Electron repulsion integrals

```
prefac = 1
f0 = Subscript[F, 0]
f1 = Subscript[F, 1]
f2 = Subscript[F, 2]
f3 = Subscript[F, 3]
f4 = Subscript[F, 4]
ssss0 = prefac * f0
ssss1 = prefac * f1
\mathbf{F}_1
ssss2 = prefac * f2
\mathbf{F}_2
ssss3 = prefac * f3
\mathbf{F}_3
ssss4 = prefac * f4
\mathbf{F}_4
pai = Subscript[PA, i]
paj = Subscript[PA, j]
pbj = Subscript[PB, j]
pci = Subscript[PC, i]
pcj = Subscript[PC, j]
wpi = Subscript[WP, i]
wpj = Subscript[WP, j]
qck = Subscript[QC, k]
qdl = Subscript[QD, 1]
wqk = Subscript[WQ, k]
wql = Subscript[WQ, 1]
dij = Subscript[\delta, ij]
djk = Subscript[\delta, jk]
dik = Subscript[\delta, ik]
dil = Subscript[\delta, il]
djl = Subscript[\delta, jl]
dkl = Subscript[\delta, kl]
psss0 = Collect[Expand[pai * ssss0 + wpi * ssss1],
   {f0, f1, f2, f3, f4, dij, dk1, djk, dil}]
F_0 PA_i + F_1 WP_i
psss1 = Collect[Expand[pai * ssss1 + wpi * ssss2],
   {f0, f1, f2, f3, f4, dij, dk1, djk, dil}]
F_1 PA_i + F_2 WP_i
```

```
psss2 = Collect[Expand[pai * ssss2 + wpi * ssss3],
   {f0, f1, f2, f3, f4, dij, dk1, djk, dil}]
F_2 PA_i + F_3 WP_i
psss3 = Collect[Expand[pai * ssss3 + wpi * ssss4],
   {f0, f1, f2, f3, f4, dij, dk1, djk, dil}]
F_3 PA_i + F_4 WP_i
spss0 = Collect[Expand[pbj * ssss0 + wpj * ssss1],
   {f0, f1, f2, f3, f4, dij, dk1, djk, dil}]
F_0 PB_{\dagger} + F_1 WP_{\dagger}
spss1 = Collect[Expand[pbj * ssss1 + wpj * ssss2],
   {f0, f1, f2, f3, f4, dij, dk1, djk, dil}]
F_1 PB_{\dagger} + F_2 WP_{\dagger}
spss2 = Collect[Expand[pbj * ssss2 + wpj * ssss3],
   {f0, f1, f2, f3, f4, dij, dk1, djk, dil}]
F_2 PB_1 + F_3 WP_1
spss3 = Collect[Expand[pbj * ssss3 + wpj * ssss4],
   {f0, f1, f2, f3, f4, dij, dk1, djk, dil}]
F_3 PB_1 + F_4 WP_1
psps0 =
 Collect[Expand[qck * psss0 + wqk * psss1 + (dik / (2*(\xi+\eta))) * ssss1],
   {f0, f1, f2, f3, f4, dij, dk1, djk, dil}]
F_0 PA_i QC_k + F_2 WP_i WQ_k + F_1 \left[ QC_k WP_i + PA_i WQ_k + \frac{\delta_{ik}}{2 (\zeta + \eta)} \right]
psps1 =
 \texttt{Collect}[\texttt{Expand}[\texttt{qck} * \texttt{psss1} + \texttt{wqk} * \texttt{psss2} + (\texttt{dik} / (2 * (\xi + \eta))) * \texttt{ssss2}],
   {f0, f1, f2, f3, f4, dij, dk1, djk, dil}]
F_1 PA_i QC_k + F_3 WP_i WQ_k + F_2 \left[ QC_k WP_i + PA_i WQ_k + \frac{\delta_{ik}}{2(\zeta + \eta)} \right]
spps0 =
 Collect[Expand[qck * spss0 + wqk * spss1 + (djk / (2*(\xi+\eta))) * ssss1],
   {f0, f1, f2, f3, f4, dij, dk1, djk, dil}]
F_0 PB_j QC_k + F_2 WP_j WQ_k + F_1 \left(QC_k WP_j + PB_j WQ_k + \frac{\delta_{jk}}{2 (\zeta + \eta)}\right)
spps1 =
 \texttt{Collect}[\texttt{Expand}[\texttt{qck} * \texttt{spss1} + \texttt{wqk} * \texttt{spss2} + (\texttt{djk} / (2 * (\xi + \eta))) * \texttt{ssss2}],
   {f0, f1, f2, f3, f4, dij, dk1, djk, dil}]
 F_1 PB_j QC_k + F_3 WP_j WQ_k + F_2 \left( QC_k WP_j + PB_j WQ_k + \frac{\delta_{jk}}{2 (\zeta + n)} \right)
```

$$\begin{aligned} & \text{ppss0} = \text{Collect} \left[\text{Expand} \right[\\ & \text{pbj} * \text{psss0} * \text{wpj} * \text{psss1} * \left(\text{dij} \middle/ \left(2 * \mathcal{E} \right) \right) * \left(\text{ssss0} - \left(\rho \middle/ \mathcal{E} \right) * \text{ssss1} \right) \right], \\ & \left\{ \text{f0, f1, f2, f3, f4, dij, dk1, djk, di1} \right\} \end{aligned} \\ & F_2 \, \text{WPi} \, \text{WPj} + F_0 \left(\text{PAi} \, \text{PBj} + \frac{\delta_{ij}}{2 \, \mathcal{E}} \right) + F_1 \left(\text{PBj} \, \text{WPi} + \text{PAi} \, \text{WPj} - \frac{\rho \, \delta_{ij}}{2 \, \mathcal{E}^2} \right) \end{aligned} \\ & \text{ppss1} = \text{Collect} \left[\text{Expand} \right[\\ & \text{pbj} * \text{psss1} + \text{wpj} * \text{psss2} + \left(\text{dij} \middle/ \left(2 * \mathcal{E} \right) \right) * \left(\text{ssss1} - \left(\rho \middle/ \mathcal{E} \right) * \text{ssss2} \right) \right], \\ & \left\{ \text{f0, f1, f2, f3, f4, dij, dk1, djk, di1} \right\} \end{aligned} \\ & F_3 \, \text{WPi} \, \text{WPj} + F_1 \left(\text{PAi} \, \text{PBj} + \frac{\delta_{ij}}{2 \, \mathcal{E}} \right) + F_2 \left(\text{PBj} \, \text{WPi} + \text{PAi} \, \text{WPj} - \frac{\rho \, \delta_{ij}}{2 \, \mathcal{E}^2} \right) \end{aligned} \\ & \text{ppss2} = \text{Collect} \left[\text{Expand} \right[\\ & \text{pbj} * \text{psss2} + \text{wpj} * \text{psss3} + \left(\text{dij} \middle/ \left(2 * \mathcal{E} \right) \right) * \left(\text{ssss2} - \left(\rho \middle/ \mathcal{E} \right) * \text{ssss3} \right) \right], \\ & \left\{ \text{f0, f1, f2, f3, f4, dij, dk1, djk, di1} \right\} \end{aligned} \\ & F_4 \, \text{WPi} \, \text{WPj} + F_2 \left(\text{PAi} \, \text{PBj} + \frac{\delta_{ij}}{2 \, \mathcal{E}} \right) + F_3 \left(\text{PBj} \, \text{WPi} + \text{PAi} \, \text{WPj} - \frac{\rho \, \delta_{ij}}{2 \, \mathcal{E}^2} \right) \end{aligned} \\ & \text{ppps0} = \text{Collect} \left[\text{Expand} \left[\text{qck} * \text{ppss0} + \text{wqk} * \text{ppss1} + \left(1 \middle/ \left(2 * \left(\mathcal{E} + \eta \right) \right) \right) * \left(\text{dik} * \text{spss1} + \text{djk} * \text{psss1} \right) \right], \\ & \left\{ \text{f0, f1, f2, f3, f4, dij, dk1, djk, di1} \right\} \end{aligned}$$

$$\begin{split} \mathbf{F_1} &\left(\mathbf{PB_j} \ \mathbf{QC_k} \ \mathbf{WP_i} + \mathbf{PA_i} \ \mathbf{QC_k} \ \mathbf{WP_j} + \mathbf{PA_i} \ \mathbf{PB_j} \ \mathbf{WQ_k} + \\ &\left(-\frac{\rho \ \mathbf{QC_k}}{2 \ \mathcal{E}^2} + \frac{\mathbf{WQ_k}}{2 \ \mathcal{E}}\right) \ \delta_{ij} + \frac{\mathbf{PB_j} \ \delta_{ik}}{2 \ (\mathcal{E} + \eta)} + \frac{\mathbf{PA_i} \ \delta_{jk}}{2 \ (\mathcal{E} + \eta)}\right) + \\ \mathbf{F_2} &\left(\mathbf{QC_k} \ \mathbf{WP_i} \ \mathbf{WP_j} + \mathbf{PB_j} \ \mathbf{WP_i} \ \mathbf{WQ_k} + \mathbf{PA_i} \ \mathbf{WP_j} \ \mathbf{WQ_k} - \\ \end{split}$$

$$\frac{\rho \, \mathtt{WQ}_{k} \, \delta_{\mathtt{i}\mathtt{j}}}{2 \, \underline{\varsigma}^{2}} + \frac{\mathtt{WP}_{\mathtt{j}} \, \delta_{\mathtt{i}\mathtt{k}}}{2 \, (\underline{\varsigma} + \underline{\eta})} + \frac{\mathtt{WP}_{\mathtt{i}} \, \delta_{\mathtt{j}\mathtt{k}}}{2 \, (\underline{\varsigma} + \underline{\eta})}\right)$$

$$\begin{split} & \texttt{ppps1} = \texttt{Collect}[\texttt{Expand}[\texttt{qck} * \texttt{ppss1} + \texttt{wqk} * \texttt{ppss2} + \\ & \quad (\texttt{1} / (\texttt{2} * (\texttt{\zeta} + \eta))) * (\texttt{dik} * \texttt{spss2} + \texttt{djk} * \texttt{psss2})], \\ & \quad \{\texttt{f0, f1, f2, f3, f4, dij, dkl, djk, dil}\}] \\ & \quad F_4 \; \texttt{WP}_i \; \texttt{WP}_j \; \texttt{WQ}_k + F_1 \; \left(\texttt{PA}_i \; \texttt{PB}_j \; \texttt{QC}_k + \frac{\texttt{QC}_k \; \delta_{ij}}{2 \; \zeta}\right) + \end{split}$$

$$F_{2} \left(PB_{j} QC_{k} WP_{i} + PA_{i} QC_{k} WP_{j} + PA_{i} PB_{j} WQ_{k} + PA_{i} PB_{i} PB_{j} WQ_{k} + PA_{i} PB_{i} PB_{i} PB_{i} PB_{i} PB_{i} PB_{i} PB_{i} PB_{i} PB_{i} PB_$$

$$\left(-\frac{\rho \ QC_k}{2 \ \zeta^2} + \frac{WQ_k}{2 \ \zeta}\right) \ \delta_{ij} + \frac{PB_j \ \delta_{ik}}{2 \ (\zeta + \eta)} + \frac{PA_i \ \delta_{jk}}{2 \ (\zeta + \eta)}\right) +$$

$$F_{3}\left(QC_{k}\;\text{WP}_{\mathtt{i}}\;\text{WP}_{\mathtt{j}}\;+\;PB_{\mathtt{j}}\;\text{WP}_{\mathtt{i}}\;\text{WQ}_{k}\;+\;PA_{\mathtt{i}}\;\text{WP}_{\mathtt{j}}\;\text{WQ}_{k}\;-\;\frac{\rho\;\text{WQ}_{k}\;\mathcal{S}_{\mathtt{i}\mathtt{j}}}{2\;\mathcal{\zeta}^{2}}\;+\;\frac{\text{WP}_{\mathtt{j}}\;\mathcal{S}_{\mathtt{i}k}}{2\;\left(\mathcal{\zeta}+\eta\right)}\;+\;\frac{\text{WP}_{\mathtt{i}}\;\mathcal{S}_{\mathtt{j}k}}{2\;\left(\mathcal{\zeta}+\eta\right)}\;\right)$$

$$\begin{split} & \text{pppp0} = \text{Collect} \big[\text{Expand} \big[\text{qd1} * \text{ppps0} + \\ & \text{wq1} * \text{ppps1} + (1 / (2 * (\xi + \eta))) * (\text{di1} * \text{spps1} + \text{dj1} * \text{ppss1}) + \\ & (\text{dk1} / (2 * \eta)) * (\text{ppss0} - (\rho / \eta) * \text{ppss1}) \big], \\ & \{ \text{f0}, \, \text{f1}, \, \text{f2}, \, \text{f3}, \, \text{f4}, \, \text{dij}, \, \text{dk1}, \, \text{djk}, \, \text{di1} \} \big] \\ & F_4 \, \text{WP}_i \, \text{WP}_j \, \text{WQ}_k \, \text{WQ}_1 + \\ & F_3 \, \bigg(\text{QD}_1 \, \text{WP}_i \, \text{WP}_j \, \text{WQ}_k + \text{QC}_k \, \text{WP}_i \, \text{WP}_j \, \text{WQ}_1 + \text{PB}_j \, \text{WP}_i \, \text{WQ}_k \, \text{WQ}_1 + \text{PA}_i \, \text{WP}_j \, \text{WQ}_k \, \text{WQ}_1 - \\ & \frac{\rho \, \text{WQ}_k \, \text{WQ}_1 \, \delta_{1j}}{2 \, \xi^2} + \frac{\text{WP}_j \, \text{WQ}_k \, \delta_{j1}}{2 \, (\xi + \eta)} - \frac{\rho \, \text{WP}_i \, \text{WP}_j \, \delta_{k1}}{2 \, (\xi + \eta)} + \\ & \frac{\text{WP}_i \, \text{WQ}_1 \, \delta_{jk}}{2 \, (\xi + \eta)} + \frac{\text{WP}_i \, \text{WQ}_k \, \delta_{j1}}{2 \, (\xi + \eta)} - \frac{\rho \, \text{WP}_i \, \text{WP}_j \, \delta_{k1}}{2 \, \eta^2} \bigg) + \\ & F_0 \, \bigg(\text{PA}_i \, \text{PB}_j \, \text{QC}_k \, \text{QD}_1 + \frac{\text{PA}_i \, \text{PB}_j \, \delta_{k1}}{2 \, \eta} + \delta_{ij} \, \bigg(\frac{\text{QC}_k \, \text{QD}_1}{2 \, \xi} + \frac{\delta_{k1}}{4 \, \xi \, \eta} \bigg) \bigg) + \\ & F_2 \, \bigg(\text{QC}_k \, \text{QD}_1 \, \text{WP}_i \, \text{WP}_j + \text{PB}_j \, \text{QD}_1 \, \text{WP}_i \, \text{WQ}_k + \text{PA}_i \, \text{QD}_1 \, \text{WP}_j \, \text{WQ}_k + \\ & P_B_j \, \text{QC}_k \, \text{WP}_i \, \text{WP}_j + \text{PB}_j \, \text{QD}_1 \, \text{WP}_i \, \text{WQ}_k + \text{PA}_i \, \text{PB}_j \, \text{WQ}_k \, \text{WQ}_1 + \\ & \frac{QD_1 \, \text{WP}_j \, \delta_{ik}}{2 \, (\xi + \eta)} + \frac{PB_j \, \text{WQ}_1 \, \delta_{ik}}{2 \, (\xi + \eta)} + \frac{QC_k \, \text{WP}_j}{2 \, (\xi + \eta)} + \frac{PB_j \, \text{WQ}_k \, \text{WQ}_1 + \\ & \frac{QD_1 \, \text{WP}_j \, \delta_{ik}}{2 \, (\xi + \eta)} + \frac{PA_i \, \text{WQ}_1}{2 \, (\xi + \eta)} + \frac{\delta_{i1}}{2 \, (\xi + \eta)} \bigg) \, \delta_{i1} + \\ & \frac{QD_1 \, \text{WP}_j \, \delta_{ik}}{2 \, (\xi + \eta)} + \frac{PA_i \, \text{WQ}_1}{2 \, (\xi + \eta)} + \frac{\delta_{i1}}{2 \, (\xi + \eta)} \bigg) \, \delta_{jk} + \frac{PB_j \, \text{WQ}_k \, \delta_{j1}}{2 \, (\xi + \eta)} + \\ & \frac{PA_i \, \text{WQ}_k \, \delta_{j1}}{2 \, (\xi + \eta)} + \frac{\delta_{i1} \, \delta_{j1}}{4 \, (\xi + \eta)^2} + \left(-\frac{\rho \, \text{PB}_j \, \text{WP}_i}{2 \, (\xi + \eta)} + \frac{\rho^2 \, \delta_{k1}}{2 \, (\xi + \eta)} \right) \, \delta_{k1} + \\ & \frac{PA_i \, \text{PQ}_k \, \text{QQ}_k}{2 \, 2} - \frac{\rho \, \text{QC}_k \, \text{WQ}_1}{2 \, (\xi + \eta)} + \frac{PB_j \, \text{QC}_k \, \delta_{j1}}{2 \, (\xi + \eta)} + \frac{PB_j \, \text{QC}_k \, \delta_{j1}}{2 \, (\xi + \eta)} + \frac{PA_i \, \text{WP}_j}{2 \, (\xi + \eta)} \bigg) \, \delta_{k1} + \\ & \frac{PA_i$$

Overlap, Potential and Kinetic Integrals

ss PAi

 $pp = Simplify[pbj*ps + (dij/2 \zeta) ss]$

$$\operatorname{ss} \operatorname{PA}_{i} \operatorname{PB}_{j} + \frac{1}{2} \operatorname{ss} \zeta \delta_{ij}$$

sks = Simplify[ξ (3 - 2 ξ * R^2) ss]

$$ss \xi (3 - 2 R^2 \xi)$$

 $pks = Simplify[pai*sks + 2 \xi*ps]$

$$ss \xi (5 - 2 R^2 \xi) PA_i$$

 $pkp = Simplify[pbj*pks + (dij/2\zeta)*sks + 2\xi*pp]$

$$-\frac{1}{2}\operatorname{ss}\xi\left(2\left(-7+2R^{2}\xi\right)PA_{i}PB_{j}+\zeta\left(-5+2R^{2}\xi\right)\delta_{ij}\right)$$

 $scs0 = Simplify[2 Sqrt[\zeta/\pi] * ss * f0]$

$$\frac{2\,\text{ss}\,\sqrt{\zeta}\,\,F_0}{\sqrt{\pi}}$$

 $scs1 = Simplify[2 Sqrt[\zeta/\pi] * ss * f1]$

$$rac{2\,\,\mathrm{ss}\,\sqrt{\zeta}\,\,\,\mathrm{F}_1}{\sqrt{\pi}}$$

 $scs2 = Simplify[2 Sqrt[\zeta/\pi] * ss * f2]$

$$\frac{2\,\text{ss}\,\sqrt{\zeta}\,\,F_2}{\sqrt{\pi}}$$

pcs0 = Simplify[pai * scs0 - pci * scs1]

$$\frac{\text{2 ss}\,\sqrt{\zeta}\ (\text{F}_{\text{0}}\,\text{PA}_{\text{i}}\,\text{-}\,\text{F}_{\text{1}}\,\text{PC}_{\text{i}})}{\sqrt{\pi}}$$

pcs1 = Simplify[pai * scs1 - pci * scs2]

$$\frac{2 \, \text{ss} \, \sqrt{\zeta} \, \left(\text{F}_1 \, \text{PA}_{\text{i}} - \text{F}_2 \, \text{PC}_{\text{i}} \right)}{\sqrt{\pi}}$$

pcp0 = Simplify[pbj * pcs0 - pcj * pcs1 + (dij / 2 \(\mathcal{G}\)) (scs0 - scs1)]

$$\underline{\text{ss}\,\sqrt{\zeta}}\,\,\left(2\,\,F_{2}\,\,PC_{\dot{1}}\,\,PC_{\dot{j}}\,+\,F_{0}\,\,\left(2\,\,PA_{\dot{1}}\,\,PB_{\dot{j}}\,+\,\mathcal{\zeta}\,\,\delta_{\dot{1}\dot{j}}\right)\,\,-\,F_{1}\,\,\left(2\,\,PB_{\dot{j}}\,\,PC_{\dot{1}}\,+\,2\,\,PA_{\dot{1}}\,\,PC_{\dot{j}}\,+\,\mathcal{\zeta}\,\,\delta_{\dot{1}\dot{j}}\right)\right)$$