```
(* F[2, {0}] = electron, F[2, {1}] = muon, V[1] = photon *)
$LoadAddOns = {"FeynArts"};
<< FeynCalc`
$FAVerbose = 0;

MakeBoxes[p1, TraditionalForm] := "\!\(\*SubscriptBox[\(p\), \(1\)]\)";
MakeBoxes[p2, TraditionalForm] := "\!\(\*SubscriptBox[\(p\), \(2\)]\)";
MakeBoxes[p3, TraditionalForm] := "\!\(\*SubscriptBox[\(p\), \(3\)]\)";
MakeBoxes[p4, TraditionalForm] := "\!\(\*SubscriptBox[\(p\), \(3\)]\)";
FeynCalc 10.0.0 (dev version). For help, use the
online documentation, visit the forum and have a look at the supplied
examples. The PDF-version of the manual can be downloaded here.</pre>
```

If you use FeynCalc in your research, please evaluate FeynCalcHowToCite[] to learn how to cite this software.

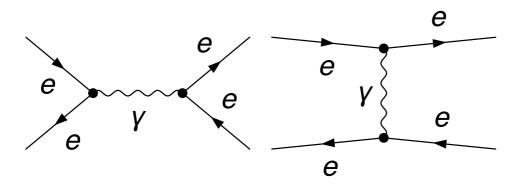
Please keep in mind that the proper academic attribution of our work is crucial to ensure the future development of this package!

FeynArts 3.12 (24 May 2024) patched for use with FeynCalc, for documentation see the manual or visit www.feynarts.de.

If you use FeynArts in your research, please cite

• T. Hahn, Comput. Phys. Commun., 140, 418–431, 2001, arXiv:hep-ph/0012260

```
In[\bullet]:= (* QED: e- e+ \rightarrow e- e+ (Bhabha) *)
     topology = CreateTopologies[0, 2 → 2];
     feynman1 =
       InsertFields[topology, \{F[2, \{1\}], -F[2, \{1\}]\} \rightarrow \{F[2, \{1\}], -F[2, \{1\}]\},
        InsertionLevel → {Classes}, Restrictions → QEDOnly];
     Paint[feynman1, Numbering → None, SheetHeader → False,
       ColumnsXRows → {4, 1}, ImageSize → {1032, 256}];
     amplitude1[0] = FCFAConvert[CreateFeynAmp[feynman1], IncomingMomenta → {p1, p2},
       OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
       ChangeDimension → 4, List → False, SMP → True, Contract → True]
     FCClearScalarProducts[];
     SetMandelstam[s, t, u, p1, p2, -p3, -p4,
       SMP["m e"], SMP["m e"], SMP["m e"]];
     squareamplitude1[0] = (amplitude1[0] (ComplexConjugate[amplitude1[0]])) //
           FeynAmpDenominatorExplicit //
         FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify // Simplify
     masslesssquareamplitude1[0] =
      squareamplitude1[0] // ReplaceAll[#, {SMP["m_e"] → 0}] & // Simplify
     (* output = feynman diagrams, amplitude,
     squared amplitude, massless squared amplitude *)
```



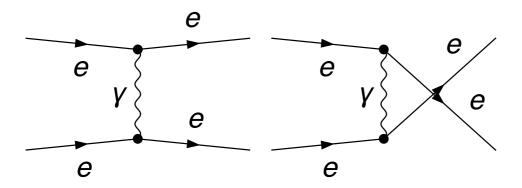
$$\frac{ \mathrm{e}^{2} \left(\varphi \left(\, \overline{p_{3}} \, , m_{e} \, \right) \right) . \overline{\gamma}^{\mathrm{Lor1}} . \left(\varphi \left(\, \overline{p_{1}} \, , m_{e} \, \right) \right) \left(\varphi \left(\, -\overline{p_{2}} \, , m_{e} \, \right) \right) . \overline{\gamma}^{\mathrm{Lor1}} . \left(\varphi \left(\, -\overline{p_{4}} \, , m_{e} \, \right) \right) }{ \left(\, \overline{p_{4}} - \overline{p_{2}} \, \right)^{2} }$$

$$\frac{ \mathrm{e}^{2} \left(\varphi \left(\, -\overline{p_{2}} \, , m_{e} \, \right) \right) . \overline{\gamma}^{\mathrm{Lor2}} . \left(\varphi \left(\, \overline{p_{1}} \, , m_{e} \, \right) \right) \left(\varphi \left(\, \overline{p_{3}} \, , m_{e} \, \right) \right) . \overline{\gamma}^{\mathrm{Lor2}} . \left(\varphi \left(\, -\overline{p_{4}} \, , m_{e} \, \right) \right) }{ \left(\, \overline{p_{3}} + \overline{p_{4}} \, \right)^{2} }$$

$$\frac{2 e^{4} \left(8 m_{e}^{4} \left(s^{2}+s t+t^{2}\right)-4 m_{e}^{2} \left(s^{3}+s^{2} \left(u-2 t\right)+s t \left(3 u-2 t\right)+t^{2} \left(t+u\right)\right)+s^{4}+s^{2} u^{2}+2 s t u^{2}+t^{4}+t^{2} u^{2}\right)}{s^{2} t^{2}}$$

$$\frac{2 e^4 (s^4 + s^2 u^2 + 2 s t u^2 + t^4 + t^2 u^2)}{s^2 t^2}$$

```
In[\bullet]:= (* QED: e- e- \rightarrow e- e- *)
     topology = CreateTopologies[0, 2 \rightarrow 2];
     feynman2 =
       InsertFields[topology, \{F[2, \{1\}], F[2, \{1\}]\} \rightarrow \{F[2, \{1\}], F[2, \{1\}]\},
        InsertionLevel → {Classes}, Restrictions → QEDOnly];
     Paint[feynman2, Numbering → None, SheetHeader → False,
       ColumnsXRows → {4, 1}, ImageSize → {1032, 256}];
     amplitude2[0] = FCFAConvert[CreateFeynAmp[feynman1], IncomingMomenta → {p1, p2},
       OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
       ChangeDimension → 4, List → False, SMP → True, Contract → True]
     FCClearScalarProducts[];
     SetMandelstam[s, t, u, p1, p2, -p3, -p4,
       SMP["m e"], SMP["m e"], SMP["m e"]];
     squareamplitude2[0] = (amplitude2[0] (ComplexConjugate[amplitude2[0]])) //
           FeynAmpDenominatorExplicit //
          FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify // Simplify
     masslesssquareamplitude2[0] =
      squareamplitude2[0] // ReplaceAll[#, {SMP["m_e"] → 0}] & // Simplify
     (* output = feynman diagrams, amplitude,
     squared amplitude, massless squared amplitude *)
```



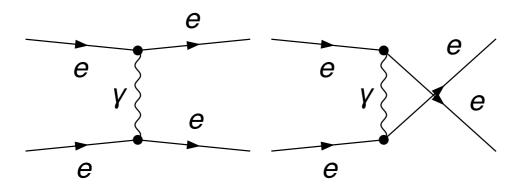
$$\frac{\mathrm{e}^{2}\left(\varphi\left(\overline{p_{3}},m_{e}\right)\right).\overline{\gamma}^{\mathrm{Lor1}}.\left(\varphi\left(\overline{p_{1}},m_{e}\right)\right)\left(\varphi\left(-\overline{p_{2}},m_{e}\right)\right).\overline{\gamma}^{\mathrm{Lor1}}.\left(\varphi\left(-\overline{p_{4}},m_{e}\right)\right)}{\left(\overline{p_{4}}-\overline{p_{2}}\right)^{2}}$$

$$\frac{\mathrm{e}^{2}\left(\varphi\left(-\overline{p_{2}},m_{e}\right)\right).\overline{\gamma}^{\mathrm{Lor2}}.\left(\varphi\left(\overline{p_{1}},m_{e}\right)\right)\left(\varphi\left(\overline{p_{3}},m_{e}\right)\right).\overline{\gamma}^{\mathrm{Lor2}}.\left(\varphi\left(-\overline{p_{4}},m_{e}\right)\right)}{\left(\overline{p_{3}}+\overline{p_{4}}\right)^{2}}$$

Out[
$$\circ$$
] =
$$\frac{2 e^{4} \left(8 m_{e}^{4} \left(s^{2} + s t + t^{2}\right) - 4 m_{e}^{2} \left(s^{3} + s^{2} \left(u - 2 t\right) + s t \left(3 u - 2 t\right) + t^{2} \left(t + u\right)\right) + s^{4} + s^{2} u^{2} + 2 s t u^{2} + t^{4} + t^{2} u^{2}\right)}{s^{2} t^{2}}$$

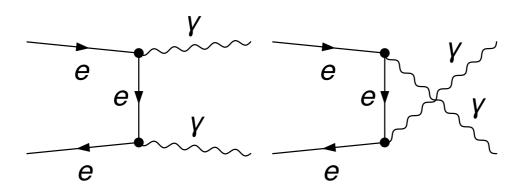
Out[
$$\circ$$
] =
$$\frac{2 e^4 (s^4 + s^2 u^2 + 2 s t u^2 + t^4 + t^2 u^2)}{s^2 t^2}$$

```
In[\bullet]:= (* QED: e+ e+ \rightarrow e+ e+ *)
     topology = CreateTopologies[0, 2 → 2];
     feynman3 =
       InsertFields[topology, \{F[2, \{1\}], F[2, \{1\}]\} \rightarrow \{F[2, \{1\}], F[2, \{1\}]\},
        InsertionLevel → {Classes}, Restrictions → QEDOnly];
     Paint[feynman3, Numbering → None, SheetHeader → False,
       ColumnsXRows → {4, 1}, ImageSize → {1032, 256}];
     amplitude3[0] = FCFAConvert[CreateFeynAmp[feynman3], IncomingMomenta → {p1, p2},
       OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
       ChangeDimension → 4, List → False, SMP → True, Contract → True]
     FCClearScalarProducts[];
     SetMandelstam[s, t, u, p1, p2, -p3, -p4,
       SMP["m e"], SMP["m e"], SMP["m e"]];
     squareamplitude3[0] = (amplitude3[0] (ComplexConjugate[amplitude3[0]])) //
           FeynAmpDenominatorExplicit //
         FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify // Simplify
     masslesssquareamplitude3[0] =
      squareamplitude3[0] // ReplaceAll[#, {SMP["m_e"] → 0}] & // Simplify
     (* output = feynman diagrams, amplitude,
     squared amplitude, massless squared amplitude *)
```



$$\begin{array}{l} \text{Out} [\circ] = \\ & \frac{e^2 \left(\varphi \left(\, \overline{p_4} \, , m_e \, \right) \right) . \overline{\gamma}^{\text{Lor1}} . \left(\varphi \left(\, \overline{p_1} \, , m_e \, \right) \right) . \left(\varphi \left(\, \overline{p_3} \, , m_e \, \right) \right) . \overline{\gamma}^{\text{Lor1}} . \left(\varphi \left(\, \overline{p_2} \, , m_e \, \right) \right)}{\left(\, \overline{p_3} - \overline{p_2} \, \right)^2} - \\ & \frac{e^2 \left(\varphi \left(\, \overline{p_3} \, , m_e \, \right) \right) . \overline{\gamma}^{\text{Lor2}} . \left(\varphi \left(\, \overline{p_1} \, , m_e \, \right) \right) . \left(\varphi \left(\, \overline{p_4} \, , m_e \, \right) \right) . \overline{\gamma}^{\text{Lor2}} . \left(\varphi \left(\, \overline{p_2} \, , m_e \, \right) \right)}{\left(\, \overline{p_4} - \overline{p_2} \, \right)^2} \\ \text{Out} [\circ] = \\ & \frac{2 \, e^4 \left(-4 \, m_e^2 \left(s \left(t^2 + 3 \, t \, u + u^2 \right) + t^3 - 2 \, t^2 \, u - 2 \, t \, u^2 + u^3 \right) + 8 \, m_e^4 \left(t^2 + t \, u + u^2 \right) + s^2 \left(t + u \right)^2 + t^4 + u^4 \right)}{t^2 \, u^2} \\ \text{Out} [\circ] = \\ & \frac{2 \, e^4 \left(s^2 \left(t + u \right)^2 + t^4 + u^4 \right)}{t^2 \, u^2} \end{array}$$

```
In[*]:= (* QED: e- e+ → photon photon (annihilation) *)
     topology = CreateTopologies[0, 2 \rightarrow 2];
     feynman4 = InsertFields[topology, \{F[2, \{1\}], -F[2, \{1\}]\} \rightarrow \{V[1], V[1]\},
        InsertionLevel → {Classes}, Restrictions → QEDOnly];
     Paint[feynman4, Numbering → None, SheetHeader → False,
       ColumnsXRows \rightarrow {4, 1}, ImageSize \rightarrow {1032, 256}];
     amplitude4[0] = FCFAConvert[CreateFeynAmp[feynman4], IncomingMomenta → {p1, p2},
       OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
       ChangeDimension → 4, TransversePolarizationVectors → {p3, p4},
       List → False, SMP → True, Contract → True]
     FCClearScalarProducts[];
     SetMandelstam[s, t, u, p1, p2, -p3, -p4, SMP["m_e"], SMP["m_e"], 0, 0];
     squareamplitude4[0] = (amplitude4[0] (ComplexConjugate[amplitude4[0]])) //
              FeynAmpDenominatorExplicit //
             DoPolarizationSums[#, p3, 0] & // DoPolarizationSums[#, p4, 0] & //
           FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify //
        TrickMandelstam[#, {s, t, u, 2 SMP["m_e"]^2}] & // Simplify
     masslesssquareamplitude4[0] =
      squareamplitude4[0] // ReplaceAll[#, {SMP["m_e"] → 0}] & // Simplify
     (* output = feynman diagrams, amplitude,
     squared amplitude, massless squared amplitude *)
```

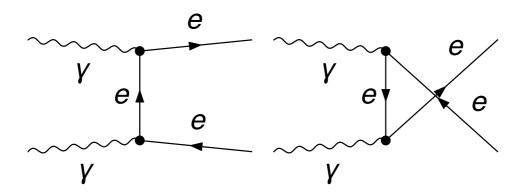


Out[*] =
$$-\frac{e^{2} (\varphi (-\overline{p_{2}}, m_{e})).(\overline{\gamma} \cdot \overline{\varepsilon}^{*}(p_{3})).(\overline{\gamma} \cdot (\overline{p_{3}} - \overline{p_{2}}) + m_{e}).(\overline{\gamma} \cdot \overline{\varepsilon}^{*}(p_{4})).(\varphi (\overline{p_{1}}, m_{e}))}{(\overline{p_{2}} - \overline{p_{3}})^{2} - m_{e}^{2}} - \frac{e^{2} (\varphi (-\overline{p_{2}}, m_{e})).(\overline{\gamma} \cdot \overline{\varepsilon}^{*}(p_{4})).(\overline{\gamma} \cdot (\overline{p_{4}} - \overline{p_{2}}) + m_{e}).(\overline{\gamma} \cdot \overline{\varepsilon}^{*}(p_{3})).(\varphi (\overline{p_{1}}, m_{e}))}{(\overline{p_{2}} - \overline{p_{4}})^{2} - m_{e}^{2}}$$

$$Out[*] = \frac{2 e^{4} (m_{e}^{4} (3 t^{2} + 14 t u + 3 u^{2}) - m_{e}^{2} (t^{3} + 7 t^{2} u + 7 t u^{2} + u^{3}) - 6 m_{e}^{8} + t u (t^{2} + u^{2}))}{(t - m_{e}^{2})^{2} (u - m_{e}^{2})^{2}}$$

$$Out[*] = \frac{2 e^{4} (t^{2} + u^{2})}{(t^{2} + u^{2})^{2}}$$

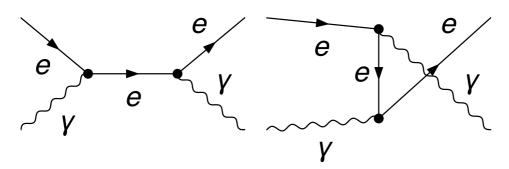
```
In[*]:= (* QED: photon photon → e- e+ (pair creation)*)
     topology = CreateTopologies[0, 2 \rightarrow 2];
     feynman5 = InsertFields[topology, \{V[1], V[1]\} \rightarrow \{F[2, \{1\}], -F[2, \{1\}]\},
        InsertionLevel → {Classes}, Restrictions → QEDOnly];
     Paint[feynman5, Numbering → None, SheetHeader → False,
       ColumnsXRows \rightarrow {4, 1}, ImageSize \rightarrow {1032, 256}];
     amplitude5[0] = FCFAConvert[CreateFeynAmp[feynman5], IncomingMomenta → {p1, p2},
       OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
       ChangeDimension → 4, TransversePolarizationVectors → {p1, p2},
       List → False, SMP → True, Contract → True]
     FCClearScalarProducts[];
     SetMandelstam[s, t, u, p1, p2, -p3, -p4, 0, 0, SMP["m_e"], SMP["m_e"]];
     squareamplitude5[0] = (amplitude5[0] (ComplexConjugate[amplitude5[0]])) //
              FeynAmpDenominatorExplicit //
             DoPolarizationSums[#, p1, 0] & // DoPolarizationSums[#, p2, 0] & //
           FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify //
        TrickMandelstam[#, {s, t, u, 2 SMP["m_e"]^2}] & // Simplify
     masslesssquareamplitude5[0] =
      squareamplitude5[0] // ReplaceAll[#, {SMP["m_e"] → 0}] & // Simplify
     (* output = feynman diagrams, amplitude,
     squared amplitude, massless squared amplitude *)
```



$$\begin{array}{l} \text{Out}\{\circ\}=\\ &\frac{\mathrm{e}^2\left(\varphi\left(\,\overline{p_3}\,,m_e\,\right)\right).(\overline{\gamma}\cdot\overline{\varepsilon}(p_2)).(\overline{\gamma}\cdot(\overline{p_3}-\overline{p_2})+m_e).(\overline{\gamma}\cdot\overline{\varepsilon}(p_1)).(\varphi\left(\,-\overline{p_4}\,,m_e\,\right))}{(\,\overline{p_2}-\overline{p_3}\,)^2-m_e^2} \\ &\frac{\mathrm{e}^2\left(\varphi\left(\,\overline{p_3}\,,m_e\,\right)\right).(\overline{\gamma}\cdot\overline{\varepsilon}(p_1)).(\overline{\gamma}\cdot(\overline{p_2}-\overline{p_4})+m_e).(\overline{\gamma}\cdot\overline{\varepsilon}(p_2)).(\varphi\left(\,-\overline{p_4}\,,m_e\,\right))}{(\,\overline{p_4}-\overline{p_2}\,)^2-m_e^2} \\ &\frac{2\,\mathrm{e}^4\left(m_e^4\left(3\,t^2+14\,t\,u+3\,u^2\right)-m_e^2\left(t^3+7\,t^2\,u+7\,t\,u^2+u^3\right)-6\,m_e^8+t\,u\left(t^2+u^2\right)\right)}{\left(t-m_e^2\right)^2\left(u-m_e^2\right)^2} \end{array}$$

Out[*] =
$$\frac{2 e^4 (t^2 + u^2)}{t u}$$

```
In[\cdot]:= (* QED: e- photon \rightarrow e- photon (Compton)*)
     topology = CreateTopologies[0, 2 \rightarrow 2];
     feynman6 = InsertFields[topology, \{F[2, \{1\}], V[1]\} \rightarrow \{F[2, \{1\}], V[1]\},
         InsertionLevel → {Classes}, Restrictions → QEDOnly];
     Paint[feynman6, Numbering → None, SheetHeader → False,
       ColumnsXRows \rightarrow {4, 1}, ImageSize \rightarrow {1032, 256}];
     amplitude6[0] = FCFAConvert[CreateFeynAmp[feynman6], IncomingMomenta → {p1, p2},
       OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
       ChangeDimension → 4, TransversePolarizationVectors → {p2, p4},
       List → False, SMP → True, Contract → True]
     FCClearScalarProducts[];
     SetMandelstam[s, t, u, p1, p2, -p3, -p4, SMP["m_e"], 0, SMP["m_e"], 0];
     squareamplitude6[0] = (amplitude6[0] (ComplexConjugate[amplitude6[0]])) //
               FeynAmpDenominatorExplicit //
             DoPolarizationSums[#, p2, 0] & // DoPolarizationSums[#, p4, 0] & //
           FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify //
         TrickMandelstam[#, {s, t, u, 2 SMP["m_e"]^2}] & // Simplify
     masslesssquareamplitude6[0] =
      squareamplitude6[0] // ReplaceAll[#, {SMP["m_e"] → 0}] & // Simplify
     (* output = feynman diagrams, amplitude,
     squared amplitude, massless squared amplitude *)
```

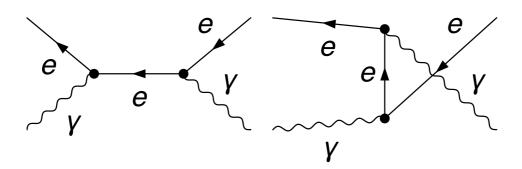


$$\begin{array}{l} \text{Out} [\circ] = \\ -\frac{\mathrm{e}^2 \left(\varphi \left(\overline{p_3} \,, m_e\right)\right).(\overline{\gamma} \cdot \overline{\varepsilon}(p_2)).(\overline{\gamma} \cdot (\overline{p_3} - \overline{p_2}) + m_e).(\overline{\gamma} \cdot \overline{\varepsilon}^*(p_4)).(\varphi \left(\overline{p_1} \,, m_e\right))}{\left(\overline{p_2} - \overline{p_3}\right)^2 - m_e^2} \\ -\frac{\mathrm{e}^2 \left(\varphi \left(\overline{p_3} \,, m_e\right)\right).(\overline{\gamma} \cdot \overline{\varepsilon}^*(p_4)).(\overline{\gamma} \cdot (\overline{p_3} + \overline{p_4}) + m_e).(\overline{\gamma} \cdot \overline{\varepsilon}(p_2)).(\varphi \left(\overline{p_1} \,, m_e\right))}{\left(-\overline{p_3} - \overline{p_4}\right)^2 - m_e^2} \\ \text{Out} [\circ] = \\ \frac{2\,\mathrm{e}^4 \left(-m_e^4 \left(3\,s^2 + 14\,s\,u + 3\,u^2\right) + m_e^2 \left(s^3 + 7\,s^2\,u + 7\,s\,u^2 + u^3\right) + 6\,m_e^8 - s\,u\left(s^2 + u^2\right)\right)}{\left(s - m_e^2\right)^2 \left(u - m_e^2\right)^2} \end{array}$$

Out[•] =
$$-\frac{2e^{4}(s^{2} + u^{2})}{c}$$

Out[0]=

```
In[•]:= (* QED: e+ photon → e+ photon *)
     topology = CreateTopologies[0, 2 → 2];
     feynman7 = InsertFields[topology, \{-F[2, \{1\}], V[1]\} \rightarrow \{-F[2, \{1\}], V[1]\},
        InsertionLevel → {Classes}, Restrictions → QEDOnly];
     Paint[feynman7, Numbering → None, SheetHeader → False,
       ColumnsXRows \rightarrow {4, 1}, ImageSize \rightarrow {1032, 256}];
     amplitude7[0] = FCFAConvert[CreateFeynAmp[feynman7], IncomingMomenta → {p1, p2},
       OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
       ChangeDimension → 4, TransversePolarizationVectors → {p2, p4},
       List → False, SMP → True, Contract → True]
     FCClearScalarProducts[];
     SetMandelstam[s, t, u, p1, p2, -p3, -p4, SMP["m_e"], 0, SMP["m_e"], 0];
     squareamplitude7[0] = (amplitude7[0] (ComplexConjugate[amplitude7[0]])) //
              FeynAmpDenominatorExplicit //
             DoPolarizationSums[#, p2, 0] & // DoPolarizationSums[#, p4, 0] & //
           FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify //
        TrickMandelstam[#, {s, t, u, 2 SMP["m_e"]^2}] & // Simplify
     masslesssquareamplitude7[0] =
      squareamplitude7[0] // ReplaceAll[#, {SMP["m_e"] → 0}] & // Simplify
     (* output = feynman diagrams, amplitude,
     squared amplitude, massless squared amplitude *)
```

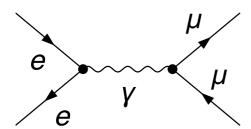


$$\frac{e^{2} \left(\varphi \left(-\overline{p_{1}},m_{e}\right)\right).(\overline{\gamma}\cdot\overline{\varepsilon}^{*}(p_{4})).(\overline{\gamma}\cdot(\overline{p_{2}}-\overline{p_{3}})+m_{e}).(\overline{\gamma}\cdot\overline{\varepsilon}(p_{2})).(\varphi \left(-\overline{p_{3}},m_{e}\right))}{(\overline{p_{3}}-\overline{p_{2}})^{2}-m_{e}^{2}}+\frac{e^{2} \left(\varphi \left(-\overline{p_{1}},m_{e}\right)\right).(\overline{\gamma}\cdot\overline{\varepsilon}(p_{2})).(\overline{\gamma}\cdot(-\overline{p_{3}}-\overline{p_{4}})+m_{e}).(\overline{\gamma}\cdot\overline{\varepsilon}^{*}(p_{4})).(\varphi \left(-\overline{p_{3}},m_{e}\right))}{(\overline{p_{3}}+\overline{p_{4}})^{2}-m_{e}^{2}}$$

$$Out[\circ] = \frac{2 e^{4} \left(-m_{e}^{4} \left(3 s^{2}+14 s u+3 u^{2}\right)+m_{e}^{2} \left(s^{3}+7 s^{2} u+7 s u^{2}+u^{3}\right)+6 m_{e}^{8}-s u \left(s^{2}+u^{2}\right)\right)}{\left(s-m_{e}^{2}\right)^{2} \left(u-m_{e}^{2}\right)^{2}}$$

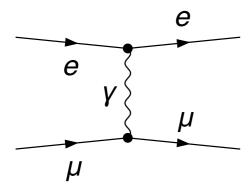
$$Out[\circ] = \frac{2 e^{4} \left(s^{2}+u^{2}\right)}{-\frac{2 e^{4} \left(s^{2}+u^{2}\right)}{2}}$$

```
In[•]:= (* QED: e- e+ → mu- mu+ *)
     topology = CreateTopologies[0, 2 \rightarrow 2];
     feynman8 =
       InsertFields[topology, \{F[2, \{1\}], -F[2, \{1\}]\} \rightarrow \{F[2, \{2\}], -F[2, \{2\}]\},
         InsertionLevel → {Classes}, Restrictions → QEDOnly];
     Paint[feynman8, Numbering → None, SheetHeader → False,
       ColumnsXRows → {4, 1}, ImageSize → {1032, 256}];
     amplitude8[0] = FCFAConvert[CreateFeynAmp[feynman8], IncomingMomenta → {p1, p2},
       OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
       ChangeDimension → 4, List → False, SMP → True, Contract → True]
     FCClearScalarProducts[];
     SetMandelstam[s, t, u, p1, p2, -p3, -p4,
       SMP["m e"], SMP["m e"], SMP["m mu"], SMP["m mu"]];
     squareamplitude8[0] = (amplitude8[0] (ComplexConjugate[amplitude8[0]])) //
           FeynAmpDenominatorExplicit //
          FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify // Simplify
     masslesssquareamplitude8[0] = squareamplitude8[0] //
         ReplaceAll[#, \{SMP["m_e"] \rightarrow 0, SMP["m_mu"] \rightarrow 0\}] \& // Simplify
     (* output = feynman diagrams, amplitude,
     squared amplitude, massless squared amplitude *)
```



$$\begin{array}{l} Out[\circ] = \\ & - \frac{\mathrm{e}^{2} \left(\varphi \left(- \overline{p_{2}} \; , m_{e} \right) \right) . \overline{\gamma}^{\mathrm{Lor2}} . \left(\varphi \left(\; \overline{p_{1}} \; , m_{e} \right) \right) \left(\varphi \left(\; \overline{p_{3}} \; , m_{\mu} \right) \right) . \overline{\gamma}^{\mathrm{Lor2}} . \left(\varphi \left(- \overline{p_{4}} \; , m_{\mu} \right) \right)}{\left(\; \overline{p_{3}} \; + \; \overline{p_{4}} \right)^{2}} \\ Out[\circ] = \\ & \underline{2 \; \mathrm{e}^{4} \left(2 \; m_{e}^{2} \left(2 \; m_{\mu}^{2} + s - t - u \right) + 2 \; m_{e}^{4} + 2 \; m_{\mu}^{4} + 2 \; m_{\mu}^{2} \left(s - t - u \right) + t^{2} + u^{2} \right)}}{s^{2}} \\ Out[\circ] = \\ \end{array}$$

```
In[\bullet]:= (* QED: e- mu- \rightarrow e- mu- *)
     topology = CreateTopologies[0, 2 → 2];
     feynman9 =
       InsertFields[topology, \{F[2, \{1\}], F[2, \{2\}]\} \rightarrow \{F[2, \{1\}], F[2, \{2\}]\},
         InsertionLevel → {Classes}, Restrictions → QEDOnly];
     Paint[feynman9, Numbering → None, SheetHeader → False,
       ColumnsXRows → {4, 1}, ImageSize → {1032, 256}];
     amplitude9[0] = FCFAConvert[CreateFeynAmp[feynman9], IncomingMomenta → {p1, p2},
       OutgoingMomenta → {p3, p4}, UndoChiralSplittings → True,
       ChangeDimension → 4, List → False, SMP → True, Contract → True]
     FCClearScalarProducts[];
     SetMandelstam[s, t, u, p1, p2, -p3, -p4,
       SMP["m e"], SMP["m mu"], SMP["m e"], SMP["m mu"]];
     squareamplitude9[0] = (amplitude9[0] (ComplexConjugate[amplitude9[0]])) //
           FeynAmpDenominatorExplicit //
          FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // DiracSimplify // Simplify
     masslesssquareamplitude9[0] = squareamplitude9[0] //
         ReplaceAll[#, \{SMP["m_e"] \rightarrow 0, SMP["m_mu"] \rightarrow 0\}] \& // Simplify
     (* output = feynman diagrams, amplitude,
     squared amplitude, massless squared amplitude *)
```



$$\begin{array}{l} \text{Out} [\circ] = \\ -\frac{\mathrm{e}^2 \left(\varphi \left(\,\overline{p_3}\,, m_e\,\right)\right).\overline{\gamma}^{\mathrm{Lor2}}.(\varphi \left(\,\overline{p_1}\,, m_e\,\right)) \left(\varphi \left(\,\overline{p_4}\,, m_\mu\,\right)\right).\overline{\gamma}^{\mathrm{Lor2}}.(\varphi \left(\,\overline{p_2}\,, m_\mu\,\right))}{\left(\,\overline{p_4} - \overline{p_2}\,\right)^2} \\ \text{Out} [\circ] = \\ \frac{2\,\mathrm{e}^4 \left(-2\,m_e^2 \left(-2\,m_\mu^2 + s - t + u\right) + 2\,m_e^4 + 2\,m_\mu^4 - 2\,m_\mu^2 \left(s - t + u\right) + s^2 + u^2\right)}{t^2} \\ \text{Out} [\circ] = \\ \frac{2\,\mathrm{e}^4 \left(s^2 + u^2\right)}{t^2} \\ \end{array}$$

In[0]:= Print["\tCPU Time used: ", Round[N[TimeUsed[], 4], 0.001], " s."]; CPU Time used: 5.838 s.

In[0]:= FeynCalcHowToCite[]

- V. Shtabovenko, R. Mertig and F. Orellana, arXiv:2312.14089.
- V. Shtabovenko, R. Mertig and F. Orellana, Comput.Phys.Commun. 256 (2020) 107478, arXiv:2001.04407.
- V. Shtabovenko, R. Mertig and F. Orellana, Comput.Phys.Commun. 207 (2016) 432–444, arXiv:1601.01167.
- R. Mertig, M. Böhm, and A. Denner, Comput. Phys. Commun. 64 (1991) 345–359.

Out[0]=

Null