

Lecture 2: Atomic Data Types/Homogeneous vectors

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R can be summarized in three principles (John M. Chambers, 2016)

- Everything that exists in R is an **object**.
- Everything that happens in R is a **function** call.
- **Interfaces** to other languages are a part of R.

1 R Objects

- An object in R is (internally) represented as a pair: (**symbol**, **value**).
- A **symbol** is assigned a **value** by the use of an arrow pointing to the left (**<-**).
- There are **less favored** ways:
 - A simple equality sign (**=**).
 - Using the **assign()** function.

1.1 Examples

- Clean up the global environment i.e. remove all objects from the current R environment.

Recommended!

```
rm(list=ls())  
ls()
```

```
character(0)
```

- **preferred** way to assign variables

```
x <- 5.0  
x
```

```
[1] 5
```

- alternative 1: mainly used to assign default function arguments

```
y = 5.0  
y
```

```
[1] 5
```

```
mysamplevariance <- function(x, av=0){  
  
  n <- length(x)  
  if(n>1){  
    return(1.0/(n-1)*sum((x-av)^2))  
  }  
  else{  
    stop("ERROR:: Dividing by zero (n==1) || (n==0) ")  
  }  
}
```

```
x <- rnorm(10)  
mysamplevariance(x)
```

```
[1] 0.9242733
```

```
mysamplevariance(x,mean(x))
```

```
[1] 0.9227859
```

```
var(x)
```

```
[1] 0.9227859
```

- alternative 2: even less used

```
assign("z", 5.0)
```

```
z
```

```
[1] 5
```

- functions are objects

```
f <- mean
```

```
f
```

```
function (x, ...)
```

```
UseMethod("mean")
```

```
<bytecode: 0x5599c43b4f60>
```

```
<environment: namespace:base>
```

```
val <- f(1:10)
```

```
val
```

```
[1] 5.5
```

"Nothing exists except atoms and empty space; everything else is opinion". (Democritos)

2 Atomic Data Types

2.1 The core/atomic data types

- R has the following 6 **atomic** data types:
 - logical (i.e. boolean)
 - integer
 - double
 - character (i.e. string)
 - complex
 - raw (i.e. byte)

The latter 2 types (i.e. complex and especially raw) are less common.

The **typeof()** function determines the **INTERNAL** storage/type of an R object.

2.1.1 Examples

- boolean/logical values: either **TRUE** or **FALSE**

```
x1 <- TRUE
x1
```

```
[1] TRUE
```

```
typeof(x1)
```

```
[1] "logical"
```

- integer values ($\in \mathbb{Z}$):

```
x2 <- 3L
x2
```

```
[1] 3
```

```
typeof(x2)
```

```
[1] "integer"
```

- double (precision) values:

```
x3 <- 3.14
x3
```

```
[1] 3.14
```

```
typeof(x3)
```

```
[1] "double"
```

- character values/strings

```
x4 <- "Hello world"
x4
```

```
[1] "Hello world"
```

```
typeof(x4)
```

```
[1] "character"
```

- complex values ($\in \mathbb{C}$):

```
x5 <- 2.0 + 3i
x5
```

```
[1] 2+3i
```

```
typeof(x5)
```

```
[1] "complex"
```

2.2 Operations on atomic data types

- **logical** operators: `==`, `!=`, `&&`, `||`, `!`
- **numerical** operators: `+`, `-`, `*`, `/`, `^`, `**` (same as the caret), but also:
 - integer division: `%/%`
 - modulo operation: `%%`
 - **Note**: matrix multiplication will be performed using `%*%`
- **character/string** manipulation:
 - `nchar()`:
 - `paste()`:
 - `cat()`:
 - `sprintf()`:
 - `substr()`:
 - `strsplit()`:
 - **Note**: Specialized R libraries were developed to manipulate strings e.g. *stringr*
- explicit **cast**/conversion: <https://data-flair.training/blogs/r-string-manipulation/>
 - `as.{logical, integer, double, complex, character}()`
- explicit **test** of the type of a variable:
 - `is.{logical, integer, double, complex, character}()`

2.2.1 Examples

- Logical operators:

```
x <-3
y <-7
(x<=3) &&(y==7)
```

```
[1] TRUE
```

```
!(y<7)
```

```
[1] TRUE
```

- Mathematical operations

```
2**4
```

```
[1] 16
```

```
7%%4
```

```
[1] 3
```

```
7/4
```

```
[1] 1.75
```

```
7%/%4
```

```
[1] 1
```

- String operations

```
s <- "Hello"
nchar(s)
```

```
[1] 5
```

```
news <- paste(s,"World")
news
```

```
[1] "Hello World"
```

```
sprintf("My new string:%20s\n", news)
```

```
[1] "My new string:          Hello World\n"
```

```
city <- "Witwatersrand"
substr(city,4,8)
```

```
[1] "water"
```

- Conversion and testing of types

```
s <- "Hello World"
is.character(s)
```

```
[1] TRUE
```

```
s1 <- "-500"
is.character(s1)
```

```
[1] TRUE
```

```
s2 <- as.double(s1)
is.character(s2)
```

```
[1] FALSE
```

```
is.double(s2)
```

```
[1] TRUE
```

```
s3 <- as.complex(s2)
s3
```

```
[1] -500+0i
```

```
sqrt(s3)
```

```
[1] 0+22.36068i
```


2.2.2 Exercise

- - Calculate $\log_2(10)$ using R's **log()** function
 - Perform the inverse operation and check that you get 10 back
- Let $z = 3 + 4i$
 - Use R's **Re()**, **Im()** functions to extract the real and imaginary parts of z .
 - Calculate the modulus of z using R's **Mod()** function and check whether you the same answer using $\sqrt{\Re(z)^2 + \Im(z)^2}$.
 - Calculate the argument of z using R's **Arg()** function and check whether you have the same answer using $\arctan\left(\frac{\Im(z)}{\Re(z)}\right)$.

3 Atomic vectors

- An **atomic** vector is a data structure containing elements of **only one atomic** data type. Therefore, an atomic vector is **homogeneous**.
- Atomic vectors are stored in a **linear** fashion.
- R does **NOT** have scalars:
 - An atomic vector of **length 1** plays the role of a scalar.
 - Vectors of **length 0** also exist (and they have some use!).
- A **list** is a vector not necessarily of the atomic type.
A list is also known as a **recursive/generic** vector (*vide infra*).

3.1 Creation of atomic vectors

Atomic vectors can be created in a multiple ways:

- Use of the **vector()** function.
- Use of the **c()** function (**c** stands for concatenate).
- Use of the column operator **:**
- Use of the **seq()** and **rep()** functions.

The length of a vector can be retrieved using the **length()** function.

3.1.1 Examples

- use of the **vector()** function:

```
x <- vector() # Empty vector (Default:'logical')
x
```

```
logical(0)
```

```
length(x)
```

```
[1] 0
```

```
typeof(x)
```

```
[1] "logical"
```

```
x <- vector(mode="complex", length=4)
x
```

```
[1] 0+0i 0+0i 0+0i 0+0i
```

```
length(x)
```

```
[1] 4
```

```
x
```

```
[1] 0+0i 0+0i 0+0i 0+0i
```

```
x[1] <- 4
```

```
x
```

```
[1] 4+0i 0+0i 0+0i 0+0i
```

- use of the `c()` function:

```
x1 <- c(3, 2, 5.2, 7)
x1
```

```
[1] 3.0 2.0 5.2 7.0
```

```
x2 <- c(8, 12, 13)
x2
```

```
[1] 8 12 13
```

```
x3 <- c(x2, x1)
x3
```

```
[1] 8.0 12.0 13.0 3.0 2.0 5.2 7.0
```

```
x4 <- c(FALSE, TRUE, FALSE)
x4
```

```
[1] FALSE TRUE FALSE
```

```
x5 <- c("Hello", "Salt", "Lake", "City")
x5
```

```
[1] "Hello" "Salt" "Lake" "City"
```

- use of the column operator:

```
y1 <- 1:10
y1
```

```
[1] 1 2 3 4 5 6 7 8 9 10
```

```
y2 <- 5:-5
y2
```

```
[1] 5 4 3 2 1 0 -1 -2 -3 -4 -5
```

```
y3 <- 2.3:10
y3
```

```
[1] 2.3 3.3 4.3 5.3 6.3 7.3 8.3 9.3
```

```
y4 <- 2.0*7:1
y4
```

```
[1] 14 12 10 8 6 4 2
```

```
y5 <- 1:7-1
y5
```

```
[1] 0 1 2 3 4 5 6
```

- `seq()` and `rep()` functions

```
z1 <- seq(from=1, to=15, by=3)
z1
```

```
[1] 1 4 7 10 13
```

```
z2 <- seq(from=-2,to=5,length=4)
z2

[1] -2.0000000  0.3333333  2.6666667  5.0000000
```

```
z3 <- rep(c(3,2,4), time=2)
z3
```

```
[1] 3 2 4 3 2 4
```

```
z4 <- rep(c(3,2,4), each=3)
z4
```

```
[1] 3 3 3 2 2 2 4 4 4
```

```
z5 <- rep(c(1,7), each=2, time=3)
z5
```

```
[1] 1 1 7 7 1 1 7 7 1 1 7 7
```

```
length(z5)
```

```
[1] 12
```

3.2 Operations on vectors: element-wise

- All operations on vectors in R happen **element by element** (cfr. *NumPy*).
- **Vector Recycling**:

If 2 vectors of **different** lengths are involved in an operation, the **shortest vector** will be repeated until all elements of the longest vector are matched.

A message will be sent to the stdout.

3.2.1 Examples

```
x <- -3:3
x
```

```
[1] -3 -2 -1  0  1  2  3
```

```
y <- 1:7
y
```

```
[1] 1 2 3 4 5 6 7
```

```
xy <- x*y
xy
```

```
[1] -3 -4 -3  0  5 12 21
```

```
xpy <- x^y
xpy
```

```
[1] -3  4 -1  0  1 64 2187
```

```
x <- 0:10
y <- 1:2
length(x)
```

```
[1] 11
```

```
length(y)
```

```
[1] 2
```

```
x
```

```
[1] 0 1 2 3 4 5 6 7 8 9 10
```

```
y
```

```
[1] 1 2
```

```
x+y
```

```
Warning in x + y: longer object length is not a multiple of shorter object
length
```

```
[1] 1 3 3 5 5 7 7 9 9 11 11
```

3.3 Retrieving elements of vectors

- Indexing: starts at **1** (**not 0** like C/C++, Python, Java, ...) see also: [Edsger Dijkstra: Why numbering should start at zero](#)
- Use of vector with indices to extract values.
- Advanced features:
 - use of boolean values to extract values.
 - the membership operator: **%in%**.
 - the deselect/omit operator: **-**
 - **which()**: returns the indices for which the condition is true.
 - **any()/all()** functions.
 - * **any()** : **TRUE** if at least 1 value is true
 - * **all()** : **TRUE** if all values are true

3.3.1 Examples

- Use of a simple index:

```
x <- seq(2,100,by=15)
x[4]
```

```
[1] 47
```

```
x[1]
```

```
[1] 2
```

- Select several indices at once using vectors:

```
x
[1]  2 17 32 47 62 77 92
x[3:5]
[1] 32 47 62
x[c(1,3,5,7)]
[1]  2 32 62 92
x[seq(1,7,by=2)]
[1]  2 32 62 92
```

- Extraction via booleans (i.e. retain only those values that are equal to **TRUE**):

```
x
[1]  2 17 32 47 62 77 92
x>45
[1] FALSE FALSE FALSE  TRUE  TRUE  TRUE  TRUE
x[x>45]
[1] 47 62 77 92
```

- Use of the **%in%** operator:

```
x
[1]  2 17 32 47 62 77 92
10 %in% x
[1] FALSE
62 %in% x
[1] TRUE
c(32,33,43) %in% x
[1]  TRUE FALSE FALSE
!(c(32,33,43) %in% x)
[1] FALSE  TRUE  TRUE
```

- Negate/filter out the elements with **negative** indices:

```
x
[1]  2 17 32 47 62 77 92
```

```
x[-c(2,4,6)]
```

```
[1] 2 32 62 92
```

```
z <- x[-1] - x[-length(x)]
```

```
z
```

```
[1] 15 15 15 15 15 15
```

- The `which()` function returns **only those indices** of which the condition/expression is **true**.

```
# Sample 10 numbers from N(0,1)
```

```
vecnum <- rnorm(n=10)
```

```
vecnum
```

```
[1] -1.0458804 -0.4743288 1.3041170 1.6578032 0.3665113 1.6729210
```

```
[7] 1.8984460 0.1194658 -1.2261825 -2.0904415
```

```
which(vecnum>1.0)
```

```
[1] 3 4 6 7
```

- Use of the `any()/all()` functions.

```
y <- seq(0,100,by=10)
```

```
x
```

```
[1] 2 17 32 47 62 77 92
```

```
y
```

```
[1] 0 10 20 30 40 50 60 70 80 90 100
```

```
any(x<y)
```

```
Warning in x < y: longer object length is not a multiple of shorter object length
```

```
[1] TRUE
```

```
all(x[6:7]>y[2:3])
```

```
[1] TRUE
```

3.4 Hash tables

A **hash table** is a data structure which implements an associative array or dictionary. It is an abstract data which maps data to keys.

- There are several ways to create one:
 - Map names to an existing vector
 - Add names when creating the vector
- To remove the map, map the names to NULL

3.4.1 Examples

- Creation of 2 independent vectors

```
capitals <- c("Albany", "Providence", "Hartford", "Boston", "Montpelier", "Concord", "Augusta")
states <- c("NY", "RI", "CT", "MA", "VT", "NH", "ME")
capitals
```

```
[1] "Albany"      "Providence" "Hartford"   "Boston"     "Montpelier"
[6] "Concord"     "Augusta"
```

```
states
```

```
[1] "NY" "RI" "CT" "MA" "VT" "NH" "ME"
```

```
capitals[3]
```

```
[1] "Hartford"
```

- Create the hashtable/dictionary

```
# Method 1
```

```
names(capitals) <- states
capitals
```

```
      NY      RI      CT      MA      VT      NH
"Albany" "Providence" "Hartford" "Boston" "Montpelier" "Concord"
      ME
"Augusta"
```

```
capitals["MA"]
```

```
      MA
"Boston"
```

```
names(capitals)
```

```
[1] "NY" "RI" "CT" "MA" "VT" "NH" "ME"
```

```
# Method 2
```

```
phonecode <- c("801"="SLC", "206"="Seattle", "307"="Wyoming")
phonecode
```

```
      801      206      307
"SLC" "Seattle" "Wyoming"
```

```
phonecode["801"]
```

```
      801
"SLC"
```

- Dissociate the 2 vectors


```
names(capitals) <- NULL
capitals
```

```
[1] "Albany"      "Providence" "Hartford"   "Boston"     "Montpelier"
[6] "Concord"     "Augusta"
```

3.5 NA (Not Available values)

- **NA**: stands for ‘Not Available’/Missing values
- has length of 1.
- **is.na()**: test all elements of a vector for NA values.
- some functions e.g. **mean()** return NA when an instance of NA is present.

3.5.1 Examples

- Check of the NA availability

```
x <- c(NA, 1, 2, NA)
is.na(x)
```

```
[1] TRUE FALSE FALSE TRUE
```

- Functions on a vector containing NA

```
mean(x)
```

```
[1] NA
```

```
mean(x, na.rm=TRUE)
```

```
[1] 1.5
```

3.6 Alia

Still to be developed!

- boolean: Vector operators vs. unique value
- **&&** vs. **&**.
- **||** vs. **|**.
- **xor()**

3.7 Exercises

- Use the **seq()** function to generate the following sequence:
6 13 20 27 34 41 48
- R has its own inversion function, **rev()**, e.g.:

```
x <- seq(from=2,to=33,by=3)
x
```

```
[1] 2 5 8 11 14 17 20 23 26 29 32
y <- rev(x)
y
```

```
[1] 32 29 26 23 20 17 14 11 8 5 2
```

Invert the vector `x` without invoking the `rev()` function.

- Create the following R vector using **only** the `seq()` and `rep()` functions:
-8 -8 -8 -8 0 8 8 8 16 16 16 16
- Create the following vector:
-512 -216 -64 -8 0 8 64 216 512 1000
- Generate a random vector of integers using the following code:

```
x <- sample(x=0:1000, size=100, replace=TRUE)
```

- Invoke the above code to generate the vector `x`
- Find if there are any integers in the vector `x` which can be divided by 4 and 6
- Find those numbers and their corresponding indices in the vector `x`.
- The Taylor series for $\ln(1+x)$ is converging when $|x| < 1$ and is given by:

$$\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \frac{x^5}{5} - \frac{x^6}{6} + \dots$$

Calculate the sum of the first 10, 15, 20 terms in the above expression to approximate $\ln(1.2)$. Compare with R's value i.e.: `log(1.2)`.

- The **logarithmic** return in finance is defined as:

$$R_t = \ln \left(\frac{P_t}{P_{t-1}} \right)$$

- Generate a financial time series using the following R code:

```
thecasino <- abs(rcauchy(1000))+1.E-6
```

- Calculate the **logarithmic return** for the financial time series `thecasino`.
Your adjusted time series will be 1 element shorter in length than the original one.
Compare your result with `diff(log(thecasino))`.
- Monte-Carlo approximation of π

Let `S1` be the square spanned by the following 4 vertices: $\{(0,0), (0,1), (1,0), (1,1)\}$.
Let `S2` be the first quadrant of the unit-circle $\mathcal{C} : x^2 + y^2 = 1$.

The ratio ρ defined as:

$$\rho := \frac{\text{Area S2}}{\text{Area S1}} = \frac{\text{\#Points in S2}}{\text{\#Points in S1}}$$

allows us to estimate $\frac{\pi}{4}$ numerically.

Therefore:

- Sample 100000 independent x -coordinates from `Unif`.
- Sample 100000 independent y -coordinates from `Unif`.
- Calculate an approximate value for π using the Monte-Carlo approach.

Note: The uniform distribution $[0,1)$ (`Unif`) can be sampled using `runif()`.

"It is my experience that proofs involving matrices can be shortened by 50% if one throws the matrices out" (Emil Artin)

4 Matrices & Arrays

Matrices and arrays are **homogeneous atomic vectors** with an **extra** attribute: dimension

By default, the elements are stored in a **column-major** fashion. (cfr. **Fortran**). However, we can store the elements in **row-major** order (cfr. **C**) as well.

4.1 Creation of matrices

Matrices can be created in different ways:

- use of the `matrix()` function
- use of `rbind()/cbind()`
- set the `attributes()` of a vector
- special functions like e.g. `diag()`

4.1.1 Examples

- use of the `matrix()` function:

The `matrix()` function creates a matrix based on a vector.

By default, the elements are stored in a **column-major** fashion.

The use of the flag `byrow=TRUE` will store the data in a **row-major** fashion.

```
A <- matrix(data=1:10, nrow=2) # Column-major (like Fortran)
A
```

```
      [,1] [,2] [,3] [,4] [,5]
[1,]     1     3     5     7     9
[2,]     2     4     6     8    10
```

```
B <- matrix(data=c(2,3,893,0.17), nrow=2, ncol=2)
B
```

```
      [,1] [,2]
[1,]     2 893.00
[2,]     3  0.17
```

```
C <- matrix(data=1:10, nrow=2, byrow=TRUE) # Row-major (like C, C++)
C
```

```
      [,1] [,2] [,3] [,4] [,5]
[1,]     1     2     3     4     5
[2,]     6     7     8     9    10
```

- use of the `rbind()/cbind()` functions:

- `rbind()`: Bind several vectors (as rows) into a matrix.
- `cbind()`: Bind several vectors (as columns) into a matrix.

```
A <- rbind(1:10,11:20)
```

```
A
```

```
      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
[1,]    1    2    3    4    5    6    7    8    9   10
[2,]   11   12   13   14   15   16   17   18   19   20
```

```
typeof(A)
```

```
[1] "integer"
```

```
class(A)
```

```
[1] "matrix" "array"
```

```
B <- cbind(1:5,6:10,11:15)
```

```
B
```

```
      [,1] [,2] [,3]
[1,]    1    6   11
[2,]    2    7   12
[3,]    3    8   13
[4,]    4    9   14
[5,]    5   10   15
```

```
class(B)
```

```
[1] "matrix" "array"
```

- modifying the `dim` attribute.

The **fundamental** difference between an R vector and matrix is the presence (in the case of matrices) of a non NULL `dim` attribute.

We can easily convert a vector into a matrix by setting the dimensions of the vector:

- through the `dim()` function.
- through the `attr()` function.

The inverse can be done as well by setting the `dim` attribute of matrix to NULL.

4.1.2 Examples

```
A <- 1:10
```

```
typeof(A)
```

```
[1] "integer"
```

```
class(A)
```

```
[1] "integer"
```

```
dim(A)
```

```
NULL
```

```
# Matrix
B <- matrix(1:10,nrow=2,ncol=5,byrow=TRUE)
typeof(B)
```

```
[1] "integer"
```

```
class(B)
```

```
[1] "matrix" "array"
```

```
dim(B)
```

```
[1] 2 5
```

```
# Vector
A <- 1:10
A
```

```
[1] 1 2 3 4 5 6 7 8 9 10
```

```
dim(A)
```

```
NULL
```

```
typeof(A)
```

```
[1] "integer"
```

```
class(A)
```

```
[1] "integer"
```

```
# OPTION I: Using the dim function transform a vector into a matrix
dim(A) <- c(2,5)
A
```

```
      [,1] [,2] [,3] [,4] [,5]
[1,]    1    3    5    7    9
[2,]    2    4    6    8   10
```

```
dim(A)
```

```
[1] 2 5
```

```
typeof(A)
```

```
[1] "integer"
```

```
class(A)
```

```
[1] "matrix" "array"
```

```
# Converting the matrix back to a vector
dim(A) <- NULL
dim(A)
```

```
NULL
```

```
typeof(A)
```

```
[1] "integer"
```

```
class(A)
```

```
[1] "integer"
```

```
# Option II: More general way
# Convert vector into a matrix
A <- 1:8
A
```

```
[1] 1 2 3 4 5 6 7 8
```

```
class(A)
```

```
[1] "integer"
```

```
attr(A, 'dim') <- c(2,4)
```

```
A
```

```
      [,1] [,2] [,3] [,4]
[1,]    1    3    5    7
[2,]    2    4    6    8
```

```
class(A)
```

```
[1] "matrix" "array"
```

```
# Convert matrix into a vector.
attr(A, 'dim') <- NULL
A
```

```
[1] 1 2 3 4 5 6 7 8
```

```
class(A)
```

```
[1] "integer"
```

4.2 Operations on matrices

- Operations like `*`, `/`, `+` happen element-wise.
- There are also more specialized functions:
 - the mean over rows and columns (`rowMeans()`, `colMeans()`)
 - linear algebra functions (`%*%`, `t()`, ...)

4.2.1 Examples

- Operations (by **default: element-by-element**):

```
A <- matrix(1:10, nrow=2)
B <- matrix(seq(10, 100, by=10), nrow=2)
```

```
A
      [,1] [,2] [,3] [,4] [,5]
[1,]    1    3    5    7    9
[2,]    2    4    6    8   10
```

```
B
      [,1] [,2] [,3] [,4] [,5]
[1,]   10   30   50   70   90
[2,]   20   40   60   80  100
```

```
A*B
      [,1] [,2] [,3] [,4] [,5]
[1,]   10   90  250  490  810
[2,]   40  160  360  640 1000
```

```
C <- matrix(rep(2,10), nrow=2)
C**A
```

```
      [,1] [,2] [,3] [,4] [,5]
[1,]     2     8    32   128  512
[2,]     4    16    64   256 1024
```

- Calculate **row and column means** :

```
# Means of rows and columns
A
```

```
      [,1] [,2] [,3] [,4] [,5]
[1,]     1     3     5     7     9
[2,]     2     4     6     8    10
```

```
rowMeans(A)
```

```
[1] 5 6
```

```
colMeans(A)
```

```
[1] 1.5 3.5 5.5 7.5 9.5
```

- Matrix multiplication** (`%*%`) :

```
A <- matrix(1:6, nrow=2)
A
```

```
      [,1] [,2] [,3]
[1,]     1     3     5
[2,]     2     4     6
```

```
B <- matrix(seq(10,120,by=10), nrow=3)
B
```

```
      [,1] [,2] [,3] [,4]
[1,]   10   40   70  100
[2,]   20   50   80  110
[3,]   30   60   90  120
```

```
C <- A%*%B
C
```

```
      [,1] [,2] [,3] [,4]
[1,]  220  490  760 1030
[2,]  280  640 1000 1360
```

```
dim(C)
```

```
[1] 2 4
```

- **Linear algebra** routines

Some of the more common ones in R:

- **solve()** : invert a square matrix
- **diag()**
 - **extracts** the diagonal of a matrix when a matrix is provided.
 - **creates** a diagonal matrix when a vector is provided.
- **eigen()** : calculates the **eigenvalues** and **eigenvectors** of a matrix
- **det()** : calculates the **determinant** of a matrix.
- **t()**: calculates the **transpose**¹ of a matrix.

```
# Invert matrix A
A <- matrix(c(1, 3, 2, 4), ncol = 2, byrow = T)
Ainv <- solve(A)
Ainv %*% A
```

```
      [,1] [,2]
[1,]    1    0
[2,]    0    1
```

```
# Create a diagonal matrix
C <- diag(c(1,4,7))
C
```

```
      [,1] [,2] [,3]
[1,]    1    0    0
[2,]    0    4    0
[3,]    0    0    7
```

```
# Extract the diagonal elements
D <- matrix(1:8,nrow=4)
D
```

¹Can also be used for dataframes (see later)


```

      [,1] [,2]
[1,]    1    5
[2,]    2    6
[3,]    3    7
[4,]    4    8

```

```
diag(D)
```

```
[1] 1 6
```

```
# Calculate eigenvalues and eigenvectors of A
```

```
r <- eigen(A)
```

```
r
```

```
eigen() decomposition
```

```
$values
```

```
[1] 5.3722813 -0.3722813
```

```
$vectors
```

```

      [,1]      [,2]
[1,] -0.5657675 -0.9093767
[2,] -0.8245648  0.4159736

```

```
# Eigenvalues
```

```
r$values
```

```
[1] 5.3722813 -0.3722813
```

```
# Matrix with eigenvectors
```

```
r$vectors
```

```

      [,1]      [,2]
[1,] -0.5657675 -0.9093767
[2,] -0.8245648  0.4159736

```

```
# Diagonal Matrix (Similarity Transformation)
```

```
solve(r$vectors) %*% A %*% r$vectors
```

```

      [,1]      [,2]
[1,] 5.372281e+00  0.0000000
[2,] -3.330669e-16 -0.3722813

```

Note that under the hood R calls **BLAS** and **LAPACK**.

```
# Find the version used of BLAS and LAPACK
```

```
La_library()
```

```
[1] "/usr/lib/x86_64-linux-gnu/lapack/liblapack.so.3.7.1"
```

```
extSoftVersion()["BLAS"]
```

```
BLAS
```

```
"/usr/lib/x86_64-linux-gnu/blas/libblas.so.3.7.1"
```

4.3 Hash Tables

5 Other types

- Attributes
- Special types:
 - Factors
 - Date
 - Time
- NA, NaN, NULL

Other topics on Data structures

- List
- Dataframe & Tibble
- IO (read.csv, read.file)
- Names
- Subsetting, `[[` vs. `[]`

Conditionals & Loops

- if, else, else if switch and elseif
- for
- while
- repeat
- return()

Environments

- search(), attach, detach
- library

Functions

- lexical scoping
- simple functions
- args(), formals()
- default arg, ...
- lazy evaluation
- closure
- anonymous functions
- make your own operators
- loop functions: `{l,s,m}apply`, `split`

Capita selecta

- profiling, debugging