

```
const defaultparser = TensorParser()
```

```
"""
```

```
@notensor(block)
```

Marks a block which should be ignored within an `@tensor` environment. Has no effect outside of `@tensor`.

```
"""
```

```
macro notensor(ex::Expr)
```

```
    return esc(ex)
```

```
end
```

```
"""
```

```
@tensor(block)
```

Specify one or more tensor operations using Einstein's index notation. Indices can be chosen to be arbitrary Julia variable names, or integers. When contracting several

tensors together, this will be evaluated as pairwise contractions in left to right order, unless the so-called NCON style is used (positive integers for contracted indices and negative indices for open indices).

A second argument to the `@tensor` macro can be provided of the form `order=(...)`, where

the list specifies the contraction indices in the order in which they will be contracted.

```
"""
```

```
macro tensor(ex::Expr)
```

```
    return esc(defaultparser(ex))
```

```
end
```

```
macro tensor(ex::Expr, orderex::Expr)
```

```
    parser = TensorParser()
```

```
    if !(orderex.head == :(:) && orderex.args[1] == :order &&
```

```
        orderex.args[2] isa Expr && orderex.args[2].head == :tuple)
```

```
        throw(ArgumentError("unkown first argument in @tensor, should be `order = (...),`"))
```

```
    end
```

```
    indexorder = map(normalizeindex, orderex.args[2].args)
```

```
    parser.contractiontreebuilder = network->indexordertree(network, indexorder)
```

```
    return esc(parser(ex))
```

```
end
```

```
"""
```

```
@tensoropt(optex, block)
```

```
@tensoropt(block)
```

Specify one or more tensor operations using Einstein's index notation. Indices can be chosen to be arbitrary Julia variable names, or integers. When contracting several

tensors together, the macro will determine (at compile time) the optimal contraction order depending on the cost associated to the individual indices. If no `optex` is provided, all indices are assumed to have an abstract scaling χ which is optimized in the asymptotic limit of large χ .

The cost can be specified in the following ways:

```
```julia
@tensoropt (a=>χ,b=>χ^2,c=>2*χ,e=>5) C[a,b,c,d] := A[a,e,c,f,h]*B[f,g,e,b]*C[g,d,h]
asymptotic cost as specified for listed indices, unlisted indices have cost 1
(any symbol for χ can be used)
@tensoropt (a,b,c,e) C[a,b,c,d] := A[a,e,c,f,h]*B[f,g,e,b]*C[g,d,h]
asymptotic cost χ for indices a,b,c,e, other indices (d,f) have cost 1
@tensoropt !(a,b,c,e) C[a,b,c,d] := A[a,e,c,f,h]*B[f,g,e,b]*C[g,d,h]
cost 1 for indices a,b,c,e; other indices (d,f) have asymptotic cost χ
@tensoropt C[a,b,c,d] := A[a,e,c,f,h]*B[f,g,e,b]*C[g,d,h]
asymptotic cost χ for all indices (a,b,c,d,e,f)
```
```

Note that `@tensoropt` will optimize any tensor contraction sequence it encounters in the (block of) expressions. It will however not break apart expressions that have been explicitly grouped with parenthesis, i.e. in

```
```julia
@tensoropt C[a,b,c,d] := A[a,e,c,f,h]*(B[f,g,e,b]*C[g,d,h])
```
```

it will always contract `B` and `C` first. For a single tensor contraction sequence, the optimal contraction order and associated (asymptotic) cost can be obtained using `@optimalcontractiontree`.

```
#####
macro tensoropt(expressions...)
    if length(expressions) == 1
        ex = expressions[1]
        optdict = optdata(ex)
    elseif length(expressions) == 2
        optex = expressions[1]
        ex = expressions[2]
        optdict = optdata(optex, ex)
    end

    parser = TensorParser()
    parser.contractiontreebuilder = network->optimaltree(network, optdict)[1]
    return esc(parser(ex))
end

#####

@tensoropt_verbose(optex, block)
@tensoropt_verbose(block)
```

Similar to `@tensoropt`, but prints information details regarding the optimization process to the standard output.

```
#####
macro tensoropt_verbose(expressions...)
    if length(expressions) == 1
        ex = expressions[1]
        optdict = optdata(ex)
    elseif length(expressions) == 2
        optex = expressions[1]
        ex = expressions[2]
        optdict = optdata(optex, ex)
    end
```

```

end

parser = TensorParser()
parser.contractiontreebuilder =
    network->optimaltree(network, optdict; verbose = true)[1]
return esc(parser(ex))
end

macro optimalcontractiontree(expressions...)
    if length(expressions) == 1
        ex = expressions[1]
        optdict = optdata(ex)
    elseif length(expressions) == 2
        optex = expressions[1]
        ex = expressions[2]
        optdict = optdata(optex, ex)
    end

    if isassignment(ex) || isdefinition(ex)
        ex = getrhs(ex)
    end
    if !(ex.head == :call && ex.args[1] == :*)
        error("cannot compute optimal contraction tree for this expression")
    end
    network = [getindices(ex.args[k]) for k = 2:length(ex.args)]
    tree, cost = optimaltree(network, optdict)
    return tree, cost
end

#####

@ncon(tensorlist, indexlist; order = ..., output = ...)

```

Contract the tensors in `tensorlist` (of type `Vector` or `Tuple`) according to the network as specified by `indexlist`. Here, `indexlist` is a list (i.e. a `Vector` or `Tuple`) with the same length as `tensorlist` whose entries are themselves lists (preferably `Vector{Int}`) where every integer entry provides a label for corresponding index/dimension of the corresponding tensor in `tensorlist`. Positive integers are used to label indices that need to be contracted, and such thus appear in two different entries within `indexlist`, whereas negative integers are used to label indices of the output tensor, and should appear only once.

By default, contractions are performed in the order such that the indices being contracted over are labelled by increasing integers, i.e. first the contraction corresponding to label `1` is performed. The output tensor had an index order corresponding to decreasing (negative, so increasing in absolute value) index labels. The keyword arguments `order` and `output` allow to change these defaults.

The advantage of the macro `@ncon` over the function call `ncon` is that the former automatically generates a unique symbol that hooks into the cache. Furthermore, if `tensorlist` is not just some variable but an actual list (as a tuple with parentheses or a vector with square brackets) at the call site, the `@ncon` macro will scan for conjugation calls, e.g. `conj(A)`, and replace this with just `A` but build a matching list of conjugation flags to be specified to `ncon`. This makes it more convenient to specify tensor conjugation, without paying the cost of actively performing the conjugation beforehand.

See also the function `[ncon](@ref)`.

"""

```
macro ncon(args...)
    if length(args) == 2
        return _nconmacro(args[1], args[2])
    else
        return _nconmacro(args[2], args[3], args[1])
    end
end

function _nconmacro(tensors, indices, kwargs = nothing)
    if !(tensors isa Expr) # there is not much that we can do
        if kwargs === nothing
            ex = Expr(:call, :ncon, tensors, indices,
                      Expr(:call, :fill, false, Expr(:call, :length, tensors)),
                      QuoteNode(gensym()))
        else
            ex = Expr(:call, :ncon, kwargs, tensors, indices,
                      Expr(:call, :fill, false, Expr(:call, :length, tensors)),
                      QuoteNode(gensym()))
        end
        return esc(ex)
    end
    if tensors.head == :vect || tensors.head == :tuple
        tensorargs = tensors.args
    elseif tensors.head == :ref
        tensorargs = tensors.args[2:end]
    else
        throw(ArgumentError("invalid @ncon syntax"))
    end
    if any(isa(ta, Expr) && ta.head === :... for ta in tensorargs)
        throw(ArgumentError("@ncon does not support splats (...) in tensor lists.))
    end
    conjlist = fill(false, length(tensorargs))
    for i = 1:length(tensorargs)
        if tensorargs[i] isa Expr
            if tensorargs[i].head == :call && tensorargs[i].args[1] == :conj
                tensorargs[i] = tensorargs[i].args[2]
                conjlist[i] = true
            end
        end
    end
    if tensors.head == :ref
        tensorex = Expr(:ref, tensors.args[1], tensorargs...)
    end
end
```

```
else
  tensorex = Expr(:ref, :Any, tensorargs...)
end
if kwargs === nothing
  ex = Expr(:call, :ncon, tensorex, indices, conjlist, QuoteNode(gensym()))
else
  ex = Expr(:call, :ncon, kwargs, tensorex, indices, conjlist,
QuoteNode(gensym()))
end
return esc(ex)
end
```