Piero Macaluso s252894

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Machine Learning and Artificial Intelligence 2018/2019 Prof. Barbara Caputo

#### 1 Linear SVM

In the first part of this homework I trained, validated and finally tested a Linear SVM, using the C with the highest accuracy in validation. The essential part of the code is algorithm 1.

Algorithm 1: Searching the best value of C in Linear SVM

```
acc = np.empty(7)
78
        c_i = 1e-3
79
        c_best = 1e-3
80
        a_best = 0
81
        i = 1
       xx, yy = make_meshgrid(x[:, 0], x[:, 1])
83
       while c_i \le 1e3:
84
           clf = svm.LinearSVC(C=c_i, random_state=r_state)
85
           acc[i - 1] = clf.fit(x_train, y_train).score(x_val, y_val) * 100
86
           if acc[i - 1] > a_best:
87
               c_best = c_i
88
               a_best = acc[i - 1]
89
           ax = fig.add\_subplot(4, 2, i)
           plot_data(ax, x_train, y_train, xx, yy, clf)
91
           ax.set_xlim(xx.min(), xx.max())
92
           ax.set_ylim(yy.min(), yy.max())
93
           ax.set_xlabel('Sepal length')
           ax.set_ylabel('Sepal width')
95
           ax.set_xticks(())
96
           ax.set_yticks(())
97
98
           ax.legend()
           ax.set_title('C=\frac{2.2E}{A}=\frac{2.1f}{}' % (c_i, acc[i - 1]))
99
           c_i = c_i * 10
100
           i = i + 1
101
       fig.suptitle("Linear SVM - C tuning - C_best = %2.2E A_best = %2.1f%%" % (c_best,
            a_best), fontsize=14,
                    fontweight='bold')
104
```

As we can see from the plots figs. 1 and 2 on page 3 and on page 4, the best accuracy found on validation set was 73.33%, with C equal to 1e-1. I noticed that boundaries became more and more precise on the training set with the increment of C.

C is the hyper parameter of SVM that represents the penalty for misclassifying a data point, so it describe how much we want to avoid misclassification during the training. When C is large, the optimization will choose a smaller-margin hyperplane, because the classifier is heavily penalized for misclassified data. The larger is C, the better the classification on training set will be. On the contrary, when C is small, the optimizer will use a larger-margin separating hyperplane, causing the misclassification of more training data points.

After this training, I tests the data on the test set obtaining a greater accuracy, it goes very well with an accuracy of 88.89% as we can see in fig. 3 on page 4. I tried to repeat the code a lot of times using a different random\_state variable, obtaining validation values from 60% to 90%. This may be due to the initial state of the algorithm of SVM or the splitting of the data

in training, validation and test sets: maybe one time the is more overfitting on the training data, next time less. We may conclude that this type of validation is not stable and may be influenced by overfitting (see section 4 on page 10).

## Linear SVM - C tuning - C\_best = 1.00E+01 A\_best = 73.3%

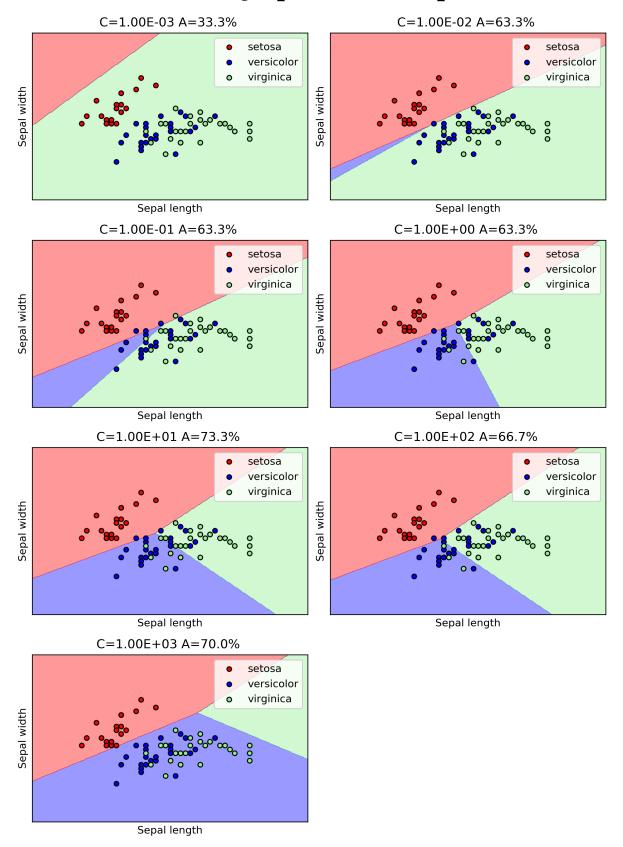


Figure 1: Decision Boundaries changing C in Linear SVM on Training set

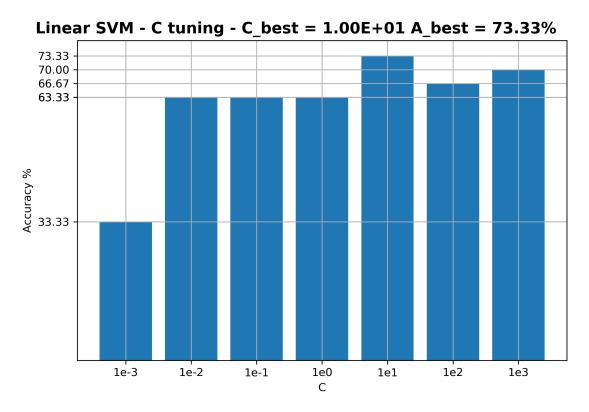


Figure 2: Accuracy changing C in Linear SVM

# Linear SVM with validation accuracy of 73.33% $_{\text{C}=1.00\text{E}+01}$ $\text{A}{=}88.89\%$

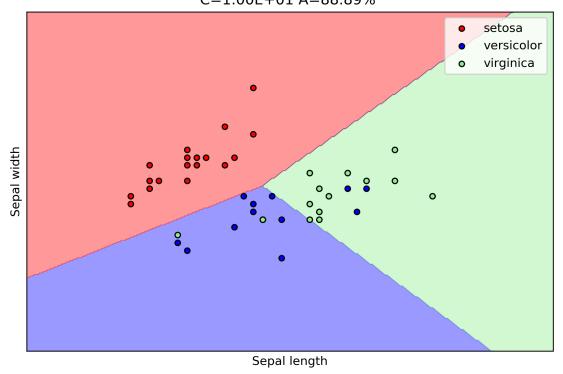


Figure 3: Results on the test set

### 2 RBF Kernel

In the second part of this homework, I used SVM with Gaussian RBF kernel eq. (1).

$$exp(-\gamma \mid\mid x - x'\mid\mid^2) \tag{1}$$

This time I had to find the best pair of C (explained in section 1 on page 1) and  $\gamma$  (Gamma).

**Gamma parameter** can be explained as the *spread* of the kernel and therefore the decision region. When gamma is **low**, the *curve* of the decision boundary is very low and thus the decision region is very broad. When gamma is **high**, the *curve* of the decision boundary is high, which creates islands of decision-boundaries around data points.

Firstly, I repeated the steps of the previous section in order to find the best accuracy modifying C and using the Gamma calculated by sklearn under the hood as we can see in algorithm 2. This time the boundaries are **not as linear as** the ones of Linear SVM because of the introduction of the Gaussian RBF kernel. Thanks to this approach, I found a better training accuracy (76.67%) compared to the Linear SVM one, and a test accuracy near to the validation one (75.56%) with C = 1e-1 as we can see in figs. 4 to 6 on pages 6–7.

I used the the code of algorithm 1 on page 1 changing the classifier on line 88 with the one in algorithm 2 .

#### Algorithm 2: RBF Kernel SVM Classifier

```
clf = svm.SVC(kernel='rbf', C=c_i, random_state=r_state)
```

Finally, I performed the grid search of the best pair of C and Gamma with algorithm 3. This time I obtained an high accuracy in validation (80.00%) and also on the test set (86.67%) with a C = 1e0 and  $\gamma = 1e-1$  as we can see in figs. 7 and 8 on page 8.

Algorithm 3: Searching the best value of C and Gamma in RBF Kernel SVM

```
# Grid Search of C and Gamma
211
212
        c = np.array([1e-3, 1e-2, 1e-1, 1e0, 1e1, 1e2, 1e3])
        gamma = np.array(
213
            [1e-9, 1e-8, 1e-7, 1e-6, 1e-5, 1e-4, 1e-3, 1e-2, 1e-1, 1e0, 1e1, 1e2, 1e3,
                1e4, 1e5, 1e6, 1e7, 1e8, 1e9])
        c_best = c.min()
215
        g_best = gamma.min()
216
        a_best = 0
217
       res = np.zeros([c.shape[0], gamma.shape[0]])
218
        for c_i, i in zip(c, range(0, c.shape[0])):
219
           for gamma_i, j in zip(gamma, range(0, gamma.shape[0])):
220
               clf = svm.SVC(kernel='rbf', gamma=gamma_i, C=c_i, random_state=r_state)
               res[i, j] = clf.fit(x_train, y_train).score(x_val, y_val) * 100
               if res[i, j] > a_best:
223
                   c_best = c_i
224
                   g_best = gamma_i
225
                   a_best = res[i, j]
```

I repeated this code a lot of times and, even then, I found a great variation of results in validation and test scores (see section 4 on page 10).

## RBF Kernel - C/G tuning - C\_best=1.00E-01 A\_best=76.67%

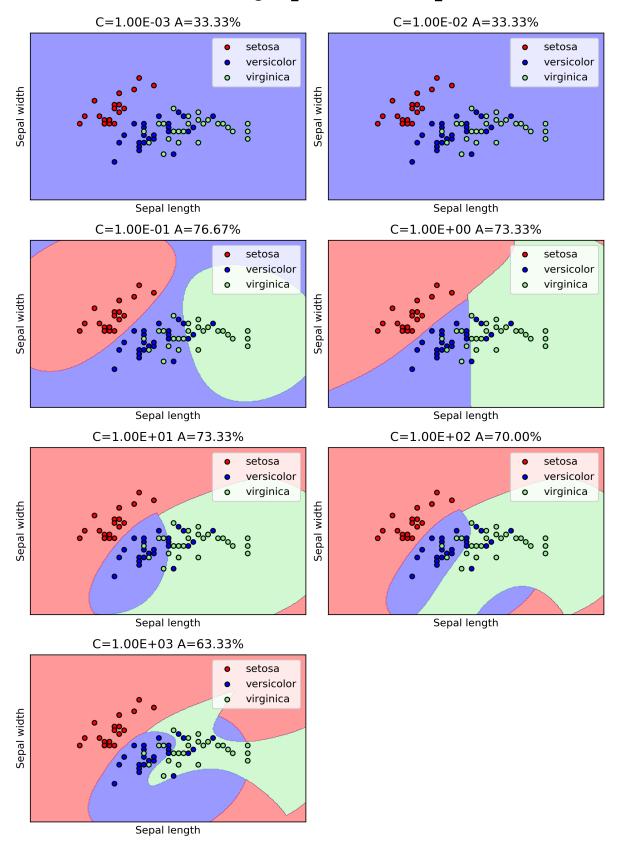


Figure 4: Decision Boundaries changing C in RBF Kernel SVM on Training set

## RBF Kernel - C/G tuning - C\_best=1.00E-01 A\_best=76.67%

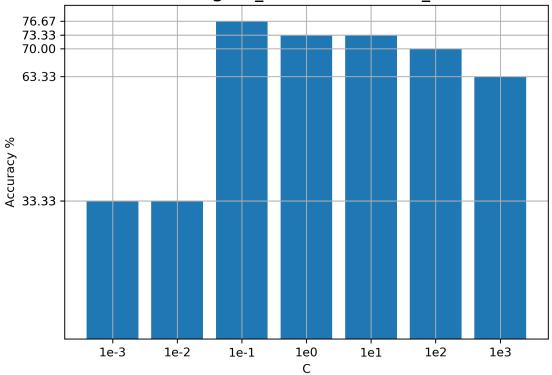


Figure 5: Accuracy changing C in RBF Kernel SVM

# RBF Kernel with validation accuracy of 76.67% $_{\text{C}=1.00\text{E-}01}$ $_{\text{A}=75.56\%}$

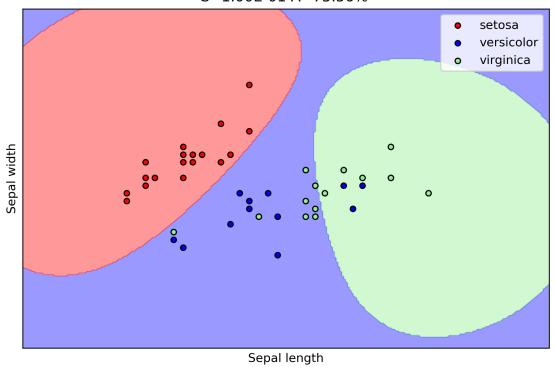


Figure 6: Results on the test set

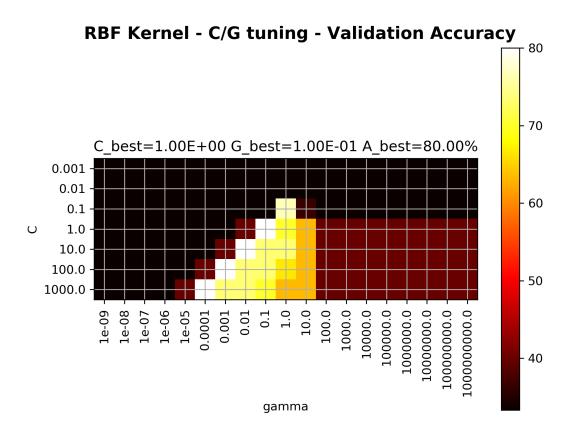


Figure 7: Grid Search of C and Gamma in RBF Kernel SVM on Training set

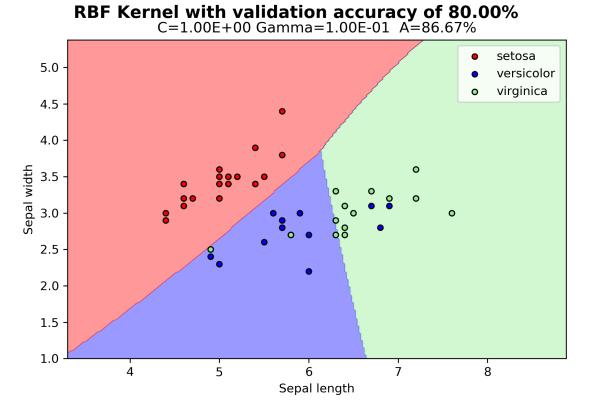


Figure 8: Results on the test set

### 3 K-Fold

In the last part of the homework, I merged training and validation sets and I performed a **k-fold** crossvalidation with k = 5 using algorithm 4.

Algorithm 4: Validation using k-fold with k = 5

```
# 5-fold validation
264
        c_best = c.min()
265
        g_best = gamma.min()
        a_best = 0
267
        k = 5
        kf = KFold(n_splits=k, shuffle=True, random_state=r_state)
269
        scores = np.zeros([len(gamma), len(c)])
        for i, gamma_i in enumerate(gamma):
271
           for j, c_i in enumerate(c):
               temp = np.zeros(kf.n_splits)
273
               for k_i, (train_index, test_index) in enumerate(kf.split(x_train)):
                   clf = svm.SVC(kernel='rbf', gamma=gamma_i, C=c_i)
                   clf.fit(x_train[train_index], y_train[train_index])
                   temp[k_i] = clf.score(x_train[test_index], y_train[test_index]) * 100
277
               acc_av = np.average(temp)
278
               if acc_av > a_best:
279
                   c_best = c_i
280
                   g_best = gamma_i
281
                   a_best = acc_av
282
```

I obtained an in validation equal to 76.19%, but a test accuracy 82.22% with a C = 1e2 and  $\gamma = 1e-3$  as we can see in fig. 9.

The final score is good, although it is lower than some of the final scores found in previous sections. I tried to run the code multiple times changing random\_state and I have always found values from 75% to 85% (see section 4 on the next page).

# RBF Kernel K-Fold with validation accuracy of 76.19% C=1.00E+02 Gamma=1.00E-03 A=82.22%

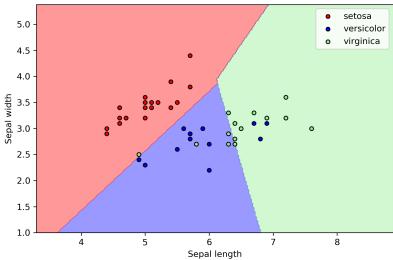


Figure 9: Results on the test set

### 4 Final Comments

Because of the continuous variation of results for different random\_state, I decided to implement a simple Python script (testing.py) to calculate the average of the results of the three main type of parameter tuning in order to find something remarkable. The result obtained over 200 repetitions can be found in tables 1 and 2.

Table 1: Accuracy distribution

<b>Accuracy (%)</b> (200 rep.)	AVG Validation	STD Validation	AVG Test	STD Test
Linear SVM	$\approx 80$	pprox 7	$\approx 73$	$\approx 7$
RBF Kernel SVM	$\approx 82$	$\approx 6$	$\approx 76$	$\approx 6$
RBF Kernel SVM (k-fold)	$\approx 81$	$\approx 2$	$\approx 78$	$\approx 5$

Table 2: Min and Max

<b>Accuracy</b> (%) (200 rep.)	MIN Validation	MAX Validation	MIN Test	MAX Test
Linear SVM	$\approx 60$	$\approx 95$	$\approx 50$	$\approx 95$
RBF Kernel SVM	$\approx 60$	$\approx 95$	$\approx 60$	$\approx 95$
RBF Kernel SVM (k-fold)	$\approx 75$	$\approx 87$	$\approx 60$	$\approx 95$

Now we have something that could be noteworthy: the first two type of parameter tuning algorithms have a larger variance than the last one. Therefore, the validation averages are almost the same, but the test ones no. Indeed, we can find an higher test accuracy on the third type.

From these results, we can conclude that the validation done with k-fold crossvalidation is more stable than the other ones and it is useful to avoid overfitting problem.

#### 5 Code Execution

### 5.1 Requirements

- Python 3
- All dependencies in requirements.txt.
  - \$ pip install -r requirements.txt to install them

#### 5.2 Usage

• \$ python main.py
Execute the code

#### 5.3 Reproducibility

In order to reproduce the same data for this experiment you have to change the global variable r\_state (line) from None to 252894 which is my badge number.

# Attachments

- Source Code:
  - main.py
  - requirements.txt
  - testing.py