Hw.

X: feature

Decision Tree

Training data set: Who buys computer?					

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

age:

in come:

	7 - 1	10 0	
< 30	2	3	
3140	4	O	
740	3	2	
high	2	2	
med	4	2	
Low	3	1	
yes	6	1	
Nο	3	5	
0	0	2	

credit ex

Student:

No 3 5

ex 3 3

-air 6 2

Class

1)
$$9u_1$$
 $Closs$ $(9,5)$ $*$
 $2 i_1 i_2 i_3 i_4 i_5 i_5 i_5 i_6 i_6 i_7 i_6 i_7 i_6 i_7 i_8 i_7 i_8$

Info (D) = $\frac{7}{14}$ I (6,1) + $\frac{7}{14}$ I (3,4) student = $\frac{7}{14}$ [- $\frac{6}{7}$ log 2 ($\frac{6}{7}$) - $\frac{1}{7}$ log 2 ($\frac{1}{7}$) + $\frac{7}{14}$ [- $\frac{3}{7}$ log 2 ($\frac{3}{7}$) - $\frac{4}{7}$ log 2 ($\frac{4}{7}$)]

: Info(D) = 0.7883 (student)
student

$$True_{i}(0) = \frac{1}{13} True_{i}(1) = \frac{1}{2} True_{i}(1) = \frac{1}{2} Res_{i}(\frac{1}{2}) = \frac{1}{2} Res_{$$

$$T_{n}f_{0}(0) = \frac{2}{5} T(2,0) + \frac{3}{3} T(0,3)$$

$$= \frac{2}{5} \left[-\frac{2}{2} \log_{2}(\frac{2}{2}) - \frac{2}{5} \log_{2}(\frac{0}{2}) \right] + \frac{3}{5} \left[-\frac{9}{3} \log_{3}(\frac{0}{3}) - \frac{3}{3} \log_{3}(\frac{1}{3}) \right]$$

$$= \frac{2}{5} \left[-\frac{2}{5} \log_{2}(\frac{1}{3}) - \frac{1}{2} \log_{2}(\frac{1}{3}) \right] + \frac{3}{5} \left[-\frac{9}{3} \log_{3}(\frac{0}{3}) - \frac{3}{3} \log_{3}(\frac{1}{3}) \right]$$

$$I_{n}f_{0}(0) = \frac{2}{5} T(1,1) + \frac{3}{3} T(1,2)$$

$$= \frac{2}{5} \left[-\frac{1}{5} \log_{2}(\frac{1}{3}) - \frac{1}{2} \log_{2}(\frac{1}{3}) \right] + \frac{3}{5} \left[-\frac{1}{3} \log_{3}(\frac{1}{3}) - \frac{2}{3} \log_{3}(\frac{2}{3}) \right]$$

$$I_{n}f_{0}(0) = 0.9509 (\text{credit})$$

$$G_{n}in(\text{income}) = 0.971 - 0.4 + 0.5710$$

$$G_{n}in(\text{income}) = 0.971 - 0.4 + 0.5710$$

$$G_{n}in(\text{income}) = 0.971 - 0.7501 = 0.0201$$

$$G_{n}in(\text{income}) = 0.971 - 0.0201$$

$$G_{n}in(\text{income}) = 0$$

$$= -\frac{3}{5} \log_2\left(\frac{3}{5}\right) - \frac{2}{5} \log_2\left(\frac{2}{5}\right)$$

an feature In fo (D) = $\frac{3}{5}$ I (2,1) + $\frac{2}{5}$ I (1,1) $= \frac{3}{5} \left[-\frac{2}{3} \log_2 \left(\frac{1}{3} \right) - \frac{1}{3} \log_2 \left(\frac{1}{3} \right) \right]$ Info (D) = 0.9509 income In fo (D) = $\frac{3}{5}$ I(1,1) + $\frac{2}{5}$ I(1,1) $=\frac{3}{5}\left[-\frac{2}{3}\log_{2}\left(\frac{2}{3}\right)-\frac{1}{3}\log_{2}\left(\frac{1}{3}\right)\right]+\frac{2}{5}\left[-\frac{1}{3}\log_{2}\left(\frac{1}{3}\right)-\frac{1}{3}\log_{2}\left(\frac{1}{3}\right)\right]$ Info (D) = 0.9509 student In fo (D) = $\frac{2}{5}$ I (0, 2) + $\frac{3}{5}$ I (3,0) $=\frac{2}{5}\left[-\frac{0}{2}\log_2\left(\frac{0}{2}\right)-\frac{1}{2}\log_2\left(\frac{2}{2}\right)\right]+\frac{3}{5}\left[-\frac{3}{3}\log_2\left(\frac{3}{3}\right)-\frac{0}{3}\log_2\left(\frac{3}{3}\right)\right]$ Info (D) credit Gain (income) = 0.971 - 0.9509 = 0.0201 Gain (student) = 0.9710 - 0.9509 = 0.0201 Qain (credit_ratting) = 0.971-0 = 0.971 og e 31...40 740 Buy (redit - rating Student yes ex cellent fair Not Buy Buy Not Buy