

```

In[1]:= (* F[1, {0}] = electron neutrino,
F[1, {1}] = muon neutrino, F[1, {2}] = tau neutrino,
F[2, {0}] = electron, F[2, {1}] = muon, F[2, {2}] = tau,
F[3, {0}] = up, F[3, {1}] = charm, F[3, {2}] = top,
F[4, {0}] = down, F[4, {1}] = strange, F[4, {2}] = bottom,
V[1] = photon, V[2] = Z, V[3] = W-, S[1] = H *)
$LoadAddOns = {"FeynArts"};
<< FeynCalc`
$FAVerbose = 0;

```

```

MakeBoxes[p1, TraditionalForm] := "\!\(\*SubscriptBox[\(p\), \{1\}]\)";
MakeBoxes[p2, TraditionalForm] := "\!\(\*SubscriptBox[\(p\), \{2\}]\)";
MakeBoxes[p3, TraditionalForm] := "\!\(\*SubscriptBox[\(p\), \{3\}]\)";
MakeBoxes[p4, TraditionalForm] := "\!\(\*SubscriptBox[\(p\), \{4\}]\)";

```

FeynCalc 10.0.0 (dev version). For help, use the

online documentation, visit the forum and have a look at the supplied examples. The PDF-version of the manual can be downloaded [here](#).

If you use FeynCalc in your research, please

evaluate `FeynCalcHowToCite[]` to learn how to cite this software.

Please keep in mind that the proper academic attribution

of our work is crucial to ensure the future development of this package!

FeynArts 3.12 (24 May 2024) patched for use with FeynCalc, for documentation see the manual or visit www.feynarts.de.

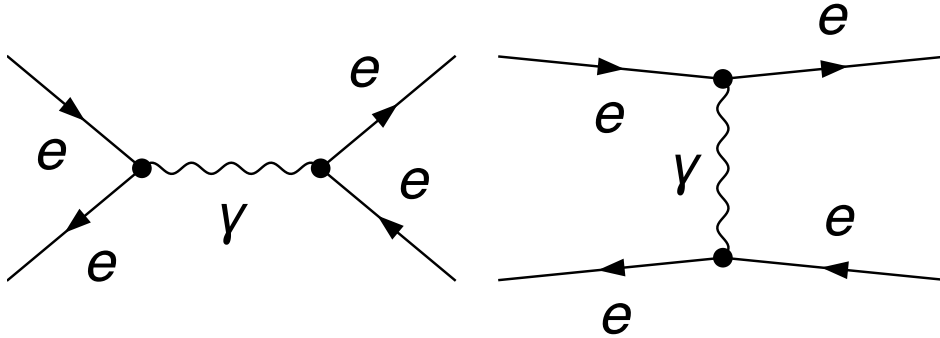
If you use FeynArts in your research, please cite

- T. Hahn, Comput. Phys. Commun., 140, 418–431, 2001, arXiv:hep-ph/0012260

```

In[8]:= (* QED: e- e+ → e- e+ (Bhabha) *)
topology = CreateTopologies[0, 2 → 2];
feynman1 =
  InsertFields[topology, {F[2, {1}], -F[2, {1}]} → {F[2, {1}], -F[2, {1}]},
    InsertionLevel → {Classes}, Restrictions → QEDOnly];
Paint[feynman1, Numbering → None, SheetHeader → False,
  ColumnsXRows → {4, 1}, ImageSize → {1032, 256}];
amplitude1[0] = FCFAConvert[CreateFeynAmp[feynman1], IncomingMomenta → {p1, p2},
  OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
  ChangeDimension → 4, List → False, SMP → True, Contract → True]
FCClearScalarProducts[];
SetMandelstam[s, t, u, p1, p2, -p3, -p4,
  SMP["m_e"], SMP["m_e"], SMP["m_e"], SMP["m_e"]];
squareamplitude1[0] = (amplitude1[0] (ComplexConjugate[amplitude1[0]])) //
  FeynAmpDenominatorExplicit //
  FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify // Simplify
masslesssquareamplitude1[0] =
  squareamplitude1[0] // ReplaceAll[#, {SMP["m_e"] → 0}] & // Simplify
(* output = feynman diagrams, amplitude,
  squared amplitude, massless squared amplitude *)

```



Out[11]=

$$\frac{e^2 (\varphi(\overline{p}_3, m_e)) \cdot \bar{\gamma}^{\text{Lor1}} \cdot (\varphi(\overline{p}_1, m_e)) (\varphi(-\overline{p}_2, m_e)) \cdot \bar{\gamma}^{\text{Lor1}} \cdot (\varphi(-\overline{p}_4, m_e))}{(\overline{p}_4 - \overline{p}_2)^2} - \frac{e^2 (\varphi(-\overline{p}_2, m_e)) \cdot \bar{\gamma}^{\text{Lor2}} \cdot (\varphi(\overline{p}_1, m_e)) (\varphi(\overline{p}_3, m_e)) \cdot \bar{\gamma}^{\text{Lor2}} \cdot (\varphi(-\overline{p}_4, m_e))}{(\overline{p}_3 + \overline{p}_4)^2}$$

Out[14]=

$$\frac{2 e^4 (8 m_e^4 (s^2 + s t + t^2) - 4 m_e^2 (s^3 + s^2 (u - 2 t) + s t (3 u - 2 t) + t^2 (t + u)) + s^4 + s^2 u^2 + 2 s t u^2 + t^4 + t^2 u^2)}{s^2 t^2}$$

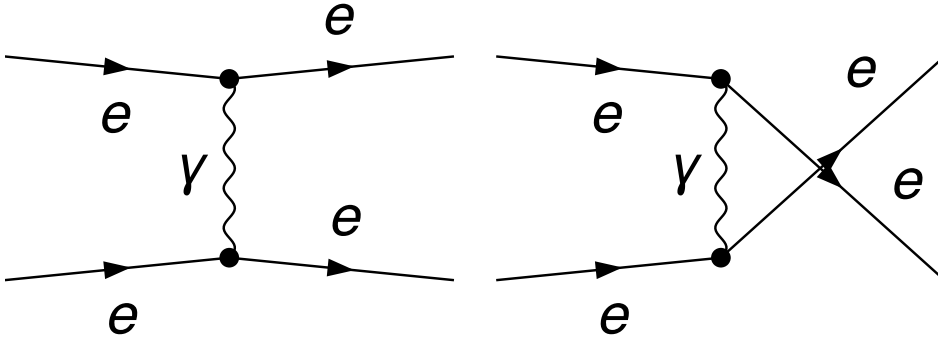
Out[15]=

$$\frac{2 e^4 (s^4 + s^2 u^2 + 2 s t u^2 + t^4 + t^2 u^2)}{s^2 t^2}$$

```

In[16]:= (* QED: e- e- → e- e- *)
topology = CreateTopologies[0, 2 → 2];
feynman2 =
  InsertFields[topology, {F[2, {1}], F[2, {1}]} → {F[2, {1}], F[2, {1}]},
    InsertionLevel → {Classes}, Restrictions → QEDOnly];
Paint[feynman2, Numbering → None, SheetHeader → False,
  ColumnsXRows → {4, 1}, ImageSize → {1032, 256}];
amplitude2[0] = FCFAConvert[CreateFeynAmp[feynman1], IncomingMomenta → {p1, p2},
  OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
  ChangeDimension → 4, List → False, SMP → True, Contract → True]
FCClearScalarProducts[];
SetMandelstam[s, t, u, p1, p2, -p3, -p4,
  SMP["m_e"], SMP["m_e"], SMP["m_e"], SMP["m_e"]];
squareamplitude2[0] = (amplitude2[0] (ComplexConjugate[amplitude2[0]])) //
  FeynAmpDenominatorExplicit //
  FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify // Simplify
masslesssquareamplitude2[0] =
  squareamplitude2[0] // ReplaceAll[#, {SMP["m_e"] → 0}] & // Simplify
(* output = feynman diagrams, amplitude,
  squared amplitude, massless squared amplitude *)

```



Out[19]=

$$\frac{e^2 (\varphi(\bar{p}_3, m_e) \cdot \bar{\gamma}^{\text{Lor1}} \cdot (\varphi(\bar{p}_1, m_e) (\varphi(-\bar{p}_2, m_e) \cdot \bar{\gamma}^{\text{Lor1}} \cdot (\varphi(-\bar{p}_4, m_e)))}{(\bar{p}_4 - \bar{p}_2)^2} - \frac{e^2 (\varphi(-\bar{p}_2, m_e) \cdot \bar{\gamma}^{\text{Lor2}} \cdot (\varphi(\bar{p}_1, m_e) (\varphi(\bar{p}_3, m_e) \cdot \bar{\gamma}^{\text{Lor2}} \cdot (\varphi(-\bar{p}_4, m_e)))}{(\bar{p}_3 + \bar{p}_4)^2}$$

Out[22]=

$$\frac{2 e^4 (8 m_e^4 (s^2 + s t + t^2) - 4 m_e^2 (s^3 + s^2 (u - 2 t) + s t (3 u - 2 t) + t^2 (t + u)) + s^4 + s^2 u^2 + 2 s t u^2 + t^4 + t^2 u^2)}{s^2 t^2}$$

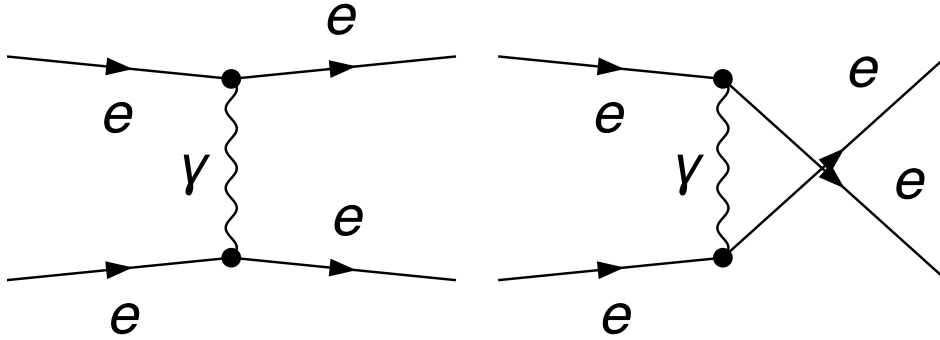
Out[23]=

$$\frac{2 e^4 (s^4 + s^2 u^2 + 2 s t u^2 + t^4 + t^2 u^2)}{s^2 t^2}$$

```

In[24]:= (* QED: e+ e+ → e+ e+ *)
topology = CreateTopologies[0, 2 → 2];
feynman3 =
  InsertFields[topology, {F[2, {1}], F[2, {1}]} → {F[2, {1}], F[2, {1}]},
    InsertionLevel → {Classes}, Restrictions → QEDOnly];
Paint[feynman3, Numbering → None, SheetHeader → False,
  ColumnsXRows → {4, 1}, ImageSize → {1032, 256}];
amplitude3[0] = FCFAConvert[CreateFeynAmp[feynman3], IncomingMomenta → {p1, p2},
  OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
  ChangeDimension → 4, List → False, SMP → True, Contract → True]
FCClearScalarProducts[];
SetMandelstam[s, t, u, p1, p2, -p3, -p4,
  SMP["m_e"], SMP["m_e"], SMP["m_e"], SMP["m_e"]];
squareamplitude3[0] = (amplitude3[0] (ComplexConjugate[amplitude3[0]])) //
  FeynAmpDenominatorExplicit //
  FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify // Simplify
masslesssquareamplitude3[0] =
  squareamplitude3[0] // ReplaceAll[#, {SMP["m_e"] → 0}] & // Simplify
(* output = feynman diagrams, amplitude,
  squared amplitude, massless squared amplitude *)

```



Out[27]=

$$\frac{e^2 (\varphi(\overline{p}_4, m_e) \cdot \bar{\gamma}^{\text{Lor1}} \cdot (\varphi(\overline{p}_1, m_e) (\varphi(\overline{p}_3, m_e) \cdot \bar{\gamma}^{\text{Lor1}} \cdot (\varphi(\overline{p}_2, m_e))) - (\overline{p}_3 - \overline{p}_2)^2)}{(\overline{p}_3 - \overline{p}_2)^2} - \frac{e^2 (\varphi(\overline{p}_3, m_e) \cdot \bar{\gamma}^{\text{Lor2}} \cdot (\varphi(\overline{p}_1, m_e) (\varphi(\overline{p}_4, m_e) \cdot \bar{\gamma}^{\text{Lor2}} \cdot (\varphi(\overline{p}_2, m_e))) - (\overline{p}_4 - \overline{p}_2)^2)}{(\overline{p}_4 - \overline{p}_2)^2}$$

Out[30]=

$$\frac{2 e^4 (-4 m_e^2 (s (t^2 + 3 t u + u^2) + t^3 - 2 t^2 u - 2 t u^2 + u^3) + 8 m_e^4 (t^2 + t u + u^2) + s^2 (t + u)^2 + t^4 + u^4)}{t^2 u^2}$$

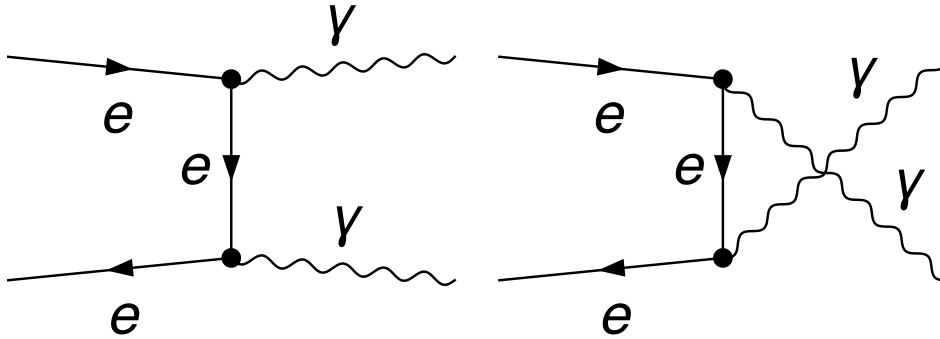
Out[31]=

$$\frac{2 e^4 (s^2 (t + u)^2 + t^4 + u^4)}{t^2 u^2}$$

```

In[32]:= (* QED: e- e+ → photon photon (annihilation) *)
topology = CreateTopologies[0, 2 → 2];
feynman4 = InsertFields[topology, {F[2, {1}], -F[2, {1}]} → {V[1], V[1]},
  InsertionLevel → {Classes}, Restrictions → QEDOnly];
Paint[feynman4, Numbering → None, SheetHeader → False,
  ColumnsXRows → {4, 1}, ImageSize → {1032, 256}];
amplitude4[0] = FCFAConvert[CreateFeynAmp[feynman4], IncomingMomenta → {p1, p2},
  OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
  ChangeDimension → 4, TransversePolarizationVectors → {p3, p4},
  List → False, SMP → True, Contract → True]
FCClearScalarProducts[];
SetMandelstam[s, t, u, p1, p2, -p3, -p4, SMP["m_e"], SMP["m_e"], 0, 0];
squareamplitude4[0] = (amplitude4[0] (ComplexConjugate[amplitude4[0]])) //
  FeynAmpDenominatorExplicit //
  DoPolarizationSums[#, p3, 0] & // DoPolarizationSums[#, p4, 0] & //
  FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify //
  TrickMandelstam[#, {s, t, u, 2 SMP["m_e"]^2}] & // Simplify
masslesssquareamplitude4[0] =
  squareamplitude4[0] // ReplaceAll[#, {SMP["m_e"] → 0}] & // Simplify
(* output = feynman diagrams, amplitude,
squared amplitude, massless squared amplitude *)

```



$$\begin{aligned}
 \text{Out[35]} = & \frac{e^2 (\varphi(-\bar{p}_2, m_e)) \cdot (\bar{\gamma} \cdot \bar{\epsilon}^*(p_3)) \cdot (\bar{\gamma} \cdot (\bar{p}_3 - \bar{p}_2) + m_e) \cdot (\bar{\gamma} \cdot \bar{\epsilon}^*(p_4)) \cdot (\varphi(\bar{p}_1, m_e))}{(\bar{p}_2 - \bar{p}_3)^2 - m_e^2} - \\
 & \frac{e^2 (\varphi(-\bar{p}_2, m_e)) \cdot (\bar{\gamma} \cdot \bar{\epsilon}^*(p_4)) \cdot (\bar{\gamma} \cdot (\bar{p}_4 - \bar{p}_2) + m_e) \cdot (\bar{\gamma} \cdot \bar{\epsilon}^*(p_3)) \cdot (\varphi(\bar{p}_1, m_e))}{(\bar{p}_2 - \bar{p}_4)^2 - m_e^2}
 \end{aligned}$$

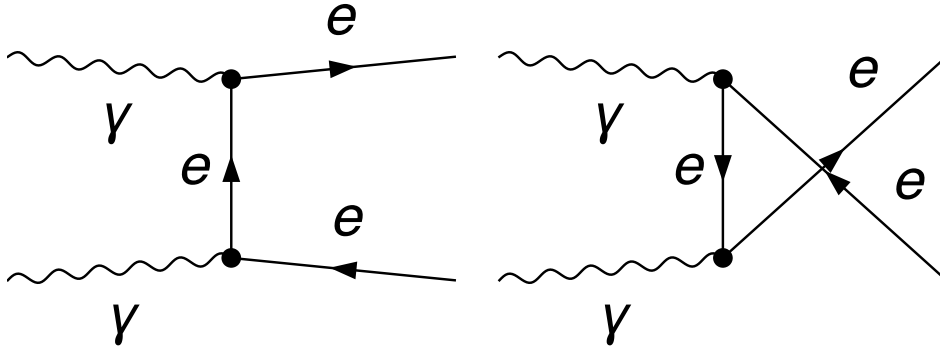
$$\text{Out[38]} = \frac{2 e^4 (m_e^4 (3 t^2 + 14 t u + 3 u^2) - m_e^2 (t^3 + 7 t^2 u + 7 t u^2 + u^3) - 6 m_e^8 + t u (t^2 + u^2))}{(t - m_e^2)^2 (u - m_e^2)^2}$$

$$\text{Out[39]} = \frac{2 e^4 (t^2 + u^2)}{t u}$$

```

In[40]:= (* QED: photon photon → e- e+ (pair creation)*)
topology = CreateTopologies[0, 2 → 2];
feynman5 = InsertFields[topology, {V[1], V[1]} → {F[2, {1}], -F[2, {1}]},
  InsertionLevel → {Classes}, Restrictions → QEDOnly];
Paint[feynman5, Numbering → None, SheetHeader → False,
  ColumnsXRows → {4, 1}, ImageSize → {1032, 256}];
amplitude5[0] = FCFAConvert[CreateFeynAmp[feynman5], IncomingMomenta → {p1, p2},
  OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
  ChangeDimension → 4, TransversePolarizationVectors → {p1, p2},
  List → False, SMP → True, Contract → True]
FCClearScalarProducts[];
SetMandelstam[s, t, u, p1, p2, -p3, -p4, 0, 0, SMP["m_e"], SMP["m_e"]];
squareamplitude5[0] = (amplitude5[0] (ComplexConjugate[amplitude5[0]])) //
  FeynAmpDenominatorExplicit //
  DoPolarizationSums[#, p1, 0] & // DoPolarizationSums[#, p2, 0] & //
  FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify //
  TrickMandelstam[#, {s, t, u, 2 SMP["m_e"]^2}] & // Simplify
masslesssquareamplitude5[0] =
  squareamplitude5[0] // ReplaceAll[#, {SMP["m_e"] → 0}] & // Simplify
(* output = feynman diagrams, amplitude,
squared amplitude, massless squared amplitude *)

```



$$\begin{aligned}
\text{Out[43]} = & \frac{e^2 (\varphi(\vec{p}_3, m_e) \cdot (\vec{\gamma} \cdot \vec{E}(p_2)) \cdot (\vec{\gamma} \cdot (\vec{p}_3 - \vec{p}_2) + m_e) \cdot (\vec{\gamma} \cdot \vec{E}(p_1)) \cdot (\varphi(-\vec{p}_4, m_e)))}{(\vec{p}_2 - \vec{p}_3)^2 - m_e^2} + \\
& \frac{e^2 (\varphi(\vec{p}_3, m_e) \cdot (\vec{\gamma} \cdot \vec{E}(p_1)) \cdot (\vec{\gamma} \cdot (\vec{p}_2 - \vec{p}_4) + m_e) \cdot (\vec{\gamma} \cdot \vec{E}(p_2)) \cdot (\varphi(-\vec{p}_4, m_e)))}{(\vec{p}_4 - \vec{p}_2)^2 - m_e^2}
\end{aligned}$$

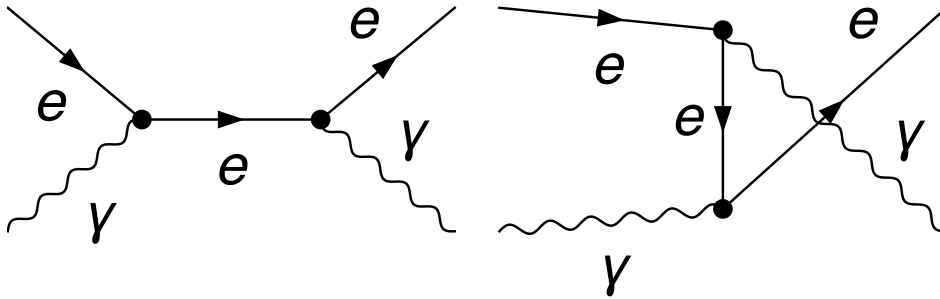
$$\text{Out[46]} = \frac{2 e^4 (m_e^4 (3 t^2 + 14 t u + 3 u^2) - m_e^2 (t^3 + 7 t^2 u + 7 t u^2 + u^3) - 6 m_e^8 + t u (t^2 + u^2))}{(t - m_e^2)^2 (u - m_e^2)^2}$$

$$\text{Out[47]} = \frac{2 e^4 (t^2 + u^2)}{t u}$$

```

In[48]:= (* QED: e- photon → e- photon (Compton)*)
topology = CreateTopologies[0, 2 → 2];
feynman6 = InsertFields[topology, {F[2, {1}], V[1]} → {F[2, {1}], V[1]},
  InsertionLevel → {Classes}, Restrictions → QEDOnly];
Paint[feynman6, Numbering → None, SheetHeader → False,
  ColumnsXRows → {4, 1}, ImageSize → {1032, 256}];
amplitude6[0] = FCFAConvert[CreateFeynAmp[feynman6], IncomingMomenta → {p1, p2},
  OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
  ChangeDimension → 4, TransversePolarizationVectors → {p2, p4},
  List → False, SMP → True, Contract → True]
FCClearScalarProducts[];
SetMandelstam[s, t, u, p1, p2, -p3, -p4, SMP["m_e"], 0, SMP["m_e"], 0];
squareamplitude6[0] = (amplitude6[0] (ComplexConjugate[amplitude6[0]])) //
  FeynAmpDenominatorExplicit //
  DoPolarizationSums[#, p2, 0] & // DoPolarizationSums[#, p4, 0] & //
  FermionSpinSum[#, ExtraFactor → 1 / 2 ^ 2] & // DiracSimplify //
  TrickMandelstam[#, {s, t, u, 2 SMP["m_e"] ^ 2}] & // Simplify
masslesssquareamplitude6[0] =
  squareamplitude6[0] // ReplaceAll[#, {SMP["m_e"] → 0}] & // Simplify
(* output = feynman diagrams, amplitude,
  squared amplitude, massless squared amplitude *)

```



$$\begin{aligned}
 \text{Out[51]} = & \frac{e^2 (\varphi(\bar{p}_3, m_e) \cdot (\bar{\gamma} \cdot \bar{\epsilon}(p_2)) \cdot (\bar{\gamma} \cdot (\bar{p}_3 - \bar{p}_2) + m_e) \cdot (\bar{\gamma} \cdot \bar{\epsilon}^*(p_4)) \cdot (\varphi(\bar{p}_1, m_e)))}{(\bar{p}_2 - \bar{p}_3)^2 - m_e^2} - \\
 & \frac{e^2 (\varphi(\bar{p}_3, m_e) \cdot (\bar{\gamma} \cdot \bar{\epsilon}^*(p_4)) \cdot (\bar{\gamma} \cdot (\bar{p}_3 + \bar{p}_4) + m_e) \cdot (\bar{\gamma} \cdot \bar{\epsilon}(p_2)) \cdot (\varphi(\bar{p}_1, m_e)))}{(-\bar{p}_3 - \bar{p}_4)^2 - m_e^2}
 \end{aligned}$$

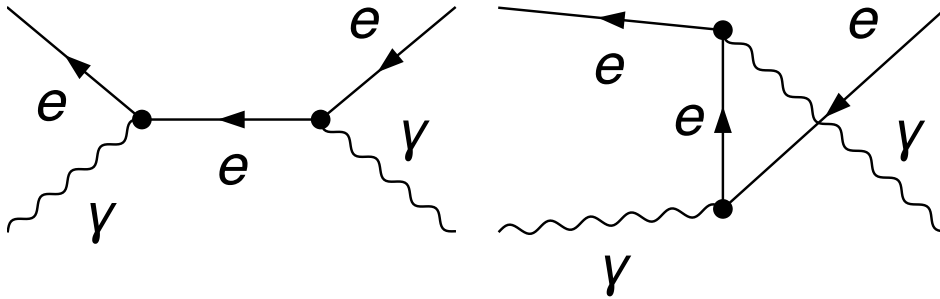
$$\text{Out[54]} = \frac{2 e^4 (-m_e^4 (3 s^2 + 14 s u + 3 u^2) + m_e^2 (s^3 + 7 s^2 u + 7 s u^2 + u^3) + 6 m_e^8 - s u (s^2 + u^2))}{(s - m_e^2)^2 (u - m_e^2)^2}$$

$$\text{Out[55]} = \frac{2 e^4 (s^2 + u^2)}{s u}$$

```

In[56]:= (* QED: e+ photon → e+ photon *)
topology = CreateTopologies[0, 2 → 2];
feynman7 = InsertFields[topology, {-F[2, {1}], V[1]} → {-F[2, {1}], V[1]},
  InsertionLevel → {Classes}, Restrictions → QEDOnly];
Paint[feynman7, Numbering → None, SheetHeader → False,
  ColumnsXRows → {4, 1}, ImageSize → {1032, 256}];
amplitude7[0] = FCFAConvert[CreateFeynAmp[feynman7], IncomingMomenta → {p1, p2},
  OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
  ChangeDimension → 4, TransversePolarizationVectors → {p2, p4},
  List → False, SMP → True, Contract → True]
FCClearScalarProducts[];
SetMandelstam[s, t, u, p1, p2, -p3, -p4, SMP["m_e"], 0, SMP["m_e"], 0];
squareamplitude7[0] = (amplitude7[0] (ComplexConjugate[amplitude7[0]])) //
  FeynAmpDenominatorExplicit //
  DoPolarizationSums[#, p2, 0] & // DoPolarizationSums[#, p4, 0] & //
  FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify //
  TrickMandelstam[#, {s, t, u, 2 SMP["m_e"]^2}] & // Simplify
masslesssquareamplitude7[0] =
  squareamplitude7[0] // ReplaceAll[#, {SMP["m_e"] → 0}] & // Simplify
(* output = feynman diagrams, amplitude,
  squared amplitude, massless squared amplitude *)

```



$$\begin{aligned}
 \text{Out[59]} = & \frac{e^2 (\varphi(-\vec{p}_1, m_e) \cdot (\vec{\gamma} \cdot \vec{\epsilon}(p_4)) \cdot (\vec{\gamma} \cdot (\vec{p}_2 - \vec{p}_3) + m_e) \cdot (\vec{\gamma} \cdot \vec{\epsilon}(p_2)) \cdot (\varphi(-\vec{p}_3, m_e)))}{(\vec{p}_3 - \vec{p}_2)^2 - m_e^2} + \\
 & \frac{e^2 (\varphi(-\vec{p}_1, m_e) \cdot (\vec{\gamma} \cdot \vec{\epsilon}(p_2)) \cdot (\vec{\gamma} \cdot (-\vec{p}_3 - \vec{p}_4) + m_e) \cdot (\vec{\gamma} \cdot \vec{\epsilon}(p_4)) \cdot (\varphi(-\vec{p}_3, m_e)))}{(\vec{p}_3 + \vec{p}_4)^2 - m_e^2}
 \end{aligned}$$

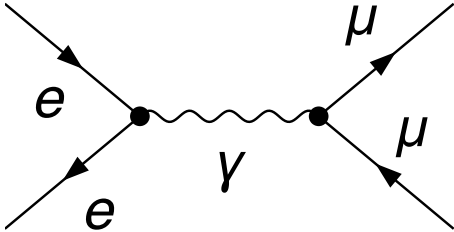
$$\text{Out[62]} = \frac{2 e^4 (-m_e^4 (3 s^2 + 14 s u + 3 u^2) + m_e^2 (s^3 + 7 s^2 u + 7 s u^2 + u^3) + 6 m_e^8 - s u (s^2 + u^2))}{(s - m_e^2)^2 (u - m_e^2)^2}$$

$$\text{Out[63]} = -\frac{2 e^4 (s^2 + u^2)}{s u}$$


```

In[64]:= (* QED: e- e+ → mu- mu+ *)
topology = CreateTopologies[0, 2 → 2];
feynman8 =
  InsertFields[topology, {F[2, {1}], -F[2, {1}]} → {F[2, {2}], -F[2, {2}]},
    InsertionLevel → {Classes}, Restrictions → QEDOnly];
Paint[feynman8, Numbering → None, SheetHeader → False,
  ColumnsXRows → {4, 1}, ImageSize → {1032, 256}];
amplitude8[0] = FCFAConvert[CreateFeynAmp[feynman8], IncomingMomenta → {p1, p2},
  OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
  ChangeDimension → 4, List → False, SMP → True, Contract → True]
FCClearScalarProducts[];
SetMandelstam[s, t, u, p1, p2, -p3, -p4,
  SMP["m_e"], SMP["m_e"], SMP["m_mu"], SMP["m_mu"]];
squareamplitude8[0] = (amplitude8[0] (ComplexConjugate[amplitude8[0]])) //
  FeynAmpDenominatorExplicit //
  FermionSpinSum[#, ExtraFactor → 1/2^2] & // DiracSimplify // Simplify
masslesssquareamplitude8[0] = squareamplitude8[0] //
  ReplaceAll[#, {SMP["m_e"] → 0, SMP["m_mu"] → 0}] & // Simplify
(* output = feynman diagrams, amplitude,
  squared amplitude, massless squared amplitude *)

```



$$\text{Out[67]=} \quad -\frac{e^2 (\varphi(-\overline{p_2}, m_e)) \cdot \overline{\gamma}^{\text{Lor}2} (\varphi(\overline{p_1}, m_e)) (\varphi(\overline{p_3}, m_\mu)) \cdot \overline{\gamma}^{\text{Lor}2} (\varphi(-\overline{p_4}, m_\mu))}{(\overline{p_3} + \overline{p_4})^2}$$

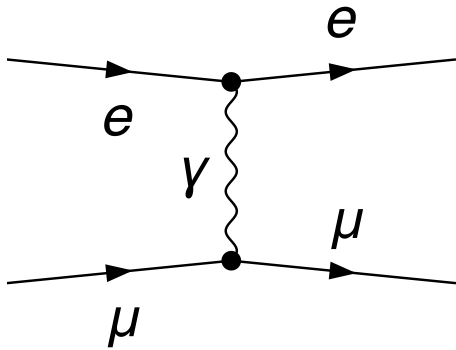
$$\text{Out[70]=} \quad \frac{2 e^4 (2 m_\mu^2 (2 m_\mu^2 + s - t - u) + 2 m_e^4 + 2 m_\mu^4 + 2 m_\mu^2 (s - t - u) + t^2 + u^2)}{s^2}$$

$$\text{Out[71]=} \quad \frac{2 e^4 (t^2 + u^2)}{s^2}$$

```

In[72]:= (* QED: e- mu- → e- mu- *)
topology = CreateTopologies[0, 2 → 2];
feynman9 =
  InsertFields[topology, {F[2, {1}], F[2, {2}]} → {F[2, {1}], F[2, {2}]},
    InsertionLevel → {Classes}, Restrictions → QEDOnly];
Paint[feynman9, Numbering → None, SheetHeader → False,
  ColumnsXRows → {4, 1}, ImageSize → {1032, 256}];
amplitude9[0] = FCFAConvert[CreateFeynAmp[feynman9], IncomingMomenta → {p1, p2},
  OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
  ChangeDimension → 4, List → False, SMP → True, Contract → True]
FCClearScalarProducts[];
SetMandelstam[s, t, u, p1, p2, -p3, -p4,
  SMP["m_e"], SMP["m_mu"], SMP["m_e"], SMP["m_mu"]];
squareamplitude9[0] = (amplitude9[0] (ComplexConjugate[amplitude9[0]])) //
  FeynAmpDenominatorExplicit //
  FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify // Simplify
masslesssquareamplitude9[0] = squareamplitude9[0] //
  ReplaceAll[#, {SMP["m_e"] → 0, SMP["m_mu"] → 0}] & // Simplify
(* output = feynman diagrams, amplitude,
  squared amplitude, massless squared amplitude *)

```



$$\text{Out[75]} = -\frac{e^2 (\varphi(\overline{p}_3, m_e) \cdot \overline{\gamma}^{\text{Lor}2} \cdot (\varphi(\overline{p}_1, m_e)) (\varphi(\overline{p}_4, m_\mu) \cdot \overline{\gamma}^{\text{Lor}2} \cdot (\varphi(\overline{p}_2, m_\mu)))}{(\overline{p}_4 - \overline{p}_2)^2}$$

$$\text{Out[78]} = \frac{2 e^4 (-2 m_e^2 (-2 m_\mu^2 + s - t + u) + 2 m_e^4 + 2 m_\mu^4 - 2 m_\mu^2 (s - t + u) + s^2 + u^2)}{t^2}$$

$$\text{Out[79]} = \frac{2 e^4 (s^2 + u^2)}{t^2}$$

```

In[80]:= Print["\tCPU Time used: ", Round[N[TimeUsed[]], 4], 0.001, " s."];
          CPU Time used: 5.838 s.

```

```

In[81]:= FeynCalcHowToCite[]

```

- V. Shtabovenko, R. Mertig and F. Orellana, arXiv:2312.14089.
- V. Shtabovenko, R. Mertig and F. Orellana,
Comput.Phys.Commun. 256 (2020) 107478, arXiv:2001.04407.
- V. Shtabovenko, R. Mertig and F. Orellana,
Comput.Phys.Commun. 207 (2016) 432–444, arXiv:1601.01167.
- R. Mertig, M. Böhm, and A. Denner, Comput. Phys. Commun. 64 (1991) 345–359.

Out[81]=

Null