Jecture 11: entropy

last time we considered a minimal system: a single spin in a magnetic field, tradeoff between E and T

kanning goals

- recall the probabilistic

definition of entropy

- understand that macroscopic

behavior results from the compromise

between energy and entropy

of states is also important for behavior, quantified by entropy

 $5 = -k_BT \sum_{\underline{s}} P(\underline{s}) \log P(\underline{s})$ — high when probabilities uniform, low when concentrated if all states equally probable, then we have

where N is the number of states, so eff measures "effective to of states"

consider a system with two energy levels: EA and EB assume there are NA A states and NB B states, then

$$P(A) = \sum_{G \in A} \frac{e^{-\beta E_A}}{Z} = N_A \frac{e^{-\beta E_A}}{Z}$$

$$= \frac{1}{2} \exp(-\beta E_A - \log N_A) \qquad P_A(S)$$

$$= \frac{1}{2} \exp(-\beta (E_A + \frac{1}{\beta} \sum_{S \in A} N_A \log N_A))$$

$$= \frac{1}{2} \exp(-\beta (E_A - \frac{1}{\beta} S_A)) = \frac{e^{-\beta E_A}}{Z}$$

FA is the free energy of state A, Et and ST -> FI, higher probability

to macroscopic properties can be dominated by high energy states if there are many of them, and if temperature is high

* notebook example, magnetization free energies

if time. Linterest: connection w information theory