

Hands-on Introduction to R*

Section 4: Heterogeneous vectors (Lists & Dataframes) and IO

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In the first part of this section, two kinds¹ of **heterogeneous** vectors will be discussed:

- lists
- data frames (& tibbles)

Input-output (IO) in R forms the subject of the latter part.

1 R Lists

A **list** is a vector that **may** contain one or more **components**.

The components can be **heterogeneous** objects (atomic types, functions, lists², ...).

Under the hood, the list is implemented as a vector of pointers to its top-level components.

The list's length equals the number of top-level components.

1.1 Creation of a list

An R list can be created in several ways:

- using the `list()` function (most common)
- via the `vector()` function
- via a cast using the `as.list()` function

1.1.1 Examples

- use of the `list()` function

```
# Creating an empty list
x1 <- list()
str(x1)
```

```
list()
typeof(x1):list    class(x1):list    length(x1):0
```

```
# A more realistic list
x2 <- list(1:10, c("hello", "world"),
          3+4i, matrix(data=1:6, nrow=2, ncol=3, byrow=TRUE))
str(x2)
```

```
List of 4
 $ : int [1:10] 1 2 3 4 5 6 7 8 9 10
 $ : chr [1:2] "hello" "world"
 $ : cplx 3+4i
 $ : int [1:2, 1:3] 1 4 2 5 3 6
typeof(x2):list    class(x2):list    length(x2):4
```

¹R also has the pairlist. This topic will not be discussed in this section. People interested in this subject, should have a look at [R-internals](#).

²Due to this feature, they are also called **recursive** vectors.

```
# Using existing names
x3 <- list(x=1, y=2, str1="hello", str2="world", vec=1:5)
str(x3)
```

```
List of 5
 $ x    : num 1
 $ y    : num 2
 $ str1: chr "hello"
 $ str2: chr "world"
 $ vec  : int [1:5] 1 2 3 4 5
```

```
# Applying names to a list
x4 <- list(matrix(data=1:4,nrow=2,ncol=2), c(T,F,T,T), "hello")
names(x4) <- c("mymat","mybool","mystr")
str(x4)
```

```
List of 3
 $ mymat : int [1:2, 1:2] 1 2 3 4
 $ mybool: logi [1:4] TRUE FALSE TRUE TRUE
 $ mystr  : chr "hello"
```

- use `vector()` function:

Allows to create/allocate an empty vector of a certain length.

```
# Allocate a vector of length 5
x5 <- vector(mode="list", length=5)
str(x5)
```

```
List of 5
 $ : NULL
 $ : NULL
 $ : NULL
 $ : NULL
 $ : NULL
```

- using the `as.list()` function

```
x6 <- as.list(matrix(5:10,nrow=2))
str(x6)
```

```
List of 6
 $ : int 5
 $ : int 6
 $ : int 7
 $ : int 8
 $ : int 9
 $ : int 10
```

Note: The ‘inverse’ operation is `unlist()`

```
x7 <- unlist(x6)
str(x7)
```

```
int [1:6] 5 6 7 8 9 10
```

1.2 Accessor operators `[]`, `[[]]`, `$` in R.

1.2.1 General statements

The operator `[[i]]` selects **only one component** (in cases of lists) or **only one element** in case of homogeneous vectors.

The operator `[]` allows to select **one or more components** (in the case of lists) or **one or more elements** in the case of homogeneous vectors.

The `$` operator can **only** be used for **generic/recursive vectors**.

If you use the `$` operator to other objects you will obtain an **error**.

The `$` operator can **only** be followed by a string or a non-computable index.

1.2.2 Homogenous vectors

In praxi, for homogeneous vectors there is hardly any difference between `[[]]` and `[]` **except** that `[[]]` does **NOT** allow to select more than **one** element.

Note: The operator `[[]]` can be used as a tool of defensive programming.

1.2.2.1 Examples

```
a <- seq(from=1,to=30,by=3)
a
```

```
[1] 1 4 7 10 13 16 19 22 25 28
```

```
# Extraction of ONE element
cat(sprintf(" a[[2]] : %d\n", a[[2]]))
```

```
a[[2]] : 4
```

```
cat(sprintf(" a[2] : %d\n", a[2]))
```

```
a[2] : 4
```

```
# Extraction of MORE than 1 element using [[]] => ERROR
a[[c(2,3)]]
```

```
Error in a[[c(2, 3)]]: attempt to select more than one element in vectorIndex
```

but:

```
# Extraction of MORE than 1 element using [] => OK
a[c(2,3)]
```

```
[1] 4 7
```

1.2.3 Heterogeneous vectors (i.e. lists and derived classes)

We stated earlier that the operator `[[]]` allows to select **only one** component.

It also means that this operator selects **the component as is** (matrix, list, function,...).

The operator `[]` allows to select more than **one** component.

Therefore, in order to return potentially heterogeneous components it **always** returns a **list** even if only one component were to be returned.

1.2.3.1 Examples

```
str(x2)
```

```
List of 4
 $ : int [1:10] 1 2 3 4 5 6 7 8 9 10
 $ : chr [1:2] "hello" "world"
 $ : cplx 3+4i
 $ : int [1:2, 1:3] 1 4 2 5 3 6
```

```
# Selection using [[]]
x24 <- x2[[4]]
x24
```

```
      [,1] [,2] [,3]
[1,]    1    2    3
[2,]    4    5    6
```

```
class(x24)
```

```
[1] "matrix" "array"
```

```
typeof(x24)
```

```
[1] "integer"
```

```
length(x24)
```

```
[1] 6
```

```
# Selection using []
x24 <- x2[4]
x24
```

```
[[1]]
      [,1] [,2] [,3]
[1,]     1     2     3
[2,]     4     5     6
```

```
class(x24)
```

```
[1] "list"
```

```
typeof(x24)
```

```
[1] "list"
```

```
length(x24)
```

```
[1] 1
```

```
# Select third el. of the FIRST component
```

```
x13 <- x2[[1]][3]
```

```
x13
```

```
[1] 3
```

which is the same as:

```
v1 <- x2[[1]]
```

```
v1[3]
```

```
[1] 3
```

Heterogeneous vectors are also known as **recursive/generic** vectors, as can be seen in the following example:

```
# A more advanced 'recursive' example
```

```
v <- list(v1=1:4,
          lst1=list(a=3, b=2, c=list(x=5,y=7, v2=seq(from=7,to=12))))
```

```
# Extracting the component as a homogeneous vector
```

```
v[[2]][[3]][[3]]
```

```
[1] 7 8 9 10 11 12
```

```
class(v[[2]][[3]][[3]])
```

```
[1] "integer"
```

```
# Extracting as a list
v[[2]][[3]][3]
```

```
$v2
[1] 7 8 9 10 11 12
```

```
class(v[[2]][[3]][3])
```

```
[1] "list"
```

We can extract the same data using names if available:

```
v$lst1$c$v2
```

```
[1] 7 8 9 10 11 12
```

```
# List of function objects
lstfunc <- list(cube=function(x){x**3},
               quartic=function(x){x**4})
lstfunc$cube(5)
```

```
[1] 125
```

```
lstfunc$quartic(5)
```

```
[1] 625
```

1.2.4 Exercises

- Let's consider the following list:

```
lstex1 <- list(
  list(
    seq(from=4,to=40,by=5),
    "hello world",
    list(
      matrix(100:119,nrow=5),
      "bye",
      c(7,13,17),
      list(451,-1,-17)
    )
  )
)
```

Extract the following data from `mylistex1`:

- the elements 7 13 as a vector.
- the second column of `matrix(100:119,nrow=5)` as a matrix.
- -1 as a scalar.
- -1 as a list.
- **all** numerical values into a vector. (Hint: `unlist()`)

1.3 Modifying lists

- **Removal/deletion** of components:

Set the list element which refers to the component to **NULL**.

The list will be **automatically** re-indexed and its length adjusted.

```
mylst1 <- list(a=1:10, b=seq(1,5), matrix(1:10, nrow=2),  
              "hello", "world", 1:5 )  
str(mylst1)
```

List of 6

```
$ a: int [1:10] 1 2 3 4 5 6 7 8 9 10  
$ b: int [1:5] 1 2 3 4 5  
$   : int [1:2, 1:5] 1 2 3 4 5 6 7 8 9 10  
$   : chr "hello"  
$   : chr "world"  
$   : int [1:5] 1 2 3 4 5
```

```
# Removal of the 5th component  
mylst1[[5]] <- NULL  
str(mylst1)
```

List of 5

```
$ a: int [1:10] 1 2 3 4 5 6 7 8 9 10  
$ b: int [1:5] 1 2 3 4 5  
$   : int [1:2, 1:5] 1 2 3 4 5 6 7 8 9 10  
$   : chr "hello"  
$   : int [1:5] 1 2 3 4 5
```

- **Appending** an object:

Assign the object (obj) to the list element with index `length(lst)+1`

```
# Creation of a list mylst2  
mylst2 <- list( 1:5, 'a' , 'b')  
str(mylst2)
```

List of 3

```
$ : int [1:5] 1 2 3 4 5  
$ : chr "a"  
$ : chr "b"
```

```
# Appending a Boolean vector to the existing list mylst2  
mylst2[[length(mylst2)+1]] <- c(T,F,T)  
str(mylst2)
```

List of 4

```
$ : int [1:5] 1 2 3 4 5  
$ : chr "a"
```



```
$ : chr "b"
$ : logi [1:3] TRUE FALSE TRUE
```

If you set the index to a number which is **larger** than `length(lst) + 1` all the new intermittent list elements will be set to `NULL`.

You can get rid of these additional `NULL` values by **subsequently** deleting them.

```
# Insert a component at an index > length(mylist2)+1
# -> we will get some intermittent NULL values.
mylist2[[7]] <- "value"
str(mylist2)
```

```
List of 7
 $ : int [1:5] 1 2 3 4 5
 $ : chr "a"
 $ : chr "b"
 $ : logi [1:3] TRUE FALSE TRUE
 $ : NULL
 $ : NULL
 $ : chr "value"
```

```
# Delete the NULL values! Start from the end!
mylist2[[6]] <- NULL
mylist2[[5]] <- NULL
str(mylist2)
```

```
List of 5
 $ : int [1:5] 1 2 3 4 5
 $ : chr "a"
 $ : chr "b"
 $ : logi [1:3] TRUE FALSE TRUE
 $ : chr "value"
```

- **Insertion** of new components

Create a new vector containing three parts:

- the ‘left’ sublist
- the new components
- the ‘right’ sublist

```
str(mylist2)
```

```
List of 5
 $ : int [1:5] 1 2 3 4 5
 $ : chr "a"
 $ : chr "b"
 $ : logi [1:3] TRUE FALSE TRUE
 $ : chr "value"
```

```
# Add new component at index 4
newlst2 <- c(mylst2[1:3], "NEW", mylst2[4:length(mylst2)])
str(newlst2)
```

```
List of 6
 $ : int [1:5] 1 2 3 4 5
 $ : chr "a"
 $ : chr "b"
 $ : chr "NEW"
 $ : logi [1:3] TRUE FALSE TRUE
 $ : chr "value"
```

1.3.1 Exercises

- Create the following list:

```
lstex2 <- list(1:10,
               matrix(seq(from=1,to=20), nrow=4),
               5+3i,
               list('a','d','b'),
               "UoU",
               c(T,F,T,T,T),
               "Hello"
              )
```

Perform some operations (deletions, insertions, modifications) on `lstex2` such that `lstex2` takes on the following form:

```
lstex2 <- list( matrix(seq(from=1,to=20), nrow=4),
               "Hello UoU",
               list('a','b','c','d'),
               c(T,F,T,T,T)
              )
```

1.4 Functions: return multiple objects

If a function needs to return **multiple objects** a list **must** be used.

1.4.1 Example

```
func01 <- function(n)
{
  x <- n*(n+1)/2
  y <- cbind(1:n,(1:n)^2)
  return(list('x'=x,'y'=y))
}
n <- 8
res <- func01(n)
```

```
res$x
```

```
[1] 36
```

```
res$y
```

```
      [,1] [,2]
[1,]     1     1
[2,]     2     4
[3,]     3     9
[4,]     4    16
[5,]     5    25
[6,]     6    36
[7,]     7    49
[8,]     8    64
```

1.4.2 Exercises

- Write the function `countOcc(content)` which returns
 - the occurrence of each letter in the string `content`.
 - the occurrence of each non-letter character in the string `content`.

If we use the text of the First Amendment of the Bill of Rights³ as argument for `countOcc`,

```
# Split the text to make it readable
l1 <- "Congress shall make no law respecting an establishment of religion,"
l2 <- "or prohibiting the free exercise thereof;"
l3 <- "or abridging the freedom of speech, or of the press;"
l4 <- "or the right of the people peaceably to assemble,"
l5 <- "and to petition the government for a redress of grievances."
# Glue the chunks {l1,l2,l3,l4,l5} together
firstamend <- paste(l1, l2, l3, l4, l5, sep=" ")
```

we obtain the following output:

```
res <- countOccurrence(firstamend)
res
```

```
$countAlpha
```

```
  a  b  c  d  e  f  g  h  i  k  l  m  n  o  p  r  s  t  v  w  x  y
12  5  6  4 38  9  9 12 14  1  8  5 13 21  8 20 15 17  2  1  1  1
```

```
$countNonAlpha
```

```
  ,  ;  .
44  3  2  1
```

Note/hints:

- We don't distinguish lowercase letters from uppercase letters.
- `strsplit()` : splits a string into its characters.
- `tolower()` : converts letters to their lower case counterparts.
- `unique()` : extracts the unique elements of a vector.

³The text was obtained from https://www.law.cornell.edu/constitution/first_amendment

- R has a built-in vector `letters`.

2 R Dataframes

A data frame is a list with three attributes:

- **names** : component names
- **row.names** : row names
- **class**: **data.frame**

From the above, we can infer that a data frame has the **same** row names for each component (columns). The components of a data frame can be vectors, factors, numerical matrices, lists or other data frames.

In praxi, a **data frame** can be conceptualized as a **generalized (i.e. heterogeneous) matrix/table** where each column has its own type but where each column has the same number of rows.

2.1 Creating a data frame

- use of the **data.frame** function.
- some IO functions generate a data frame when they read a file. e.g. **read.table()**, **read.csv()**.

2.1.1 Examples

```
# Creation of a data frame using the data.frame function:
vec1 <- c("Smith", "Jensen", "McFall", "Johnson",
          "Brown", "Williams", "Wilson", "Roberts")
vec2 <- c(4, 3, 0, 6, 2, 0, 5, 1)
vec3 <- c(100000, 80000, 140000, 120000, 60000, 30000, 170000, 100000)
vec4 <- c("Salt Lake", "Provo", "Park City", "Provo",
          "Logan", "Ogden", "Provo", "Salt Lake")
df1 <- data.frame(family=vec1, nchildren=vec2, income=vec3, location=vec4)
df1
```

```
# A tibble: 8 x 4
  family    nchildren income location
  <chr>      <dbl>   <dbl> <chr>
1 Smith          4 100000 Salt Lake
2 Jensen         3  80000 Provo
3 McFall         0 140000 Park City
4 Johnson        6 120000 Provo
5 Brown          2  60000 Logan
6 Williams       0  30000 Ogden
7 Wilson         5 170000 Provo
8 Roberts        1 100000 Salt Lake
```

```
# Creation of a data frame after reading a data file
df2 <- read.table(file="./data/seaice.txt", header=TRUE)
cat(sprintf("Length(df2) :%d\n", length(df2)))
```

```
Length(df2) :2
```

```
cat(sprintf("Dim. of df2 :\n"))
```

Dim. of df2 :

```
dim(df2)
```

```
[1] 37  2
```

Note:

- Since R4.0.0, the default value for the argument `stringsAsFactors` in the function `data.frame()` has been set to `FALSE`.
- The functions `head()` and `tail()` display the first n , respectively last n lines (default: 6) of a data frame.

```
# Head of data frame df2 with the first 6 lines (default)  
head(df2)
```

```
# A tibble: 6 x 2  
  Year   Ice  
  <int> <dbl>  
1  1979  7.2  
2  1980  7.85  
3  1981  7.25  
4  1982  7.45  
5  1983  7.52  
6  1984  7.17
```

```
# Tail of data frame df2 with the last 4 line  
tail(df2, n=4)
```

```
# A tibble: 4 x 2  
  Year   Ice  
  <int> <dbl>  
1  2012  3.85  
2  2013  5.09  
3  2014  5.11  
4  2015  4.56
```

2.2 Accessing elements of a data frame

As we discussed previously, a data frame is a list with some extra attributes. But, it has also features of a (heterogeneous) matrix.

Therefore, the elements of a data frame can be accessed in **two** different ways:

- using the list syntax
- using the matrix syntax

2.2.1 Examples

- Using the list syntax:

```
# Extract the names of the components (columns)
names(df1)

[1] "family"      "nchildren" "income"     "location"
```

```
# Extract the list's second component as a vector
str(df1[[2]])

num [1:8] 4 3 0 6 2 0 5 1
cat(sprintf("df1[[2]]:%s\n", typeof(df1[[2]])))

df1[[2]]:double
```

```
# Extract the list's second component as a list (dataframe)
df1[2]
```

```
# A tibble: 8 x 1
  nchildren
    <dbl>
1         4
2         3
3         0
4         6
5         2
6         0
7         5
8         1

str(df1[2])

'data.frame':  8 obs. of  1 variable:
 $ nchildren: num  4 3 0 6 2 0 5 1
cat(sprintf("df1[2]:%s\n", typeof(df1[2])))

df1[2]:list
```

```
# Extract a list's component using its name
df1$location
```

```
[1] "Salt Lake" "Provo"      "Park City" "Provo"      "Logan"      "Ogden"
[7] "Provo"      "Salt Lake"

str(df1$location)

chr [1:8] "Salt Lake" "Provo" "Park City" "Provo" "Logan" "Ogden" "Provo" ...
```

- Using the matrix syntax

```
colnames(df1)

[1] "family"      "nchildren" "income"      "location"

rownames(df1)

[1] "1" "2" "3" "4" "5" "6" "7" "8"
```

```
# Extract a few elements
df1[3,3]
```

```
[1] 140000

df1[8,4]

[1] "Salt Lake"
```

```
# Extract a column => vector
df1[, 3]

[1] 100000  80000 140000 120000  60000  30000 170000 100000

df1[, 'income']

[1] 100000  80000 140000 120000  60000  30000 170000 100000
```

```
# Extract a column but preserve a dataframe
df1[, 'income', drop=FALSE]
```

```
# A tibble: 8 x 1
  income
  <dbl>
1 100000
2  80000
3 140000
4 120000
5  60000
6  30000
7 170000
8 100000

typeof(df1[, 'income', drop=FALSE])

[1] "list"
```

```
# Extract everything except fourth column
df1[c(1,4,5), -4]
```

```
# A tibble: 3 x 3
  family nchildren income
```



```

      <chr>      <dbl> <dbl>
1 Smith          4 100000
2 Johnson        6 120000
3 Brown          2  60000

```

```

# Find all the family with an income >=100,000
ind <- which(df1$income >= 100000)
df1[ind,'family']

```

```
[1] "Smith"  "McFall" "Johnson" "Wilson" "Roberts"
```

2.3 Modifying the data frame

- Adding columns and rows:
use the **cbind()** and **rbind()** functions (as in the case of matrices)

```

# Create a new data frame
v1 <- 1:10
v2 <- 11:20
v3 <- 21:30
mydf1 <- data.frame(x=v1, y=v2, z=v3)
mydf1

```

```

# A tibble: 10 x 3
      x     y     z
  <int> <int> <int>
1     1    11    21
2     2    12    22
3     3    13    23
4     4    14    24
5     5    15    25
6     6    16    26
7     7    17    27
8     8    18    28
9     9    19    29
10    10    20    30

```

```

# Add a new column
mydf2 <- cbind(mydf1, w=31:40)
mydf2

```

```

# A tibble: 10 x 4
      x     y     z     w
  <int> <int> <int> <int>
1     1    11    21    31
2     2    12    22    32
3     3    13    23    33
4     4    14    24    34
5     5    15    25    35
6     6    16    26    36

```

7	7	17	27	37
8	8	18	28	38
9	9	19	29	39
10	10	20	30	40

```
# Add a new row
mydf3 <- rbind(mydf2, c(11,21,31,41))
mydf3
```

```
# A tibble: 11 x 4
      x     y     z     w
  <dbl> <dbl> <dbl> <dbl>
1     1     1    11    21    31
2     2     2    12    22    32
3     3     3    13    23    33
4     4     4    14    24    34
5     5     5    15    25    35
6     6     6    16    26    36
7     7     7    17    27    37
8     8     8    18    28    38
9     9     9    19    29    39
10    10    10    20    30    40
11    11    11    21    31    41
```

- Remove columns and rows:

```
# Remove columns
mydf3$z <- NULL      # Syntax 1
mydf3[,2] <- NULL    # Syntax 2
mydf3
```

```
# A tibble: 11 x 2
      x     w
  <dbl> <dbl>
1     1    31
2     2    32
3     3    33
4     4    34
5     5    35
6     6    36
7     7    37
8     8    38
9     9    39
10    10    40
11    11    41
```

```
# Remove row
mydf3 <- mydf3[-c(4,7,8),]
mydf3
```

```
# A tibble: 8 x 2
      x     w
  <dbl> <dbl>
1     1    31
```

2	2	32
3	3	33
4	5	35
5	6	36
6	9	39
7	10	40
8	11	41

2.4 Attach and detach operations

- `attach()`: allows to use a data frame's variables without invoking the name of the data frame, i.e. inserts the data frame on the **search path**.
- `detach()`: undo the `attach()` operation but can also unload a library.
- `search()`: gives an array of the **attached** packages and R objects (usually data frames).

This topic will be discussed in more detail in a future section i.e. (**Environments**).

2.4.1 Examples

- Use of the `attach()` and `search()` functions:

```
# Prior to attaching mydf1
mydf1
```

```
# A tibble: 10 x 3
      x     y     z
  <int> <int> <int>
1     1    11    21
2     2    12    22
3     3    13    23
4     4    14    24
5     5    15    25
6     6    16    26
7     7    17    27
8     8    18    28
9     9    19    29
10    10    20    30
```

```
search()
```

```
[1] ".GlobalEnv"      "package:r2symbols" "package:stats"
[4] "package:graphics" "package:grDevices" "package:utils"
[7] "package:datasets" "package:methods"    "Autoloads"
[10] "package:base"
```

```
x
```

```
Error in eval(expr, envir, enclos): object 'x' not found
```

```
# attach the data frame
attach(mydf1)
search()
```

```
[1] ".GlobalEnv"      "mydf1"           "package:r2symbols"
[4] "package:stats"   "package:graphics" "package:grDevices"
[7] "package:utils"   "package:datasets" "package:methods"
[10] "Autoloads"       "package:base"
```

```
x
```

```
[1] 1 2 3 4 5 6 7 8 9 10
```

- Use of the `detach()` function:

```
# attach the data frame
```

```
detach(mydf1)
```

```
search()
```

```
[1] ".GlobalEnv"      "package:r2symbols" "package:stats"
[4] "package:graphics" "package:grDevices" "package:utils"
[7] "package:datasets" "package:methods"   "Autoloads"
[10] "package:base"
```

```
x
```

```
Error in eval(expr, envir, enclos): object 'x' not found
```

3 Input-Output (IO)

3.1 Functionality in Base R

3.2 Other options:

- library `readr`
 - supports a lot of formats (csv, tcsv, delim, ...)
 - allows column specification
 - faster than Base R's read/write operations
 - uses a `tibble` instead of a `data frame`.
 - for more info: [R for Data Science - Chapter 11.Data import](#)
- library `data.table`
 - very fast IO: optimal for large read (`fread()`) and write (`fwrite()`) operations
 - memory efficient
 - low-level parallelism (use of multiple CPU threads)