Lecture 2: Atomic Data Types/Homogeneous vectors

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Contents

R can be summarized in three principles (John M. Chambers, 2016)

- Everything that exists in R is an **object**.
- Everything that happens in R is a **function** call.
- **Interfaces** to other languages are a part of R.

1 R Objects

- An object in R is (internally) represented as a pair: (**symbol**, **value**).
- A **symbol** is assigned a **value** by the use of an arrow pointing to the left (**<-**).
- There are **less favored** ways:
    - A simple equality sign (**=**).
    - Using the **assign()** function.

1.1 Examples

- Clean up the global environment i.e. remove all objects from the current R environment. Recommended!

```r
rm(list=ls())
ls()
```

```
## character(0)
```

- **preferred** way to assign variables

```r
x <- 5.0
x
```

```
## [1] 5
```

- alternative 1: mainly used to assign default function arguments

```r
y = 5.0
y
```

```
## [1] 5
```

```r
mysamplevariance <- function(x, av=0){

  n <- length(x)
  if(n>1){
      return(1.0/(n-1)*sum((x-av)^2))
  }
  else{
      stop("ERROR:: Dividing by zero (n==1) || (n==0) ")
  }
}

x <- rnorm(10)
mysamplevariance(x)
```

```
## [1] 0.6419987
```

```r
mysamplevariance(x,mean(x))
```

```
## [1] 0.6391902
```

```
var(x)
```

```
## [1] 0.6391902
```

- alternative 2: even less used

```
assign("z", 5.0)
z
```

```
## [1] 5
```

- functions are objects

```
f <- mean
f
```

```
## function (x, ...)
## UseMethod("mean")
## <bytecode: 0x557831848f90>
## <environment: namespace:base>
```

```
val <- f(1:10)
val
```

```
## [1] 5.5
```

"Nothing exists except atoms and empty space; everything else is opinion". (Democritos)

2   Atomic Data Types

2.1   The core/atomic data types

- R has the following 6 **atomic** data types:
    - logical (i.e. boolean)
    - integer
    - double
    - character (i.e. string)
    - complex
    - raw (i.e. byte)

The latter 2 types (i.e. complex and especially raw) are less common.

The **typeof()** function determines the **INTERNAL** storage/type of an R object.

2.1.1   Examples

- boolean/logical values: either **TRUE** or **FALSE**

```
x1 <- TRUE
x1
```

```
## [1] TRUE
```

```
typeof(x1)
```

```
## [1] "logical"
```

- integer values ($\in \mathbb{Z}$):

```
x2 <- 3L
x2
```

```
## [1] 3
```

```
typeof(x2)
```

```
## [1] "integer"
```

- double (precision) values:

```
x3 <- 3.14
x3
```

```
## [1] 3.14
```

```
typeof(x3)
```

```
## [1] "double"
```

- character values/strings

```r
x4 <- "Hello world"
x4
```

```
## [1] "Hello world"
```

```r
typeof(x4)
```

```
## [1] "character"
```

- complex values ($\in \mathbb{C}$):

```r
x5 <- 2.0 + 3i
x5
```

```
## [1] 2+3i
```

```r
typeof(x5)
```

```
## [1] "complex"
```

2.2 Operations on atomic data types

- **logical** operators: **==**, **!=**, **&&**, **||**, **!**
- **numerical** operators: **+**, **-**, *****, **/**, **^**, ****** (same as the caret), but also:
  - integer division: **%/%**
  - modulo operation: **%%**
  - **Note**: matrix multiplication will be performed using **%*%**
- **character/string** manipulation:
  - **nchar()**:
  - **paste()**:
  - **cat()**:
  - **sprintf()**:
  - **substr()**:
  - **strsplit()**:
  - **Note**: Specialized R libraries were developed to manipulate strings e.g. *stringr*
- explicit **cast**/conversion: https://data-flair.training/blogs/r-string-manipulation/
  - **as.{logical, integer, double, complex, character}()**
- explicit **test** of the type of a variable:
  - **is.{logical, integer, double, complex, character}()**

2.2.1 Examples

- Logical operators:

```
x <-3
y <-7
(x<=3) && (y==7)
```

```
## [1] TRUE
```

```
!(y<7)
```

```
## [1] TRUE
```

- Mathematical operations

```
2**4
```

```
## [1] 16
```

```
7%%4
```

```
## [1] 3
```

```
7/4
```

```
## [1] 1.75
```

```
7%/%4
```

```
## [1] 1
```

- String operations

```r
s <- "Hello"
nchar(s)
```

```
## [1] 5
```

```r
news <- paste(s,"World")
news
```

```
## [1] "Hello World"
```

```r
sprintf("My new string:%20s\n", news)
```

```
## [1] "My new string:         Hello World\n"
```

```r
city <- "Witwatersrand"
substr(city,4,8)
```

```
## [1] "water"
```

- Conversion and testing of types

```r
s <- "Hello World"
is.character(s)
```

```
## [1] TRUE
```

```r
s1 <- "-500"
is.character(s1)
```

```
## [1] TRUE
```

```r
s2 <- as.double(s1)
is.character(s2)
```

```
## [1] FALSE
```

```r
is.double(s2)
```

```
## [1] TRUE
```

```r
s3 <- as.complex(s2)
s3
```

```
## [1] -500+0i
```

```r
sqrt(s3)
```

```
## [1] 0+22.36068i
```

3 Atomic vectors

- An **atomic** vector is a data structure containing elements of **only one atomic** data type. Therefore, an atomic vector is **homogeneous**.
- Atomic vectors are stored in a **linear** fashion.
- R does **NOT** have scalars:
    - An atomic vector of **length 1** plays the role of a scalar.
    - Vectors of **length 0** also exist (and they have some use!).
- A **list** is a vector not necessarily of the atomic type.
  A list is also known as a **recursive/generic** vector (*vide infra*).

3.1 Creation of atomic vectors

Atomic vectors can be created in a multiple ways:

- Use of the **vector()** function.
- Use of the **c()** function (**c** stands for concatenate).
- Use of the column operator **:**
- Use of the **seq()** and **rep()** functions.

The length of a vector can be retrieved using the **length()** function.

3.1.1 Examples

- use of the **vector()** function:

```r
x <- vector()  # Empty vector (Default:'logical')
x
```

```
## logical(0)
```

```r
length(x)
```

```
## [1] 0
```

```r
typeof(x)
```

```
## [1] "logical"
```

```r
x <- vector(mode="complex", length=4)
x
```

```
## [1] 0+0i 0+0i 0+0i 0+0i
```

```r
length(x)
```

```
## [1] 4
```

```r
x
```

```
## [1] 0+0i 0+0i 0+0i 0+0i
```

```r
x[1] <- 4
x
```

```
## [1] 4+0i 0+0i 0+0i 0+0i
```

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- use of the **c()** function:

```r
x1 <- c(3, 2, 5.2, 7)
x1
```

```
## [1] 3.0 2.0 5.2 7.0
```

```r
x2 <- c(8, 12, 13)
x2
```

```
## [1]  8 12 13
```

```r
x3 <- c(x2, x1)
x3
```

```
## [1]  8.0 12.0 13.0  3.0  2.0  5.2  7.0
```

```r
x4 <- c(FALSE,TRUE,FALSE)
x4
```

```
## [1] FALSE  TRUE FALSE
```

```r
x5 <- c("Hello", "Salt", "Lake", "City")
x5
```

```
## [1] "Hello" "Salt"  "Lake"  "City"
```

- use of the column operator:

```r
y1 <- 1:10
y1
```

```
##  [1]  1  2  3  4  5  6  7  8  9 10
```

```r
y2 <- 5:-5
y2
```

```
##  [1]  5  4  3  2  1  0 -1 -2 -3 -4 -5
```

```r
y3 <- 2.3:10
y3
```

```
## [1] 2.3 3.3 4.3 5.3 6.3 7.3 8.3 9.3
```

```r
y4 <- 2.0*7:1
y4
```

```
## [1] 14 12 10  8  6  4  2
```

```r
y5 <- 1:7-1
y5
```

```
## [1] 0 1 2 3 4 5 6
```

- **seq()** and **rep()** functions

```r
z1 <- seq(from=1, to=15, by=3)
z1
```

```
## [1]  1  4  7 10 13
```

```
z2 <- seq(from=-2,to=5,length=4)
z2
```

```
## [1] -2.0000000  0.3333333  2.6666667  5.0000000
```

```
z3 <- rep(c(3,2,4), time=2)
z3
```

```
## [1] 3 2 4 3 2 4
```

```
z4 <- rep(c(3,2,4), each=3)
z4
```

```
## [1] 3 3 3 2 2 2 4 4 4
```

```
z5 <- rep(c(1,7), each=2, time=3)
z5
```

```
##  [1] 1 1 7 7 1 1 7 7 1 1 7 7
```

```
length(z5)
```

```
## [1] 12
```

3.2   Operations on vectors: element-wise

- All operations on vectors in R happen **element by element** (cfr. *NumPy*).
- **Vector Recycling**:

  If 2 vectors of **different** lengths are involved in an operation, the **shortest vector** will be repeated until all elements of the longest vector are matched.
  A message will be sent to the stdout.

3.2.1   Examples

```
x <- -3:3
x
```

```
## [1] -3 -2 -1  0  1  2  3
```

```
y <- 1:7
y
```

```
## [1] 1 2 3 4 5 6 7
```

```
xy <- x*y
xy
```

```
## [1] -3 -4 -3  0  5 12 21
```

```
xpy <- x^y
xpy
```

```
## [1]   -3    4   -1    0    1   64 2187
```

```
x <- 0:10
y <- 1:2
length(x)
```

```
## [1] 11
```

```
length(y)
```

```
## [1] 2
```

```
x
```

```
##  [1]  0  1  2  3  4  5  6  7  8  9 10
```

```
y
```

```
## [1] 1 2
```

```
x+y
```

```
## Warning in x + y: longer object length is not a multiple of shorter object
## length
```

```
##  [1]  1  3  3  5  5  7  7  9  9 11 11
```

3.3 Retrieving elements of vectors

- Indexing: starts at **1** (**not 0** like C/C++, Python, Java, ...) see also: Edsger Dijkstra: Why numbering should start at zero
- Use of vector with indices to extract values.
- Advanced features:
    - use of boolean values to extract values.
    - the membership operator: **%in%**.
    - the deselect/omit operator: **-**
    - **which()**: returns the indices for which the condition is true.
    - **any()**/**all()** functions.
        * **any()** : **TRUE** if at least 1 value is true
        * **all()** : **TRUE** if all values are true

3.3.1 Examples

- Use of a simple index:

```
x <- seq(2,100,by=15)
x[4]
```

```
## [1] 47
```

```
x[1]
```

```
## [1] 2
```

- Select several indices at once using vectors:

```r
x
```

```
## [1]  2 17 32 47 62 77 92
```

```r
x[3:5]
```

```
## [1] 32 47 62
```

```r
x[c(1,3,5,7)]
```

```
## [1]  2 32 62 92
```

```r
x[seq(1,7,by=2)]
```

```
## [1]  2 32 62 92
```

- Extraction via booleans (i.e. retain only those values that are equal to **TRUE**):

```r
x
```

```
## [1]  2 17 32 47 62 77 92
```

```r
x>45
```

```
## [1] FALSE FALSE FALSE  TRUE  TRUE  TRUE  TRUE
```

```r
x[x>45]
```

```
## [1] 47 62 77 92
```

- Use of the **%in%** operator:

```r
x
```

```
## [1]  2 17 32 47 62 77 92
```

```r
10 %in% x
```

```
## [1] FALSE
```

```r
62 %in% x
```

```
## [1] TRUE
```

```r
c(32,33,43) %in% x
```

```
## [1]  TRUE FALSE FALSE
```

```r
!(c(32,33,43) %in% x)
```

```
## [1] FALSE  TRUE  TRUE
```

- Negate/filter out the elements with **negative** indices:

```r
x
```

```
## [1]  2 17 32 47 62 77 92
```

```r
x[-c(2,4,6)]
```

```
## [1]  2 32 62 92
```

```r
z <- x[-1] - x[-length(x)]
z
```

```
## [1] 15 15 15 15 15 15
```

- The **which()** function returns **only those indices** of which the condition/expression is **true**.

```r
# Sample 10 numbers from N(0,1)
vecnum <- rnorm(n=10)
vecnum
```

```
##  [1] -0.19371730 -0.69018091 -0.24617161 -1.46502003 -1.12541291  0.23315338
##  [7]  0.87982503  0.27693414  1.54932465 -0.07705855
```

```r
which(vecnum>1.0)
```

```
## [1] 9
```

- Use of the **any()**/**all()** functions.

```r
y <- seq(0,100,by=10)
x
```

```
## [1]  2 17 32 47 62 77 92
```

```r
y
```

```
##  [1]   0  10  20  30  40  50  60  70  80  90 100
```

```r
any(x<y)
```

```
## Warning in x < y: longer object length is not a multiple of shorter object
## length
```

```
## [1] TRUE
```

```r
all(x[6:7]>y[2:3])
```

```
## [1] TRUE
```

3.4 Hash tables

A **hash table** is a data structure which implements an associative array or dictionary. It is an abstract data which maps data to keys.

- There are several ways to create one:
    - Map names to an existing vector
    - Add names when creating the vector
- To remove the map, map the names to NULL

3.4.1 Examples

- Creation of 2 independent vectors

```r
capitals <- c("Albany", "Providence", "Hartford", "Boston", "Montpelier", "Concord", "Augusta")
states <- c("NY", "RI", "CT", "MA", "VT", "NH", "ME")
capitals
```

```
## [1] "Albany"     "Providence" "Hartford"   "Boston"     "Montpelier"
## [6] "Concord"    "Augusta"
```

```r
states
```

```
## [1] "NY" "RI" "CT" "MA" "VT" "NH" "ME"
```

```r
capitals[3]
```

```
## [1] "Hartford"
```

- Create the hashtable/dictionary

```r
# Method 1
names(capitals) <- states
capitals
```

```
##           NY           RI           CT           MA           VT           NH
##     "Albany" "Providence"   "Hartford"     "Boston" "Montpelier"   "Concord"
##           ME
##    "Augusta"
```

```r
capitals["MA"]
```

```
##        MA
## "Boston"
```

```r
names(capitals)
```

```
## [1] "NY" "RI" "CT" "MA" "VT" "NH" "ME"
```

```r
# Method 2
phonecode <- c("801"="SLC", "206"="Seattle", "307"="Wyoming")
phonecode
```

```
##       801       206       307
##     "SLC" "Seattle" "Wyoming"
```

```r
phonecode["801"]
```

```
##   801
## "SLC"
```

- Dissociate the 2 vectors

```
names(capitals) <- NULL
capitals
```

```
## [1] "Albany"     "Providence" "Hartford"   "Boston"     "Montpelier"
## [6] "Concord"    "Augusta"
```

3.5   NA (Not Available values)

- **NA**: stands for 'Not Available'/Missing values
- has length of 1.
- **is.na()**: test all elements of a vector for NA values.
- some functions e.g. **mean()** return NA when an instance of NA is present.

3.5.1   Examples

- Check of the NA availability

```
x <- c(NA, 1, 2, NA)
is.na(x)
```

```
## [1]  TRUE FALSE FALSE  TRUE
```

- Functions on a vector containing NA

```
mean(x)
```

```
## [1] NA
```

```
mean(x, na.rm=TRUE)
```

```
## [1] 1.5
```

3.6   Alia

Still to be developed!

- boolean: Vector operators vs. unique value
- && vs. &.
- || vs. |.
- xor()

```
"It is my experience that proofs involving matrices can be
shortened by 50% if one throws the matrices out" (Emil Artin)
```

4 Matrices & Arrays

Matrices and arrays are **homogeneous atomic vectors** with
an **extra** attribute: dimension

By default, the elements are stored in a **column-major** fashion. (cfr. **Fortran**).
However, we can store the elements in **row-major** order (cfr. **C**) as well.

4.1 Creation of matrices

Matrices can be created in different ways:

- use of the **matrix()** function
- use of **rbind()/cbind()**
- set the **attributes()** of a vector
- special functions like e.g. **diag()**

4.1.1 Examples

- use of the **matrix()** function:

The **matrix()** function creates a matrix based on a vector.
By default, the elements are stored in a **column-major** fashion.

The use of the flag `byrow=TRUE` will store the data in a **row-major** fashion.

```
A <- matrix(data=1:10, nrow=2)    # Column-major (like Fortran)
A
```

```
##      [,1] [,2] [,3] [,4] [,5]
## [1,]    1    3    5    7    9
## [2,]    2    4    6    8   10
```

```
B <- matrix(data=c(2,3,893,0.17), nrow=2, ncol=2)
B
```

```
##      [,1]   [,2]
## [1,]    2 893.00
## [2,]    3   0.17
```

```
C <- matrix(data=1:10, nrow=2, byrow=TRUE)    # Row-major (like C, C++)
C
```

```
##      [,1] [,2] [,3] [,4] [,5]
## [1,]    1    2    3    4    5
## [2,]    6    7    8    9   10
```

- use of the **rbind()/cbind()** functions:

- **rbind()**: Bind several vectors (as rows) into a matrix.
- **cbind()**: Bind several vectors (as columns) into a matrix.

```r
A <- rbind(1:10,11:20)
A
```

```
##      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
## [1,]    1    2    3    4    5    6    7    8    9    10
## [2,]   11   12   13   14   15   16   17   18   19    20
```

```r
typeof(A)
```

```
## [1] "integer"
```

```r
class(A)
```

```
## [1] "matrix" "array"
```

```r
B <- cbind(1:5,6:10,11:15)
B
```

```
##      [,1] [,2] [,3]
## [1,]    1    6   11
## [2,]    2    7   12
## [3,]    3    8   13
## [4,]    4    9   14
## [5,]    5   10   15
```

```r
class(B)
```

```
## [1] "matrix" "array"
```

- modifying the **dim** attribute.

The **fundamental** difference between an R vector and matrix is the presence (in the case of matrices) of a non NULL **dim** attribute.

We change easily convert a vector into a matrix by setting the dimensions of the vector:

- through the **dim()** function.
- through the **attr()** function.

The inverse can be done as well by setting the **dim** attribute of matrix to NULL.

4.1.2 Examples

```r
A <- 1:10
typeof(A)
```

```
## [1] "integer"
```

```r
class(A)
```

```
## [1] "integer"
```

```r
dim(A)
```

```
## NULL
```

```
# Matrix
B <- matrix(1:10,nrow=2,ncol=5,byrow=TRUE)
typeof(B)
```

```
## [1] "integer"
```

```
class(B)
```

```
## [1] "matrix" "array"
```

```
dim(B)
```

```
## [1] 2 5
```

```
# Vector
A <- 1:10
A
```

```
##  [1]  1  2  3  4  5  6  7  8  9 10
```

```
dim(A)
```

```
## NULL
```

```
typeof(A)
```

```
## [1] "integer"
```

```
class(A)
```

```
## [1] "integer"
```

```
# OPTION I: Using the dim function transform a vector into a matrix
dim(A) <- c(2,5)
A
```

```
##      [,1] [,2] [,3] [,4] [,5]
## [1,]    1    3    5    7    9
## [2,]    2    4    6    8   10
```

```
dim(A)
```

```
## [1] 2 5
```

```
typeof(A)
```

```
## [1] "integer"
```

```
class(A)
```

```
## [1] "matrix" "array"
```

```
# Converting the matrix back to a vector
dim(A) <- NULL
dim(A)
```

```
## NULL
```

```
typeof(A)
```

```
## [1] "integer"
```

```
class(A)
```

```
## [1] "integer"
```

```
# Option II: More general way
# Convert vector into a matrix
A <- 1:8
A
```

```
## [1] 1 2 3 4 5 6 7 8
```

```
class(A)
```

```
## [1] "integer"
```

```
attr(A,'dim') <- c(2,4)
A
```

```
##      [,1] [,2] [,3] [,4]
## [1,]    1    3    5    7
## [2,]    2    4    6    8
```

```
class(A)
```

```
## [1] "matrix" "array"
```

```
# Convert matrix into a vector.
attr(A, 'dim') <- NULL
A
```

```
## [1] 1 2 3 4 5 6 7 8
```

```
class(A)
```

```
## [1] "integer"
```

4.2 Operations on matrices

- Operations like ***,/, +** happpen element-wise.
- There are also more specialized functions:
  - the mean over rows and columns (**rowMeans()**, **colMeans()**)
  - linear algebra functions (**%*%**, **t()**, ...)

4.2.1 Examples

- Operations (by **default: element-by-element**):

```
A <- matrix(1:10, nrow=2)
B <- matrix( seq(10, 100, by=10), nrow=2)
A
```

```
##      [,1] [,2] [,3] [,4] [,5]
## [1,]    1    3    5    7    9
## [2,]    2    4    6    8   10
B
```

```
##      [,1] [,2] [,3] [,4] [,5]
## [1,]   10   30   50   70   90
## [2,]   20   40   60   80  100
```

```
A*B
```

```
##      [,1] [,2] [,3] [,4] [,5]
## [1,]   10   90  250  490  810
## [2,]   40  160  360  640 1000
```

```
C <- matrix(rep(2,10), nrow=2)
C**A
```

```
##      [,1] [,2] [,3] [,4] [,5]
## [1,]    2    8   32  128  512
## [2,]    4   16   64  256 1024
```

- Calculate **row and column means** :

```
# Means of rows and columns
A
```

```
##      [,1] [,2] [,3] [,4] [,5]
## [1,]    1    3    5    7    9
## [2,]    2    4    6    8   10
```

```
rowMeans(A)
```

```
## [1] 5 6
```

```
colMeans(A)
```

```
## [1] 1.5 3.5 5.5 7.5 9.5
```

- **Matrix multiplication** (%*%) :

```
A <- matrix(1:6, nrow=2)
A
```

```
##      [,1] [,2] [,3]
## [1,]    1    3    5
## [2,]    2    4    6
```

```
B <- matrix(seq(10,120,by=10), nrow=3)
B
```

```
##      [,1] [,2] [,3] [,4]
## [1,]   10   40   70  100
## [2,]   20   50   80  110
## [3,]   30   60   90  120
```

```
C <- A%*%B
C
```

```
##      [,1] [,2] [,3] [,4]
## [1,]  220  490  760 1030
## [2,]  280  640 1000 1360
```

```
dim(C)
```

```
## [1] 2 4
```

- **Linear algebra** routines

Some of the more common ones in R:

- **solve()** : **invert** a square matrix

- **diag()**

    - **extracts** the diagonal of a matrix when a matrix is provided.

    - **creates** a diagonal matrix when a vector is provided.

- **eigen()** : calculates the **eigenvalues** and **eigenvectors** of a matrix

- **det()** : calculates the **determinant** of a matrix.

- **t()**: calculates the **transpose**[1] of a matrix.

```
# Invert matrix A
A <- matrix(c(1, 3, 2, 4), ncol = 2, byrow = T)
Ainv <- solve(A)
Ainv %*% A
```

```
##      [,1] [,2]
## [1,]    1    0
## [2,]    0    1
```

```
# Create a diagonal matrix
C <- diag(c(1,4,7))
C
```

```
##      [,1] [,2] [,3]
## [1,]    1    0    0
## [2,]    0    4    0
## [3,]    0    0    7
```

```
# Extract the diagonal elements
D <- matrix(1:8,nrow=4)
D
```

---

[1]Can also be used for dataframes (see later)

```
##      [,1] [,2]
## [1,]    1    5
## [2,]    2    6
## [3,]    3    7
## [4,]    4    8
```

```
diag(D)
```

```
## [1] 1 6
```

```
# Calculate eigenvalues and eigenvectors of A
r <- eigen(A)
r
```

```
## eigen() decomposition
## $values
## [1]  5.3722813 -0.3722813
##
## $vectors
##            [,1]       [,2]
## [1,] -0.5657675 -0.9093767
## [2,] -0.8245648  0.4159736
```

```
# Eigenvalues
r$values
```

```
## [1]  5.3722813 -0.3722813
```

```
# Matrix with eigenvectors
r$vectors
```

```
##            [,1]       [,2]
## [1,] -0.5657675 -0.9093767
## [2,] -0.8245648  0.4159736
```

```
# Diagonal Matrix (Similarity Transformation)
solve(r$vectors) %*% A %*% r$vectors
```

```
##               [,1]       [,2]
## [1,]  5.372281e+00  0.0000000
## [2,] -3.330669e-16 -0.3722813
```

Note that under the hood R calls BLAS and LAPACK.

```
# Find the version used of BLAS and LAPACK
La_library()
```

```
## [1] "/usr/lib/x86_64-linux-gnu/lapack/liblapack.so.3.7.1"
```

```
extSoftVersion()["BLAS"]
```

```
##                                                     BLAS
## "/usr/lib/x86_64-linux-gnu/blas/libblas.so.3.7.1"
```

4.3   Hash Tables

5 Other types

- Attributes
- Special types:
  - Factors
  - Date
  - Time
- NA, NaN, NULL

Other topics on Data structures

- List

- Dataframe & Tibble

- IO (read.csv, read.file)

- Names

- Subsetting, [[]] vs. []

Conditionals & Loops

- if, else, else if switch and elseif
- for
- while
- repeat
- return()

Environments

- search(), attach, detach
- library

Functions

- lexical scoping
- simple functions
- args(), formals()
- default arg, . . .
- lazy evaluation
- closure
- anonymous functions
- make your own operators
- loop functions: {l,s,m}apply, split

Capita selecta

- profiling, debugging