{3}{5} + \frac{2}{5} \log_2 \frac{2}{5} \right)$$

$$= 0.9710$$

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$$\text{Info}(D) = (8,4) = -\frac{8}{12} \log_2 \left(\frac{8}{12} \right) - \frac{4}{12} \log_2 \left(\frac{4}{12} \right)$$

$$\text{Info}(D) = 0.9183$$

$$\text{Info}_{\text{age}}(D) = \frac{4}{12} I(2,2) + \frac{3}{12} I(3,0) + \frac{5}{12} I(3,2) = 0.738$$

$$\text{Gain}(\text{age}) = \text{Info}(D) - \text{Info}_{\text{age}}(D) = 0.9183 - 0.738 = 0.1803$$

$$\text{Info}_{\text{income}}(D) = \frac{4}{12} I(2,2) + \frac{3}{12} I(2,1) + \frac{5}{12} I(4,1) = 0.863$$

$$\text{Gain}(\text{income}) = 0.0553$$

$$\text{Info}_{\text{student}}(D) = \frac{6}{12} I(3,3) + \frac{6}{12} I(5,1) = 0.825$$

$$\text{Gain}(\text{student}) = 0.0933$$

$$\text{Info}_{\text{credit_rating}}(D) = \frac{6}{12} I(3,3) + \frac{6}{12} I(5,1) = 0.825$$

$$\text{Gain}(\text{credit_rating}) = 0.1703$$

เลือก $\text{Gain}(\text{age})$ เพราะมีค่ามากที่สุด คือ 0.1803 #