

```
# Tensor factorization
```

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#-----
```

```
const OFA = OrthogonalFactorizationAlgorithm
```

```
import LinearAlgebra: svd!, svd
```

```
const SVDAlg = Union{SVD, SDD}
```

```
Base.@deprecate(
```

```
    svd(t::AbstractTensorMap, leftind::IndexTuple, rightind::IndexTuple;
        trunc::TruncationScheme = notrunc(), p::Real = 2, alg::SVDAlg = SDD()),
    tsvd(t, leftind, rightind; trunc = trunc, p = p, alg = alg))
```

```
Base.@deprecate(
```

```
    svd(t::AbstractTensorMap;
        trunc::TruncationScheme = notrunc(), p::Real = 2, alg::SVDAlg = SDD()),
    tsvd(t; trunc = trunc, p = p, alg = alg))
```

```
Base.@deprecate(
```

```
    svd!(t::AbstractTensorMap;
        trunc::TruncationScheme = notrunc(), p::Real = 2, alg::SVDAlg = SDD()),
    tsvd(t; trunc = trunc, p = p, alg = alg))
```

```
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```

```
    tsvd(t::AbstractTensorMap, leftind::Tuple, rightind::Tuple;
        trunc::TruncationScheme = notrunc(), p::Real = 2, alg::Union{SVD, SDD} =
SDD())
    -> U, S, V, ε
```

Compute the (possibly truncated) singular value decomposition such that $\text{`norm(permute}(t, \text{`leftind}, \text{`rightind}) - U * S * V) \approx \epsilon$, where ϵ thus represents the truncation error.

If `leftind and `rightind are not specified, the current partition of left and right indices of `t is used. In that case, less memory is allocated if one allows the data in `t to be destroyed/overwritten, by using $\text{`tsvd}!(t, \text{trunc} = \text{notrunc}(), p = 2)\text{`}$.

A truncation parameter `trunc can be specified for the new internal dimension, in which

case a truncated singular value decomposition will be computed. Choices are:

- * $\text{`notrunc}()$: no truncation (default);
- * $\text{`truncerr}(\eta::\text{Real})$: truncates such that the p -norm of the truncated singular values is smaller than η times the p -norm of all singular values;
- * $\text{`truncdim}(\chi::\text{Int})$: truncates such that the equivalent total dimension of the internal vector space is no larger than χ ;
- * $\text{`truncspace}(V)$: truncates such that the dimension of the internal vector space is smaller than that of V in any sector.
- * $\text{`trunbelow}(\chi::\text{Real})$: truncates such that every singular value is larger than χ ;

The method `tsvd also returns the truncation error ϵ , computed as the p norm of the

singular values that were truncated.

The keyword ``alg`` can be equal to ``SVD()`` or ``SDD()``, corresponding to the underlying LAPACK algorithm that computes the decomposition (``_gesvd`` or ``_gesdd``).

Orthogonality requires ``spacetype(t)<:InnerProductSpace``, and ``svd(!)`` is currently only implemented for ``spacetype(t)<:EuclideanSpace``.

====

```
tsvd(t::AbstractTensorMap, p1::IndexTuple, p2::IndexTuple; kwargs...) =
    tsvd!(permute(t, p1, p2; copy = true); kwargs...)
```

====

```
    leftorth(t::AbstractTensorMap, leftind::Tuple, rightind::Tuple;
        alg::OrthogonalFactorizationAlgorithm = QRpos()) -> Q, R
```

Create orthonormal basis ``Q`` for indices in ``leftind``, and remainder ``R`` such that ``permute(t, leftind, rightind) = Q*R``.

If ``leftind`` and ``rightind`` are not specified, the current partition of left and right indices of ``t`` is used. In that case, less memory is allocated if one allows the data in ``t`` to be destroyed/overwritten, by using ``leftorth!(t, alg = QRpos())``.

Different algorithms are available, namely ``QR()``, ``QRpos()``, ``SVD()`` and ``Polar()``. ``QR()``

and ``QRpos()`` use a standard QR decomposition, producing an upper triangular matrix ``R``.

``Polar()`` produces a Hermitian and positive semidefinite ``R``. ``QRpos()`` corrects the

standard QR decomposition such that the diagonal elements of ``R`` are positive. Only ``QRpos()`` and ``Polar()`` are unique (no residual freedom) so that they always return the same result for the same input tensor ``t``.

Orthogonality requires ``spacetype(t)<:InnerProductSpace``, and ``leftorth(!)`` is currently only implemented for ``spacetype(t)<:EuclideanSpace``.

====

```
leftorth(t::AbstractTensorMap, p1::IndexTuple, p2::IndexTuple; kwargs...) =
    leftorth!(permute(t, p1, p2; copy = true); kwargs...)
```

====

```
    rightorth(t::AbstractTensorMap, leftind::Tuple, rightind::Tuple;
        alg::OrthogonalFactorizationAlgorithm = LQpos()) -> L, Q
```

Create orthonormal basis ``Q`` for indices in ``rightind``, and remainder ``L`` such that ``permute(t, leftind, rightind) = L*Q``.

If ``leftind`` and ``rightind`` are not specified, the current partition of left and right indices of ``t`` is used. In that case, less memory is allocated if one allows the data in ``t``

to be destroyed/overwritten, by using ``rightorth!(t, alg = LQpos())``.

Different algorithms are available, namely ``LQ()``, ``LQpos()``, ``RQ()``, ``RQpos()``, ``SVD()`` and ``Polar()``. ``LQ()`` and ``LQpos()`` produce a lower triangular matrix ``L`` and are computed using a QR decomposition of the transpose. ``RQ()`` and ``RQpos()`` produce an upper triangular remainder ``L`` and only works if the total left dimension is smaller than or equal to the total right dimension. ``LQpos()`` and ``RQpos()`` add an additional correction such that the diagonal elements of ``L`` are positive. ``Polar()`` produces a Hermitian and positive semidefinite ``L``. Only ``LQpos()``, ``RQpos()`` and ``Polar()`` are unique (no residual freedom) so that they always return the same result for the same input tensor ``t``.

Orthogonality requires ``spacetype(t)<:InnerProductSpace``, and ``rightorth(!)`` is currently only implemented for ``spacetype(t)<:EuclideanSpace``.

====

```
rightorth(t::AbstractTensorMap, p1::IndexTuple, p2::IndexTuple; kwargs...) =
    rightorth!(permute(t, p1, p2; copy = true); kwargs...)
```

====

```
leftnull(t::AbstractTensor, leftind::Tuple, rightind::Tuple;
        alg::OrthogonalFactorizationAlgorithm = QRpos()) -> N
```

Create orthonormal basis for the orthogonal complement of the support of the indices in ``leftind``, such that ``N' * permute(t, leftind, rightind) = 0``.

If ``leftind`` and ``rightind`` are not specified, the current partition of left and right indices of ``t`` is used. In that case, less memory is allocated if one allows the data in ``t`` to be destroyed/overwritten, by using ``leftnull!(t, alg = QRpos())``.

Different algorithms are available, namely ``QR()`` (or equivalently, ``QRpos()``), ``SVD()`` and ``SDD()``. The first assumes that the matrix is full rank and requires ``iszero(atol)`` and ``iszero(rtol)``. With ``SVD()`` and ``SDD()``, ``rightnull`` will use the corresponding singular value decomposition, and one can specify an absolute or relative tolerance for which singular values are to be considered zero, where ``max(atol, norm(t)*rtol)`` is used as upper bound.

Orthogonality requires ``spacetype(t)<:InnerProductSpace``, and ``leftnull(!)`` is currently only implemented for ``spacetype(t)<:EuclideanSpace``.

====

```
leftnull(t::AbstractTensorMap, p1::IndexTuple, p2::IndexTuple; kwargs...) =
    leftnull!(permute(t, p1, p2; copy = true); kwargs...)
```

```
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```

```
    rightnull(t::AbstractTensor, leftind::Tuple, rightind::Tuple;
              alg::OrthogonalFactorizationAlgorithm = LQ(),
              atol::Real = 0.0,
              rtol::Real = eps(real(float(one(eltype(t))))) * iszero(atol)) -> N
```

Create orthonormal basis for the orthogonal complement of the support of the indices in
``rightind``, such that ``permute(t, leftind, rightind)*N' = 0``.

If ``leftind`` and ``rightind`` are not specified, the current partition of left and right indices of ``t`` is used. In that case, less memory is allocated if one allows the data in ``t`` to be destroyed/overwritten, by using ``rightnull!(t, alg = LQpos())``.

Different algorithms are available, namely ``LQ()`` (or equivalently, ``LQpos()``), ``SVD()`` and ``SDD()``. The first assumes that the matrix is full rank and requires ``iszero(atol)`` and ``iszero(rtol)``. With ``SVD()`` and ``SDD()``, ``rightnull`` will use the corresponding singular value decomposition, and one can specify an absolute or relative tolerance for which singular values are to be considered zero, where ``max(atol, norm(t)*rtol)`` is used as upper bound.

Orthogonality requires ``spacetype(t)<:InnerProductSpace``, and ``rightnull(!)`` is currently only implemented for ``spacetype(t)<:EuclideanSpace``.

```
====
```

```
rightnull(t::AbstractTensorMap, p1::IndexTuple, p2::IndexTuple; kwargs...) =
    rightnull!(permute(t, p1, p2; copy = true); kwargs...)
```

```
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```

```
    eigen(t::AbstractTensor, leftind::Tuple, rightind::Tuple; kwargs...) -> D, V
```

Compute eigenvalue factorization of tensor ``t`` as linear map from ``rightind`` to ``leftind``.

If ``leftind`` and ``rightind`` are not specified, the current partition of left and right indices of ``t`` is used. In that case, less memory is allocated if one allows the data in ``t`` to be destroyed/overwritten, by using ``eigen!(t)``. Note that the permuted tensor on which ``eigen!`` is called should have equal domain and codomain, as otherwise the eigenvalue decomposition is meaningless and cannot satisfy

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```

```
permute(t, leftind, rightind) * V = V * D
```

```

Accepts the same keyword arguments `scale`, `permute` and `sortby` as `eigen` of dense matrices. See the corresponding documentation for more information.

See also `eig` and `eigh`

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```
LinearAlgebra.eigen(t::AbstractTensorMap, p1::IndexTuple, p2::IndexTuple;
kwargs...) =
    eig!(permute(t, p1, p2; copy = true); kwargs...)
```

```
=====
```

```
eig(t::AbstractTensor, leftind::Tuple, rightind::Tuple; kwargs...) -> D, V
```

Compute eigenvalue factorization of tensor `t` as linear map from `rightind` to `leftind`.

The function `eig` assumes that the linear map is not hermitian and returns type stable

complex valued `D` and `V` tensors for both real and complex valued `t`. See `eigh` for hermitian linear maps

If `leftind` and `rightind` are not specified, the current partition of left and right

indices of `t` is used. In that case, less memory is allocated if one allows the data in

`t` to be destroyed/overwritten, by using `eig!(t)`. Note that the permuted tensor on

which `eig!` is called should have equal domain and codomain, as otherwise the eigenvalue

decomposition is meaningless and cannot satisfy

```
```
```

```
permute(t, leftind, rightind) * V = V * D
```

```

Accepts the same keyword arguments `scale`, `permute` and `sortby` as `eigen` of dense matrices. See the corresponding documentation for more information.

See also `eigen` and `eigh`.

```
=====
```

```
eig(t::AbstractTensorMap, p1::IndexTuple, p2::IndexTuple; kwargs...) =
    eig!(permute(t, p1, p2; copy = true); kwargs...)
```

```
=====
```

```
eigh(t::AbstractTensorMap{<:EuclideanSpace}, leftind::Tuple, rightind::Tuple)
-> D, V
```

Compute eigenvalue factorization of tensor `t` as linear map from `rightind` to `leftind`.

The function `eigh` assumes that the linear map is hermitian and `D` and `V` tensors with

the same `eltype` as `t`. See `eig` and `eigen` for non-hermitian tensors.

Hermiticity

requires that the tensor acts on inner product spaces, and the current implementation

requires ``spacety(t) <: EuclideanSpace``.

If ``leftind`` and ``rightind`` are not specified, the current partition of left and right

indices of ``t`` is used. In that case, less memory is allocated if one allows the data in

``t`` to be destroyed/overwritten, by using ``eigh!(t)``. Note that the permuted tensor on

which ``eigh!`` is called should have equal domain and codomain, as otherwise the eigenvalue

decomposition is meaningless and cannot satisfy

```

```
permute(t, leftind, rightind) * V = V * D
```

```

See also ``eigen`` and ``eig``.

====

```
eigh(t::AbstractTensorMap, p1::IndexTuple, p2::IndexTuple) =  
    eigh!(permute(t, p1, p2; copy = true))
```

====

```
isposdef(t::AbstractTensor{<:EuclideanSpace}, leftind::Tuple, rightind::Tuple)  
-> ::Bool
```

Test whether a tensor ``t`` is positive definite as linear map from ``rightind`` to ``leftind``.

If ``leftind`` and ``rightind`` are not specified, the current partition of left and right

indices of ``t`` is used. In that case, less memory is allocated if one allows the data in

``t`` to be destroyed/overwritten, by using ``isposdef!(t)``. Note that the permuted tensor on

which ``isposdef!`` is called should have equal domain and codomain, as otherwise it is

meaningless

Accepts the same keyword arguments ``scale``, ``permute`` and ``sortby`` as ``eigen`` of dense

matrices. See the corresponding documentation for more information.

====

```
LinearAlgebra.isposdef(t::AbstractTensorMap, p1::IndexTuple, p2::IndexTuple) =  
    isposdef!(permute(t, p1, p2; copy = true))
```

```
tsvd(t::AbstractTensorMap; trunc::TruncationScheme = NoTruncation(),  
      p::Real = 2, alg::Union{SVD, SDD} = SDD()) =  
    tsvd!(copy(t); trunc = trunc, p = p, alg = alg)
```

```
leftorth(t::AbstractTensorMap; alg::OFA = QRpos(), kwargs...) =  
    leftorth!(copy(t); alg = alg, kwargs...)
```

```
rightorth(t::AbstractTensorMap; alg::OFA = LQpos(), kwargs...) =  
    rightorth!(copy(t); alg = alg, kwargs...)
```

```

leftnull(t::AbstractTensorMap; alg::OFA = QR(), kwargs...) =
    leftnull!(copy(t); alg = alg, kwargs...)
rightnull(t::AbstractTensorMap; alg::OFA = LQ(), kwargs...) =
    rightnull!(copy(t); alg = alg, kwargs...)
LinearAlgebra.eigen(t::AbstractTensorMap; kwargs...) = eigen!(copy(t); kwargs...)
eig(t::AbstractTensorMap; kwargs...) = eig!(copy(t); kwargs...)
eigh(t::AbstractTensorMap; kwargs...) = eigh!(copy(t); kwargs...)
LinearAlgebra.isposdef(t::AbstractTensorMap) = isposdef!(copy(t))

# Orthogonal factorizations (mutation for recycling memory):
# only correct if Euclidean inner product
#-----
leftorth!(t::AdjointTensorMap{S}; alg::OFA = QRpos()) where {S<:EuclideanSpace} =
    map(adjoint, reverse(rightorth!(adjoint(t); alg = alg')))

rightorth!(t::AdjointTensorMap{S}; alg::OFA = LQpos()) where {S<:EuclideanSpace} =
    map(adjoint, reverse(leftorth!(adjoint(t); alg = alg')))

leftnull!(t::AdjointTensorMap{S}; alg::OFA = QR(), kwargs...) where
{S<:EuclideanSpace} =
    adjoint(rightnull!(adjoint(t); alg = alg', kwargs...))

rightnull!(t::AdjointTensorMap{S}; alg::OFA = LQ(), kwargs...) where
{S<:EuclideanSpace} =
    adjoint(leftnull!(adjoint(t); alg = alg', kwargs...))

function tsvd!(t::AdjointTensorMap{S};
    trunc::TruncationScheme = NoTruncation(),
    p::Real = 2,
    alg::Union{SVD, SDD} = SDD()) where {S<:EuclideanSpace}
    u, s, vt, err = tsvd!(adjoint(t); trunc = trunc, p = p, alg = alg)
    return adjoint(vt), adjoint(s), adjoint(u), err
end

function leftorth!(t::TensorMap{<:EuclideanSpace};
    alg::Union{QR, QRpos, QL, QLpos, SVD, SDD, Polar} = QRpos(),
    atol::Real = zero(float(real(eltype(t)))),
    rtol::Real = (alg ∈ (SVD(), SDD())) ?
zero(float(real(eltype(t)))) :
    eps(real(float(one(eltype(t))))) * iszero(atol))
    if !iszero(rtol)
        atol = max(atol, rtol * norm(t))
    end
    I = sectortype(t)
    S = spacetype(t)
    A = storagetype(t)
    Qdata = SectorDict{I, A}()
    Rdata = SectorDict{I, A}()
    dims = SectorDict{I, Int}()
    for c in blocksectors(domain(t))
        isempty(block(t, c)) && continue
        Q, R = _leftorth!(block(t, c), alg, atol)
        Qdata[c] = Q
    end
end

```

```

        Rdata[c] = R
        dims[c] = size(Q, 2)
    end
    V = S(dims)
    if alg isa Polar
        @assert V ≅ domain(t)
        W = domain(t)
    elseif length(domain(t)) == 1 && domain(t) ≅ V
        W = domain(t)
    elseif length(codomain(t)) == 1 && codomain(t) ≅ V
        W = codomain(t)
    else
        W = ProductSpace(V)
    end
    return TensorMap(Qdata, codomain(t)←W), TensorMap(Rdata, W←domain(t))
end

function leftnull!(t::TensorMap{<:EuclideanSpace};
    alg::Union{QR, QRpos, SVD, SDD} = QRpos(),
    atol::Real = zero(float(real(eltype(t)))),
    rtol::Real = (alg ∉ (SVD(), SDD())) ?
zero(float(real(eltype(t)))) :
    eps(real(float(one(eltype(t))))) * iszero(atol))
    if !iszero(rtol)
        atol = max(atol, rtol * norm(t))
    end
    I = sectortype(t)
    S = spacetype(t)
    A = storagetype(t)
    V = codomain(t)
    Ndata = SectorDict{I, A}()
    dims = SectorDict{I, Int}()
    for c in blocksectors(V)
        N = _leftnull!(block(t, c), alg, atol)
        Ndata[c] = N
        dims[c] = size(N, 2)
    end
    W = S(dims)
    return TensorMap(Ndata, V←W)
end

function rightorth!(t::TensorMap{<:EuclideanSpace};
    alg::Union{LQ, LQpos, RQ, RQpos, SVD, SDD, Polar} = LQpos(),
    atol::Real = zero(float(real(eltype(t)))),
    rtol::Real = (alg ∉ (SVD(), SDD())) ?
zero(float(real(eltype(t)))) :
    eps(real(float(one(eltype(t))))) * iszero(atol))
    if !iszero(rtol)
        atol = max(atol, rtol * norm(t))
    end
    I = sectortype(t)
    S = spacetype(t)
    A = storagetype(t)
    Ldata = SectorDict{I, A}()

```



```

Qdata = SectorDict{I, A}()
dims = SectorDict{I, Int}()
for c in blocksectors(codomain(t))
    isempty(block(t,c)) && continue
    L, Q = _rightorth!(block(t, c), alg, atol)
    Ldata[c] = L
    Qdata[c] = Q
    dims[c] = size(Q, 1)
end
V = S(dims)
if alg isa Polar
    @assert V ≅ codomain(t)
    W = codomain(t)
elseif length(codomain(t)) == 1 && codomain(t) ≅ V
    W = codomain(t)
elseif length(domain(t)) == 1 && domain(t) ≅ V
    W = domain(t)
else
    W = ProductSpace(V)
end
return TensorMap(Ldata, codomain(t)←W), TensorMap(Qdata, W←domain(t))
end

```

```

function rightnull!(t::TensorMap{<:EuclideanSpace};
    alg::Union{LQ, LQpos, SVD, SDD} = LQpos(),
    atol::Real = zero(float(real(eltype(t)))),
    rtol::Real = (alg ∉ (SVD(), SDD())) ?
zero(float(real(eltype(t)))) :
    eps(real(float(one(eltype(t))))) * iszero(atol))
    if !iszero(rtol)
        atol = max(atol, rtol*norm(t))
    end
    I = sectortype(t)
    S = spacetype(t)
    A = storagetype(t)
    V = domain(t)
    Ndata = SectorDict{I, A}()
    dims = SectorDict{I, Int}()
    for c in blocksectors(V)
        N = _rightnull!(block(t, c), alg, atol)
        Ndata[c] = N
        dims[c] = size(N, 1)
    end
    W = S(dims)
    return TensorMap(Ndata, W←V)
end

```

```

function tsvd!(t::TensorMap{<:EuclideanSpace};
    trunc::TruncationScheme = NoTruncation(),
    p::Real = 2,
    alg::Union{SVD, SDD} = SDD())
    S = spacetype(t)
    I = sectortype(t)
    A = storagetype(t)

```

```

Ar = similarstorage{t, real(eltype(t))}
Udata = SectorDict{I, A}{}
Σdata = SectorDict{I, Ar}{} # this will contain the singular values as matrix
Vdata = SectorDict{I, A}{}
dims = SectorDict{sector{t}, Int}{}
if isempty(blocksectors(t))
    W = S(dims)
    truncerr = zero(real(eltype(t)))
    return TensorMap(Udata, codomain(t)←W), TensorMap(Σdata, W←W),
           TensorMap(Vdata, W←domain(t)), truncerr
end
for (c, b) in blocks(t)
    U, Σ, V = _svd!(b, alg)
    Udata[c] = U
    Vdata[c] = V
    if @isdefined Σdata # cannot easily infer the type of Σ, so use this construction
        Σdata[c] = Σ
    else
        Σdata = SectorDict{c=>Σ}
    end
    dims[c] = length(Σ)
end
if !isa(trunc, NoTruncation)
    Σdata, truncerr = _truncate!(Σdata, trunc, p)
    truncdims = SectorDict{I, Int}{}
    for c in blocksectors(t)
        truncdim = length(Σdata[c])
        if truncdim != 0
            truncdims[c] = truncdim
            if truncdim != dims[c]
                Udata[c] = Udata[c][:, 1:truncdim]
                Vdata[c] = Vdata[c][1:truncdim, :]
            end
        else
            delete!(Udata, c)
            delete!(Vdata, c)
            delete!(Σdata, c)
        end
    end
    dims = truncdims
    W = S(dims)
else
    W = S(dims)
    if length(domain(t)) == 1 && domain(t)[1] ≅ W
        W = domain(t)[1]
    elseif length(codomain(t)) == 1 && codomain(t)[1] ≅ W
        W = codomain(t)[1]
    end
    truncerr = abs(zero(eltype(t)))
end
for (c, Σ) in Σdata
    Σdata[c] = copyto!(similar(Σ, length(Σ), length(Σ)), Diagonal(Σ))
end

```

```

        return TensorMap(Udata, codomain(t)←W), TensorMap(Σmdata, W←W),
            TensorMap(Vdata, W←domain(t)), truncerr
    end

function LinearAlgebra.ishermitian(t::TensorMap)
    domain(t) == codomain(t) || return false
    spacetype(t) <: EuclideanSpace || return false # hermiticity only defined for
    euclidean
    for (c, b) in blocks(t)
        ishermitian(b) || return false
    end
    return true
end

LinearAlgebra.eigen!(t::TensorMap) = ishermitian(t) ? eigh!(t) : eig!(t)

function eigh!(t::TensorMap{<:EuclideanSpace}; kwargs...)
    domain(t) == codomain(t) ||
        throw(SpaceMismatch("`eigh!` requires domain and codomain to be the same"))
    S = spacetype(t)
    I = sectortype(t)
    A = storagetype(t)
    Ar = similarstoragetype(t, real(eltype(t)))
    Ddata = SectorDict{I, Ar}()
    Vdata = SectorDict{I, A}()
    dims = SectorDict{I, Int}()
    for (c, b) in blocks(t)
        values, vectors = eigen!(Hermitian(b); kwargs...)
        d = length(values)
        Ddata[c] = copyto!(similar(values, (d, d)), Diagonal(values))
        Vdata[c] = vectors
        dims[c] = d
    end
    if length(domain(t)) == 1
        W = domain(t)[1]
    else
        W = S(dims)
    end
    return TensorMap(Ddata, W←W), TensorMap(Vdata, domain(t)←W)
end

function eig!(t::TensorMap; kwargs...)
    domain(t) == codomain(t) ||
        throw(SpaceMismatch("`eig!` requires domain and codomain to be the same"))
    S = spacetype(t)
    I = sectortype(t)
    T = complex(eltype(t))
    Ac = similarstoragetype(t, T)
    Ddata = SectorDict{I, Ac}()
    Vdata = SectorDict{I, Ac}()
    dims = SectorDict{I, Int}()
    for (c, b) in blocks(t)
        values, vectors = eigen!(b; kwargs...)
        d = length(values)
    end

```

```

Ddata[c] = copyto!(similar(values, T, (d, d)), Diagonal(values))
if eltype(vectors) == T
    Vdata[c] = vectors
else
    Vdata[c] = copyto!(similar(vectors, T), vectors)
end
dims[c] = d
end
if length(domain(t)) == 1
    W = domain(t)[1]
else
    W = S(dims)
end
return TensorMap(Ddata, W←W), TensorMap(Vdata, domain(t)←W)
end

function LinearAlgebra.isposdef!(t::TensorMap)
    domain(t) == codomain(t) ||
        throw(SpaceMismatch("`isposdef` requires domain and codomain to be the
same"))
    spacetype(t) <: EuclideanSpace || return false
    for (c, b) in blocks(t)
        isposdef!(b) || return false
    end
    return true
end
end

```