

Modelling for Combinatorial Optimisation (1DL451) and Constraint Programming (1DL442)

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MiniZinc Exercises (optional)

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Comprehensions are a crucial part of efficient MiniZinc models. Here are exercises to help you get started with writing complex comprehensions in the assignments and project. For a more basic introduction to comprehensions, see Section 2.2.1 of the MiniZinc Handbook at <https://www.minizinc.org/doc-latest/en/modelling2.html>. Skeleton code for the exercises is at <https://pierre-flener.github.io/courses/COCP/assignments/exercises>.

1 Repeating Numbers

Consider an array A of m parameters, and a parameter n . Define, using an array comprehension, the array $B = [A[1], A[1], \dots, A[2], A[2], \dots, A[m], A[m], \dots]$ of length $m \cdot n$ containing n repetitions of each element of A .

Example: $A = [1, 2, 1]$ and $n = 2$ should give $B = [1, 1, 2, 2, 1, 1]$.

Listing 1: Skeleton code for Ex1.mzn

```
int: n = 2;
int: m = 3;
array[1..m] of int: A = [1, 2, 1];

array[1..m*n] of int: B = [... | ...];
```

2 Repeating Numbers Again

Consider an array A of m parameters, and a parameter n . Define, using an array comprehension, the array $B = [A[1], A[2], \dots, A[m], A[1], A[2], \dots, A[m], \dots]$ of length $m \cdot n$ consisting of n concatenations of A .

Example: $A = [1, 2, 3]$ and $n = 3$ should give $B = [1, 2, 3, 1, 2, 3, 1, 2, 3]$.

Listing 2: Skeleton code for Ex2.mzn

```
int: n = 3;
int: m = 3;
array[1..m] of int: A = [1, 2, 3];

array[1..m*n] of int: B = [ ... | ... ];
```

3 Counting

Consider a 2D array A of n rows and m columns of parameters. Define, using an array comprehension, the array B of length n where at each index i in B is the number of occurrences of the value 5 in row i of A.

Example: A = [|1,2,3|4,5,6|7,8,9|5,5,5|] should give B = [0,1,0,3].

Listing 3: Skeleton code for Ex3.mzn

```
int: n = 4;
int: m = 3;
array[1..n, 1..m] of int: A = [|1,2,3|4,5,6|7,8,9|5,5,5|];

array[1..n] of int: B = [ ... | ... ];
```

4 Expression on Variables

Consider an array X of n variables in the domain 1..n*n. Define, using an array comprehension, the array Y of variables denoting the absolute differences in each unordered pair of separate variables in X. Define also the index set of Y (or use the keyword `int`). By constraining both X and Y to each have all-different values, we get a model for the Golomb ruler (see <https://mathworld.wolfram.com/GolombRuler.html>).

Example: If X = [8,4,2,1], then Y should contain the values 4,6,7,2,3,1, in some order.

Listing 4: Skeleton code for Ex4.mzn

```
include "globals.mzn";

int: n = 4;

array[1..n] of var 1..n*n: X;
array[...] of var int: Y = [ ... | ... ];

constraint all_different(X);
constraint all_different(Y);
```

5 Sorting

Consider two arrays A and B of n parameters. Define, using an array comprehension, the array C containing the elements of B but sorted as if it was A. That is B[i] occurs before B[j] in C if and only if A[i] ≤ A[j]. **Hint:** Use `arg_sort` in the generator of the comprehension.

Example: A = [2,1,3] and B = [9,7,5] should give C = [7,9,5].

Listing 5: Skeleton code for Ex5.mzn

```
include "globals.mzn";

int: n = 3;
array[1..n] of int: A = [2,1,3];
array[1..n] of int: B = [9,7,5];

array[1..n] of int: C = [ ... | ... ];
```

6 2D Array

Consider an integer parameter n . Define, using an array comprehension, the 2D array A with 3 columns, the rows being $[f, s, f \cdot n + s]$ for each f and s with $1 \leq f < s \leq n$.

Hint: Use `array2d` in order to cast a generated 1D array into a 2D one.

Example: $n=4$ should give `[|1, 2, 6|1, 3, 7|1, 4, 8|2, 3, 11|2, 4, 12|3, 4, 16|]`.

Listing 6: Skeleton code for Ex6.mzn

```
int: n = 4;  
  
array[...,...] of ...: A = ...;
```