

1.5 [4] <§1.6> Consider three different processors P1, P2, and P3 executing the same instruction set. P1 has a 3 GHz clock rate and a CPI of 1.5. P2 has a 2.5 GHz clock rate and a CPI of 1.0. P3 has a 4.0 GHz clock rate and has a CPI of 2.2.

a. Which processor has the highest performance expressed in instructions per second?

Number of instructions per second = Clock Rate / CPI

$$P1: (3 * 10^9) / 1.5 = 2 * 10^9 \text{ IPS}$$

$$P2: (2.5 * 10^9) / 1 = 2.5 * 10^9 \text{ IPS}$$

$$P3: (4 * 10^9) / 2.2 = 1.8 * 10^9 \text{ IPS}$$

=> P2 has the highest performance expressed in instructions per second.

b. If the processors each execute a program in 10 seconds, find the number of cycles and the number of instructions.

Number of cycles = Clock Rate * Execution Time in seconds

$$P1: 3 * 10^9 * 10 = 3 * 10^{10} \text{ cycles}$$

$$P2: 2.5 * 10^9 * 10 = 2.5 * 10^{10} \text{ cycles}$$

$$P3: 4 * 10^9 * 10 = 4 * 10^{10} \text{ cycles}$$

Number of instructions = IPS * Execution Time in seconds

$$P1: 2 * 10^9 * 10 = 2 * 10^{10} \text{ instructions}$$

$$P2: 2.5 * 10^9 * 10 = 2.5 * 10^{10} \text{ instructions}$$

$$P3: 1.8 * 10^9 * 10 = 1.8 * 10^{10} \text{ instructions}$$

c. We are trying to reduce the execution time by 30% but this leads to an increase of 20% in the CPI. What clock rate should we have to get this time reduction?

Clock Rate = Number of instructions * CPI / Execution Time

$$\text{New execution time: } 10 - (30\% * 10 / 100\%) = 10 - 3 = 7 \text{ seconds}$$

New CPI:

$$\text{- P1: } 1.5 + (20\% * 1.5 / 100\%) = 1.8$$

$$\text{- P2: } 1 + (20\% * 1 / 100\%) = 1.2$$

- P1: $2.2 + (20\% * 2.2 / 100\%) = 2.64$

Clock Rate:

(All answers are divided by 10^9 to get GHz)

P1: $[(2 * 10^{10}) * (1.8)] / 7 = 5.143 \text{ GHz}$

P2: $[(2.5 * 10^{10}) * (1.2)] / 7 = 4.286 \text{ GHz}$

P3: $(1.8 * 10^{10}) * (2.64) / 7 = 6.789 \text{ GHz}$

1.6 [20] Consider two different implementations of the same instruction set architecture. The instructions can be divided into four classes according to their CPI (class A, B, C, and D). P1 with a clock rate of 2.5 GHz and CPIs of 1, 2, 3, and 3, and P2 with a clock rate of 3 GHz and CPIs of 2, 2, 2, and 2.

Given a program with a dynamic instruction count of $1.0E6$ instructions are divided into classes as follows: 10% class A, 20% class B, 50% class C, and 20% class D, which implementation is faster?

Execution Time = Number of instructions * CPI / Clock Rate

P1: $10^6 * [(1 * 0.1) + (2 * 0.2) + (3 * 0.5) + (3 * 0.2)] / 2.5 * 10^9 = 1.04 * 10^{-3} \text{ sec} = 1.04 \text{ mili sec}$

P2: $10^6 * [(2 * 0.1) + (2 * 0.2) + (2 * 0.5) + (2 * 0.2)] / 3 * 10^9 = 0.67 * 10^{-3} \text{ sec} = 0.67 \text{ mili sec}$

=> P2 is faster

a. What is the global CPI for each implementation?

Global CPI = Execution Time * clock rate / Number of instructions

P1: $1.04 * 10^{-3} * 2.5 * 10^9 / 10^6 = 2.6$

P2: $0.67 * 10^{-3} * 3 * 10^9 / 10^6 = 2.01$

b. Find the clock cycles required in both cases.

clock cycles = Global CPI * Number of instructions

P1: $2.6 * 10^6$

P2: $2.01 * 10^6$