

The steps of the method:

- Generate data (x) have student distribution.
- Arrange the data in ascending order.
- We calculate $s_j = j/n$, $j = \lceil na \rceil, \dots, \lfloor nb \rfloor$, $a < b$ are fixed constants taken from the interval $(0,1)$.
In my program I take $a = 0.0001, b = 0.4$ where do we get the best results.
Then number value of j it should be $nn = \text{floor}(n * b) - \text{ceil}(n * a) + 1$ and n sample size that you Generate it. In this case we used loop as follows:

```
for jj=1:nn;
s1(jj)=ceil(n*a)+(jj-1);
end
Finally we find  $s_j$  as  $s = s1/n$ 
```

- Let Q_n be the empirical quantile function defined as

$$Q_n(s) = X_{k,n} \quad \text{if} \quad \frac{k-1}{n} < s \leq \frac{k}{n}, \quad k = 1, 2, \dots, n.$$

I find it as the following code:

```
for j = 1 : nn
for ir = 1 : n
if (s(j)) > ((n - ir)/n) and (s(j)) ≤ ((n + 1 - ir)/n);
Qt(j) = Qn(ir);
end
end
end
```

- Then $y = \log(Qt)$
- Our estimator is $\hat{\kappa} = e'_1 (X'WX)^{-1} X'Wy$, Where X is matrix as $[x_1 \ x_0 \ x_2 \ x_3]$ where x_0 is vector all values are one, $x_1 = -(\log(s))$, $x_2 = (2 * \cos(2 * \pi * s))$, $x_3 = (2 * \cos(4 * \pi * s))$, $W = s$ and $e = [1 \ 0 \ 0 \ 0]$.