

Let's call N the real number of critical issues for a codebase of L lines, A the number of auditors reviewing the code and K the number of issues they've found.

Let's assume:

- Every auditor has a chance p of missing each issue (said differently a probability $1 - p$ of finding it). So, for each issue, the probability that it is found by at least one person is $(1 - p^A)$.
- On the builder side, let's assume every line there is a probability q of introducing a new vulnerability. To estimate this we take $q = k/L$, that is to say, the ratio of the found issues over the total number of lines.

We have:

$$P(N = n) = \binom{n}{L} q^n (1 - q)^{L-n}$$

$$P(K = k | N = n) = \binom{k}{n} (1 - p^A)^k p^{A(n-k)}$$

$$\begin{aligned} P(K = k) &= \sum_{i \geq k} P(K = k | N = i) P(N = i) \\ &= \sum_{i \geq k} \binom{k}{i} (1 - p^A)^k p^{A(i-k)} P(N = i) \\ &= \sum_{i \geq k} \binom{k}{i} (1 - p^A)^k p^{A(i-k)} \binom{i}{L} q^i (1 - q)^{L-i} \end{aligned}$$

So the probability that an issue was missed if we observe $K = k$ (an audit found k issues), and taking $q = \frac{K}{L}$ is:

$$\begin{aligned} P(N > k | K = k) &= 1 - P(N = k | K = k) \\ &= 1 - \frac{P(K = k | N = k) P(N = k)}{P(K = k)} \\ &= 1 - \frac{\binom{k}{k} (1 - p^A)^k \binom{k}{L} \left(\frac{k}{L}\right)^k \left(\frac{L-k}{L}\right)^{L-k}}{\sum_{i \geq k} \binom{k}{i} p^{A(i-k)} (1 - p^A)^k \binom{i}{L} \left(\frac{k}{L}\right)^i \left(\frac{L-k}{L}\right)^{L-i}} \\ &= 1 - \frac{\binom{k}{L} \left(\frac{k}{L}\right)^k \left(\frac{L-k}{L}\right)^{L-k}}{\sum_{i \geq k} \binom{k}{i} \binom{i}{L} p^{A(i-k)} \left(\frac{k}{L}\right)^i \left(\frac{L-k}{L}\right)^{L-i}} \end{aligned}$$