

Networks and Community Detection

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Abstract





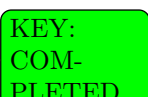
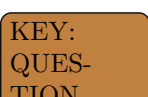
Networks are a great model for analysing and understanding real world complex systems. A very important feature of these network models is *community detection*. Community detection allows us to identify clusters in the network that are well connected amongst eachother. If a network is being used to model a real world system then finding this structure has many implications about the behaviour of the system. This essay will discuss multiple methods for community detection in networks and their applications to the analysis and understanding of real world complex systems.

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1 Introduction to Networks

Networks in the technical sense are analogous to networks in the nontechnical sense - a collection of objects paired with a number of connections that can link any two objects. *Networks: An Introduction* by Mark Newman lists *Technological Networks*, *Social Networks*, *Information Networks* and *Biological Networks* as different systems that are modelled by the technical interpretation of a network.[New10, Contents]. A brief example of a network would be something like the following: Imagine you and a number of people you speak to regularly are represented as dots (nodes or vertices) on a piece of paper. Then if any two people are friends, the dots representing those people are connected by a line (edge). If you then repeat this process by asking your acquaintances to list all their friends and so on, you will end up with a simple model of a *social network*.

SEC: Introduce Network Theory

Now that we have this model it's easy to be curious about any structure that emerges that we can detect and abuse to develop an understanding of the real world system that we are representing. The structure that this essay will explore is that of *communities*. Vaguely speaking, communities are subsets of a network that are *densely connected* amongst themselves. I.e. there is some notion of any node within a community being more closely connected to other nodes in the community than nodes outside the community in the average case. Before we dive into the details of communities and detecting them, I wish to provide some motivation by way of example of the kinds of situations that networks can arise and why they are the natural model for the related systems.

1.1 Social Networks

To better illustrate the simple notion of a social network mentioned above, I will introduce the canonical community detection example of *Zachary's Karate Club*. Zachary's Karate Club is a dataset where "The data was collected from the members of a university karate club by Wayne Zachary in 1977. Each node represents a member of the club, and each edge represents a tie between two members of the club." [kon17, Metadata]. In Figure 1, there are two different renderings of the Zachary Karate Club. Figure 1a shows the network rendered using a "spring" layout (which is a type of force directed graph drawing[Kob12]) and figure 1b shows the network rendered using a "circle" layout. These different layouts show us different parts of the underlying structure of the network. For example, in Figure 1a, it's clear which nodes in the network have the highest degree and which are of lower degree. It also allows you to see some of the community structure in the network. Meanwhile, in Figure 1b, it's much easier to see the which nodes edges in the network would need to be removed to disconnect the network in a minimal way. The reason this dataset is the canonical example of community detection is that the question that comes with it is the following: Suppose two members of the club have a disagreement which causes the club to split in two. How does the club split? In Zachary's original paper on the topic *An Information Flow Model for Conflict in Small Groups*[Zac77] he uses community detection techniques to predict how the network will split after the disagreement. Out of 34 people, Zachary correctly predicts how 33 of them will choose a side after the disagreement.

SEC: Models of Networks

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There, of course, exist different ways to represent social networks. The way

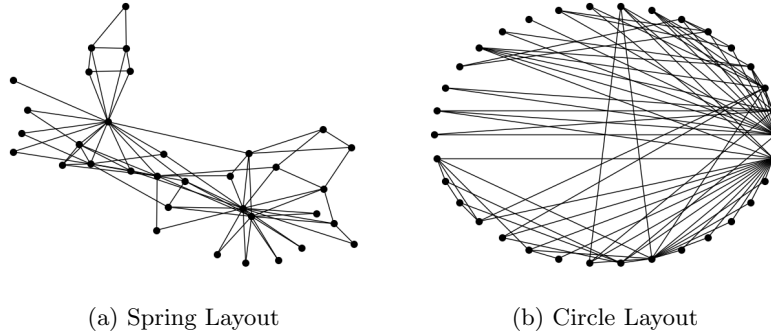


Figure 1: Two renderings of the Zachary Karate Club network using data from KONECT.cc[Kun13] and a Python library NetworkX[HSS08]

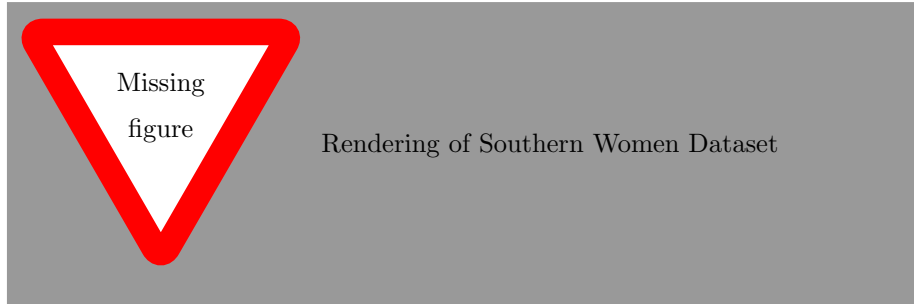


Figure 2: A rendering of the Southern Women Dataset

in which you choose to represent them depends on the question you're trying to answer. For example, one might imagine having two types of nodes in a network. One type of node will represent a person and another type of node will represent an event. An edge is drawn between a person and an event if a person attended a given event and person A is considered connected to person B if they both attended the same event. One such example of this is the *Southern Women Dataset*. [DGG41] This dataset is another example of a community detection problem because after analysis of the data, it was found that women in the group were split into two discrete subgroups.

1.2 Technological Networks

As a result of our intensely and digitally connected world, technological networks are of significant interest to researchers. The easiest example to consider is the Internet. The internet consists of many computers all connected by copper or fibre cables which signals are sent through to transmit data. As one might imagine, in the model, the computers are nodes and the cables are the edges. The internet needs to be robust against software and hardware failures and this is where the idea of community detection can help us. Saying that we want the internet to be robust is the same as saying that we want every node in the

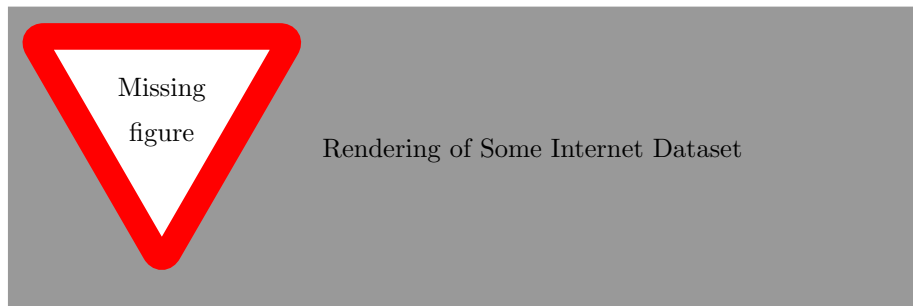


Figure 3: A rendering of the Internet

network to be strongly connected to every other node i.e. the number of possible routes between any two nodes is large. This means that, in the philosophy of community detection, we want the internet to act as one large community rather than multiple smaller communities that are loosely connected. An alternative way of looking at this is that once we've managed to identify the communities, we can then figure out which edges and nodes are the critical ones that allow passage from one community to another. This allows us to reinforce those edges and nodes to reduce the potential for failure.

Yet another example of a technological network would be the UK Power Grid. Network theory is a useful model here as with the UK Power Grid we're trying to solve exactly the same problem as with the internet — we want the system to be robust against hardware or software failures.

1.3 Information Networks

The easiest example of an information network is that which is generated by looking back through the citations on a paper recursively. If Paper A references Paper B, then we will draw a directed edge connecting Paper A to Paper B. This will generate a network that shows which papers are referenced by which other papers and how information is reused. Applying community detection to such a network would show us the different academic working groups and perhaps even different fields or subfields of a subject.

Another example of an information network is the World Wide Web which differs from the internet in that it refers to the webpages hosted on the internet rather than the servers and cables themselves. Mapping the world wide web as a network shows us communities of websites that regularly reference each other.

After this point I couldn't really find anything concrete to relate these things to community detection. Could it be worth removing them?

SEC: Definition of a Network

SEC: Different Types of Network

2 Properties of Networks

SEC: Interesting Properties of Networks

3 Community Detection

SEC: Introduction to Community Detection

SEC: Traditional Methods of Community Detection

SEC: Spectral Methods of Community Detection

4 Applications of Community Detection

SEC: Applications of Community Detection

SEC: Figure out an interesting thing to write some of my own code for

References

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