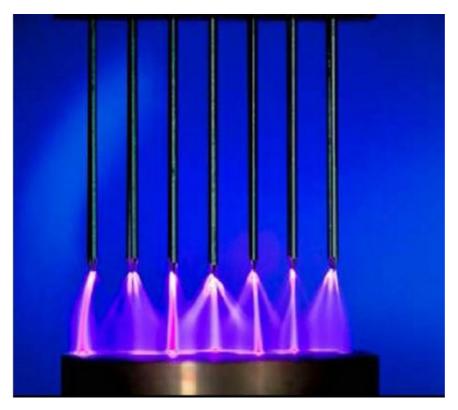
First Draft of IYPT Reference Kit 2019

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This reference kit is based on my internet searches and knowledge. Here, all the figures are from Google website. Although, it is not a comprehensive and exact solutions for the problems, but it can be considered as a background reading and an initial point for student researches. Please feel free to contact me if you have any comment or question.



1. Invent Yourself

Build a simple motor whose propulsion is based on corona discharge. Investigate how the rotor's motion depends on relevant parameters and optimize your design for maximum speed at a fixed input voltage.

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- https://www.youtube.com/watch?v=9THGyOzMXjo
- https://www.youtube.com/watch?v=WkmH2ECctzw
- https://www.youtube.com/watch?v=4zKrphJmHnQ
- https://www.youtube.com/watch?v=fEQYa7tCujg
- https://www.youtube.com/watch?v=Hfj50Jixt0A
- https://www.youtube.com/watch?v=RsvnfzmVVr4
- https://www.youtube.com/watch?v=f8JguqFxpZ4



2. Aerosol

When water flows through a small aperture, an aerosol may be formed. Investigate the parameters that determine whether an aerosol is formed rather than a jet for example. What are the properties of the aerosol?

- https://en.wikipedia.org/wiki/Aerosol
- https://en.wikipedia.org/wiki/Spray nozzle
- http://elte.prompt.hu/sites/default/files/tananyagok/AtmosphericChemist ry/ch09s02.html
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 No. PNNL-21367 Rev. 1. Pacific Northwest National Lab.(PNNL), Richland, WA (United States), 2013. https://www.osti.gov/servlets/purl/1133999
- https://webspace.clarkson.edu/projects/crcd/public_html/me437/downloa ds/P_Aerosol_Meas_Suresh.pdf
- Colbeck, Ian. Physical and chemical properties of aerosols. Blackie Academic and Professional, 1998.
- https://www.youtube.com/watch?v=fRqqNa5vyPk



3. Undertone Sound

Allow a tuning fork or another simple oscillator to vibrate against a sheet of paper with a weak contact between them. The frequency of the resulting sound can have a lower frequency than the tuning fork's fundamental frequency. Investigate this phenomenon.

- https://en.wikipedia.org/wiki/Fundamental-frequency
- https://en.wikipedia.org/wiki/Tuning_fork
- Knapman, Herbert. "An Experiment Illustrating Harmonic
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- http://moodle.wmchs.net/mod/resource/view.php?id=5392
- http://www.answers.com/Q/What_happens_when_you_tuning_fork_touche
 s_paper
- https://www.quora.com/What-occurs-when-paper-is-touched-with-a-tuning-fork



4. Funnel and Ball

A light ball (e.g. ping-pong ball) can be picked up with a funnel by blowing air through it. Explain the phenomenon and investigate the relevant parameters.

- https://en.wikipedia.org/wiki/Bernoulli%27s principle
- https://en.wikipedia.org/wiki/Coand%C4%83 effect
- http://www.abc.net.au/science/surfingscientist/pdf/teachdemo 6.pdf
- http://www.csun.edu/scied/4-discrpeant-event/discrep_events/index.htm
- https://teachingfluids.wordpress.com/2013/12/04/levitating-a-ping-pong-ball-in-a-funnel/
- https://airport.unimelb.edu.au/science/physlog/vote.php?entry=2
- http://practicalphysics.org/bernoulli-effect-demonstration.html
- http://spmphysics.onlinetuition.com.my/2013/06/experiments-related-to-bernoullis.html
- https://www.123homeschool4me.com/2016/02/anti-gravity-ping-pong-ball-science_9.html
- http://www.thecrazyscientist.com/looney-lab/experiments-2/amazing-air/superhuman-breath-2/
- http://physicscentral.com/experiment/physicsquest/upload/Turbulent-Times-Extension-Activities.pdf
- http://www.academia.edu/download/36868099/Bernoulli_s_Principle_Disp utation_2015g_doc.pdf
- https://www.youtube.com/watch?v=nsnMt8erxH8
- https://www.youtube.com/watch?v=1TQL1ju3RoQ
- https://www.youtube.com/watch?v=K80xbb82sMQ
- https://www.youtube.com/watch?v=wuAUJPUupfE
- https://www.youtube.com/watch?v=n7U0H05Kduw

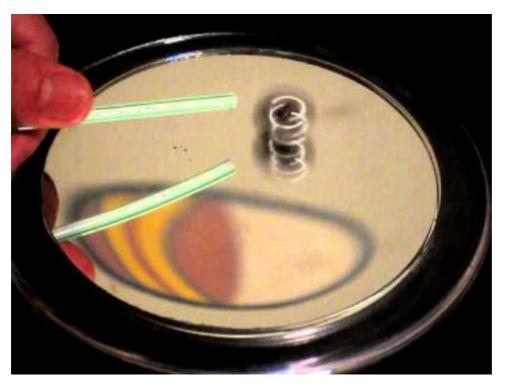


5. Filling Up a Bottle

When a vertical water jet enters a bottle, sound may be produced, and, as the bottle is filled up, the properties of the sound may change. Investigate how relevant parameters of the system such as speed and dimensions of the jet, size and shape of the bottle or water temperature affect the sound.

- https://en.wikipedia.org/wiki/Acoustic resonance
- https://en.wikipedia.org/wiki/Splash (fluid mechanics)
- Franz, G. J. "Splashes as sources of sound in liquids." *The Journal of the Acoustical Society of America* 31.8 (1959): 1080-1096.
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- Velasco, Carlos, et al. "The sound of temperature: What information do pouring sounds convey concerning the temperature of a beverage." *Journal of Sensory* Studies 28.5 (2013): 335-345.
 - https://onlinelibrary.wiley.com/doi/abs/10.1111/joss.12052
- Doel, Kees van den. "Physically based models for liquid sounds." ACM
 Transactions on Applied Perception (TAP) 2.4 (2005): 534-546.
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- https://www.quora.com/When-we-fill-a-vessel-with-water-why-does-the-sound-of-the-pouring-change-as-the-level-increases
- https://intelligentsoundengineering.wordpress.com/2017/05/20/why-can-you-hear-the-difference-between-hot-and-cold-water/
- https://www.audioblocks.com/stock-audio/filling-glass-bottle-with-water.html
- https://physics.stackexchange.com/questions/357512/why-the-sound-of-filling-water-into-a-bottle-rise-in-its-frequency
- https://www.youtube.com/watch?v=pVbaRYoSBYk
- https://www.youtube.com/watch?v=ayNzH0uygFw
- https://www.youtube.com/watch?v=X08NDXMvdz0
- http://www.cs.cornell.edu/projects/HarmonicFluids/



6. Hurricane Balls

Two steel balls that are joined together can be spun at incredibly high frequency by first spinning them by hand and then blowing on them through a tube, e.g. a drinking straw. Explain and investigate this phenomenon.

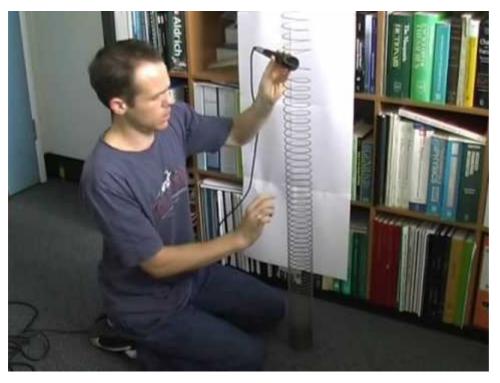
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- Andersen, W. L., and Steven Werner. "The dynamics of hurricane balls." European Journal of Physics 36.5 (2015): 055013.
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- https://makezine.com/projects/remaking-history-louis-poinsot-and-the-dancingspheres/
- https://www.youtube.com/watch?v=rFZrwMPNVvk
- https://aapt.scitation.org/doi/full/10.1119/1.4973116
- https://www.youtube.com/watch?v=cvg8laPb498
- https://www.youtube.com/watch?v=0|58SNJWDt4
- https://www.youtube.com/watch?v=CfaZyEmzlhE



7. Loud Voices

A simple cone-shaped or horn-shaped object can be used to optimize the transfer of the human voice to a remote listener. Investigate how the resulting acoustic output depends on relevant parameters such as the shape, size, and material of the cone.

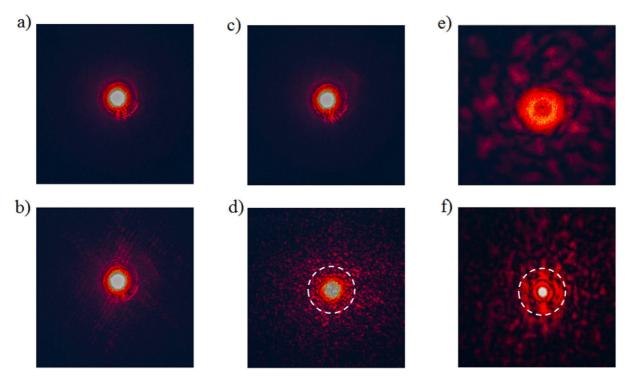
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- Kolbrek, Bjørn. "Horn Theory: An Introduction, Part." Audio Express 1 (2008): 1-8. https://www.rdacoustic.cz/wp-content/uploads/an-introduction-to-horn-theory.pdf
- Jorge, Rogério. "Nonlinear Acoustics--Perturbation Theory and Webster's Equation." arXiv preprint arXiv:1311.4238(2013). https://arxiv.org/pdf/1311.4238
- https://www.radiomuseum.org/forumdata/users/133/PDF/Speaker.pdf
- https://www.quora.com/How-does-a-megaphone-amplify-sound
- http://www.vias.org/crowhurstba/crowhurst_basic_audio_vol1_049.html
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- https://www.reddit.com/r/explainlikeimfive/comments/las2b/eli5_how_does_a_horn amplify_sound_without_adding/
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- https://www.youtube.com/watch?v=EfFsDcZxRr4
- https://www.youtube.com/watch?v=TVdrjm1BVP0



8. Sci-Fi Sound

Tapping a helical spring can make a sound like a "laser shot" in a science-fiction movie. Investigate and explain this phenomenon.

- https://en.wikipedia.org/wiki/Slinky
- https://en.wikipedia.org/wiki/Euler%E2%80%93Bernoulli beam theory
- Parker, Julian, et al. "Modeling methods for the highly dispersive slinky spring: a novel musical toy." *Proceedings of the 13th International Conference on Digital Audio Effects (DAFx'10)*. 2010.
 - http://dafx10.iem.at/papers/ParkerPenttinenBilbaoAbel_DAFx10_P80.pdf
- Lee, J., and D. J. Thompson. "Dynamic stiffness formulation, free vibration and wave motion of helical springs." *Journal of Sound and Vibration* 239.2 (2001): 297-320. https://www.sciencedirect.com/science/article/pii/S0022460X00931699
- Rutherford, Casey. "A Fresh Look at Longitudinal Standing Waves on a Spring." *The Physics Teacher* 51.1 (2013): 22-24.
 - $\frac{https://www.researchgate.net/profile/Casey_Rutherford/publication/258810726_A_Fresh_Look_at_Longitudinal_Standing_Waves_on_a_Spring/links/5695160e08ae820_ff0749c0f.pdf$
- https://www.researchgate.net/post/Why_does_tapping_in_air_not_produce_any_so und but tapping against a metal does produce sound
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- https://www.youtube.com/watch?v=CpZkNWBmKNM
- https://www.youtube.com/watch?v=7VGIBZOywlg
- https://www.youtube.com/watch?v=agtgiuSMJqM
- https://www.youtube.com/watch?v=rajPbk3CJr4
- https://www.youtube.com/watch?v=SVAd6zxjiow
- https://www.youtube.com/watch?v=XACHZbgcH5M



9. Soy Sauce Optics

Using a laser beam passing through a thin layer (about 200 μ m) of soy sauce the thermal lens effect can be observed. Investigate this phenomenon.

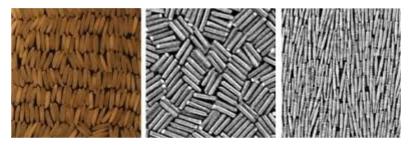
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- Sheldon, S. J., L. V. Knight, and J. M. Thorne. "Laser-induced thermal lens effect: a new theoretical model." *Applied optics*21.9 (1982): 1663-1669. https://pdfs.semanticscholar.org/ac26/ad507bc2432a136433a53e734bf872e74f42
- http://photonics.cusat.edu/Research Thermal%20lens.html
- Sivasubramanian, Dhanuskodi, Rajeswari Ponnusamy, and Vinitha Gandhiraj. "Low power optical limiting and thermal lensing in Mn doped ZnO nanoparticles." *Materials Chemistry and Physics* 159 (2015): 93-100. https://www.sciencedirect.com/science/article/pii/S0254058415002266
- Snook, Richard D., and Roger D. Lowe. "Thermal lens spectrometry. A review." Analyst 120.8 (1995): 2051-2068. http://pubs.rsc.org/en/content/articlelanding/1995/an/an9952002051#!divAbstract
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- https://www.schott.com/d/advanced_optics/3794eded-edd2-461d-aec5-0a1d2dc9c523/1.0/schott_tie-19 temperature coefficient of refractive index eng.pdf



10. Suspended Water Wheel

Carefully place a light object, such as a Styrofoam disk, near the edge of a water jet aiming upwards. Under certain conditions, the object will start to spin while being suspended. Investigate this phenomenon and its stability to external perturbations.

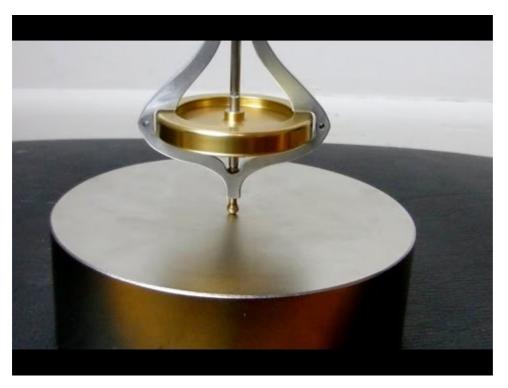
- https://en.wikipedia.org/wiki/Bernoulli%27s principle
- https://en.wikipedia.org/wiki/Magnus effect
- https://en.wikipedia.org/wiki/Coand%C4%83_effect
- https://www.researchgate.net/post/Can_you_explain_Veritasiums_Hydrodynamic_le_vitation_or_Fluid_Juggling
- https://physics.stackexchange.com/questions/356284/any-solutions-to-veritasiums-hydrodynamic-levitation
- https://sploid.gizmodo.com/what-sorcery-keeps-this-giant-ball-floating-on-a-tiny-s-1796416838
- http://forums.xkcd.com/viewtopic.php?t=123045
- https://gizmodo.com/the-physics-of-how-a-water-jet-can-keep-a-ball-floating-1445828275
- https://www.youtube.com/watch?v=mNHp8iyyIjo
- https://www.youtube.com/watch?v=WZrQy7zKM4Y
- https://www.youtube.com/watch?v=p9_aUQDGDbU&hd=1
- https://www.youtube.com/watch?v= jYoQu3PvIk
- https://www.youtube.com/watch?v=ST6hDiUBSJQ
- https://www.youtube.com/watch?v=gXfSUgiWQZ4
- https://www.youtube.com/watch?v=7IGm3MrjDX0
- https://www.youtube.com/watch?v=WZ1nvvMfdYc
- https://www.youtube.com/watch?v=IHjFx2lp_kw



11. Flat Self-Assembly

Put a number of identical hard regular-shaped particles in a flat layer on top of a vibrating plate. Depending on the number of particles per unit area, they may or may not form an ordered crystal-like structure. Investigate the phenomenon.

- Galanis, Jennifer, et al. "Spontaneous patterning of confined granular rods." *Physical review letters* 96.2 (2006): 028002. https://arxiv.org/pdf/cond-mat/0508202
- Narayan, Vijay, Narayanan Menon, and Sriram Ramaswamy. "Nonequilibrium steady states in a vibrated-rod monolayer: tetratic, nematic, and smectic correlations." *Journal of Statistical Mechanics: Theory and Experiment* 2006.01 (2006): P01005. https://arxiv.org/pdf/cond-mat/0510082
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 https://www.researchgate.net/profile/Marco_Ramaioli/publication/5915242_Vertical_ordering of rods under vertical vibration/links/54ed0a660cf28f3e65353561.pdf
- Saadatmand, Sayed Mehrrad. A Study on Vibration-induced Particle Motion under Microgravity. Diss. 2012. https://tspace.library.utoronto.ca/bitstream/1807/32879/1/Saadatmand_Mehrrad_2 01206 PhD thesis.pdf



12. Gyroscope Teslameter

A spinning gyroscope made from a conducting, but nonferromagnetic material slows down when placed in a magnetic field. Investigate how the deceleration depends on relevant parameters.

- https://en.wikipedia.org/wiki/Eddy current
- https://en.wikipedia.org/wiki/Eddy current brake
- https://en.wikipedia.org/wiki/Angular_momentum#Conservation_of_angular_mo
- https://www.youtube.com/watch?v=1ZeClejT2NY
- https://www.youtube.com/watch?v=whoylwf-i0A
- https://www.youtube.com/watch?v=SK0EdikjC24



13. Moiré Thread Counter

When a pattern of closely spaced non-intersecting lines (with transparent gaps in between) is overlaid on a piece of woven fabric, characteristic moiré fringes may be observed. Design an overlay that allows you to measure the thread count of the fabric. Determine the accuracy for simple fabrics (e.g. linen) and investigate if the method is reliable for more complex fabrics (e.g. denim or Oxford cloth).

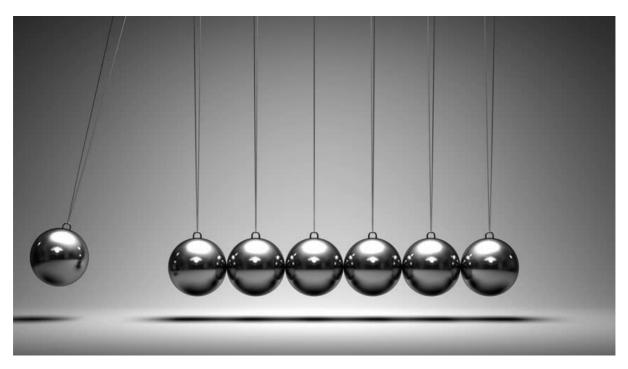
- https://en.wikipedia.org/wiki/Moir%C3%A9 pattern
- Reich, Gary. "A moiré pattern-based thread counter." *The Physics Teacher* 55.7 (2017): 426-430. https://aapt.scitation.org/doi/10.1119/1.5003746
- https://www.indiamart.com/arhamscientific/textile-testing-instruments.html
- http://www.lunometer.com/what.html
- http://www.lunometer.de/tech-e.htm



14. Looping Pendulum

Connect two loads, one heavy and one light, with a string over a horizontal rod and lift up the heavy load by pulling down the light one. Release the light load and it will sweep around the rod, keeping the heavy load from falling to the ground. Investigate this phenomenon.

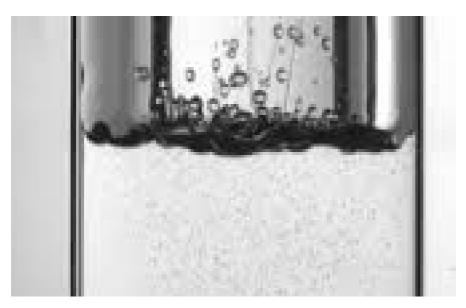
- https://en.wikipedia.org/wiki/Pendulum
- https://en.wikipedia.org/wiki/Pendulum_(mathematics)
- https://en.wikipedia.org/wiki/Centripetal_force
- https://sciencedemonstrations.fas.harvard.edu/presentations/rope-friction-around-pole
- https://en.wikipedia.org/wiki/Capstan_equation
- https://www.stevespanglerscience.com/lab/experiments/magic-pendulum/
- https://www.istitutotrento5.it/images/test/bre 15 16 looping pendulum 2 bil.pdf
- https://www.youtube.com/watch?v=SXQ9VaYm3yQ
- https://www.youtube.com/watch?v=ZyhHidThQR8
- https://www.youtube.com/watch?v=XSFXzL4vCPq



15. Newton's Cradle

The oscillations of a Newton's cradle will gradually decay until the spheres come to rest. Investigate how the rate of decay of a Newton's cradle depends on relevant parameters such as the number, material, and alignment of the spheres.

- https://en.wikipedia.org/wiki/Newton%27s_cradle
- https://en.wikipedia.org/wiki/Inelastic collision
- Hutzler, Stefan, et al. "Rocking Newton's cradle." American Journal of Physics 72.12 (2004): 1508-1516. https://openresearch-repository.anu.edu.au/bitstream/1885/95080/1/01_Hutzler_Rocking_Newton%E2%80%99s_cradle_2004.pdf
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- http://scienceblogs.com/principles/2015/11/05/energy-dissipation-in-a-physics-toy/
- http://ffden-2.phys.uaf.edu/212 spring2011.web.dir/Joel Teune/analysis.html
- James, Guillaume. "Nonlinear waves in Newton's cradle and the discrete p-Schrödinger equation." Mathematical Models and Methods in Applied Sciences 21.11 (2011): 2335-2377. https://arxiv.org/pdf/1008.1153



16. Sinking Bubbles

When a container of liquid (e.g. water) oscillates vertically, it is possible that bubbles in the liquid move downwards instead of rising. Investigate this phenomenon.

- https://en.wikipedia.org/wiki/Buoyancy
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17. Popsicle Chain Reaction

Wooden popsicle sticks can be joined together by slightly bending each of them so that they interlock in a so-called "cobra weave" chain. When such a chain has one of its ends released, the sticks rapidly dislodge, and a wave front travels along the chain. Investigate the phenomenon.

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