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# methods/simple.jl
#
# Method-based access to tensor operations using simple definitions.

# type unstable; better use tuples instead
tensorcopy(A, IA, IC=IA) = tensorcopy(A, tuple(IA...), tuple(IC...))
tensoradd(A, IA, B, IB, IC=IA) = tensoradd(A, tuple(IA...), B, tuple(IB...),
tuple(IC...))
tensortrace(A, IA, IC = unique2(IA)) = tensortrace(A, tuple(IA...), tuple(IC...))
tensorcontract(A, IA, B, IB, IC = symdiff(IA, IB)) =
    tensorcontract(A, tuple(IA...), B, tuple(IB...), tuple(IC...))
tensorproduct(A, IA, B, IB, IC = vcat(IA, IB)) = tensorproduct(A, tuple(IA...), B,
tuple(IB...), tuple(IC...))

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```

    tensorcopy(A, IA, IC = IA)

```

Creates a copy of `A`, where the dimensions of `A` are assigned indices from the iterable `IA` and the indices of the copy are contained in `IC`. Both iterables should contain the same elements in a different order.

The result of this method is equivalent to `permutedims(A, p)` where  $p$  is the permutation such that  $IC = IA[p]$ . The implementation of `tensorcopy` is however more efficient on

average, especially if `Threads.nthreads() > 1`.

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function tensorcopy(A, IA::Tuple, IC::Tuple=IA)
    indCinA = add_indices(IA, IC)
    C = similar_from_indices(eltype(A), indCinA, (), A, :N)
    add!(1, A, :N, 0, C, indCinA)
    return C
end

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```

    tensoradd(A, IA, B, IB, IC = IA)

```

Returns the result of adding arrays `A` and `B` where the iterabels `IA` and `IB` denote how the array data should be permuted in order to be added. More specifically, the result of this method is equivalent to

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```julia
tensorcopy(A, IA, IC) + tensorcopy(B, IB, IC)
```

```

but without creating the temporary permuted arrays.

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```

function tensoradd(A, IA::Tuple, B, IB::Tuple, IC::Tuple=IA)
    T = promote_type(eltype(A), eltype(B))
    indCinA = add_indices(IA, IC)
    C = similar_from_indices(T, indCinA, (), A, :N)
    add!(1, A, :N, 0, C, indCinA)
    indCinB = add_indices(IB, IC)

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    add!(1, B, :N, 1, C, indCinB)
    return C
end

```

```

"""
    tensortrace(A, IA [, IC])

```

Trace or contract pairs of indices of array `A`, by assigning them an identical indices in the iterable `IA`. The untraced indices, which are assigned a unique index, can be reordered according to the optional argument `IC`. The default value corresponds to the order in which they appear. Note that only pairs of indices can be contracted, so that every index in `IA` can appear only once (for an untraced index) or twice (for an index in a contracted pair).

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"""
function tensortrace(A, IA::Tuple, IC::Tuple)
    indCinA, cindA1, cindA2 = trace_indices(IA, IC)
    C = similar_from_indices(eltype(A), indCinA, (), A, :N)
    trace!(1, A, :N, 0, C, indCinA, cindA1, cindA2)
    return C
end

```

```

"""
    tensorcontract(A, IA, B, IB[, IC])

```

Contract indices of array `A` with corresponding indices in array `B` by assigning them identical labels in the iterables `IA` and `IB`. The indices of the resulting array correspond to the indices that only appear in either `IA` or `IB` and can be ordered by specifying the optional argument `IC`. The default is to have all open indices of array `A` followed by all open indices of array `B`. Note that inner contractions of an array should be handled first with `tensortrace`, so that every label can appear only once in `IA` or `IB` separately, and once (for open index) or twice (for contracted index) in the union of `IA` and `IB`.

The contraction can be performed by a native Julia algorithm without creating any temporaries, or by first permuting the arrays such that the contraction becomes equivalent to a matrix product, which is then performed by BLAS. The latter is typically faster for large arrays. The choice of method is globally controlled by the methods [`enable_blas()`](@ref) and [`disable_blas()`](@ref).

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"""
function tensorcontract(A, IA::Tuple, B, IB::Tuple, IC::Tuple)
    oindA, cindA, oindB, cindB, indCinoAB = contract_indices(IA, IB, IC)

    T = promote_type(eltype(A), eltype(B))
    C = similar_from_indices(T, oindA, oindB, indCinoAB, (), A, B, :N, :N)

    contract!(1, A, :N, B, :N, 0, C, oindA, cindA, oindB, cindB, indCinoAB)
    return C
end

```

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```
tensorproduct(A, IA, B, IB, IC = (IA..., IB...))
```

Computes the tensor product of two arrays `A` and `B`, i.e. returns a new array `C` with `ndims(C) = ndims(A)+ndims(B)`. The indices of the output tensor are related to those of the input tensors by the pattern specified by the indices. Essentially, this is a special case of `tensorcontract` with no indices being contracted over. This method checks whether the indices indeed specify a tensor product instead of a genuine contraction.

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```
function tensorproduct(A, IA::Tuple, B, IB::Tuple, IC::Tuple = (IA..., IB...))  
    isempty(intersect(IA, IB)) || throw(IndexError("not a valid tensor product"))  
    tensorcontract(A, IA, B, IB, IC)  
end
```