A Pupil Dilation Technique to Test Developmental Differences in Visual Synchrony

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Introduction

This tutorial demonstrates how to extract population pupil dilation synchrony using a simulated dataset. The analysis focuses on comparing pupil dilation patterns between two age groups across multiple video stimuli.

⚠ Warning

The pupil dilation data used in this tutorial is simulated. Please do not interpret the results as representative of actual physiological responses.

The simulated dataset comprises:

- 2 age groups: Children and Adults
- 10 subjects per age group
- 10 video stimuli

Data Import and Visualization

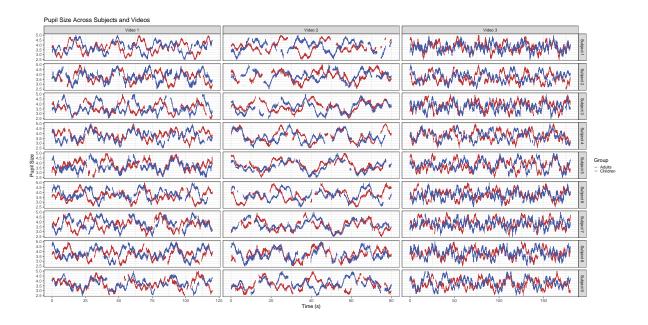
We begin by importing the necessary libraries and loading the simulated data.

```
library(tidyverse)
library(zoo)

Hz = 20
window_sizeP = Hz * 2
window_size_Ttest = Hz * 4

# read the data
db = read.csv('Simulated_data.csv')
```

Next, we visualize the pupil dilation data for both groups across all videos comparing children and adults with the same id number.



Prepare the data

To analyze pupil dilation synchrony between Children and Adults, we need to prepare our data by:

- Separating the data by age Group
- Reshaping the data to a wide format for easier analysis
- Split the data to a list of dataframes based on the videos
- Removing first column to only keep the data

We'll create two lists of dataframes, one for each age group:

```
# Create list of dataframe for children
Children_list = Children %>%
    split(.$Video) %>%
    map(select, -(1:2))

# Create list of dataframe for adults
Adults_list = Adults %>%
    split(.$Video) %>%
    map(select, -(1:2))
```

These lists contain separate dataframes for each video, with columns representing individual subjects' pupil sizes. This structure facilitates the extraction of running pupil synchrony in subsequent analyses.

Pupil Synchrony

Synchrony Calculation

To calculate the running pupil synchrony we will define three functions:

- calculate_running_correlation()
- calc_correlation()
- average_fisher_z_transform()

calculate_running_correlation()

This is the main function that uses the rollapply function from the zoo package to apply a sliding window analysis. It calculates correlations over a specified window size across the entire dataset.

```
calc_correlation()
```

This function is applied to each window of data. It performs these steps:

- Checks if more than 75% of the window contains NA values. If so, it returns NA.
- Discards columns (subjects) where more than 75% of values are NA.
- Calculates the correlation matrix for the current window using cor().
- Applies Fisher's z-transformation using average_fisher_z_transform().

average_fisher_z_transform()

This function applies Fisher's z-transformation to the correlation matrix and returns the average correlation. Here's a step-by-step breakdown:

- Checks if a significant portion of columns have NA values.
- Extracts the lower triangle of the correlation matrix.
- Adjusts perfect correlations slightly to avoid infinite z-scores.
- Applies Fisher's z-transformation using atanh().
- Calculates the mean z-score.
- Converts the mean z-score back to the correlation scale using tanh().

Note

The Fisher z-transformation is a statistical method used to convert correlation coefficients into z-scores. It is used in this analysis because the correlation coefficients are not normally distributed and their variance changes depending on the strength of the correlation, which can lead to biased results when averaging or performing other statistical operations. The z-transformation normalizes the distribution of correlations and stabilizes their variance, making it possible to perform more accurate statistical analyses.

```
by.column = FALSE, align = "center", partial =
                                       TRUE)
 return(correlation_matrices)
average_fisher_z_transform = function(corr_matrix, threshold = 0.75) {
 if (sum(colSums(is.na(corr_matrix)) >= ncol(corr_matrix) - 1) > threshold *
     ncol(corr_matrix)) {
   return(NA)
 lower_tri = corr_matrix[lower.tri(corr_matrix)]
 lower_tri[lower_tri == 1] = 1 - 1e-10
 lower_tri[lower_tri == -1] = -1 + 1e-10
 z_scores = atanh(lower_tri)
 # Calculate the mean z-score and convert back to the correlation scale
 average_z_score = mean(z_scores, na.rm = TRUE)
  average_correlation = tanh(average_z_score)
  return(average_correlation)
```

Running the function and finalize the data

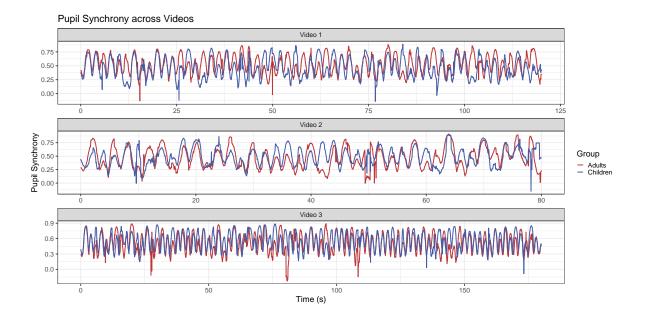
Having defined our functions, we can now apply them to the dataframes in our lists. We'll use lapply() to efficiently run the calculate_running_correlation() function on each element of our lists, which is analogous to using a for loop but more concise and often faster in R. Thanks to our data arrangement earlier, we can easily integrate the calculated synchrony values into our original dataframes by combining the list of synchrony using do.call(c,).

We start by calculating the synchrony for both children and adults:

In this code:

- We apply calculate_running_correlation() to each element in Children_list and Adults list.
- We then add the calculated synchrony values to the original dataframes, along with a *Group* identifier.
- Finally, we combine the children and adults dataframes into a single dataframe.

Now that we have our combined data, we can visualize the results:



Finding significant windows

In order to identify sections of our data where the difference in pupil synchrony between children and adults is statistically significant, we'll use a rolling t-test function. The RollingT() function:

- Converts input data to a dataframe and extracts synchrony values for children and adults.
- Checks if more than the treshold of the values in either group's window are NA. If so, it returns NA for both p-value and t-statistic to avoid unreliable results.
- If there are sufficient non-NA values, it performs a two-sided t-test comparing the synchrony values between children and adults.
- Returns the resulting p-value and t-statistic.

```
return(c(Pval = NA, t_value = NA))
} else {
   test_result = t.test(Child_window, Adu_window, paired = FALSE, alternative =
   "two.sided")
   return(c(Pval = test_result$p.value, t_value = test_result$statistic))
}
```

Running rolling ttest

Now that we have our RollingT function, we can apply it to our synchrony data. However, before running the function, we need to prepare our data in a specific format. This preparation involves:

- Reshaping the data to a wide format
- Separating the data by video stimulus
- Arrange the data by Video and Seconds
- Split the data to a list of dataframes based on the videos

Once the data is ready we run use lappply() to run on each dataframe in the list a rollapply() function that calls the previously defined RollingT() function.

After obtaining the results, we'll:

- Attach the extracted p-values and t-values to the original dataframe
- Correct the p-values for each video using the false discovery rate (FDR) method to account for multiple comparisons
- We create a column to indicate whether the corrected p-value is less than 0.05, providing a quick reference for statistical significance. (True False)

Find significant chunks

After obtaining our p-values and applying false discovery rate correction, we'll identify contiguous chunks of significant differences between children and adults in pupil synchrony.

- We create a column to identify contiguous significant periods in each video
- Summarizing each streak to get its start time, end time, and duration
- Keep only chunks that last 2 seconds or more

Finally after extracting all this information we plot the pupil dilation synchorny and highlighting the chunks of data where there is a significant difference.

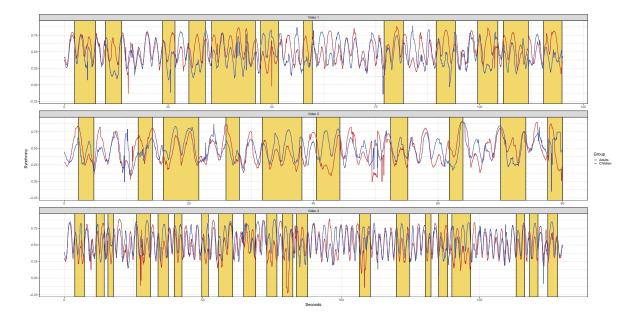
```
## Identify contiguous chunks of significant results
Streak_Significance = TTest_result %>%
    group_by(Video) %>%

# Create a streak column to identify contiguous significant periods
mutate(Streak = cumsum(!Significance)) %>%
    ungroup() %>%

filter(Significance == TRUE) %>%
    group_by(Streak, Video) %>%
    summarize(
    START = min(Seconds, na.rm = T), # Start time of the significant chunk
    END = max(Seconds, na.rm = T), # End time of the significant chunk
    DUR = END - START # Duration of the chunk
) %>%
    filter(DUR >= 2) # Retain only chunks with a duration of 2 seconds or more
```

```
# Plot pupil synchrony and the significant chunks
ggplot(Final_synchrony, aes(y = Synchrony, x = Seconds, color = Group))+
geom_rect(
   inherit.aes = FALSE, data = Streak_Significance,
   aes(xmin = START, xmax = END, ymin = -Inf, ymax = Inf),
   fill = '#F2D76A', color = 'black'
) +

geom_line(linewidth = 1.2) +
facet_wrap(~Video, ncol=1, scales = 'free_x')+
scale_color_manual(values = c("#BD3538", "#455BA6")) +
theme_bw(base_size = 20)
```



Randomization

In the paper we compared the chunks found in the pupil dilation with a reference database. This database consisted of 1000 iterations where we randomly assigned participants to either the Children or Adults group, regardless of their actual age. The procedure is identical to what we've seen so far. However, since we want to run this procedure 1000 times, we'll utilize the parallel library. This library provides a useful function parlapply() that allows us to run multiple iterations of the same function in parallel, significantly speeding up the process.

Preparation

To start we import eh parallel library and we define some of the settings that will be needed to run this procedure in parallel.



Warning

For the purpose of this tutorial, we'll set the number of iterations to 10 to ensure the script runs quickly. It's important to note that in a full analysis, you would typically use a much larger number of iterations (such as 1000) to obtain more robust results. The process remains the same regardless of the number of iterations; increasing this number simply provides a more comprehensive randomized dataset for comparison.

```
library(parallel)
iterations = 1:10
cl = makeCluster(detectCores() -2) # Use all available cores -2
clusterExport(cl, c("db", "calculate_running_correlation",
# Load required libraries in each core
outpcl = clusterEvalQ(cl, {
 library(tidyverse)
 library(zoo)
```

Wrapping in a function

To leverage parallel processing, we need to encapsulate our analysis in a function that can be executed across multiple CPU cores. This function will perform the same steps we've previously discussed, with two key differences:

- 1. At the beginning, it randomly reassigns the age group labels (Children or Adults) to the subjects.
- 2. At the end, it adds an identifier for each iteration to our resulting dataframe.

```
Parallel_Synhc = function(x) {
  df = db \%
   group_by(Subject) %>%
   mutate(Group = sample(c('Adults', 'Children'), size = n(), replace = TRUE)) %>%
    ungroup()
  Children = df %>%
   filter(Group == 'Children') %>%
   arrange(Video) %>%
   pivot_wider(names_from = Subject, values_from = PupilSize,
                id_cols = c("Seconds", "Video"))
  Adults = df %>%
   filter(Group == 'Adults') %>%
    arrange(Video) %>%
   pivot_wider(names_from = Subject, values_from = PupilSize,
                id_cols = c("Seconds", "Video"))
  # Create list of dataframe for children
  Children_list = Children %>%
    split(.$Video) %>%
   map(select, -(1:2))
  # Create list of dataframe for adults
  Adults list = Adults %>%
   split(.$Video) %>%
   map(select, -(1:2))
  Children_synchrony = lapply(Children_list, calculate_running_correlation,
    window_sizeP = window_sizeP)
  Adults_sycnhrony = lapply(Adults_list, calculate_running_correlation, window_sizeP
   = window_sizeP)
  Children_synchrony = Children %>%
    select(1:2) %>%
   mutate(Group = 'Children',
           Synchrony = do.call(c, Children_synchrony))
```

Running the function

Now that we have defined our function, we can distribute it across multiple CPU cores using parlapply(). This function will apply our analysis to each iteration in parallel, significantly reducing computation time. Here's how we execute the process:

```
# Run the Parallel_Synhc function in parallel for each iteration
Final_synchrony_randomized = parLapply(cl, iterations, Parallel_Synhc)
stopCluster(cl) # Stop the cluster after processing is complete

# Combine the results from all iterations
Final_synchrony_randomized = bind_rows(Final_synchrony_randomized)
```

This code launches our function across the cluster, processes all iterations in parallel, and then combines the results into a single comprehensive dataframe.

Rolling Ttest

To extract the rolling t-test results from all iterations, we can apply the same approach as before. We begin by defining a cluster of CPU cores and exporting the necessary functions and variables.

```
# Initialize parallel processing
cl = makeCluster(detectCores() -2) # Use all available cores -2

# Export necessary objects and functions to each worker
clusterExport(cl, c( "window_size_Ttest", "RollingT"))

# Load required libraries in each core
outpcl = clusterEvalQ(cl, {
   library(tidyverse)
```

```
library(zoo)
})
```

As before, we wrap the rolling t-test process in a function designed to run in parallel. This function will prepare the data, apply the t-test, adjust p-values, and determine statistical significance.

```
Parallel_RollingT = function(DF) {
 Iter = DF$Iteration[1]
 Synch_Pupil_Wide = DF %>%
   pivot_wider(names_from = Group, values_from = Synchrony,
                id_cols = c("Seconds", 'Video')) %>%
   arrange(Video, Seconds)
 Video_list = Synch_Pupil_Wide %>%
    split(.$Video)
 Ttest_list = lapply(Video_list,
                       function(group_df) {
                         rollapply(group_df, width = window_size_Ttest,
                                   FUN = function(df) RollingT(df), by.column =
                                       FALSE, fill = NA, partial = TRUE)})
 TTest_result = Synch_Pupil_Wide %>%
   mutate(Pval = do.call(rbind, Ttest_list)[,1],
           Tval = do.call(rbind, Ttest_list)[,2]) %>%
    group_by(Video) %>%
   mutate(Pval.fdr = as.numeric(p.adjust(Pval, method = "fdr"))) %>%
   ungroup() %>%
   mutate( Significance = case_when(
       Pval.fdr >= 0.05 ~ FALSE,
       Pval.fdr < 0.05 ~ TRUE,
        is.na(Pval.fdr) ~ FALSE))
  return(TTest_result)
```

Finally, we prepare the data to be passed as a list, distribute it to the cluster, and run the

function for each iteration. Once all iterations have been processed, we combine the resulting dataframes into a single, consolidated dataframe.