```
# abstracttensor.jl
# Abstract Tensor type
#---
0.00
    abstract type AbstractTensorMap{S<:IndexSpace, N<sub>1</sub>, N<sub>2</sub>} end
Abstract supertype of all tensor maps, i.e. linear maps between tensor products
of vector spaces of type `S<:IndexSpace`. An `AbstractTensorMap` maps from
an input space of type `ProductSpace{S, N_2}` to an output space of type
`ProductSpace{S, N<sub>1</sub>}`.
abstract type AbstractTensorMap{S<:IndexSpace, N1, N2} end
    AbstractTensor{S<:IndexSpace, N} = AbstractTensorMap{S, N, 0}
Abstract supertype of all tensors, i.e. elements in the tensor product space
of type `ProductSpace{S, N}`, built from elementary spaces of type `S<:IndexSpace`.
An `AbstractTensor{S, N}` is actually a special case `AbstractTensorMap{S, N, 0}`,
i.e. a tensor map with only a non-trivial output space.
const AbstractTensor{S<:IndexSpace, N} = AbstractTensorMap{S, N, 0}</pre>
# tensor characteristics
Base.eltype(t::AbstractTensorMap) = eltype(typeof(t))
Base.eltype(T::Type{<:AbstractTensorMap}) = eltype(storagetype(T))</pre>
storagetype(t::AbstractTensorMap) = storagetype(typeof(t))
similarstoragetype(t::AbstractTensorMap, T) = similarstoragetype(typeof(t), T)
similarstoragetype(TT::Type{<:AbstractTensorMap}, ::Type{T}) where {T} =</pre>
    Core.Compiler.return_type(similar, Tuple{storagetype(TT), Type{T}})
spacetype(t::AbstractTensorMap) = spacetype(typeof(t))
spacetype(::Type{<:AbstractTensorMap{S}}) where {S<:IndexSpace} = S</pre>
sectortype(t::AbstractTensorMap) = sectortype(typeof(t))
sectortype(::Type{<:AbstractTensorMap{S}}) where {S<:IndexSpace} = sectortype(S)</pre>
field(t::AbstractTensorMap) = field(typeof(t))
field(::Type{<:AbstractTensorMap{S}}) where {S<:IndexSpace} = field(S)</pre>
numout(t::AbstractTensorMap) = numout(typeof(t))
numout(::Type{<:AbstractTensorMap{<:IndexSpace, N<sub>1</sub>, N<sub>2</sub>}}) where {N<sub>1</sub>, N<sub>2</sub>} = N<sub>1</sub>
numin(t::AbstractTensorMap) = numin(typeof(t))
numin(::Type{<:AbstractTensorMap{<:IndexSpace, N<sub>1</sub>, N<sub>2</sub>}}) where {N<sub>1</sub>, N<sub>2</sub>} = N<sub>2</sub>
numind(t::AbstractTensorMap) = numind(typeof(t))
numind(::Type{<:AbstractTensorMap{<:IndexSpace, N<sub>1</sub>, N<sub>2</sub>}}) where {N_1, N_2} = N_1 + N_2
const order = numind
# tensormap implementation should provide codomain(t) and domain(t)
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  codomain(t::AbstractTensorMap, i) = codomain(t)[i]
  domain(t::AbstractTensorMap, i) = domain(t)[i]
  source(t::AbstractTensorMap) = domain(t) # categorical terminology
  target(t::AbstractTensorMap) = codomain(t) # categorical terminology
  space(t::AbstractTensorMap) = HomSpace(codomain(t), domain(t))
  space(t::AbstractTensorMap, i::Int) = space(t)[i]
  dim(t::AbstractTensorMap) = dim(space(t))
  # some index manipulation utilities
  codomainind(t::AbstractTensorMap) = codomainind(typeof(t))
  codomainind(::Type{<:AbstractTensorMap{<:IndexSpace, N_1, N_2}}) where \{N_1, N_2\} =
      ntuple(n->n, N1)
  domainind(t::AbstractTensorMap) = domainind(typeof(t))
  domainind(::Type{<:AbstractTensorMap{<:IndexSpace, N_1, N_2}}) where \{N_1, N_2\} =
      ntuple(n-> N_1+n, N_2)
  allind(t::AbstractTensorMap) = allind(typeof(t))
  allind(::Type{<:AbstractTensorMap{<:IndexSpace, N_1, N_2}) where \{N_1, N_2} =
      ntuple(n->n, N_1+N_2)
  adjointtensorindex(t::AbstractTensorMap\{<:IndexSpace, N_1, N_2\}, i) where \{N_1, N_2\} =
      ifelse(i \le N_1, N_2 + i, i - N_1)
  adjointtensorindices(t::AbstractTensorMap, indices::IndexTuple) =
      map(i->adjointtensorindex(t, i), indices)
  # Equality and approximality
  function Base.:(==)(t1::AbstractTensorMap, t2::AbstractTensorMap)
       (codomain(t1) == codomain(t2) \&\& domain(t1) == domain(t2)) || return false
      for c in blocksectors(t1)
           block(t1, c) == block(t2, c) || return false
      end
      return true
  end
  function Base.hash(t::AbstractTensorMap, h::UInt)
      h = hash(codomain(t), h)
      h = hash(domain(t), h)
      for (c, b) in blocks(t)
          h = hash(c, hash(b, h))
      end
      return h
  end
  function Base.isapprox(t1::AbstractTensorMap, t2::AbstractTensorMap;
                   atol::Real=0, rtol::Real=Base.rtoldefault(eltype(t1), eltype(t2),
  atol))
      d = norm(t1 - t2)
      if isfinite(d)
           return d <= max(atol, rtol*max(norm(t1), norm(t2)))</pre>
      else
           return false
      end
  end
```

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# Conversion to Array:
# probably not optimized for speed, only for checking purposes
function Base.convert(::Type{Array}, t::AbstractTensorMap{S, N1, N2}) where {S,
N_1, N_2
    I = sectortype(t)
    if I === Trivial
        convert(Array, t[])
    else
        cod = codomain(t)
        dom = domain(t)
        local A
        for (f1, f2) in fusiontrees(t)
            F1 = convert(Array, f1)
            F2 = convert(Array, f2)
            sz1 = size(F1)
            sz2 = size(F2)
            d1 = TupleTools.front(sz1)
            d2 = TupleTools.front(sz2)
            F = reshape(reshape(F1, TupleTools.prod(d1), sz1[end])*reshape(F2,
TupleTools.prod(d2), sz2[end])', (d1..., d2...))
            if !(@isdefined A)
                if eltype(F) <: Complex</pre>
                    T = complex(float(eltype(t)))
                elseif eltype(F) <: Integer</pre>
                    T = eltype(t)
                else
                    T = float(eltype(t))
                A = fill(zero(T), (dims(cod)..., dims(dom)...))
            end
            Aslice = StridedView(A)[axes(cod, f1.uncoupled)..., axes(dom,
f2.uncoupled)...]
            axpy!(1, StridedView(_kron(convert(Array, t[f1, f2]), F)), Aslice)
        end
        return A
    end
```

end