

# back scattering

May 14, 2022

```
[1]: # %load ../../setup.py
      """
      Packages for plotting and other stuff
      version: 1.0
      author: Riasat
      """
      # %matplotlib widget

      # data loading
      import pandas as pd

      # data maipulation
      import pwlf
      import numpy as np
      from scipy.interpolate import interp1d, UnivariateSpline
      from scipy.signal import find_peaks
      from scipy import optimize

      # plotting tools
      import matplotlib.pyplot as plt

      # extra tweaks
      import warnings

      warnings.filterwarnings("ignore")

      # plot tweaks
      plt.style.use("seaborn-poster")
      pd.options.display.max_columns = None
      pd.options.display.float_format = "{:.5f}".format

      # function for extrapolation
      def extrapolate1d(x, y):
          f = interp1d(x, y, kind="linear", fill_value="extrapolate")
          a = np.arange(0, x[len(x) - 1], 0.001)
          b = f(a)
          return a, b
```

```

# function for interpolation
def interpolate1d(x, y):
    f = interp1d(x, y, kind="linear", fill_value="extrapolate")
    a = np.arange(x[0], x[len(x) - 1], 0.001)
    b = f(a)
    return a, b

# function for interpolation
def interpolate2d(x, y):
    f = interp1d(x, y, kind="quadratic", fill_value="extrapolate")
    a = np.arange(x[0], x[len(x) - 1], 0.001)
    b = f(a)
    return a, b

# function for interpolation
def interpolate3d(x, y):
    f = interp1d(x, y, kind="cubic", fill_value="extrapolate")
    a = np.arange(x[0], x[len(x) - 1], 0.001)
    b = f(a)
    return a, b

# function for polynomial fitting
def polfit(a, b, c):
    z = np.polyfit(a, b, c)
    f = np.poly1d(z)

    x = np.arange(a[0], a[len(a) - 1], 0.001)
    y = f(x)
    return x, y

# function for piecewise linear fit
def piecewise_linear_fit(x, y, segments):
    my_pwlf = pwlf.PiecewiseLinFit(x, y) # fit my data
    res = my_pwlf.fit(segments) # fit the data for n line segments
    # slopes = myPWLF.calc_slopes() # calculate slopes

    # predict for the determined points
    xHat = np.linspace(min(x), max(x), num=10000)
    yHat = my_pwlf.predict(xHat)

    # calculate statistics

```

```

# p = myPWLF.p_values(method="non-linear", step_size=1e-4) # p-values
# se = myPWLF.se # standard errors
return xHat, yHat

# curve fit
def cur_fit(x, y):
    func = lambda t, a, c, d: a * np.log(t + c) + d
    popt, pcov = optimize.curve_fit(func, x, y) # type: ignore
    xx = np.arange(x[0], x[len(x) - 1], 0.001)
    yy = func(xx, *popt)
    return xx, yy

```

## 1 Datas

```

[2]: # plateau datas
data_plateau = pd.read_excel("data.xlsx", sheet_name="plateau")
pl_voltage = data_plateau["p_voltage"]
pl_counts = data_plateau["p_counts"]

# al backscattter
data_al = pd.read_excel("data.xlsx", sheet_name='al_back')
al_thick = data_al['al_thick']
al_0 = data_al['al_0']
al_counts = data_al['al_counts']

# cu backscattter
data_cu = pd.read_excel("data.xlsx", sheet_name='cu_back')
cu_thick = data_cu['cu_thick']
cu_0 = data_cu['cu_0']
cu_counts = data_cu['cu_counts']

# ag backscattter
data_ag = pd.read_excel("data.xlsx", sheet_name='ag_back')
ag_thick = data_ag['ag_thick']
ag_0 = data_ag['ag_0']
ag_counts = data_ag['ag_counts']

```

## 2 Functions

```

[3]: # function for interpolation
def interpolate(x, y):
    f = interp1d(x, y, kind="cubic", fill_value="extrapolate")
    a = np.arange(x[0], x[len(x) - 1], 0.001)
    b = f(a)

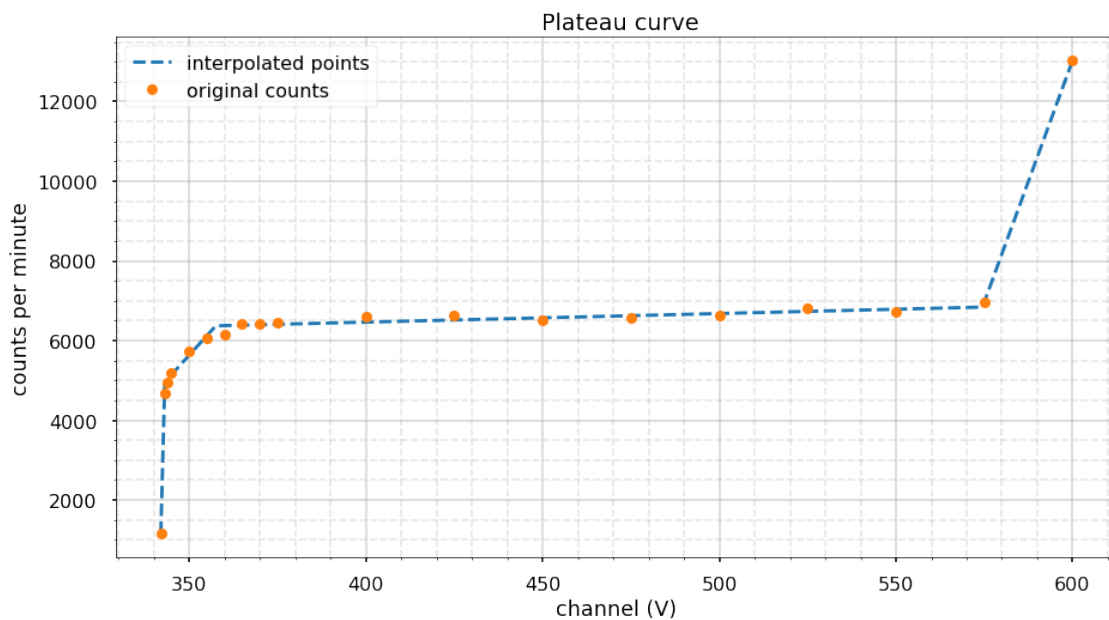
```

```
return a, b
```

### 3 Plateau

```
[4]: # %matplotlib widget
voltage_interpolated_pl, counts_interpolated_pl =
    ↳picewise_linear_fit(pl_voltage, pl_counts, 4)

plt.style.use("seaborn-poster")
plt.figure(figsize=(15, 8))
plt.title(f" Plateau curve")
plt.xlabel("channel (V)")
plt.ylabel("counts per minute")
plt.plot(voltage_interpolated_pl, counts_interpolated_pl, "--",
    ↳label="interpolated points")
plt.plot(pl_voltage, pl_counts, "o", markersize=9, label="original counts")
plt.legend(loc="upper left")
plt.grid(alpha=0.5, which="major")
plt.minorticks_on()
plt.grid(alpha=0.3, which="minor", ls="--")
plt.show()
```



I choosed the operating voltage at 400 V

## 4 Backscattering factor

```
[5]: element_name = ["Aluminium", "Copper", "Silver"]
```

### 4.1 Aluminium

```
[6]: f_al = al_counts/al_0
del_f_al = f_al*np.sqrt(1/al_0 + 1/al_counts)
print(f"{f_al}, {del_f_al}")
```

```
0    1.01006
1    1.02546
2    1.07200
3    1.06055
4    1.11021
5    1.06351
6    1.08796
7    1.01414
8    1.12189
9    1.09592
dtype: float64, 0    0.03368
1    0.03467
2    0.03577
3    0.03584
4    0.03677
5    0.03560
6    0.03626
7    0.03399
8    0.03708
9    0.03632
dtype: float64
```

```
[7]: # plotting the curves
# plt.style.use("seaborn-poster")
plt.figure(figsize=(15, 8))

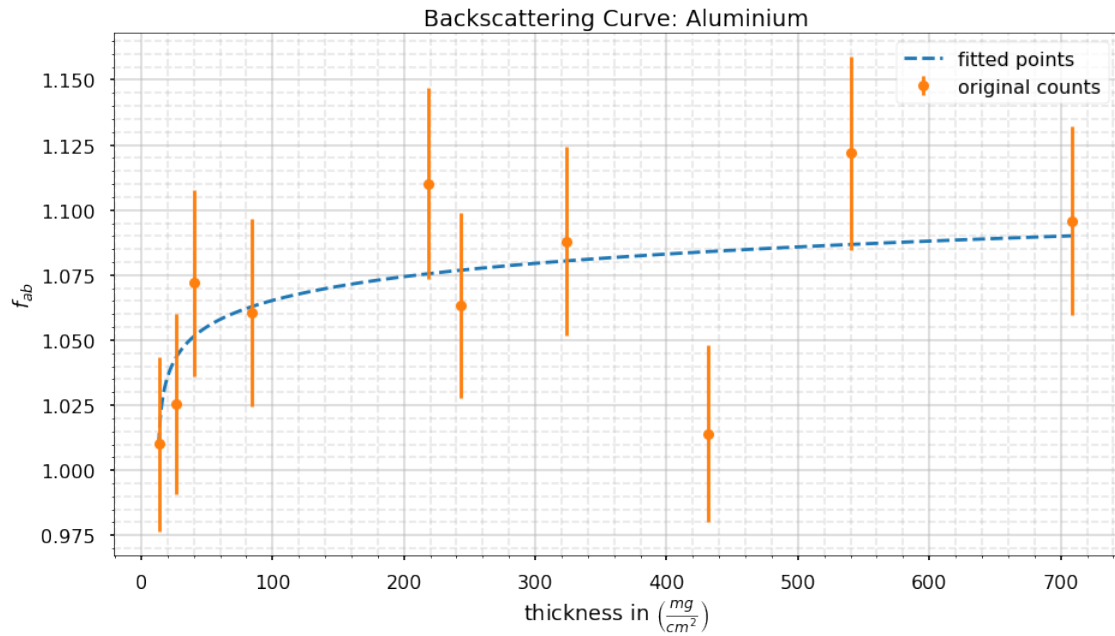
plt.title(f"Backscattering Curve: {element_name[0]}")
plt.xlabel(r"thickness in  $\frac{\text{mg}}{\text{cm}^2}$ ")
plt.ylabel(r" $f_{\text{ab}}$ ")

pxal, pyal = cur_fit(al_thick, f_al)
plt.plot(pxal, pyal, "--", label="fitted points")
plt.errorbar(al_thick, f_al, yerr=del_f_al, fmt="o", markersize=9,
             label="original counts")

plt.legend(loc="upper right")
plt.grid(alpha=0.5, which="major")
```

```
plt.minorticks_on()
plt.grid(alpha=0.3, which="minor", ls="--")

plt.show()
```



## 4.2 Copper

```
[8]: f_cu = cu_counts/cu_0
del_f_cu = f_cu*np.sqrt(1/cu_0 + 1/cu_counts)
# cu_thick_interpolate, f_cu_interpolate = polfit(cu_thick,f_cu, 4)
print(f"{f_cu}, {del_f_cu}")
```

```
0    1.21291
1    1.26791
2    1.23385
3    1.24561
4    1.23505
dtype: float64, 0    0.04294
1    0.04539
2    0.04399
3    0.04430
4    0.04407
dtype: float64
```

```
[9]: # plotting the curves
# plt.style.use("seaborn-poster")
```

```

plt.figure(figsize=(15, 8))

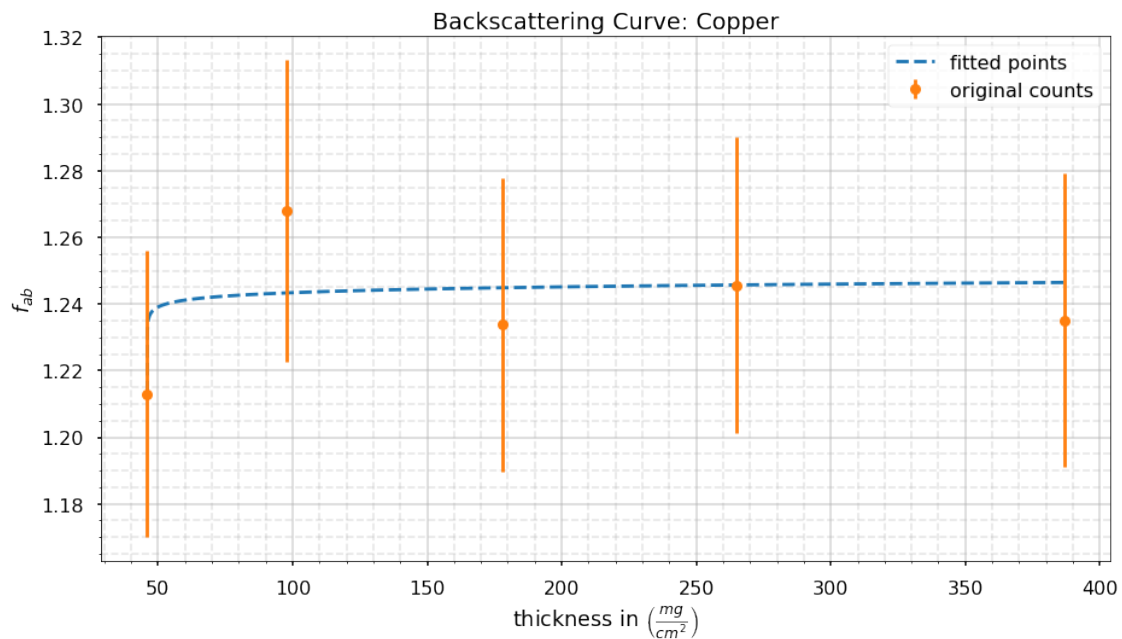
plt.title(f"Backscattering Curve: {element_name[1]}")
plt.xlabel(r"thickness in  $\left(\frac{\text{mg}}{\text{cm}^2}\right)$ ")
plt.ylabel(r"$f_{ab}$")

pxcu, pycu = cur_fit(cu_thick, f_cu)
plt.plot(pxcu, pycu, "--", label="fitted points")
plt.errorbar(cu_thick, f_cu, yerr=del_f_cu, fmt="o", markersize=9,
             label="original counts")

plt.legend(loc="upper right")
plt.grid(alpha=0.5, which="major")
plt.minorticks_on()
plt.grid(alpha=0.3, which="minor", ls="--")

plt.show()

```



### 4.3 Silver

```

[10]: f_ag = ag_counts/ag_0
del_f_ag = f_ag*np.sqrt(1/ag_0 + 1/ag_counts)
print(f"{f_ag}, {del_f_ag}")

```

```

0    1.26703
1    1.25911

```

```

2  1.27435
3  1.32500
4  1.32883
5  1.32748
6  1.33591
7  1.34225
dtype: float64, 0    0.04423
1  0.04381
2  0.04383
3  0.04625
4  0.04693
5  0.04660
6  0.04683
7  0.04705
dtype: float64

```

```

[11]: # plotting the curves
# plt.style.use("seaborn-poster")
plt.figure(figsize=(15, 8))

plt.title(f"Backscattering Curve: {element_name[2]}")
plt.xlabel(r"thickness in $\left(\frac{\text{mg}}{\text{cm}^2}\right)$")
plt.ylabel(r"$f_{\text{ab}}$")

pxag, pyag = cur_fit(ag_thick, f_ag)
plt.plot(pxag, pyag, "--", label="fitted points")
plt.errorbar(ag_thick, f_ag, yerr=del_f_ag, fmt="o", markersize=9,
             label="original counts")

plt.legend(loc="upper right")
plt.grid(alpha=0.5, which="major")
plt.minorticks_on()
plt.grid(alpha=0.3, which="minor", ls="--")

plt.show()

```



