

# Correlated Insulator and Unconventional Superconductivity in Magic-angle Graphene Superlattice

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Cao Y et al. Nature, 2018, 556(7699): 43.  
Cao Y et al. Nature, 2018, 556(7699): 80.

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- Magnetic Field Response of MA-TBG Superconductivity

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# Moiré Pattern in Twisted Bilayer Graphene

Two layers of lattice with a twist angle generate Moiré pattern and gives rise to superlattice.

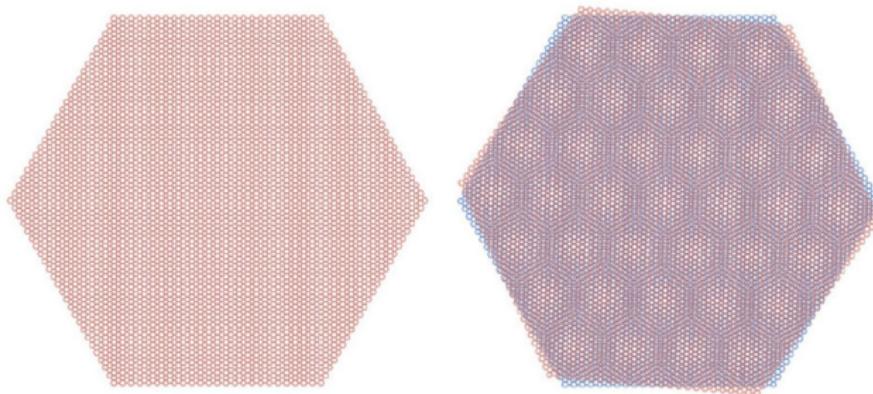


Figure: Pablo Jarillo-Herrero (MIT) at APS March Meeting 2018

Left: Untwisted bilayer graphene retains lattice structure of single layer graphene.  
Right: Moiré pattern in Twisted bilayer graphene generates an extra superlattice.

# Band Structure of Twisted Bilayer Graphene

Low-energy bands become flat when twist angle is close to the magic angles, which leads to localized profile in position space.

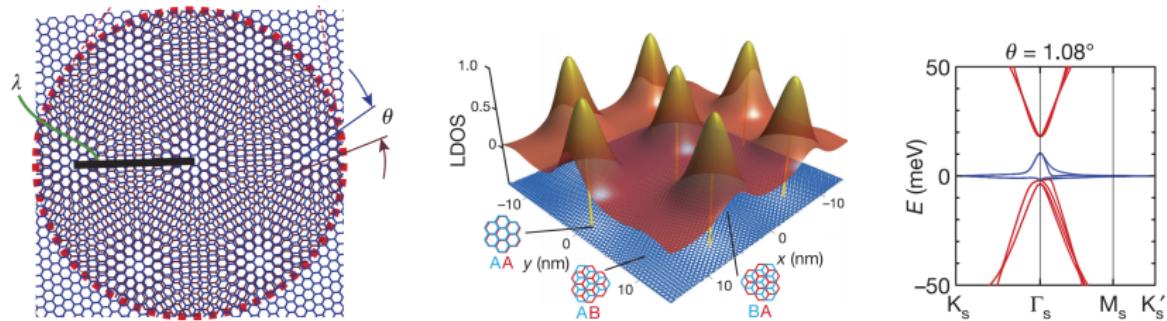


Figure: Cao Y et al. Nature, 2018, 556(7699): 80.

- Left: Superlattice constant  $\lambda = a/[2 \sin(\theta/2)]$  where  $a$  is the graphene lattice constant and  $\theta$  the twist angle.
- Middle: Normalized local density of states calculated for the flat band showing localized profile.
- Right: The band energy of MA-TBG calculated using an *ab initio* tight-binding method.

# Flat Band Created by Interlayer Hybridization

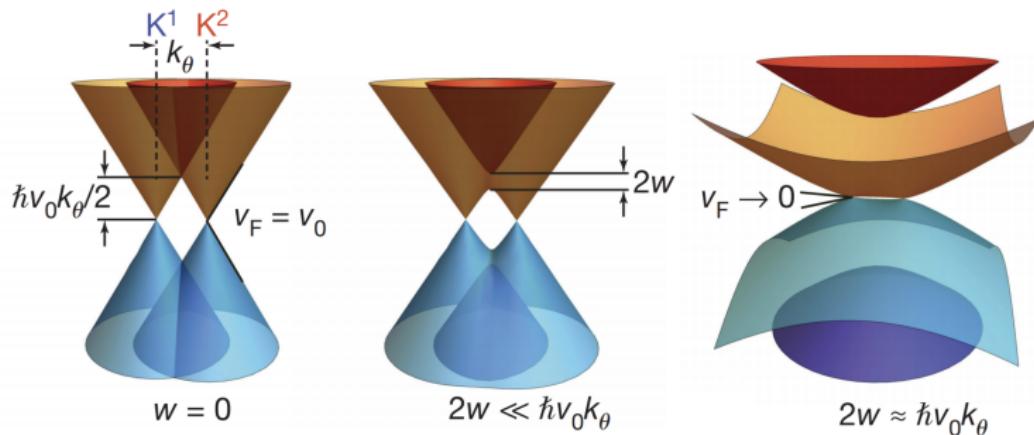


Figure: Cao Y et al. Nature, 2018, 556(7699): 80.

Left: Large twist angle, no interlayer hybridization.

Middle: Large twist angle, hybridization energy  $w$  much smaller than the height of crossing.

Right: Small twist angle, hybridization energy comparable to crossing height, band flattens.

# Band Structure of Twisted Bilayer Graphene

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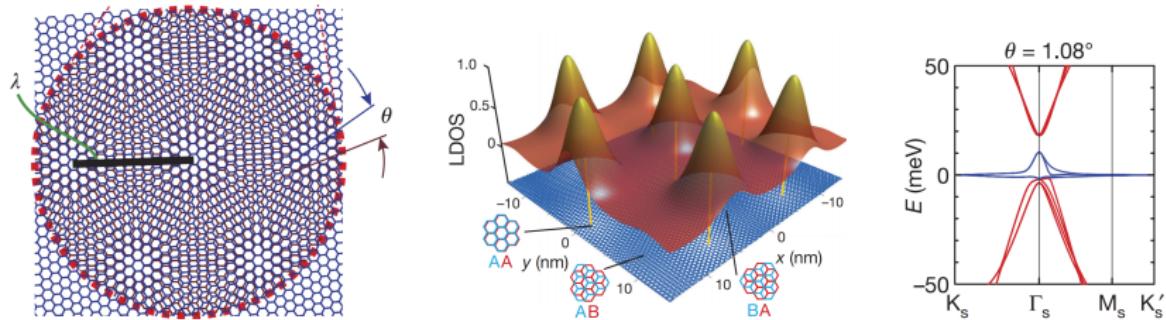


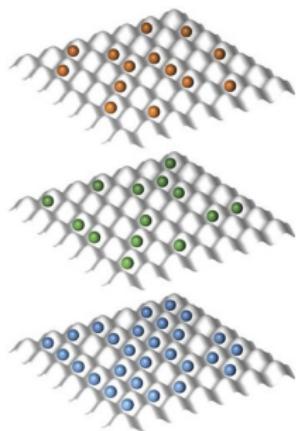
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# Lattice Platforms for Strong Correlated Physics

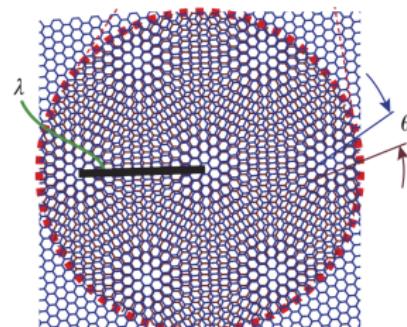
Cold Atom Optical  
Lattice Scale

~ 1 micron



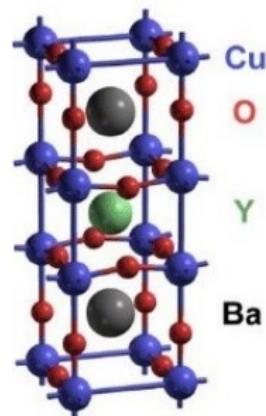
Magic-angle Graphene  
Superlattice Scale

~ 10 nm



Quantum Materials  
Lattice Scale

~ few Å



# New Platform Based on MA-TBG Superlattice

Magic-angle Twisted Bilayer Graphene is highly tunable:

- Electrostatic control of charge density
- Mechanical control of twist angle
- Pressure control of interlayer coupling (and hence magic angle and lattice constant)
- Usual control knobs (voltage, current, temperature, magnetic field ...)
- All the technologies that come with 2D device nanofabrication

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# Insulating Behaviour at Full-filling

When the twist angle is larger than the first magic angle, the system behaves normally.

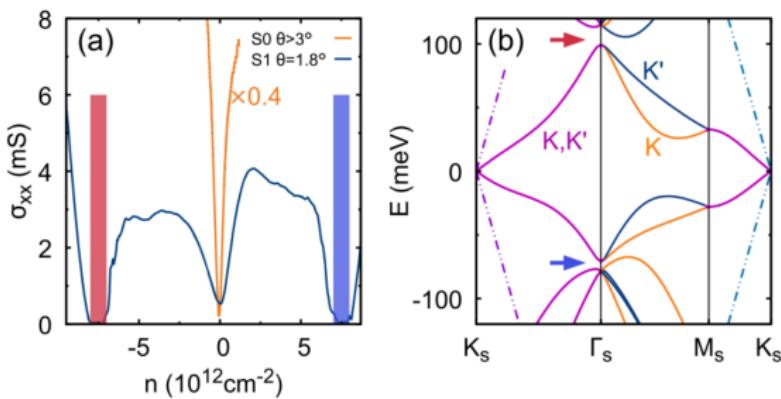


Figure: Cao Y, et al. Physical review letters, 2016, 117(11): 116804.

Left: Dependence of conductance on the charge density. Observe insulating states at full-filling.

Right: Band structure at twist angle  $1.8^\circ$ . No flat bands occur.

# Insulating Behaviour at Half-filling

When twist angle approaches the first magic angle, two new insulating states occur at half-filling.

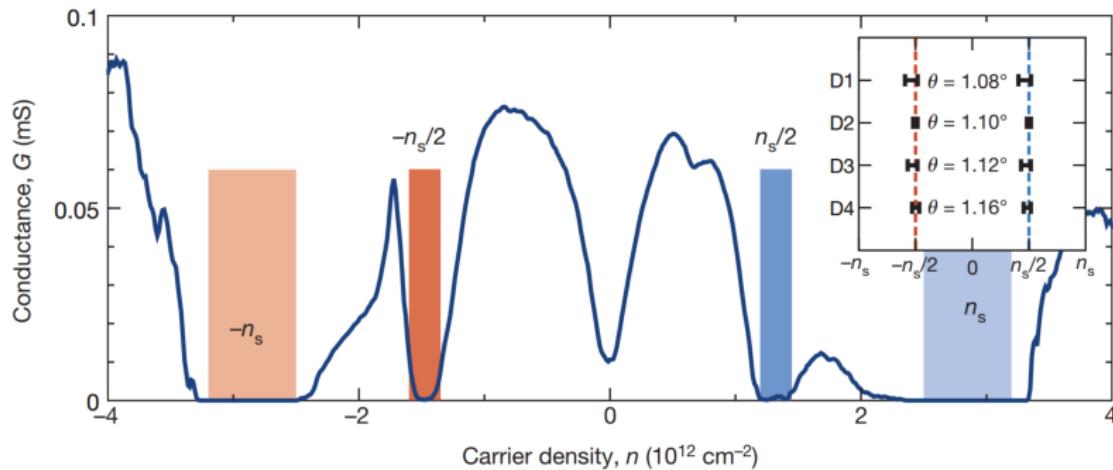


Figure: Cao Y et al. Nature, 2018, 556(7699): 80.

Dependence of conductance on the charge density of magic-angle TBG.  
Observe abnormal insulating states at half-filling.

# Metal-insulator Behaviour in Magic-angle TBG

Insulating states only occur at low temperature, which resembles the correlated Mott insulator.

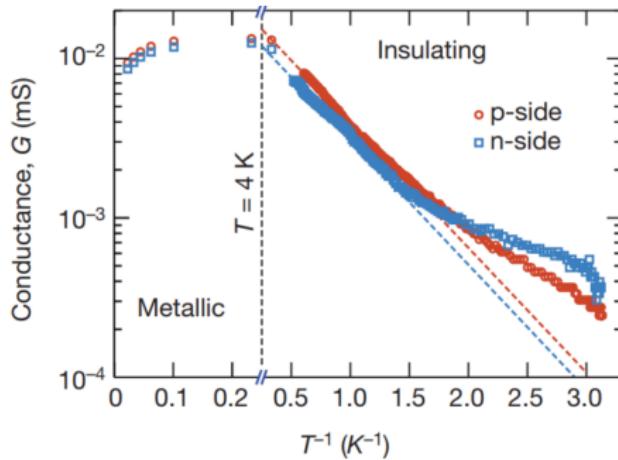


Figure: Cao Y et al. Nature, 2018, 556(7699): 80.

Dependence of conductance on inverse temperature.  
Observe insulating states below temperature 4K.

# Response to Perpendicular Magnetic Field

The insulating state starts conducting after applying a magnetic field (especially when the field is perpendicular).

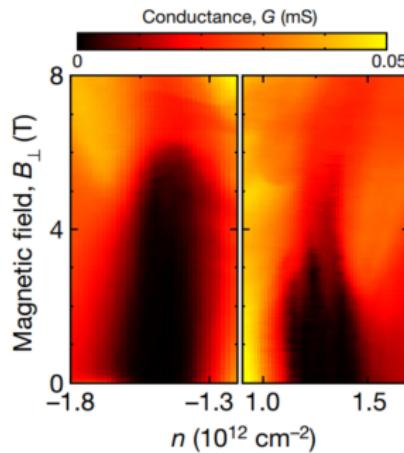


Figure: Cao Y et al. Nature, 2018, 556(7699): 80.

Dependence of conductance on perpendicular magnetic field on (Left)  $p$ -side and (Right)  $n$ -side.

# Response to Perpendicular Magnetic Field

The electron-electron interaction creates band gap and thus the insulating states. The magnetic field provides Zeeman energy which closes the band gap.

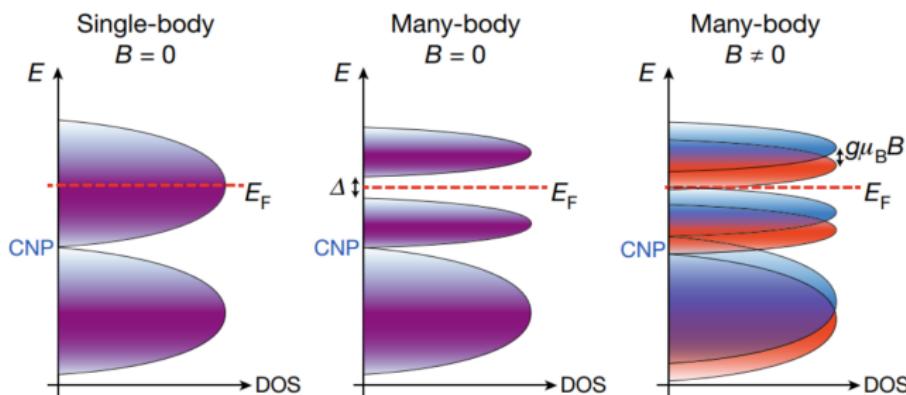


Figure: Cao Y et al. Nature, 2018, 556(7699): 80.

Schematics of the density of states (DOS) in different scenarios.  
CNP, charge neutrality point. The shape is purely illustrative.

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# First Glimpse Towards MA-TBG Superconductivity

The conductivity near the hole-doping insulating states tends to increase with decreasing temperature.

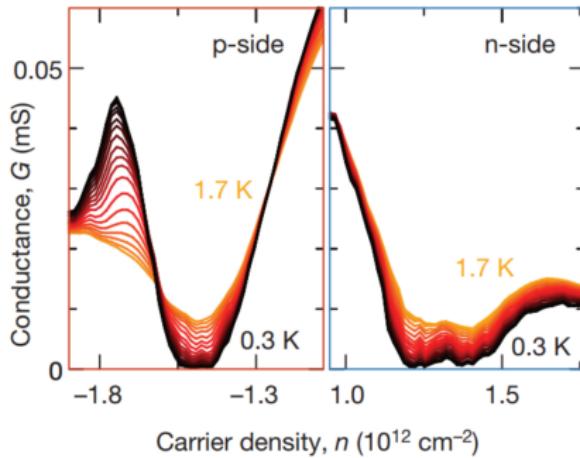
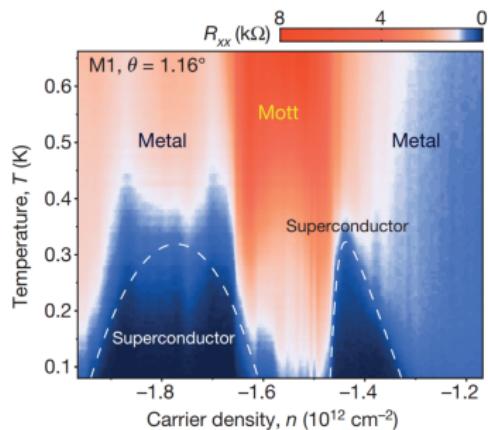


Figure: Cao Y et al. Nature, 2018, 556(7699): 80.

Temperature-dependent conductance for temperatures from about 0.3K (black) to 1.7K (orange) near (Left) *p*-side and (Right) *n*-side.

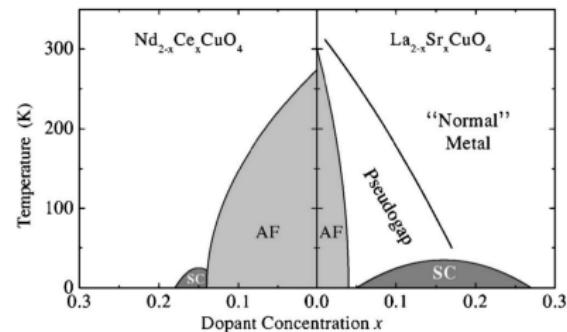
# Unconventional Superconductivity in MA-TBG

Carrier density much lower than conventional superconductor.  
Phase diagram resembles that of high- $T_c$  superconductor.



Cao Y et al. Nature, 2018, 556(7699): 43.

Resistance measured near half-filling densities versus temperature. Two superconducting domes are observed next to the half-filling state.



Lee, Nagaosa & Wen. Rev mod phys, 2006, 78(1): 17.

Schematic phase diagram of high- $T_c$  superconductors showing (right) hole doping and (left) electron doping.

# Magnetic Field Response of Superconductivity

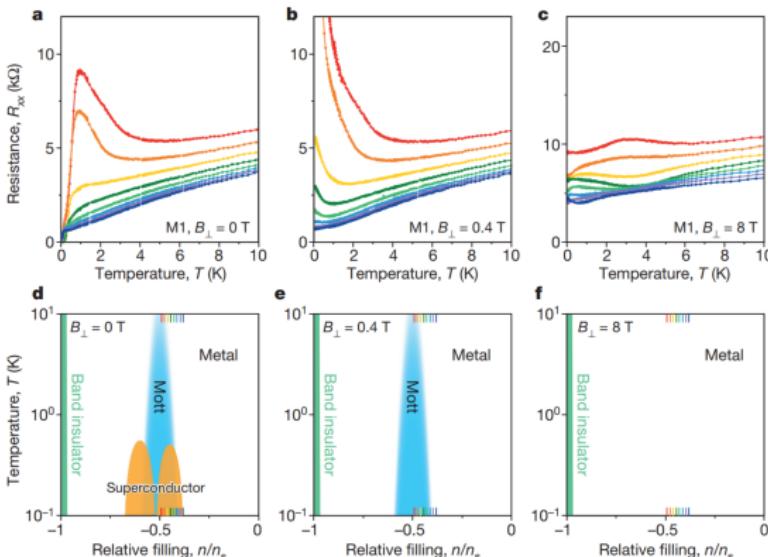


Figure: Cao Y et al. Nature, 2018, 556(7699): 43.

Above: Resistance-Temperature curve at different densities and magnetic fields.  
Below: Temperature-density phase diagrams of magic-angle TBG at different magnetic fields.

# How Strong is MA-TBG Superconductivity

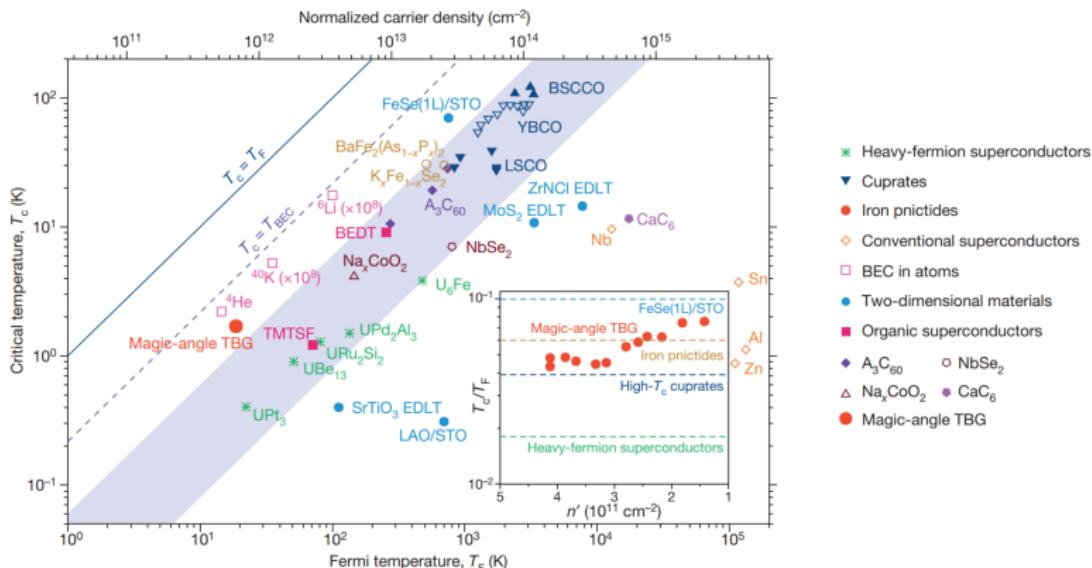


Figure: Cao Y et al. Nature, 2018, 556(7699): 43.

Logarithmic plot of critical temperature  $T_c$  versus Fermi temperature  $T_F$  for various superconductors  
MA-TBG Superconductivity is among the strongest unconventional superconductivity.

# Summary

- Magic-angle graphene superlattices  $\Rightarrow$  System with flat bands in electronic structure
- Highly-tunable platform for correlated electrons physics:
  - Control over carrier density, lattice constants, temperature, magnetic field, etc.
  - Correlated insulating at half-filling
  - Superconducting dome (resembling high- $T_c$  superconductivity)
- Magic-angle concept can be more general  $\Rightarrow$  Many new magic-angle 2D material superlattices waiting to explore!