```
# TensorMap & Tensor:
# general tensor implementation with arbitrary symmetries
0.00
    struct TensorMap{S<:IndexSpace, N<sub>1</sub>, N<sub>2</sub>, ...} <: AbstractTensorMap{S, N<sub>1</sub>, N<sub>2</sub>}
Specific subtype of [`AbstractTensorMap`](@ref) for representing tensor maps
(morphisms in
a tensor category) whose data is stored in blocks of some subtype of `DenseMatrix`.
struct TensorMap{S<:IndexSpace, N<sub>1</sub>, N<sub>2</sub>, I<:Sector,
A<:Union{<:DenseMatrix, SectorDict{I,<:DenseMatrix}}, F1, F2} <:
AbstractTensorMap{S, N<sub>1</sub>, N<sub>2</sub>}
    data::A
    codom::ProductSpace{S,N1}
    dom::ProductSpace{S,N2}
    rowr::SectorDict{I,FusionTreeDict{F1,UnitRange{Int}}}
    colr::SectorDict{I,FusionTreeDict{F2,UnitRange{Int}}}
    function TensorMap{S, N1, N2, I, A, F1, F2}(data::A,
                  codom::ProductSpace{S,N1}, dom::ProductSpace{S,N2},
                  rowr::SectorDict{I,FusionTreeDict{F1,UnitRange{Int}}},
                  colr::SectorDict{I,FusionTreeDict{F2,UnitRange{Int}}}) where
                       {S<:IndexSpace, N<sub>1</sub>, N<sub>2</sub>, I<:Sector,
A<:SectorDict{I,<:DenseMatrix},
                        F<sub>1</sub><:FusionTree{I,N<sub>1</sub>}, F<sub>2</sub><:FusionTree{I,N<sub>2</sub>}}
         eltype(valtype(data)) ⊆ field(S) ||
             @warn("eltype(data) = $(eltype(data)) ⊈ $(field(S)))", maxlog=1)
         new{S, N1, N2, I, A, F1, F2}(data, codom, dom, rowr, colr)
    end
    function TensorMap{S, N1, N2, Trivial, A, Nothing, Nothing}(data::A,
                  codom::ProductSpace{S,N1}, dom::ProductSpace{S,N2}) where
                       {S<:IndexSpace, N<sub>1</sub>, N<sub>2</sub>, A<:DenseMatrix}
         eltype(data) ⊆ field(S) ||
             @warn("eltype(data) = $(eltype(data)) ⊈ $(field(S)))", maxlog=1)
         new{S, N1, N2, Trivial, A, Nothing, Nothing}(data, codom, dom)
    end
end
const Tensor{S<:IndexSpace, N, I<:Sector, A, F<sub>1</sub>, F<sub>2</sub>} = TensorMap{S, N, 0, I, A,
F_1, F_2
const TrivialTensorMap{S<:IndexSpace, N1, N2, A<:DenseMatrix} = TensorMap{S, N1,</pre>
N<sub>2</sub>, Trivial, A, Nothing, Nothing}
function tensormaptype(::Type{S}, N1::Int, N2::Int, ::Type{T}) where {S,T}
    I = sectortype(S)
    if T <: DenseMatrix</pre>
        M = T
    elseif T <: Number</pre>
         M = Matrix\{T\}
    else
         throw(ArgumentError("the final argument of `tensormaptype` should either
be the scalar or the storage type, i.e. a subtype of `Number` or of
`DenseMatrix`"))
    end
```

```
2021/6/A 2:19 DM
    if I === Trivial
        return TensorMap{S,N1,N2,I,M,Nothing,Nothing}
    else
        F_1 = fusiontreetype(I, N_1)
        F_2 = fusiontreetype(I, N_2)
        return TensorMap{S,N1,N2,I,SectorDict{I,M},F1,F2}
    end
end
tensormaptype(S, N_1, N_2 = 0) = tensormaptype(S, N_1, N_2, Float64)
# Basic methods for characterising a tensor:
storagetype(::Type{<:TensorMap{<:IndexSpace, N1, N2, Trivial, A}}) where</pre>
    \{N_1, N_2, A < : DenseMatrix\} = A
storagetype(::Type{<:TensorMap{<:IndexSpace, N1, N2, I, <:SectorDict{I,A}}}) where</pre>
    \{N_1,N_2,I<:Sector,A<:DenseMatrix\} = A
codomain(t::TensorMap) = t.codom
domain(t::TensorMap) = t.dom
blocks(t::TensorMap\{<:IndexSpace,N_1,N_2,Trivial\}) where \{N_1,N_2\} =
    SingletonDict(Trivial()=>t.data)
blocks(t::TensorMap) = t.data
blocksectors(t::TrivialTensorMap) = TrivialOrEmptyIterator(dim(t) == 0)
blocksectors(t::TensorMap) = keys(t.data)
hasblock(t::TrivialTensorMap, ::Trivial) = true
hasblock(t::TensorMap, s::Sector) = haskey(t.data, s)
block(t::TrivialTensorMap, ::Trivial) = t.data
function block(t::TensorMap, s::Sector)
    sectortype(t) == typeof(s) || throw(SectorMismatch())
    A = valtype(t.data) # This line is useless
    if haskey(t.data, s)
        return t.data[s]
    else # at least one of the two matrix dimensions will be zero
        return storagetype(t)(undef, (blockdim(codomain(t),s), blockdim(domain(t),
s)))
    end
end
dim(t::TensorMap) = mapreduce(x->length(x[2]), +, blocks(t); init = 0)
fusiontrees(t::TrivialTensorMap) = ((nothing, nothing),)
fusiontrees(t::TensorMap) = TensorKeyIterator(t.rowr, t.colr)
# General TensorMap constructors
# without data: generic constructor from callable:
function TensorMap(f, codom::ProductSpace{S,N1}, dom::ProductSpace{S,N2}) where
{S<:IndexSpace, N<sub>1</sub>, N<sub>2</sub>}
    I = sectortype(S)
    if I == Trivial
```

tensor il 2021/6/4 3:19 DM

```
d1 = dim(codom)
        d2 = dim(dom)
        data = f((d1,d2))
        A = typeof(data)
         return TensorMap{S, N1, N2, Trivial, A, Nothing, Nothing}(data, codom, dom)
    else
        F_1 = fusiontreetype(I, N_1)
        F_2 = fusiontreetype(I, N_2)
        # TODO: the current approach is not very efficient and somewhat wasteful
         sampledata = f((1,1))
        if !isreal(I) && eltype(sampledata) <: Real</pre>
             A = typeof(complex(sampledata))
             A = typeof(sampledata)
        end
        data = SectorDict{I,A}()
         rowr = SectorDict{I, FusionTreeDict{F1, UnitRange{Int}}}()
         colr = SectorDict{I, FusionTreeDict{F2, UnitRange{Int}}}()
         for c in blocksectors(codom ← dom)
             rowrc = FusionTreeDict{F<sub>1</sub>, UnitRange{Int}}()
             colrc = FusionTreeDict{F2, UnitRange{Int}}()
             offset1 = 0
             for s1 in sectors(codom)
                 for f1 in fusiontrees(s1, c, map(isdual, codom.spaces))
                     r = (offset1 + 1):(offset1 + dim(codom, s1))
                     push!(rowrc, f1 => r)
                     offset1 = last(r)
                 end
             end
             dim1 = offset1
             offset2 = 0
             for s2 in sectors(dom)
                 for f2 in fusiontrees(s2, c, map(isdual, dom.spaces))
                     r = (offset2 + 1):(offset2 + dim(dom, s2))
                     push!(colrc, f2 => r)
                     offset2 = last(r)
                 end
             end
             dim2 = offset2
             push!(data, c=>f((dim1, dim2)))
             push!(rowr, c=>rowrc)
             push!(colr, c=>colrc)
         return TensorMap{S, N<sub>1</sub>, N<sub>2</sub>, I, SectorDict{I,A}, F<sub>1</sub>, F<sub>2</sub>}(data, codom, dom,
rowr, colr)
    end
end
# with data
function TensorMap(data::DenseArray, codom::ProductSpace{S,N1},
dom::ProductSpace{S,N2};
             tol = sqrt(eps(real(float(eltype(data)))))) where {S<:IndexSpace, N1,
N_2
```

```
2021/6/A 2:10 DM
    (d1, d2) = (dim(codom), dim(dom))
    if !(length(data) == d1*d2 || size(data) == (d1, d2) ||
        size(data) == (dims(codom)..., dims(dom)...))
        throw(DimensionMismatch())
    end
    if sectortype(S) === Trivial
        data2 = reshape(data, (d1, d2))
        A = typeof(data2)
        return TensorMap{S, N<sub>1</sub>, N<sub>2</sub>, Trivial, A, Nothing, Nothing}(data2, codom,
dom)
    else
        t = TensorMap(zeros, eltype(data), codom, dom)
        ta = convert(Array, t)
        l = length(ta)
        basis = zeros(eltype(ta), (l, dim(t)))
        qdims = zeros(real(eltype(ta)), (dim(t),))
        i = 1
        for (c,b) in blocks(t)
            for k = 1:length(b)
                b[k] = 1
                 copyto!(view(basis, :, i), reshape(convert(Array, t), (l,)))
                # TODO: change this to `copy!` once we drop support for Julia 1.4
                qdims[i] = dim(c)
                b[k] = 0
                i += 1
            end
        end
        rhs = reshape(data, (l,))
        if FusionStyle(sectortype(t)) isa UniqueFusion
            lhs = basis'*rhs
        else
            lhs = Diagonal(qdims) \ (basis'*rhs)
        end
        if norm(basis*lhs - rhs) > tol
            throw(ArgumentError("Data has non-zero elements at incompatible
positions"))
        end
        if eltype(lhs) != eltype(t)
            t2 = TensorMap(zeros, promote_type(eltype(lhs), eltype(t)), codom, dom)
        else
            t2 = t
        end
        i = 1
        for (c,b) in blocks(t2)
            for k = 1:length(b)
                b[k] = lhs[i]
                 i += 1
            end
        end
        return t2
    end
end
```

Page 4 of 11

function TensorMap(data::AbstractDict{<:Sector,<:DenseMatrix},</pre>

```
2021/6/A 2:10 DM
tancar il
  codom::ProductSpace{S,N1}, dom::ProductSpace{S,N2}) where {S<:IndexSpace, N1, N2}
       I = sectortype(S)
       I == keytype(data) || throw(SectorMismatch())
       if I == Trivial
           if dim(dom) != 0 && dim(codom) != 0
               return TensorMap(data[Trivial()], codom, dom)
           else
               return TensorMap(valtype(data)(undef, dim(codom), dim(dom)), codom,
  dom)
           end
       end
       F_1 = fusiontreetype(I, N_1)
       F_2 = fusiontreetype(I, N_2)
       rowr = SectorDict{I, FusionTreeDict{F1, UnitRange{Int}}}()
       colr = SectorDict{I, FusionTreeDict{F2, UnitRange{Int}}}()
       blockiterator = blocksectors(codom ← dom)
       for c in blockiterator
           rowrc = FusionTreeDict{F1, UnitRange{Int}}()
           colrc = FusionTreeDict{F2, UnitRange{Int}}()
           offset1 = 0
           for s1 in sectors(codom)
               for f1 in fusiontrees(s1, c, map(isdual, codom.spaces))
                    r = (offset1 + 1):(offset1 + dim(codom, s1))
                   push!(rowrc, f1 => r)
                   offset1 = last(r)
               end
           end
           offset2 = 0
           for s2 in sectors(dom)
               for f2 in fusiontrees(s2, c, map(isdual, dom.spaces))
                    r = (offset2 + 1):(offset2 + dim(dom, s2))
                   push!(colrc, f2 => r)
                   offset2 = last(r)
               end
           end
           (haskey(data, c) && size(data[c]) == (offset1, offset2)) ||
               throw(DimensionMismatch())
           push!(rowr, c=>rowrc)
           push!(colr, c=>colrc)
       end
       if !isreal(I) && eltype(valtype(data)) <: Real</pre>
           b = valtype(data)(undef, (0,0))
           V = typeof(complex(b))
           K = keytype(data)
           data2 = SectorDict{K,V}((c=>complex(data[c])) for c in blockiterator)
           A = typeof(data2)
           return TensorMap{S, N<sub>1</sub>, N<sub>2</sub>, I, A, F<sub>1</sub>, F<sub>2</sub>}(data2, codom, dom, rowr, colr)
       else
           V = valtype(data)
           K = keytype(data)
           data2 = SectorDict{K,V}((c=>data[c]) for c in blockiterator)
           A = typeof(data2)
           return TensorMap\{S, N_1, N_2, I, A, F_1, F_2\} (data2, codom, dom, rowr, colr)
       end
```

```
tensor il end
```

```
TensorMap(f,
            ::Type{T},
            codom::ProductSpace{S},
            dom::ProductSpace{S}) where {S<:IndexSpace, T<:Number} =</pre>
    TensorMap(d->f(T, d), codom, dom)
TensorMap(::Type{T},
            codom::ProductSpace{S},
            dom::ProductSpace{S}) where {S<:IndexSpace, T<:Number} =</pre>
    TensorMap(d->Array{T}(undef, d), codom, dom)
TensorMap(::UndefInitializer,
            ::Type{T},
            codom::ProductSpace{S},
            dom::ProductSpace{S}) where {S<:IndexSpace, T<:Number} =</pre>
    TensorMap(d->Array{T}(undef, d), codom, dom)
TensorMap(::UndefInitializer,
            codom::ProductSpace{S},
            dom::ProductSpace{S}) where {S<:IndexSpace} =</pre>
    TensorMap(undef, Float64, codom, dom)
TensorMap(::Type{T},
            codom::TensorSpace{S},
            dom::TensorSpace{S}) where {T<:Number, S<:IndexSpace} =</pre>
    TensorMap(T, convert(ProductSpace, codom), convert(ProductSpace, dom))
TensorMap(dataorf, codom::TensorSpace{S}, dom::TensorSpace{S}) where
{S<:IndexSpace} =
    TensorMap(dataorf, convert(ProductSpace, codom), convert(ProductSpace, dom))
TensorMap(dataorf, ::Type{T},
            codom::TensorSpace{S},
            dom::TensorSpace{S}) where {T<:Number, S<:IndexSpace} =</pre>
    TensorMap(dataorf, T, convert(ProductSpace, codom), convert(ProductSpace, dom))
TensorMap(codom::TensorSpace{S}, dom::TensorSpace{S}) where {S<:IndexSpace} =</pre>
    TensorMap(Float64, convert(ProductSpace, codom), convert(ProductSpace, dom))
TensorMap(dataorf, T::Type{<:Number}, P::TensorMapSpace{S}) where {S<:IndexSpace} =</pre>
    TensorMap(dataorf, T, codomain(P), domain(P))
TensorMap(dataorf, P::TensorMapSpace{S}) where {S<:IndexSpace} =</pre>
    TensorMap(dataorf, codomain(P), domain(P))
TensorMap(T::Type{<:Number}, P::TensorMapSpace{S}) where {S<:IndexSpace} =</pre>
    TensorMap(T, codomain(P), domain(P))
TensorMap(P::TensorMapSpace{S}) where {S<:IndexSpace} = TensorMap(codomain(P),</pre>
domain(P))
```

```
tancar il
                                                                                   2021/6/A 2:10 DM
  Tensor(dataorf, T::Type{<:Number}, P::TensorSpace{S}) where {S<:IndexSpace} =</pre>
       TensorMap(dataorf, T, P, one(P))
  Tensor(dataorf, P::TensorSpace{S}) where {S<:IndexSpace} = TensorMap(dataorf, P,</pre>
  one(P))
  Tensor(T::Type{<:Number}, P::TensorSpace{S}) where {S<:IndexSpace} = TensorMap(T,</pre>
  P, one(P))
  Tensor(P::TensorSpace{S}) where {S<:IndexSpace} = TensorMap(P, one(P))
  # Efficient copy constructors
  function Base.copy(t::TrivialTensorMap{S, N1, N2, A}) where {S, N1, N2, A}
       return TrivialTensorMap{S, N1, N2, A}(copy(t.data), t.codom, t.dom)
  function Base.copy(t::TensorMap{S, N1, N2, I, A, F1, F2}) where {S, N1, N2, I, A,
  F_1, F_2
       return TensorMap{S, N<sub>1</sub>, N<sub>2</sub>, I, A, F<sub>1</sub>, F<sub>2</sub>}(deepcopy(t.data), t.codom, t.dom,
  t.rowr, t.colr)
  end
  # Similar
  Base.similar(t::AbstractTensorMap, T::Type, codomain::VectorSpace,
  domain::VectorSpace) =
       similar(t, T, codomain←domain)
  Base.similar(t::AbstractTensorMap, codomain::VectorSpace, domain::VectorSpace) =
       similar(t, codomain←domain)
  Base.similar(t::AbstractTensorMap{S}, ::Type{T},
                    P::TensorMapSpace\{S\} = (domain(t) \rightarrow codomain(t))) where \{T,S\} =
       TensorMap(d->similarstoragetype(t, T)(undef, d), P)
  Base.similar(t::AbstractTensorMap{S}, ::Type{T}, P::TensorSpace{S}) where {T,S} =
       Tensor(d->similarstoragetype(t, T)(undef, d), P)
  Base.similar(t::AbstractTensorMap{S},
                    P::TensorMapSpace{S} = (domain(t) \rightarrow codomain(t))) where {S} =
       TensorMap(d->storagetype(t)(undef, d), P)
  Base.similar(t::AbstractTensorMap{S}, P::TensorSpace{S}) where {S} =
       Tensor(d->storagetype(t)(undef, d), P)
  function Base.complex(t::AbstractTensorMap)
       if eltype(t) <: Complex</pre>
           return t
       elseif t.data isa AbstractArray
           return TensorMap(complex(t.data), codomain(t), domain(t))
       else
           data = SectorDict(c=>complex(d) for (c,d) in t.data)
           return TensorMap(data, codomain(t), domain(t))
       end
  end
```

2021/8// 3:19 DM

```
# Conversion between TensorMap and Dict, for read and write purpose
function Base.convert(::Type{Dict}, t::AbstractTensorMap)
    d = Dict{Symbol, Any}()
    d[:codomain] = repr(codomain(t))
    d[:domain] = repr(domain(t))
    data = Dict{String,Any}()
    for (c,b) in blocks(t)
        data[repr(c)] = Array(b)
    end
    d[:data] = data
    return d
end
function Base.convert(::Type{TensorMap}, d::Dict{Symbol,Any})
    try
        codomain = eval(Meta.parse(d[:codomain]))
        domain = eval(Meta.parse(d[:domain]))
        data = SectorDict(eval(Meta.parse(c))=>b for (c,b) in d[:data])
        return TensorMap(data, codomain, domain)
    catch e # sector unknown in TensorKit.jl; user-defined, hopefully accessible
        in Main
        codomain = Base.eval(Main, Meta.parse(d[:codomain]))
        domain = Base.eval(Main, Meta.parse(d[:domain]))
        data = SectorDict(Base.eval(Main, Meta.parse(c))=>b for (c,b) in d[:data])
        return TensorMap(data, codomain, domain)
    end
end
# Getting and setting the data
@inline function Base.getindex(t::TensorMap{<:IndexSpace, N1, N2, I},</pre>
        f1::FusionTree{I,N<sub>1</sub>}, f2::FusionTree{I,N<sub>2</sub>}) where {N<sub>1</sub>,N<sub>2</sub>,I<:Sector}
    c = f1.coupled
    @boundscheck begin
        c == f2.coupled || throw(SectorMismatch())
        haskey(t.rowr[c], f1) || throw(SectorMismatch())
        haskey(t.colr[c], f2) || throw(SectorMismatch())
    end
    @inbounds begin
        d = (dims(codomain(t), f1.uncoupled)..., dims(domain(t), f2.uncoupled)...)
        return sreshape(StridedView(t.data[c])[t.rowr[c][f1], t.colr[c][f2]], d)
    end
end
@inline function Base.getindex(t::TensorMap{<:IndexSpace, N1, N2, I},</pre>
                                 sectors::Tuple{Vararg{I}}) where {N1,N2,I<:Sector}
    FusionStyle(I) isa UniqueFusion ||
        throw(SectorMismatch("Indexing with sectors only possible if unique
fusion"))
    s1 = TupleTools.getindices(sectors, codomainind(t))
    s2 = map(dual, TupleTools.getindices(sectors, domainind(t)))
```

```
2021/6/A 2:10 DM
tancar il
      c1 = length(s1) == 0 ? one(I) : (length(s1) == 1 ? s1[1] : first(<math>\otimes(s1...)))
      @boundscheck begin
           c2 = length(s2) == 0 ? one(I) : (length(s2) == 1 ? s2[1] : first(<math>\otimes(s2...)))
           c2 == c1 || throw(SectorMismatch("Not a valid sector for this tensor"))
           hassector(codomain(t), s1) && hassector(domain(t), s2)
      end
      f1 = FusionTree(s1, c1, map(isdual, tuple(codomain(t)...)))
      f2 = FusionTree(s2, c1, map(isdual, tuple(domain(t)...)))
      @inbounds begin
           return t[f1,f2]
      end
  end
  @propagate_inbounds Base.getindex(t::TensorMap, sectors::Tuple) =
       t[map(sectortype(t), sectors)]
  @propagate_inbounds Base.setindex!(t::TensorMap{<:IndexSpace, N1, N2, I},</pre>
                                        f1::FusionTree{I,N1},
                                        f2::FusionTree{I,N_2}) where {N_1,N_2,I<:Sector} =
                                        copy!(getindex(t, f1, f2), v)
  # For a tensor with trivial symmetry, allow no argument indexing
  @inline Base.getindex(t::TrivialTensorMap) =
       sreshape(StridedView(t.data), (dims(codomain(t))..., dims(domain(t))...))
  @inline Base.setindex!(t::TrivialTensorMap, v) = copy!(getindex(t), v)
  # For a tensor with trivial symmetry, fusiontrees returns (nothing, nothing)
  @inline Base.getindex(t::TrivialTensorMap, ::Nothing) = getindex(t)
  @inline Base.setindex!(t::TrivialTensorMap, v, ::Nothing, ::Nothing) =
  setindex!(t, v)
  # For a tensor with trivial symmetry, allow direct indexing
  @inline function Base.getindex(t::TrivialTensorMap, indices::Vararg{Int})
      data = t[]
      @boundscheck checkbounds(data, indices...)
      @inbounds v = data[indices...]
       return v
  end
  @inline function Base.setindex!(t::TrivialTensorMap, v, indices::Vararg{Int})
      data = t[]
      @boundscheck checkbounds(data, indices...)
      @inbounds data[indices...] = v
      return v
  end
  # Show
  function Base.summary(t::TensorMap)
      print("TensorMap(", codomain(t), " \( \ '', \) domain(t), ")")
  end
  function Base.show(io::I0, t::TensorMap{S}) where {S<:IndexSpace}</pre>
      if get(io, :compact, false)
           print(io, "TensorMap(", codomain(t), " ← ", domain(t), ")")
           return
```

```
tancar il
                                                                                2021/6/A 2:10 DM
      println(io, "TensorMap(", codomain(t), " ← ", domain(t), "):")
      if sectortype(S) == Trivial
           Base.print_array(io, t[])
           println(io)
      elseif FusionStyle(sectortype(S)) isa UniqueFusion
           for (f1,f2) in fusiontrees(t)
               println(io, "* Data for sector ", f1.uncoupled, " ← ", f2.uncoupled,
  ":")
               Base.print_array(io, t[f1,f2])
               println(io)
          end
      else
           for (f1,f2) in fusiontrees(t)
               println(io, "* Data for fusiontree ", f1, " ← ", f2, ":")
               Base.print_array(io, t[f1,f2])
               println(io)
           end
      end
  end
  # Real and imaginary parts
  function Base.real(t::AbstractTensorMap{S}) where {S}
      # `isreal` for a `Sector` returns true iff the F and R symbols are real. This
        quarantees
      # that the real/imaginary part of a tensor `t` can be obtained by just taking
      # real/imaginary part of the degeneracy data.
      if isreal(sectortype(S))
           realdata = Dict(k => real(v) for (k, v) in blocks(t))
           return TensorMap(realdata, codomain(t), domain(t))
      else
          msg = "`real` has not been implemented for `AbstractTensorMap{$(S)}`."
          throw(ArgumentError(msg))
      end
  end
  function Base.imag(t::AbstractTensorMap{S}) where {S}
      # `isreal` for a `Sector` returns true iff the F and R symbols are real. This
        guarantees
      # that the real/imaginary part of a tensor `t` can be obtained by just taking
      # real/imaginary part of the degeneracy data.
      if isreal(sectortype(S))
           imagdata = Dict(k => imag(v) for (k, v) in blocks(t))
           return TensorMap(imagdata, codomain(t), domain(t))
      else
          msg = "`imag` has not been implemented for `AbstractTensorMap{$(S)}`."
           throw(ArgumentError(msg))
      end
  end
  # Conversion and promotion:
  Base.convert(::Type{TensorMap}, t::TensorMap) = t
```

```
Base.convert(::Type{TensorMap}, t::AbstractTensorMap) =
    copy!(TensorMap(undef, eltype(t), codomain(t), domain(t)), t)
function Base.convert(T::Type{TensorMap{S,N1,N2,I,A,F1,F2}},
                        t::AbstractTensorMap{S,N1,N2}) where {S,N1,N2,I,A,F1,F2}
    if typeof(t) == T
        return t
    else
        data = Dict(c=>convert(storagetype(T), b) for (c,b) in blocks(t))
        return TensorMap(data, codomain(t), domain(t))
    end
```

end