

The steps of the method:

- Generate data (x) have student distribution.
- Arrange the data in ascending order.
- We calculate $s_j = j/n$, $j = \lceil na \rceil, \dots, \lfloor nb \rfloor$, $a < b$ are fixed constants taken from the interval $(0,1)$.
In my program I take $a = 0.0001, b = 0.4$ where do we get the best results.
Then number value of j it should be $nn = \text{floor}(n * b) - \text{ceil}(n * a) + 1$ and n sample size that you Generate it. In this case we used loop as follows:

```
for jj=1:nn;
s1(jj)=ceil(n*a)+(jj-1);
end
Finally we find  $s_j$  as  $s = s1/n$ 
```

- To clarify the unclear part:
We obtain the regression equations from the following equation:

$$\log Q_n(1 - s_j) = -\alpha \log s_j + \theta_0 + 2 \sum_{k=1}^{\tilde{p}} \theta_k \cos(2\pi k s_j),$$

I take $\tilde{p} = 2$ then the equation becomes

$$\log Q_n(1 - s_j) = -\alpha \log s_j + \theta_0 + 2 \cos(2\pi s) + 2 \cos(4\pi s),$$

we have to calculate the left-hand side, as you see it is Quantile function, we will use the theorem that says:

$$Q_n(s) = X_{k,n} \quad \text{if} \quad \frac{k-1}{n} < s \leq \frac{k}{n}, \quad k = 1, 2, \dots, n.$$

but instead of s we have $1 - s$ (left tail) so

$$\frac{n-k}{n} < s \leq \frac{n+1-k}{n}$$

in my program I take k as ir and $Qn = \text{sort}(x)$

I find it as the following code:

```

for j = 1 : nn
for ir = 1 : n
if(s(j)) > ((n - ir)/n)and(s(j)) ≤ ((n + 1 - ir)/n);
Qt(j) = Qn(ir);
end
end
end

```

- Then $y = \log(Qt)$
- Our estimator is $\hat{\kappa} = e'_1(X'WX)^{-1}X'Wy$, Where X is matrix as $[x_1 \ x_0 \ x_2 \ x_3]$ where x_0 is vector all values are one, $x_1 = -(\log(s))$, $x_2 = (2 * \cos(2 * \pi * s))$, $x_3 = (2 * \cos(4 * \pi * s))$, $W = s$ and $e = [1 \ 0 \ 0 \ 0]$.