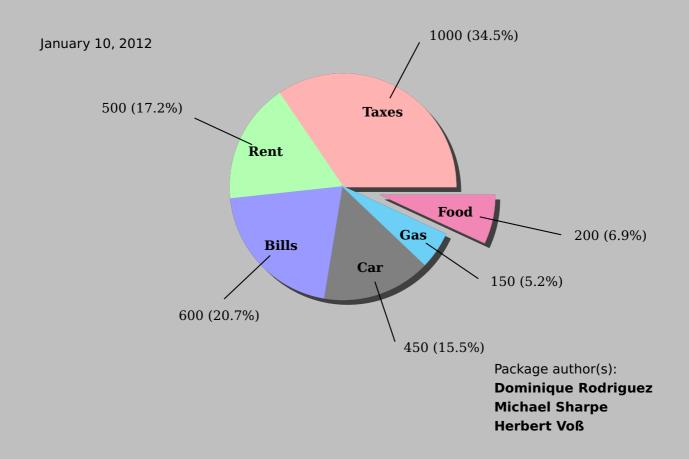
# **PSTricks**

### pstricks-add additionals Macros for pstricks v.3.57



This version of pstricks-add needs pstricks.tex version >1.04 from June 2004, otherwise the additional macros may not work as expected. The ellipsis material and the option asolid (renamed to eofill) are now part of the new pstricks.tex package, available on CTAN. pstricks-add will for ever be an experimental and dynamical package, try it at your own risk.

- It is important to load pstricks-add as the **last** PSTricks related package, otherwise a lot of the macros won't work in the expected way.
- pstricks-add uses the extended version of the keyval package. So be sure that you have installed pst-xkey which is part of the xkeyval-package, and that all packages that use the old keyval interface are loaded **before** the xkeyval.[1]
- the option tickstyle from pst-plot is no longer supported; use ticksize instead.
- the option xyLabel is no longer supported; use the option labelFontSize instead.
- if pstricks-add is loaded together with the package pst-func then InsideArrow of the \psbezier macro doesn't work!

Thanks to: Hendri Adriaens; Stefano Baroni; Martin Chicoine; Gerry Coombes; Ulrich Dirr; Christophe Fourey; Hubert Gäßlein; Jürgen Gilg; Denis Girou; Pablo Gonzáles; Peter Hutnick; Christophe Jorssen; Uwe Kern; Manuel Luque; Jens-Uwe Morawski; Tobias Nähring; Rolf Niepraschk; Alan Ristow; Christine Römer; Arnaud Schmittbuhl; John Smith; Timothy Van Zandt

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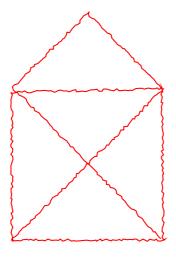
#### 1. \psGetSlope and \psGetDistance

\psGetSlope $(x_1,y_1)(x_2,y_2)\setminus\langle macro\rangle$ \psGetDistance $(x_1,y_1)(x_2,y_2)\setminus\langle macro\rangle$ 

0.0 0.85759 2.0 0.55055 -0.2 1.10112 0.00615 psGetSlope(-2,1)(3,1)\SlopeVal \SlopeVal \quad
psGetDistance(-2,1)(3,1)\DVal \DVal\\
psGetSlope(-2,1)(-3,-1)\SlopeVal \SlopeVal\quad
psGetDistance(-2,1)(-3,-1)\DVal \DVal\\
psGetSlope(-2,0)(3,-1)\SlopeVal \SlopeVal\quad
psGetDistance(-2,0)(3,-1)\DVal \DVal\\
psGetSlope(-2111,-12)(3,1)\SlopeVal \SlopeVal\quad
%\psGetDistance(-2111,-12)(3,1)\DVal ==> Overflow!

#### 2. "'Handmade"' lines :-)

```
\pslineByHand [Options] (x_1,y_1)(x_2,y_2)(x_3,y_3) \dots
```



```
begin{pspicture}(4,6)
psset{unit=2cm}

pslineByHand[linecolor=red](0,0)(0,2)
        (2,2)(2,0)(0,0)(2,2)(1,3)(0,2)(2,0)

end{pspicture}
```

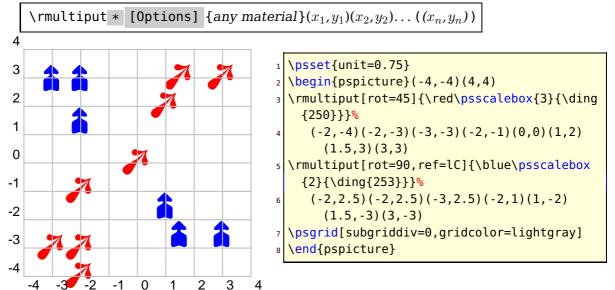
```
begin{pspicture}(\linewidth,3)
multido{\rA=0.00+0.25}{12}{\pslineByHand[linecolor=blue](0,\rA)(\linewidth,\
rA)}
lend{pspicture}
```

The amplitude and the width can be changed by the optional arguments varsteptol and VarStepEpsilon. Both are preset to VarStepEpsilon=2, varsteptol=0.8.

```
begin{pspicture}(\linewidth,3)
wultido{\rA=0.00+0.25}{12}{%
   \pslineByHand[linecolor=blue, VarStepEpsilon=4, varsteptol=2](0,\rA)(\linewidth,\rA)}
   \end{pspicture}
```

#### 3. \rmultiput: a multiple \rput

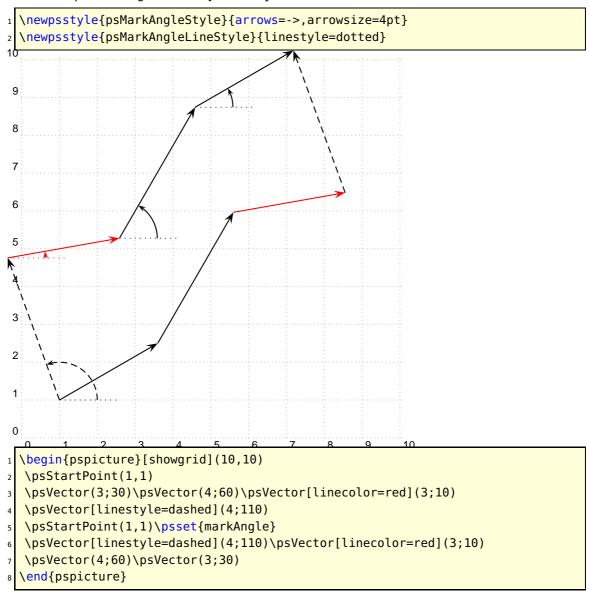
PSTricks already has a \multirput, which puts a box n times with a difference of dx and dy relative to each other. It is not possible to put it with a different distance from one point to the next. This is possible with \rmultiput:



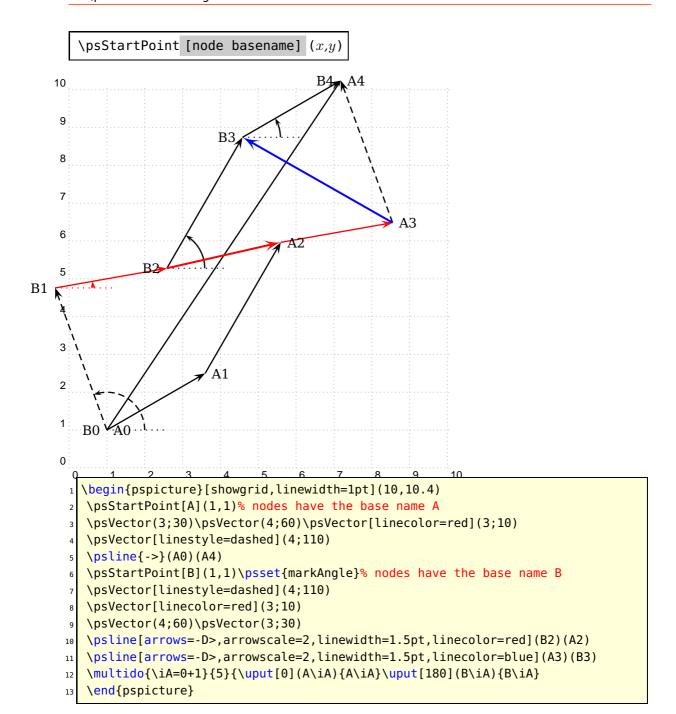
#### 4. \psVector: Drawing relative vector lines

The new macros \psStartPoint and \psVector allow to draw a series of vectors which start point refers to the endpoint of the last drawn vector. The coordinates of the endpoint are *always* interpreted relative to the last the vector. The first vector refers to the coordinates set by \psStartPoint. With the boolean argument one can draw the horizontal angle of the vector.

The style of the angle arc is saved in psMarkAngleStyle and the style for the horizontal line in psMarkAngleLineStyle and preset to



All end points of the vectors are saved in node names with the preset name Vector#, where # is the consecutive number of the nodes. Vector0 ist the starting point of the first \psVector. With the macro \psStartPoint one can set the starting point and with optional argument the name of the nodes. Vector3 is the default node name of the endpoint of the third vector or the name of the starting point of the forth vector.

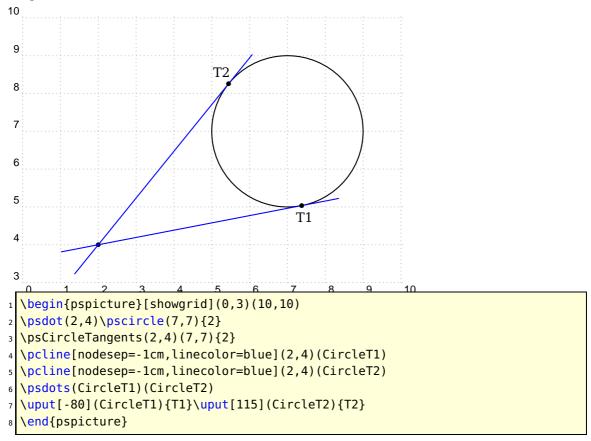


#### 5. \psCircleTangents: Calculating tangent lines of circles

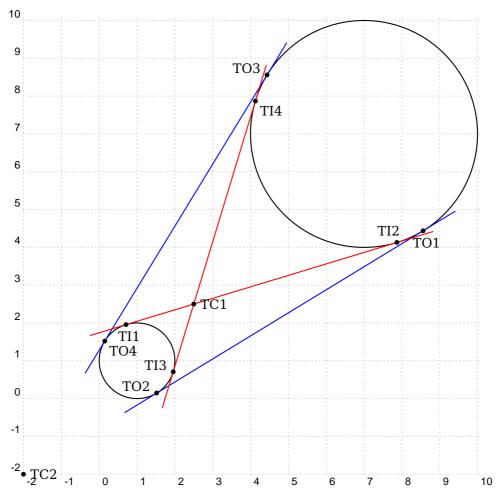
The macro calculates the points on a circle where tangent lines from another point or another circle are drawn.

```
\psCircleTangents(x1,y1)(x2,y2)\{Radius\}\\ \psCircleTangents(x1,y1)\{Radius\}(x2,y2)\{Radius\}\\
```

In the first case the coordinates of a point and the center and the radius of a circle must be given. The names of the calculates node names are CircleT1 and CircleT2.



When using the other variant of the macro two circles must be given. The macro then defines ten nodes, named CircleTC1 and CircleTC2 for the two intersection points, CircleTO1, CircleTO2, CircleTO3, and CircleTO4 for the four nodes of the outer tangent lines and CircleTI1, CircleTI2, CircleTI3, and CircleTI4 for the four nodes of the inner tangent lines.



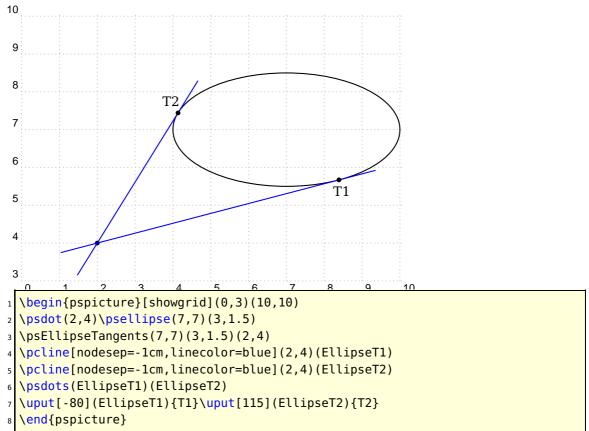
```
\begin{pspicture}[showgrid](-2,-2)(10,10)
  \pscircle(1,1){1}\pscircle(7,7){3}
  \psCircleTangents(1,1){1}(7,7){3}
  \pcline[nodesep=-1cm,linecolor=blue](CircleT01)(CircleT02)
  \pcline[nodesep=-1cm,linecolor=blue](CircleT03)(CircleT04)
  \pcline[nodesep=-1cm,linecolor=red](CircleTI1)(CircleTI2)
  \pcline[nodesep=-1cm,linecolor=red](CircleTI3)(CircleTI4)
  \psdots(CircleTC1)\psdots(CircleTC2)%
   (CircleTO1)(CircleTO2)(CircleTO3)(CircleTO4)%
   (CircleTI1)(CircleTI2)(CircleTI3)(CircleTI4)%
11 \uput[0](CircleTC1){TC1}\uput[0](CircleTC2){TC2}
12 \uput[-80](CircleTI1){TI1}\uput[115](CircleTI2){TI2}
13 \uput[150](CircleTI3){TI3}\uput[-45](CircleTI4){TI4}
14 \uput[-80](CircleT01){T01}\uput[150](CircleT02){T02}
15 \uput[150](CircleT03){T03}\uput[-45](CircleT04){T04}
  \end{pspicture}
```

## 6. \psEllipseTangents: Calculating tangent lines of an ellipse

The macro calculates the two points on an ellipse where tangent lines from an outside point are drawn.

```
\verb|\psEllipseTangents(x_0,y_0)(a,b)(x_p,y_p)|
```

The first two pairs of coordinates are the same as the ones for the default ellipse. The names of the calculates node names are EllipseT1 and EllipseT2.



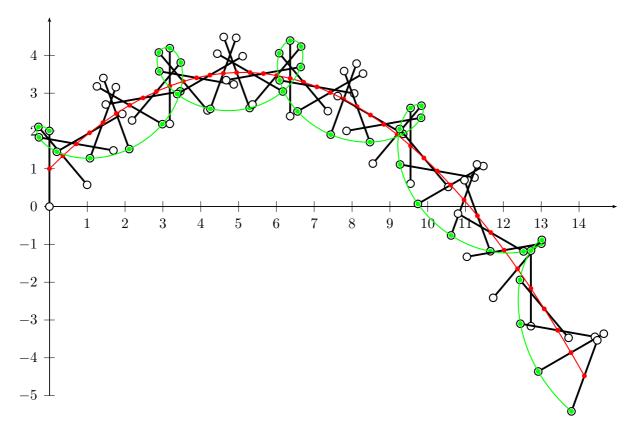
#### 7. \psrotate: Rotating objects

\rput also has an optional argument for rotating objects, but it always depends on the \rput coordinates. With \psrotate the rotating center can be placed anywhere. The rotation is done with \pscustom, all optional arguments are only valid if they are part of the \pscustom macro.

```
\verb|\psrotate| [Options]| (x,y) \{rot \ angle\} \{object\}
```

```
5
4
3
2
0
1
0
-1
0
1
```

```
\begin{pspicture}(-1,-1)(3,6)
  \def\canne{% Idea by Manuel Luque
    \protect\operatorname{\mathsf{psgrid}}[\operatorname{\mathsf{subgriddiv}}=0](-1,0)(1,5)
    \pscustom[linewidth=2mm]{\psline(0,4)\
      psarcn(0.3,4){0.3}{180}{360}}%
    \pscircle*(0.6,4){0.1}\pstriangle*(0,0)
      (0.2, -0.3)
  \def\Object{}
    \canne
    \psrotate(0.3,4){45}{\psset{linecolor=red
      !50}\canne}
    \psrotate(0.3,4){90}{\psset{linecolor=blue}
      !50}\canne}
    \psrotate(0.3,4){360}{\psset{linecolor=cyan}
10
      !50}\canne}
    \psdot[linecolor=red](0.3,4)
  \end{pspicture}
```

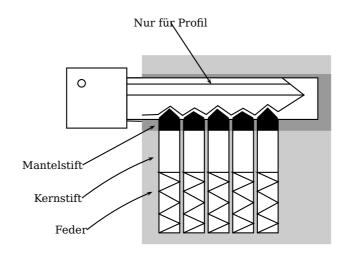


```
\begin{pspicture}(0,-6)(15,5)
        \def\majorette{\psline[linewidth=0.5mm](0,2)% Idea by Manuel Luque
                                            \pscircle[fillstyle=solid]{0.1}
                                            \pscircle[fillstyle=solid](0,2){0.1}}
            \prootember | psaxes[linewidth=0.5pt] {->} (0,0) (0,-5) (15,5)
            \pstVerb{/V0 10 def /Alpha 45 def}% vitesse initiale, angle de lancement
            \multido{\nT=0.0+0.05,\iA=0+40}{41}{%
                 \pstVerb{/nT \nT\space def}%
                 \rput(!V0 Alpha cos mul nT mul -9.81 2 div nT dup mul mul V0 Alpha sin mul
                       nT mul add) {%
                        \protection \pro
10
                              =green](0,2)}}}
            \parametricplot[linecolor=red]{0}{2}{% trajectoire du milieu
11
                   VO Alpha cos mul t mul -9.81 2 div t dup mul mul VO Alpha sin mul t mul
12
                          add 1 add}
            \parametricplot[linecolor=green,plotpoints=360]{0}{2}{% d'une extremite
13
                   V0 Alpha cos mul t mul 800 t mul sin sub % x(t)
14
                    -9.81 2 div t dup mul mul V0 Alpha sin mul t mul add 1 add 800 t mul cos
15
                          add }%y(t)
         \end{pspicture}
```

#### 8. \psComment: comments to a graphic

```
\psComment * [Options] \{arrows\}\ (x_0,y_0)(x_1,y_1)\{Text\} [line macro] [put macro]
```

By default the macro uses the \ncline macro to draw a line from the first to the second point, it can be changed with the first additional optional argument. The label is put by default with \rput, which can be changed with the last optional argument. If this is used, then the line macro has also be defined, eg \psComment(A)(B){text}[\ncarc][\ncput} At least, leave the argument empty.



```
\SpecialCoor\newpsstyle{weiss}{fillstyle=solid,fillcolor=white}
         \footnotesize\psset{unit=0.5cm,dimen=middle}
         \begin{pspicture}(-12,-4)(6,10)
         \proonup *[linecolor=black!20](-5,-3)(5,7) \proonup *[linecolor=black!40](-5,3)(5,6)
         \pscircle(-8.19,5.51){0.2}
         \psframe[fillcolor=white,fillstyle=solid](-5.8,3.6)(4.3,5.8)
         \proonup (-8.98, 3.14)(-5.8, 6.32)
        psline(0,0)(1.1,0.5)(0,1)(1.1,1.6)(0,2.2)(1.1,2.7)(0,3.2)(1.1,3.2)
10 \pspolygon*(-4.1,3.7)(-4.1,3)(-3,3)(-3.01,3.7)(-3.54,4.19)
11 \pspolygon*(1.09,3.7)(1.1,3)(2.2,3)(2.18,3.7)(1.65,4.24)
12 \pspolygon*(-2.78,3.7)(-2.8,3)(-1.7,3)(-1.71,3.7)(-2.27,4.04)
        \pspolygon*(-1.51,3.7)(-1.5,3)(-0.4,3)(-0.41,3.7)(-1.02,4.17)
14 \pspolygon*(-0.21,3.7)(-0.2,3)(0.9,3)(0.89,3.7)(0.3,4.04)
15 \mid psline(-5,3.83)(-4.15,3.86)(-3.5,4.3)(-2.85,3.81)(-2.22,4.21)(-1.6,3.86)(-0.99,4.33)
                             (-0.28, 3.83)(0.35, 4.19)(0.97, 3.83)(1.65, 4.39)(2.2, 4.01)(3.57, 4.89)(2.41, 5.8)
16
              \psline(-5,5.8)(-5.78,5.8) \psline(-5.78,5.47)(2.85,5.47)
17
              \prootember \pro
18
              \psComment*[ref=r]{->}(-8.14,1.19)(-4.31,3.27){Mantelstift}
              \psComment*[ref=r]{->}(-8.17,-0.56)(-4.37,1.59){Kernstift}[\ncarc]
20
              \psComment*[ref=r]{->}(-7.91,-2.24)(-4.44,-0.23){Feder}[\ncarc]
21
              \protect{\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\pr
23 \end{pspicture}
```

#### 9. \psChart: a pie chart

 $\verb|\psChart| [Options]| \{ comma \ separated \ value \ list \} \{ comma \ separated \ value \ list \} \{ radius \}$ 

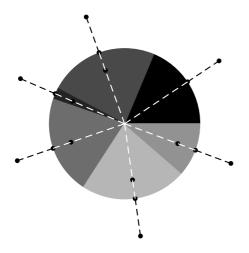
The special optional arguments for the \psChart macro are as follows:

name	description	
chartSep	distance from the pie chart center to an outraged pie piece	10pt
chartColor	gray or colored pie (values are: gray or color)	gray
userColor	a comma separated list of user defined colors for the pie	{}
chartNodeI	the position of the inner node, relative to the radius	0.75
chartNode0	the position of the outer node, relative to the radius	1.5

The first mandatory argument is the list of the values and may not be empty. The second one is a list of outraged pieces, numbered consecutively from 1 to up the total number of values. The list of user defined colors must be enclosed in braces!

The macro \psChart defines for every value three nodes at the half angle and in distances from 0.75, 1, and 1.25 times of the radius from the origin. The nodes are named as psChartI?, psChart?, and psChart0?, where ? is the number of the pie. The letter I leads to the inner node and the letter O to the outer node. The distance can be changed with the optional arguments chartNodeI and chartNodeO in the usual way with \psset{chartNodeI=...,chartNodeO=...}.

The other one is the node on the circle line. The origin is by default (0,0). Moving the pie to another position can be done as usual with the  $\protect$ rput-macro. The used colors are named internally as chartFillColor? and can be used by the user for coloring lines or text.



```
begin{pspicture}(-3,-3)(3,3)
psChart{ 23, 29, 3, 26, 28, 14 }{}{2}

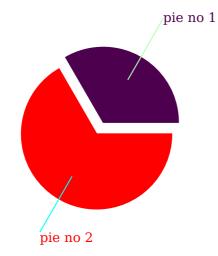
multido{\iA=1+1}{6}{%

psdot(psChart\iA)\psdot(psChartI\iA)\psdot
    (psChart0\iA)%

psline[linestyle=dashed,linecolor=white](
    psChart\iA)

psline[linestyle=dashed](psChart\iA)(
    psChart0\iA)}

end{pspicture}
```



```
1 \begin{pspicture}(-3,-3)(3,3)
2 \psChart[chartColor=color]{45,90}{1}{2}
3 \ncline[linecolor=-chartFillColor1,
4 nodesepB=-20pt]{psChart01}{psChart1}
5 \rput[l](psChart01){%
6 \textcolor{chartFillColor1}{pie no 1}}
7 \ncline[linecolor=-chartFillColor2,
8 nodesepB=-20pt]{psChart02}{psChart2}
9 \rput[lt](psChart02){%
10 \textcolor{chartFillColor2}{pie no 2}}
11 \end{pspicture}
```



```
\psframebox[fillcolor=black!20,
  fillstyle=solid]{%
\begin{pspicture}(-3.5,-3.5)
  (4.25,3.5)
\psChart[chartColor=color]%
  {23, 29, 3, 26, 28, 14, 17, 4,
      9}{}{2}
\multido{\iA=1+1}{9}{%
  \ncline[linecolor=-chartFillColor\
      iA,
      nodesepB=-10pt]{psChart0\iA}{
      psChart\iA}
  \rput[l](psChart0\iA){%
      \textcolor{chartFillColor\iA}{pie}
      no \iA}}}
\end{pspicture}}
```

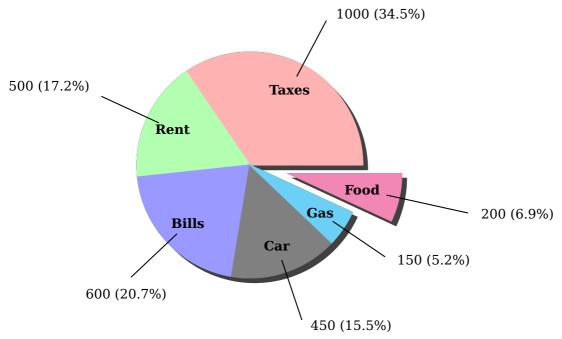


```
begin{pspicture}(-3,-3)(3,3)
psChart[userColor={red!30,green!30,
    blue!40,gray,magenta!60,cyan}]%
    { 23, 29, 3, 26, 28, 14 }{1,4}{2}
end{pspicture}
```

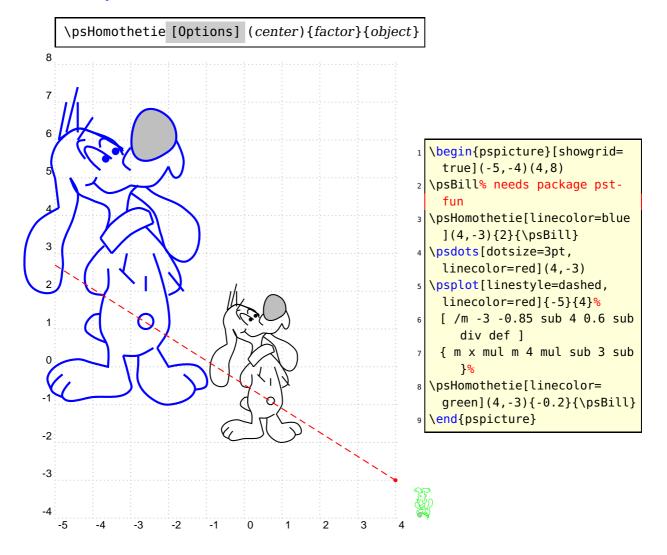
```
2
3
4
6
5
```

```
begin{pspicture}(-3,-2.5)(3,2.5)
psChart{ 23, 29, 3, 26, 28, 14 }{}{2}

multido{\iA=1+1}{6}{\rput*(psChartI\iA){\iA}}
}
end{pspicture}
```



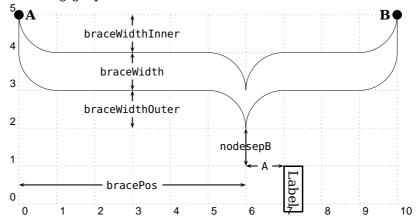
#### 10. \psHomothetie: central dilatation



#### 11. \psbrace

```
\verb|\psbrace*| [Options] (A)(B)\{text\}
```

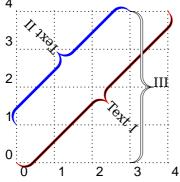
Additional to all other available options from pstricks or the other related packages, there are two new option, named braceWidth and bracePos. All important ones are shown in the following graphics and table.



A positive value for nodesepA and nodesepB shifts the label to the upper right and a negative value to the lower left. This does not depends on the value for the rotating of the label!

meaning	
default is \pslinewidth	
default is 10\pslinewidth	
default is 10\pslinewidth	
relative position (default is $0.5$ )	
x-separation (default is $0pt$ )	
y-separation (default is $0pt$ )	
additional rotating for the text (default is 0)	
reference point for the text (default is c)	
default is black	

By default the text is written perpendicular to the brace line and can be changed with the pstricks option rot=... The text parameter can take any object and may also be empty. The reference point can be any value of the combination of l (left) or r (right) and b (bottom) or B (Baseline) or C (center) or t (top), where the default is c, the center of the object.

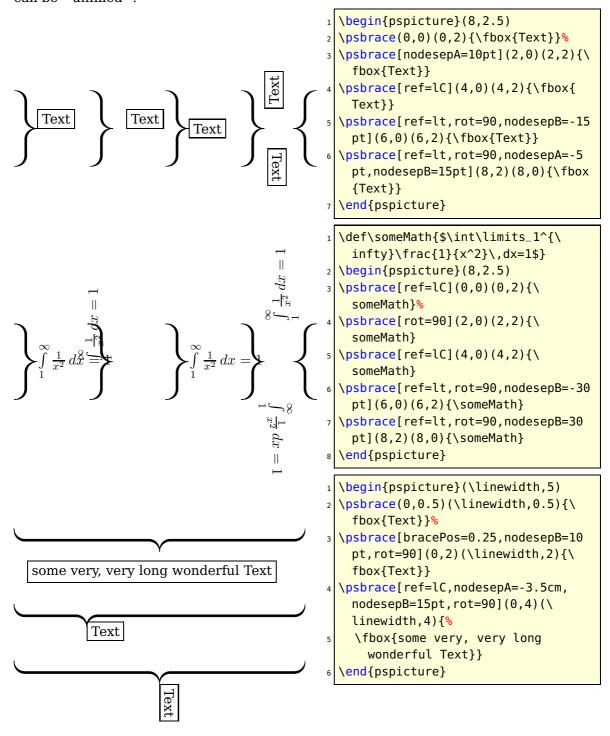


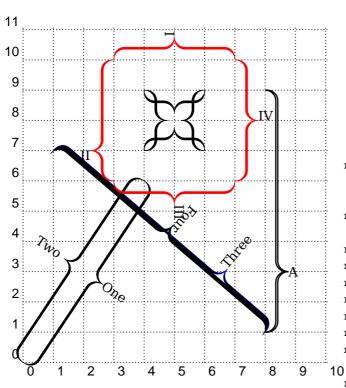
```
begin{pspicture}(4,4)
psgrid[subgriddiv=0,griddots=10]

pnode(0,0){A}
pnode(4,4){B}

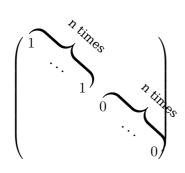
psbrace[linecolor=red,ref=lC](A)(B){Text I}
psbrace*[linecolor=blue,ref=lC](3,4)(0,1){Text II}
psbrace[fillcolor=white](3,0)(3,4){III}
end{pspicture}
```

The option \specialCoor is enabled, so that all types of coordinates are possible, (nodename), (x,y), (nodeA|nodeB), ... The star version fills the inner of the brace with the current linecolor. With the fillcolor white or any other background color the brace can be "'unfilled"'.





```
\psset{unit=0.8}
  \begin{pspicture}(10,11)
  \psgrid[subgriddiv=0,griddots=10]
  \pnode(0,0){A}
  \pnode(4,6){B}
  \psbrace[ref=lC](A)(B){One}
6
  \psbrace[rot=180,nodesepA=-5pt,ref
    =rb](B)(A){Two}
  \psbrace[linecolor=blue,bracePos
    =0.25, ref=lB](8,1)(1,7){Three}
  \psbrace[braceWidth=-1mm, rot=180,
    ref=rB](8,1)(1,7){Four}
10 \psbrace*[linearc=0.5,fillstyle=
    none,linewidth=1pt,braceWidth
   bracePos=0.25, ref=lC](8,1)(8,9){
  \psbrace(4,9)(6,9){}
12
13
  \psbrace(6,9)(6,7){}
  \psbrace(6,7)(4,7){}
  \psbrace(4,7)(4,9){}
15
  \psset{linecolor=red}
16
  \protect{psbrace*[ref=lb](7,10)(3,10){I}}
18 \psbrace*[ref=lb,bracePos
    =0.75](3,10)(3,6){II}
19 \psbrace*[ref=lb](3,6)(7,6){III}
  \psbrace*[ref=lb](7,6)(7,10){IV}
  \end{pspicture}
```



It is also possible to put a vertical brace around a default paragraph. This works by setting two invisible nodes at the beginning and the end of the paragraph. Indentation is possible with a minipage.

Some nonsense text, which is nothing more than nonsense. Some nonsense text, which is nothing more than nonsense.

Some nonsense text, which is nothing more than nonsense. Some nonsense text, which is nothing more than nonsense. Some nonsense text, which is nothing more than nonsense. Some nonsense text, which is nothing more than nonsense text, which is nothing more than nonsense. Some nonsense text, which is nothing more than nonsense text, which is nothing more than nonsense. Some nonsense text, which is nothing more than nonsense.

Some nonsense text, which is nothing more than nonsense. Some nonsense text, which is nothing more than nonsense.

Some nonsense text, which is nothing more than nonsense. Some nonsense text, which is nothing more than nonsense. Some nonsense text, which is nothing more than nonsense. Some nonsense text, which is nothing more than nonsense text, which is nothing more than nonsense. Some nonsense text, which is nothing more than nonsense. Some nonsense text, which is nothing more than nonsense text, which is nothing more than nonsense.

```
Some nonsense text, which is nothing more than nonsense.
  Some nonsense text, which is nothing more than nonsense.
  \noindent\rnode{A}{}
  \vspace*{-1ex}
  Some nonsense text, which is nothing more than nonsense.
  Some nonsense text, which is nothing more than nonsense.
  Some nonsense text, which is nothing more than nonsense.
10 Some nonsense text, which is nothing more than nonsense.
11 Some nonsense text, which is nothing more than nonsense.
12 Some nonsense text, which is nothing more than nonsense.
Some nonsense text, which is nothing more than nonsense.
14 Some nonsense text, which is nothing more than nonsense.
16 \vspace*{-2ex}\noindent\rnode{B}{}\psbrace[linecolor=red](A)(B){}
18 Some nonsense text, which is nothing more than nonsense.
19 Some nonsense text, which is nothing more than nonsense.
 \medskip\hfill\begin{minipage}{0.95\linewidth}
22 \noindent\rnode{A}{}
vspace*{-lex}
25 Some nonsense text, which is nothing more than nonsense.
26 Some nonsense text, which is nothing more than nonsense.
27 Some nonsense text, which is nothing more than nonsense.
28 Some nonsense text, which is nothing more than nonsense.
29 Some nonsense text, which is nothing more than nonsense.
  Some nonsense text, which is nothing more than nonsense.
31 Some nonsense text, which is nothing more than nonsense.
```

```
Some nonsense text, which is nothing more than nonsense.

Vvspace*{-2ex}\noindent\rnode{B}{}\psbrace[linecolor=red](A)(B){}

lend{minipage}
```

12. Random dots

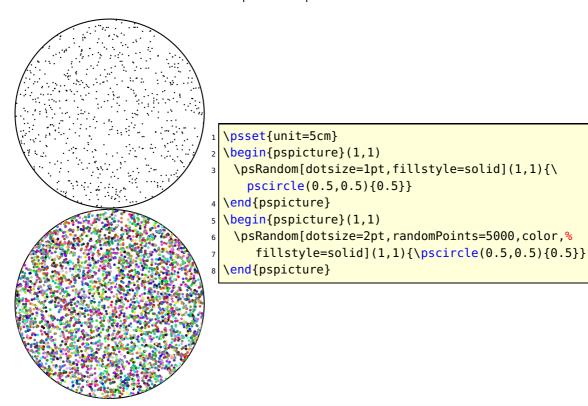
#### 12. Random dots

The syntax of the new macro  $\protect\operatorname{\mathtt{NpsRandom}}$  is:

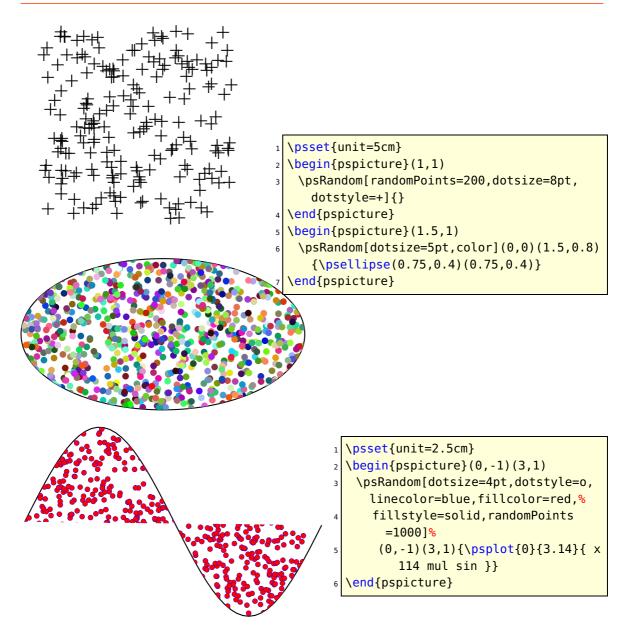
```
\label{eq:linear_problem} $$ \psRandom [Options] {} \\ \psRandom [Options] $$ (x_{Min},y_{Min}) $$ (x_{Max},y_{Max}) $$ {clip path} $$
```

If there is no area for the dots defined, then (0,0)(1,1) in the current scale setting is used for placing the dots. If there is only one  $(x_{Max},y_{Max})$  defined, then (0,0) is used for the other point. This area should be greater than the clipping path to be sure that the dots are placed over the full area. The clipping path can be everything. If no clipping path is given, then the frame (0,0)(1,1) in user coordinates is used. The new options are:

name	default	
randomPoints	1000	number of random dots
color	false	random color



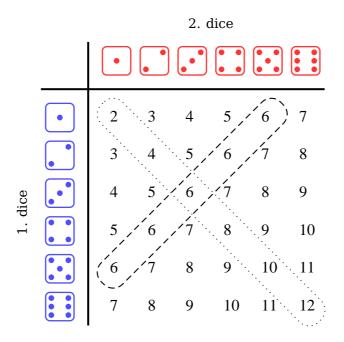
12. Random dots



13. \psDice 27

#### 13. \psDice

\psdice creates the view of a dice. The number on the dice is the only parameter. The optional parameters, like the color can be used as usual. The macro is a box of dimension zero and is placed at the current point. Use the \rput macro to place it anywhere. The optional argument unit can be used to scale the dice. the default size of the dice  $1 \text{cm} \times 1 \text{cm}$ .



```
\begin{array}{l} \begin{array}{l} \textbf{begin} \{ pspicture \} (-1, -1) (8, 8) \end{array} \end{array}
   \multido{\iA=1+1}{6}{%
    \rput(\iA,7.5){\Huge\psdice[unit=0.75,linecolor=red!80]{\iA}}
    \rput(! -0.5 7 \iA\space sub){\Huge\psdice[unit=0.75,linecolor=blue!70]{\iA
      }}%
    \multido{\iB=1+1}{6}{%
      \rput(! \iA\space 7 \iB\space sub){%
       \rnode[c]{p\iA\iB}{\makebox[1em][l]{\strut\psPrintValue[fontscale=12]{\iA
         \space \iB\space add}}}%
8 }}}
  \ncbox[linearc=0.35,nodesep=0.2,linestyle=dotted]{p11}{p66}
  \ncbox[linearc=0.35,nodesep=0.2,linestyle=dashed]{p15}{p51}
11 \rput{90}(-1.5,3.5){1. dice}
12 \rput{0}(3.5,8.5){2. dice}
13 \psline[linewidth=1.5pt](0.25,0.5)(0.25,8)
14 \psline[linewidth=1.5pt](-1,6.75)(6.5,6.75)
15 \end{pspicture}
```

14. \psFormatInt 28

#### 14. \psFormatInt

There exist some packages and a lot of code to format an integer like  $1\,000\,000$  or 1,234,567 (in Europe 1.234.567). But all packages expect a real number as argument and cannot handle macros as an argument. For this case pstricks-add has a macro \psFormatInt which can handle both:

```
1,234,567
1,234,567
1,234,567
1,234,567
1,234.567
1,234.567
1,234.567
2 \psFormatInt[intSeparator=,}]{1234567}\\
1,234.567
4 \psFormatInt[intSeparator=s\cdots]{1234567}\\
1,234.567
5 \quad \def\temp{965432}
965,432
6 \psFormatInt{\temp}
```

With the option intSeparator the symbol can be changed to any any non-number character.

#### 15. \psRelNode and \psDefPSPNodes

With these macros it is possible to put a node relative to a given line or given pspicture-environment. In the frist case the parameters are the angle and the length factor:

The length factor relates to the distance  $\overline{P_0P_1}$  and the end node name must be a valid nodename and shouldn't contain any of the special PostScript characters. There are two valid options:

name	default	meaning
angle	0	angle between the given line $\overline{P_0P_1}$ and the new one $\overline{P_0P_{endNode}}$
trueAngle   false   defines whether the angle refers to the seen lin		defines whether the angle refers to the seen line or to the math-
		ematical one, which respect the scaling factors xunit and yunit.

```
• 120
                                                                                                              150
                                                    • 180
                                                                                                                                                                                                                                          • 90
                                                                                                                                                                                                                                                                                                                                                                                  \begin{pspicture}[showgrid](7,6)
                                                                                                                                                                                                                                                                                                                                                                                              \poonup (3,3){A}\poonup (4,2){B}
                                                                                                                                                                                                                                                                                                                                                                                              \psline[nodesep=-3,linewidth=0.5pt](A
                    210
                                                                                                                                                                                                                                                                            60
                                                                                                                                                                                                                                                                                                                                                                                                             )(B)
3
                                                                                                                                                                                                                                                                                                                                                                                              \mbox{multido}{iA=0+30}{12}{\%}
                                                                                                                                                                                                                                                                                                                                                                                                          \proonup \
2 • 240
                                                                                                                                                                                                                                                                                                                                                                                                          \qdisk(C){2pt}
                                                                                                                                                                                                                                                                            30
                                                                                                                                                                                                                                                                                                                                                                                                          \uput[0](C){\iA}}
                                                                                                                                                                                                                                                                                                                                                                                    \end{pspicture}
                                                    • 270
                                                                                                                                                                                                                                            • ()
                                                                                                             • 300
                                                                                                                                                                                 330
```

In the second case the new macro \psDefPSPNodes defines nine nodes that corresponds to nine particular points (namely bottom left, bottom center, bottom right, center left, center center, center right, top left, top center, top right) of the pspicture box.

```
\begin{pspicture}[showgrid=true](-1,-1)(4,4)
P$Ptl
             PSPtc
                           PSPtr
                                       \psDefPSPNodes
                                       \psdots(PSPbl)(PSPbc)(PSPbr)
                                          (PSPcl)(PSPcc)(PSPcr)(PSPtl)(PSPtc)(
 3
                                            PSPtr)
                                       \uput[90](PSPbl){PSPbl} \uput[90](PSPbc){
 2
                                        PSPbc}
PSPcl
                           PSPcr
             PSPcc
                                       \uput[90](PSPbr){PSPbr} \uput[90](PSPcl){
                                       \uput[90](PSPcc){PSPcc} \uput[90](PSPcr){
                                        PSPcr}
 0
                                       \uput[90](PSPtl){PSPtl} \uput[90](PSPtc){
                                        PSPtc}
P$Pbl
             PSPbc
                           PSPbr
                                       \uput[90](PSPtr){PSPtr}
                                     \end{pspicture}
```

The name of the nodes are predefined as:

16. \psRelLine

```
\psset[pst-PSPNodes]{blName=PSPbl,bcName=PSPbc,brName=PSPbr,
    clName=PSPcl,ccName=PSPcc,crName=PSPcr,tlName=PSPtl,tcName=PSPtc,trName=PSPtr}
```

and can be modified in the same way.

#### 16. \psRelLine

With this macro it is possible to plot lines relative to a given one. Parameter are the angle and the length factor:

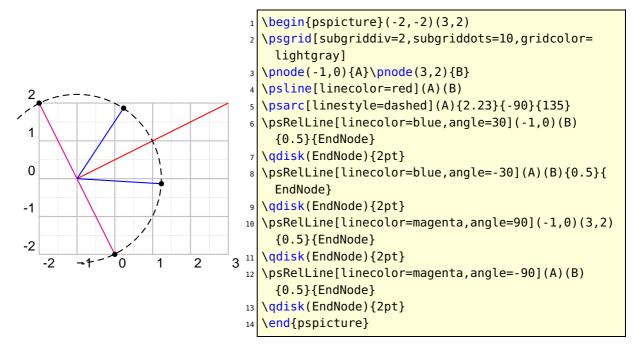
```
\label{line} $$ \psRelLine(P0)(P1)_{length\ factor}_{cond node\ name} $$ \psRelLine[arrows](P0)(P1)_{length\ factor}_{end\ node\ name} $$ \psRelLine[Options](P0)(P1)_{length\ factor}_{end\ node\ name} $$ \psRelLine[Options](P0)(P1)_{length\ factor}_{end\ node\ name} $$ $$ \psRelLine[Options](P0)(P1)_{length\ factor}_{end\ node\ name} $$
```

The length factor relates to the distance  $\overline{P_0P_1}$  and the end node name must be a valid nodename and shouldn't contain any of the special PostScript characters. There are two valid options which are described in the foregoing section for \psRelNode.

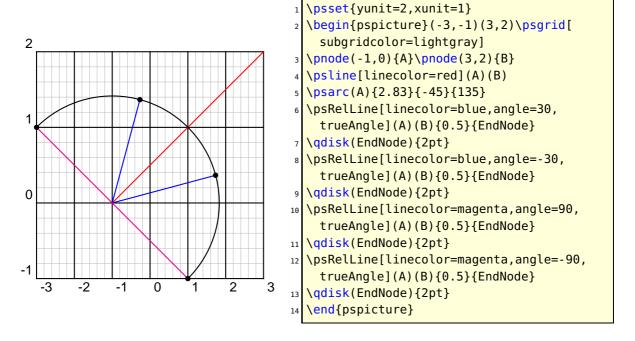
The following two figures show the same, the first one with a scaling different to 1:1, this is the reason why the end points are on an ellipse and not on a circle like in the second figure.

```
2
                                     \psset{yunit=2,xunit=1}
                                     \begin{array}{c} \mathbf{begin} \{ pspicture \} (-2, -2) (3, 2) \end{array}
                                     \psgrid[subgriddiv=2,subgriddots=10,gridcolor=
                                       lightgray]
                                     \prode(-1,0){A}\prode(3,2){B}
1
                                     \psline[linecolor=red](A)(B)
                                     \psRelLine[linecolor=blue,angle=30](-1,0)(B)
                                       {0.5}{EndNode}
                                     \qdisk(EndNode){2pt}
0
                                     \psRelLine[linecolor=blue,angle=-30](A)(B){0.5}{
                                       EndNode}
                                     \qdisk(EndNode){2pt}
                                     \psRelLine[linecolor=magenta,angle=90](-1,0)(3,2)
                                       {0.5}{EndNode}
-1
                                  11 \qdisk(EndNode){2pt}
                                     \psRelLine[linecolor=magenta,angle=-90](A)(B)
                                       {0.5}{EndNode}
                                  13 \qdisk(EndNode){2pt}
-2
                                     \end{pspicture}
```

16. \psRelLine 31

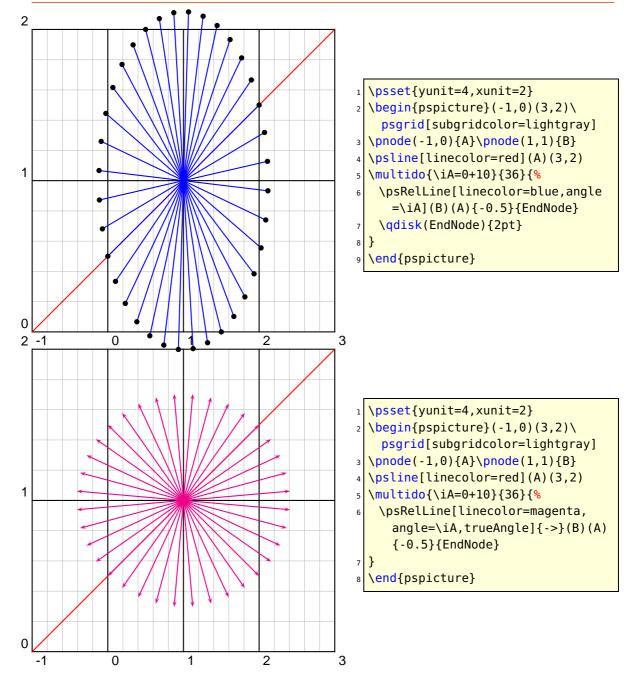


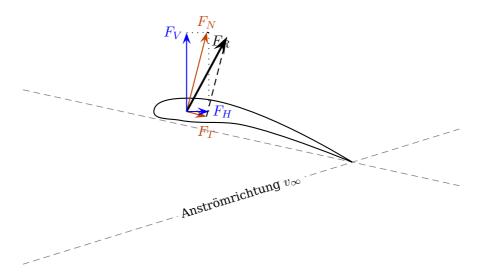
The following figure has also a different scaling, but has set the option trueAngle, all angles refer to "what you see".



Two examples using \multido to show the behaviour of the options trueAngle and angle.

16. \psRelLine





```
\psset{xunit=0.75\linewidth,yunit=0.75\linewidth,trueAngle}%
  \end{center}
  \begin{pspicture}(1,0.6)%\psgrid
   \poode(.3,.35){Vk} \poode(.375,.35){D} \poode(0,.4){DST1} \poode(1,.18){DST}
    \poode(0,.1){A1} \poode(1,.31){A1}
    { \psset{linewidth=.02,linestyle=dashed,linecolor=gray}%
     \pcline(DST1)(DST2) % <- Druckseitentangente</pre>
     \pcline(A2)(A1) % <- Anstr"omrichtung</pre>
     \lput*{:U}{\small Anstr"omrichtung $v_{\infty}$} }%
   \psIntersectionPoint(A1)(A2)(DST1)(DST2){Hk}
   \pscurve(Hk)(.4,.38)(Vk)(.36,.33)(.5,.32)(Hk)
11
    \psParallelLine[linecolor=red!75!green,arrows=->,arrowscale=2](Vk)(Hk)(D)
12
     {.1}{FtE}
    \psRelLine[linecolor=red!75!green,arrows=->,arrowscale=2,angle=90](D)(FtE)
13
     {4}{Fn}% why "4"?
   \psParallelLine[linestyle=dashed](D)(FtE)(Fn){.1}{Fnr1}
14
   \psRelLine[linestyle=dashed,angle=90](FtE)(D){-4}{Fnr2} % why "-4"?
15
   \psline[linewidth=1.5pt,arrows=->,arrowscale=2](D)(Fnr2)
16
   \psIntersectionPoint(D)([nodesep=2]D)(Fnr1)([offset=-4]Fnr1){Fh}
   \psIntersectionPoint(D)([offset=2]D)(Fnr1)([nodesep=4]Fnr1){Fv}
18
   \psline[linecolor=blue,arrows=->,arrowscale=2](D)(Fh)
   \psline[linecolor=blue,arrows=->,arrowscale=2](D)(Fv)
20
   \psline[linestyle=dotted](Fh)(Fnr1) \psline[linestyle=dotted](Fv)(Fnr1)
   \displaystyle \{.1\}[-45](Fnr1)\{\$F_{R}\}\} \quad \{.1\}[90](Fn)\{\color\{red!75!green\}\$F_{N}\}\}
   \uput{.25}[-90](FtE){\color{red!75!green}$F_{T}$}
25 \end{pspicture}
```

#### 17. \psParallelLine

With this macro it is possible to plot lines relative to a given one, which is parallel. There is no special parameter here.

```
\psParallelLine(<P0>)(<P1>)(<P2>){<length>}{<end node name>}
\psParallelLine{<arrows>}(<P0>)(<P1>)(<P2>){<length>}{<end node name>}
\psParallelLine[<options>](<P0>)(<P1>)(<P2>){<length>}{<end node name>}
\psParallelLine[<options>]{<arrows>}(<P0>)(<P1>)(<P2>){<length>}{<end node name>}
```

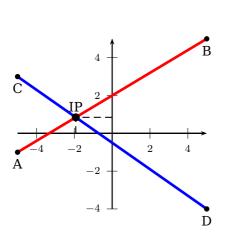
The line starts at  $P_2$ , is parallel to  $\overline{P_0P_1}$  and the length of this parallel line depends on the length factor. The end node name must be a valid nodename and shouldn't contain any of the special PostScript characters.

```
\begin{pspicture*}(-5,-4)(5,3.5)
 \psgrid[subgriddiv=0,griddots=5]
 \poonup (2, -2) {FF} \q disk(FF) {1.5pt}
 \poonup (-5,5) {A} \poonup (0,0) {0}
 \mbox{\mbox{multido}(\nCountA=-2.4+0.4){9}{%}}
   \psParallelLine[linecolor=red](0
     )(A)(0,\nCountA){9}{P1}
   \psline[linecolor=red](0,\
     nCountA)(FF)
   \psRelLine[linecolor=red](0,\
     nCountA) (FF) {9} {P2}
 \psline[linecolor=blue](A)(FF)
 \psRelLine[linecolor=blue](A)(FF)
   {5}{END1}
 \psline[linewidth=2pt,arrows
   =->](2,0)(FF)
end{pspicture*}
```

#### 18. \psIntersectionPoint

This macro calculates the intersection point of two lines, given by the four coordinates. There is no special parameter here.

```
\psIntersectionPoint(<P0>)(<P1>)(<P2>)(<P3>){<node name>}
```



```
\psset{unit=0.5cm}
  \begin{array}{c} \begin{array}{c} \mathbf{begin} \{ pspicture \} (-5, -4) (5, 5) \end{array} \end{array}
2
    \psaxes[labelFontSize=\scriptstyle,
      dx=2,Dx=2,dy=2,Dy=2]\{->\}(0,0)(-5,-4)(5,5)
    \psline[linecolor=red,linewidth=2pt](-5,-1)
    \psline[linecolor=blue,linewidth=2pt](-5,3)
      (5, -4)
    \disk(-5,-1){2pt}\setminus uput[-90](-5,-1){A}
    \q isk(5,5) \{2pt\} \setminus [-90] (5,5) \{B\}
    \qdisk(-5,3){2pt}\uput[-90](-5,3){C}
    \disk(5,-4){2pt}\uput[-90](5,-4){D}
    \protectionPoint(-5,-1)(5,5)(-5,3)(5,-4){
11
      IP}
    \qdisk(IP){3pt}\uput{0.3}[90](IP){IP}
12
    \psline[linestyle=dashed](IP|0,0)(IP)(0,0|IP)
  \end{pspicture}
```

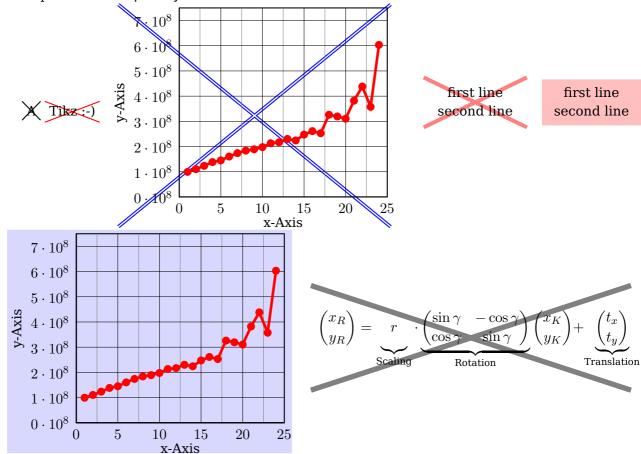
19. \psCancel

#### 19. \psCancel<sup>1</sup>

This macro works like the \cancel macro from the package of the same name but it allows as argument any contents, not only letters but also a complex graphic.

```
\psCancel * [Options] {contents}
```

All optional arguments for lines and boxes are valid and can be used in the usual way. The star option fills the underlying box rectangle with the linecolor. This can be transparent if opacity is set to a value less than 1. This can be used in presentation to strike out words, equations, and graphic objects. Lines can also be transparent when the option strokeopacity is used.



```
psCancel{A} \psCancel[linecolor=red]{Tikz :-)} \quad
psCancel[linecolor=blue,doubleline=true]{%
  \readdata{\data}{demo1.data}
  \psset{shift=*,xAxisLabel=x-Axis,yAxisLabel=y-Axis,llx=-13mm,lly=-7mm,
      xAxisLabelPos={c,-1},yAxisLabelPos={-7,c}}
  \pstScalePoints(1,0.00000001){}{}
  \begin{psgraph}[axesstyle=frame,xticksize=0 7.5,yticksize=0 25,subticksize=1,
```

<sup>1</sup> Thanks to by Stefano Baroni

19. \psCancel

```
ylabelFactor=\color=0.05, Dy=1, xsubticks=2](0,0)(25,7.5){5.5cm}{5.cm}
   \listplot[linecolor=red, linewidth=2pt, showpoints=true]{\data}
   \end{psgraph}} \qquad% end of Cancel
11 \psCancel[linewidth=3pt,linecolor=red,
     strokeopacity=0.5]{\tabular[b]{c}first line\\second line\endtabular}\quad
13 \psCancel*[linecolor=red!50,opacity=0.5]{\tabular[b]{c}first line\\second line
    \endtabular}
14 \quad
  \psCancel*[linecolor=blue!30,opacity=0.5]{%
15
   \readdata{\data}{demo1.data}
   \psset{shift=*,xAxisLabel=x-Axis,yAxisLabel=y-Axis,llx=-15mm,lly=-7mm,urx=1
       xAxisLabelPos={c,-1},yAxisLabelPos={-7,c}}
    \pstScalePoints(1,0.00000001){}{}
19
   \begin{psgraph}[axesstyle=frame,xticksize=0 7.5,yticksize=0 25,subticksize
      ylabelFactor=\cdot 10^8,Dx=5,Dy=1,xsubticks=2](0,0)(25,7.5)\{5.5cm\}\{5cm\}
21
   \listplot[linecolor=red, linewidth=2pt, showpoints=true]{\data}
22
   \end{psgraph}} \quad% end of Cancel
24 \psCancel[linewidth=4pt,strokeopacity=0.5]{\parbox{8cm}{\[
   \ \mbox{binom}\{x_R\}\{y_R\} = \mbox{wnderbrace}{r\mbox{binom}\{A\}\{B\}}_{\mbox{text}}\
25
     cdot
     \underbrace{\begin{pmatrix}
26
        \sin\gamma & -\cos\gamma \\
27
       \cos \gamma & \sin \gamma \\
28
       \end{pmatrix}_{\text{\colored}} \binom{x_K}{y_K} +
29
   \displaystyle \sum_{t=0}^{t_x}_{t_y}_{\text{translation}} \] \ end of psCancel
```

The optional argument cancelType allows to define the lines for the non star version. Possible values are x for a cross, s for a slash, and b for a backslash. It is also possible to use the long words for the slash and the backslash. An empty value is always assumed as a x.

```
first line first line first line second line second line second line second line
```

```
| \psset{linewidth=3pt,strokeopacity=0.4}
| \psCancel{\tabular[b]{c}first line\\second line\endtabular} \quad
| \psCancel[cancelType=x]{\tabular[b]{c}first line\\second line\endtabular}\quad
| \psCancel[cancelType=s]{\tabular[b]{c}first line\\second line\endtabular}\quad
| \psCancel[cancelType=b]{\tabular[b]{c}first line\\second line\endtabular}
| \psCancel[cancelTy
```

20. \psStep 38

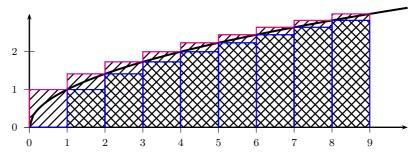
# 20. \psStep

\psStep calculates a step function for the upper or lower sum or the max/min of the Riemann integral definition of a given function. The available option is

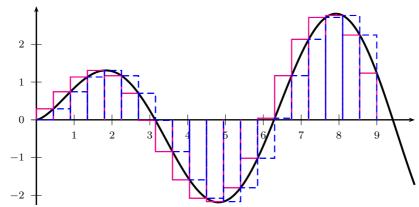
StepType=lower |upper|Riemann|infimum|supremum or alternative StepType=l |u|R|i|s with lower as the default setting. The syntax of the function is

```
\label{eq:psstep} $$ [Options] (()x1,x2){n}{function}$
```

(x1,x2) is the given interval for the step wise calculated function, n is the number of the rectangles and *function* is the mathematical function in postfix or algebraic=true notation (with algebraic=true).



```
begin{pspicture}(-0.5,-0.5)(10,3)
psaxes[labelFontSize=\scriptstyle]{->}(10,3)
psplot[plotpoints=100,linewidth=1.5pt,algebraic=true]{0}{10}{sqrt(x)}
psStep[linecolor=magenta,StepType=upper,fillstyle=hlines](0,9){9}{x sqrt}
psStep[linecolor=blue,fillstyle=vlines](0,9){9}{x sqrt}
end{pspicture}
```



```
psset{plotpoints=200}
begin{pspicture}(-0.5,-2.25)(10,3)

psaxes[labelFontSize=\scriptstyle]{->}(0,0)(0,-2.25)(10,3)

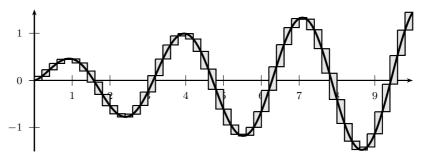
psplot[linewidth=1.5pt,algebraic=true]{0}{10}{sqrt(x)*sin(x)}

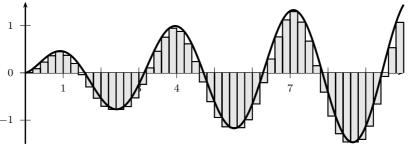
psstep[algebraic=true,linecolor=magenta,StepType=upper](0,9){20}{sqrt(x)*sin(x)}

psstep[linecolor=blue,linestyle=dashed](0,9){20}{x sqrt x RadtoDeg sin mul}

end{pspicture}
```

20. \psStep 39





```
psset{yunit=1.25cm,plotpoints=200}
begin{pspicture}(-0.5,-1.5)(10,1.5)

psaxes[labelFontSize=\scriptstyle]{->}(0,0)(0,-1.5)(10,1.5)

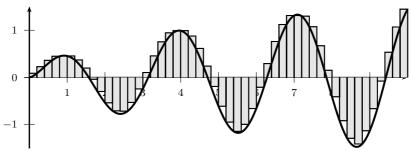
psstep[algebraic=true,StepType=infimum,fillstyle=solid,fillcolor=black
    !10](0,10){50}%

{sqrt(x)*cos(x)*sin(x)}

psplot[linewidth=1.5pt,algebraic=true]{0}{10}{sqrt(x)*cos(x)*sin(x)}

end{pspicture}
```

20. \psStep 40



```
psset{yunit=1.25cm,plotpoints=200}
begin{pspicture}(-0.5,-1.5)(10,1.5)

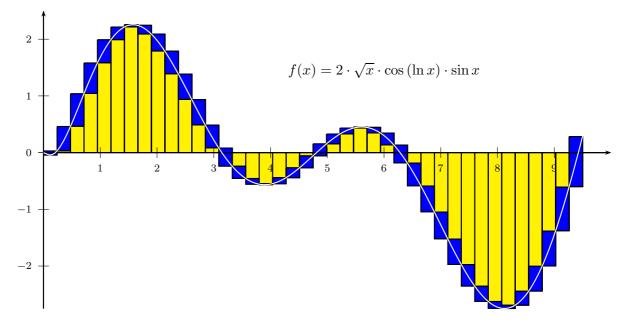
psaxes[labelFontSize=\scriptstyle]{->}(0,0)(0,-1.5)(10,1.5)

psStep[algebraic=true,StepType=supremum,fillstyle=solid,fillcolor=black
    !10](0,10){50}%

sqrt(x)*cos(x)*sin(x)}

psplot[linewidth=1.5pt,algebraic=true]{0}{10}{sqrt(x)*cos(x)*sin(x)}

end{pspicture}
```



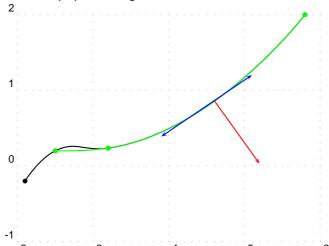
21. Tangent lines 41

# 21. Tangent lines

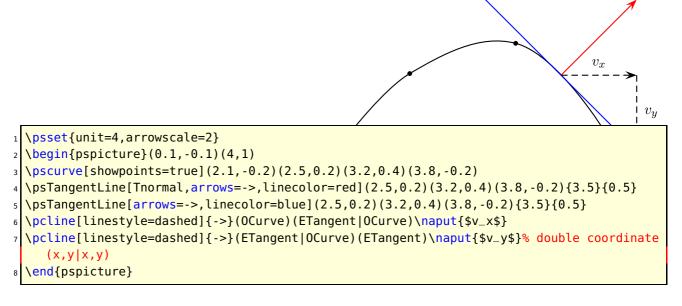
There are two macros for plotting a tangent line or the tangent normal line. The first one is  $\protect\prote$ 

#### 21.1. \psTangentLine and option Tnormal

In special cases one has to use curvature=1 1 1 for the macro \pscurve to get the same equation for the curve as \psplotTangentLine does.



The end points are saved as nodes OCurve, ETangent, and ENormal. They can be used in the default ways for nodes:



#### 21.2. \psplotTangent and option Tnormal

There is an additional option, named Derive for an alternative function (see following example) to calculate the slope of the tangent. This will be in general the first derivative, but can also be any other function. If this option is different to to the default value Perive=default, then this function is taken to calculate the slope. For the other cases, pstricks-add builds a secant with -0.00005 < x < 0.00005, calculates the slope and takes this for the tangent. This may be problematic in some cases of special functions or x values, then it may be appropriate to use the Derive option.

```
\label{local_problem} $$ \problem{$\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\problem{\p
```

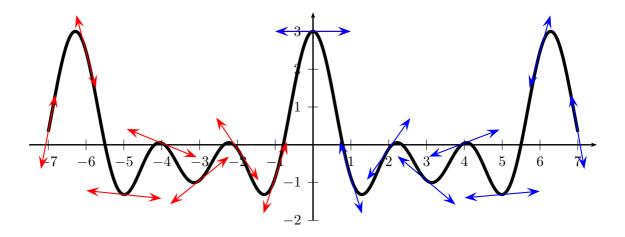
The macro expects three parameters:

x: the x value of the function for which the tangent should be calculated

dx: the dx to both sides of the x value

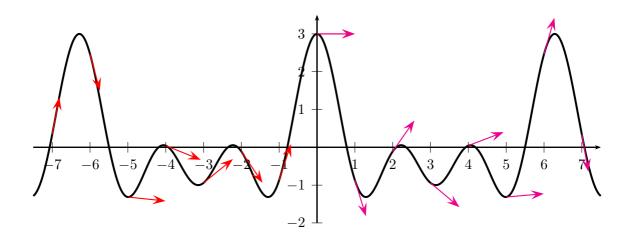
f(x): the function in infix (with option algebraic) or the default postfix (PostScript) notation

The following examples show the use of the algebraic=true option together with the Derive option. Remember that using the algebraic option implies that the angles have to be in the radian unit!



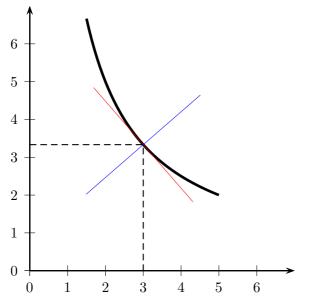
```
1 \def\F{x RadtoDeg dup dup cos exch 2 mul cos add exch 3 mul cos add}
2 \def\Fp{x RadtoDeg dup dup sin exch 2 mul sin 2 mul add exch 3 mul sin 3 mul
add neg}
3 \psset{plotpoints=1001}
4 \begin{pspicture}(-7.5,-2.5)(7.5,4)%X\psgrid
5 \psaxes{->}(0,0)(-7.5,-2)(7.5,3.5)
6 \psplot[linewidth=3\pslinewidth]{-7}{7}{\F}
7 \psset{linecolor=red, arrows=<->, arrowscale=2}
8 \multido{\n=-7+1}{8}{\psplotTangent{\n}{1}{\F}}
9 \psset{linecolor=magenta, arrows=<->, arrowscale=2}%
6 \multido{\n=0+1}{8}{\psplotTangent[linecolor=blue, Derive=\Fp]{\n}{1}{\F}}
11 \end{pspicture}
```

The star version plots only the tangent line in the positive x-direction:



```
1 \def\Falg{cos(x)+cos(2*x)+cos(3*x)} \def\Fpalg{-sin(x)-2*sin(2*x)-3*sin(3*x)}
2 \begin{pspicture}(-7.5,-2.5)(7.5,4)%\psgrid
3 \psaxes{->}(0,0)(-7.5,-2)(7.5,3.5)
4 \psplot[linewidth=1.5pt,algebraic=true,plotpoints=500]{-7.5}{7.5}{\Falg}
```

The next example shows the use of the Derive option to draw the perpendicular line to the tangent.



```
begin{pspicture}(-0.5,-0.5)(7.25,7.25)

def\Func{10 x div}

psaxes[arrowscale=1.5]{->}(7,7)

psplot[linewidth=2pt,algebraic=true]{1.5}{5}{10/x}

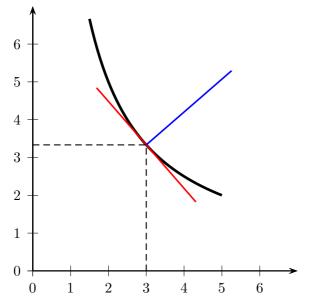
psplotTangent[linewidth=.5\pslinewidth,
    linecolor=red,algebraic=true]{3}{2}{10/x}

psplotTangent[linewidth=.5\pslinewidth,
    linecolor=blue,algebraic=true,Derive=(x*x)/10]{3}{2}{10/x}

psline[linestyle=dashed](!0 /x 3 def \Func)(!3 /x 3 def \Func)(3,0)

end{pspicture}
```

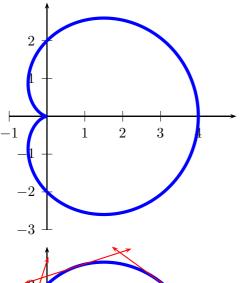
By setting the optional argument Tnormal one can plot the normal of the tangent line. It always starts at the given point.



Let's work with the classical cardioid:  $r=2(1+\cos(\theta))$  and  $\frac{dr}{d\theta}=-2\sin(\theta)$ . The Derive option always expects the  $\frac{dr}{d\theta}$  value and uses internally the equation for the derivative of implicitly defined functions:

$$\frac{dy}{dx} = \frac{r' \cdot \sin \theta + x}{r' \cdot \cos \theta - y}$$

where  $x = r \cdot \cos \theta$  and  $y = r \cdot \sin \theta$ 



```
begin{pspicture}(-1,-3)(5,3)%\psgrid[subgridcolor=
    lightgray]

psaxes{->}(0,0)(-1,-3)(5,3)

psplot[polarplot,linewidth=3\pslinewidth,linecolor=
    blue,%

plotpoints=500]{0}{360}{1 x cos add 2 mul}

end{pspicture}
```

```
begin{pspicture}(-1,-3)(5,3)%\psgrid[subgridcolor=
lightgray]

psaxes{->}(0,0)(-1,-3)(5,3)

psplot[polarplot,linewidth=3\pslinewidth,linecolor=
blue,algebraic=true,plotpoints=500]{0}{6.289}{2*(1+
cos(x))}

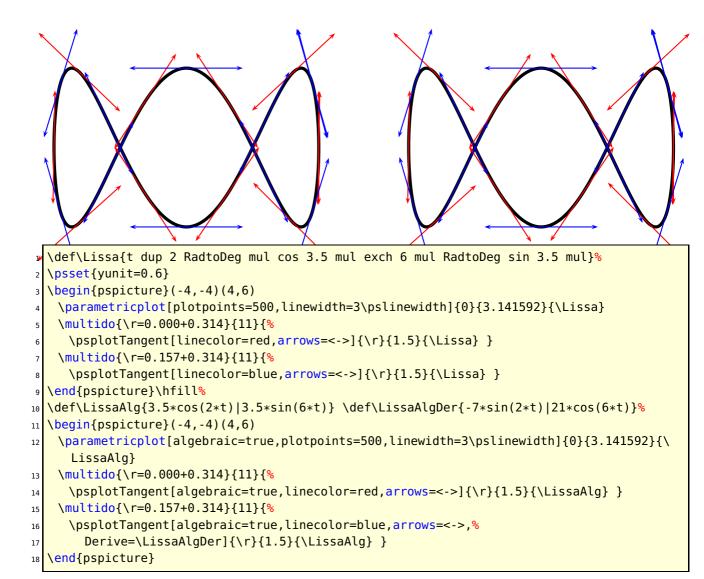
multido{\r=0.000+0.314}{21}{%

psplotTangent[polarplot,Derive=-2*sin(x),algebraic
=true,linecolor=red,arrows=<->]{\r}{1.5}{2*(1+cos(x))}}

end{pspicture}
```

Let's work with a Lissajou curve:  $\left\{ \begin{array}{l} x = 3.5\cos(2t) \\ y = 3.5\sin(6t) \end{array} \right. \text{ whose derivative is : } \left\{ \begin{array}{l} x = -7\sin(2t) \\ y = 21\cos(6t) \end{array} \right.$ 

The parameter must be the letter t instead of x and when using the algebraic=true option you must separate the two equations by a | (see example).



# 22. Successive derivatives of a function

The new PostScript function Derive has been added for plotting successive derivatives of a function. It must be used with the algebraic=true option. This function has two arguments:

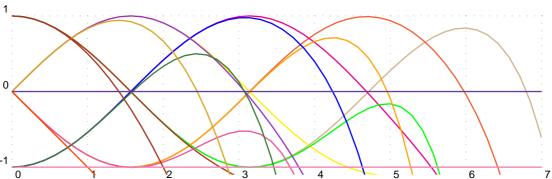
- 1. a positive integer which defines the order of the derivative; obviously 0 means the function itself!
- 2. a function of variable x which can be any function using common operators,

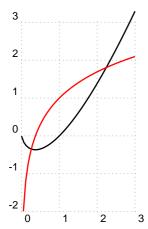
Do not think that the derivative is approximated, the internal PostScript engine will compute the real derivative using a formal derivative engine.

The following diagram contains the plot of the polynomial:

$$f(x) = \sum_{i=0}^{14} \frac{(-1)^i x^{2i}}{i!} = 1 - \frac{x^2}{2} + \frac{x^4}{4!} - \frac{x^6}{6!} + \frac{x^8}{8!} - \frac{x^{10}}{10!} + \frac{x^{12}}{12!} - \frac{x^{14}}{14!}$$

and of its first 15 derivatives. It is the sequence definition of the cosine.





```
begin{pspicture}[shift=-2.5,showgrid=true,linewidth=1pt
   ](0,-2)(3,3)

psplot[algebraic=true]{.001}{3}{x*ln(x)} % f(x)

psplot[algebraic=true,linecolor=red]{.05}{3}{Derive(1,x)}

*ln(x))} % f'(x)=1+ln(x)

end{pspicture}
```

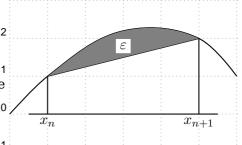
# 23. Variable step for plotting a curve

# 23.1. Theory

As you know with the \psplot macro, the curve is plotted using a piece-wise linear curve. The step is given by the parameter plotpoints. For each step between  $x_i$  and  $x_{i+1}$ , the area defined between the curve and its approximation (a segment) is majored by this formula :

$$|\varepsilon| \le \frac{M_2(f)(x_{i+1} - x_i)^3}{12}$$

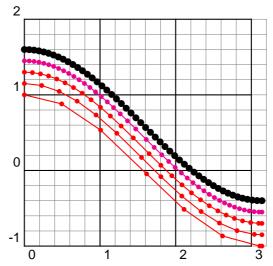
 $M_2(f)$  is a majorant of the second derivative of f in the interval  $[x_i; x_{i+1}]$ .



The parameter VarStep (false by default) activates the variable step algorithm. It is set to a tolerance defined by the parameter VarStepEpsilon (default by default, accept real value). If this parameter is not set by the user, then it is automatically computed using the default first step given by the parameter plotpoints. Then, for each step,  $f''(x_n)$  and  $f''(x_{n+1})$  are computed and the smaller is used as  $M_2(f)$ , and then the step is approximated. This means that the step is constant for second order polynomials.

#### 23.2. The cosine

Different value for the tolerance from 0.01 to 0.0001, a factor 10 between each of them. In black, there is the classic \psplot behavior, and in magenta the default variable step behavior.

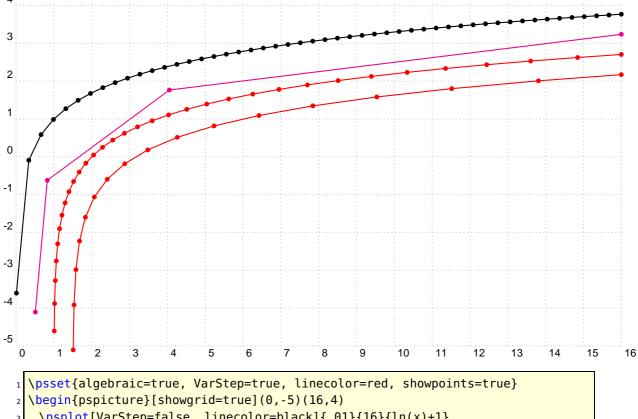


```
| \psset{algebraic=true, VarStep=true, unit=2, showpoints=true, linecolor=red}  
| \begin{pspicture}[showgrid=true](-0,-1)(3.14,2)  
| \psplot[VarStepEpsilon=.01]{0}{3.14}{cos(x)}  
| \psplot[VarStepEpsilon=.001]{0}{3.14}{cos(x)+.15}  
| \psplot[VarStepEpsilon=.0001]{0}{3.14}{cos(x)+.3}  
| \left|
| \psplot[VarStepEpsilon=.0001]{0}{3.14}{cos(x)+.3}  
| \left|
| \psplot[VarStepEpsilon=.0001]{0}{3.14}{cos(x)+.3}  
| \left|
| \psplot[VarStepEpsilon=.0001]{0}{3.14}{cos(x)+.3}  
| \psplot[VarStepEpsilon=.0001]{0}{3.14}{cos(x)+.3}  
| \psplot[VarStepEpsilon=.0001]{0}{0}{0}{0}{0}{0}  
| \text{ | \tex
```

```
psplot[linecolor=magenta]{0}{3.14}{cos(x)+.45}
psplot[VarStep=false,linewidth=1pt,linecolor=black]{-0}{3.14}{cos(x)+.6}
end{pspicture}
```

#### 23.3. The Napierian Logarithm

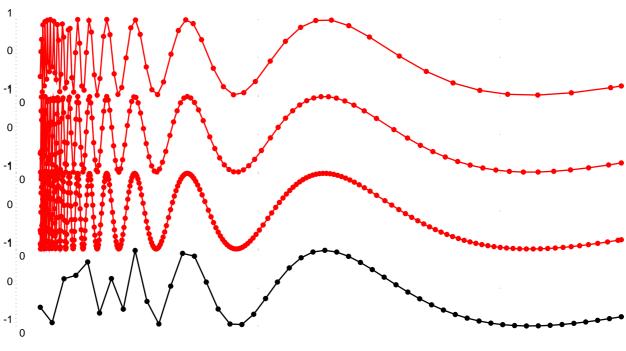
A really classic example which gives a bad beginning, the tolerance is set to 0.001.



```
psset{algebraic=true, VarStep=true, linecolor=red, showpoints=true}
begin{pspicture}[showgrid=true](0,-5)(16,4)
    \psplot[VarStep=false, linecolor=black]{.01}{16}{ln(x)+1}
    \psplot[linecolor=magenta]{.51}{16}{ln(x-1/2)+1/2}
    \psplot[VarStepEpsilon=.001]{1.01}{16}{ln(x-1)}
    \psplot[VarStepEpsilon=.01]{1.51}{16}{ln(x-1.5)-100/200}
    \end{pspicture}
```

#### 23.4. Sine of the inverse of $\boldsymbol{x}$

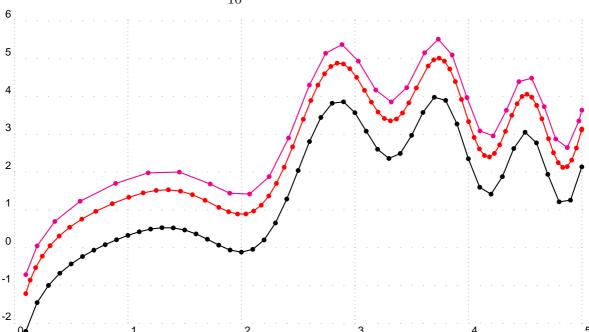
Impossible to draw, but let's try!



# 23.5. A really complicated function

Just appreciate the difference between the normal behavior and the plotting with the varStep option. The function is:

$$f(x) = x - \frac{x^2}{10} + \ln(x) + \cos(2x) + \sin(x^2) - 1$$



```
psset{xunit=3, algebraic=true, VarStep, showpoints=true}
begin{pspicture}[showgrid=true](0,-2)(5,6)

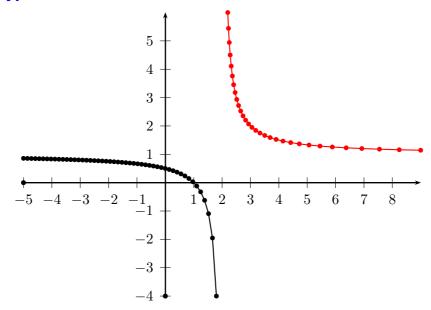
psplot[VarStepEpsilon=.0005, linecolor=red]{.1}{5}{x-x^2/10+ln(x)+cos(2*x)+sin(x^2)}

psplot[linecolor=magenta]{.1}{5}{x-x^2/10+ln(x)+cos(2*x)+sin(x^2)+.5}

psplot[VarStep=false]{.1}{5}{x-x^2/10+ln(x)+cos(2*x)+sin(x^2)-1}
end{pspicture}
```

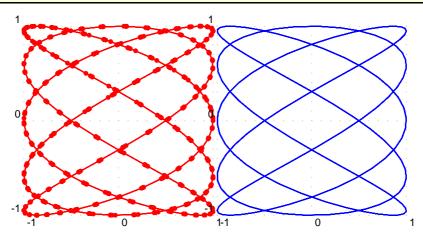
23.6. A hyperbola 53

# 23.6. A hyperbola

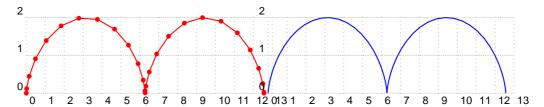


```
psset{algebraic=true, showpoints=true, unit=0.75}
begin{pspicture}(-5,-4)(9,6)
    \psplot[linecolor=black]{-5}{1.8}{(x-1)/(x-2)}
    \psplot[VarStep=true, VarStepEpsilon=.001, linecolor=red]{2.2}{9}{(x-1)/(x-2)}
    \psaxes{->}(0,0)(-5,-4)(9,6)
end{pspicture}
```

### 23.7. Using \psparametricplot

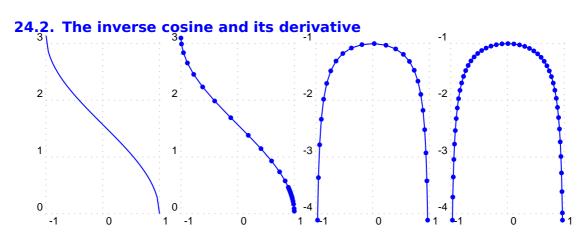


```
| \psset{unit=2.5}
| \text{begin}{pspicture}[showgrid=true](-1,-1)(1,1)
| \parametricplot[algebraic=true,linecolor=red,VarStep=true, showpoints=true,
| VarStepEpsilon=.0001]
| {0}{47.115}{cos(5*t)|sin(3*t)}
| \text{end}{pspicture}
| \text{begin}{pspicture}[showgrid=true](-1,-1)(1,1)
| \parametricplot[algebraic=true,linecolor=blue,VarStep=true, showpoints=false,
| VarStepEpsilon=.0001]
```



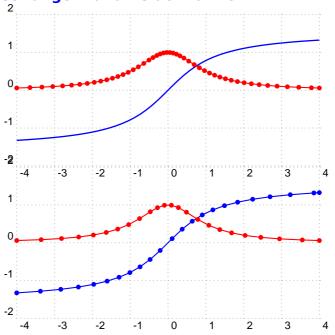
### 24. New math functions and their derivatives

```
11 \begin{pspicture}[showgrid=true](-1,0)(1,4)
12 \psplot[linecolor=red]{-.97}{.97}{Derive(1,asin(x))}
13 \end{pspicture}
14 \hspace{lem}
15 \psset{algebraic=true, VarStep, VarStepEpsilon=.0001, showpoints=true}
16 \begin{pspicture}[showgrid=true](-1,0)(1,4)
17 \psplot[linecolor=red]{-.97}{.97}{Derive(1,asin(x))}
18 \end{pspicture}
```

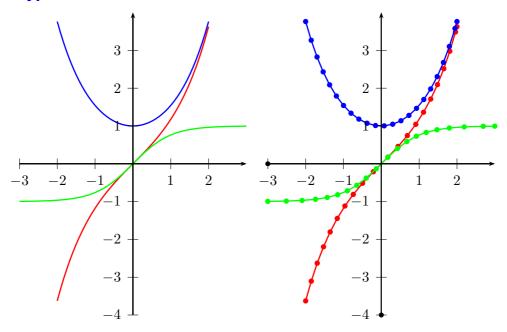


```
\psset{unit=1.5}
  \begin{pspicture}[showgrid=true](-1,0)(1,3)
   \psplot[linecolor=blue,algebraic=true]{-1}{1}{acos(x)}
  \end{pspicture}
  \hspace{1em}
  \psset{algebraic=true, VarStep, VarStepEpsilon=.001, showpoints=true}
  \begin{pspicture}[showgrid=true](-1,0)(1,3)
  \proot{psplot[linecolor=blue]{-.999}{.999}{acos(x)}}
 \end{pspicture}
10 \hspace{1em}
11 \begin{pspicture}[showgrid=true](-1,-4)(1,-1)
12 \psplot[linecolor=red]{-.97}{.97}{Derive(1,acos(x))}
13 \end{pspicture}
14 \hspace{1em}
psset{algebraic=true, VarStep, VarStepEpsilon=.0001, showpoints=true}
16 \begin{pspicture}[showgrid=true](-1,-4)(1,-1)
  \psplot[linecolor=red]{-.97}{.97}{Derive(1,acos(x))}
18 \end{pspicture}
```

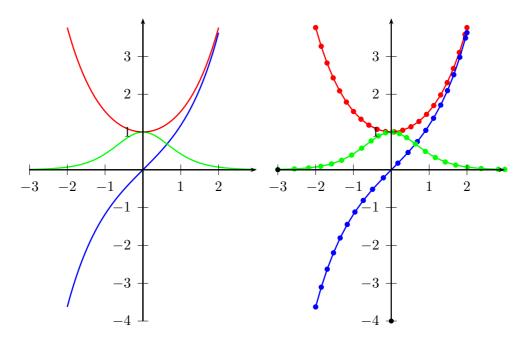
### 24.3. The inverse tangent and its derivative



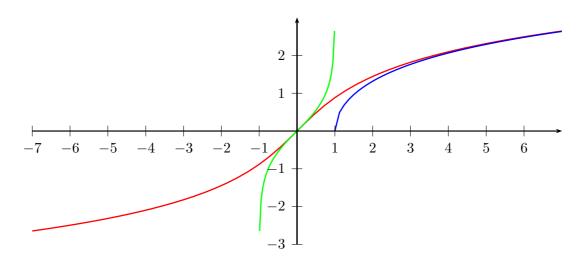
# 24.4. Hyperbolic functions

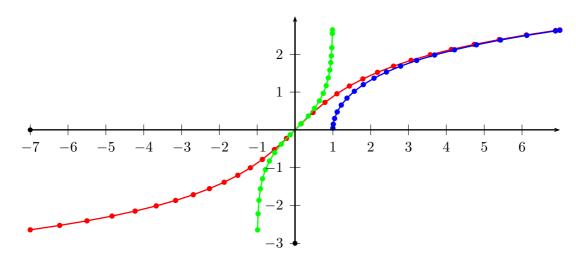


```
\begin{array}{c} \begin{array}{c} \mathbf{begin} \{ pspicture \} (-3, -4) (3, 4) \end{array} \end{array}
                                \psset{algebraic=true}
                                                \psplot[linecolor=red,linewidth=1pt]{-2}{2}{sh(x)}
                                                \psplot[linecolor=blue,linewidth=1pt]{-2}{2}{ch(x)}
                                                 \psplot[linecolor=green,linewidth=1pt]{-3}{3}{th(x)}
                                                 psaxes{->}(0,0)(-3,-4)(3,4)
                                \end{pspicture}
                                \hspace{1em}
                                \begin{array}{c} \begin{array}{c} \\ \\ \end{array} \begin{array}{c} \\ \end{array} \end{array} \begin{array}{c} \\ \end{array} \begin{array}{c} \\ \end{array} \begin{array}{c} \\ \end{array} \begin{array}{c} \\ \end{array} \end{array} \begin{array}{c} \\ \end{array} \end{array} \begin{array}{c} \\ \end{array} \end{array} \begin{array}{c} \\ \end{array} \begin{array}{c}
                              \psset{algebraic=true, VarStep=true, VarStepEpsilon=.001, showpoints=true}
                                                \psplot[linecolor=red,linewidth=1pt]{-2}{2}{sh(x)}
                                                \psplot[linecolor=blue,linewidth=1pt]{-2}{2}{ch(x)}
                                                \psplot[linecolor=green,linewidth=1pt]{-3}{3}{th(x)}
13
                                                 psaxes{->}(0,0)(-3,-4)(3,4)
                              \end{pspicture}
```

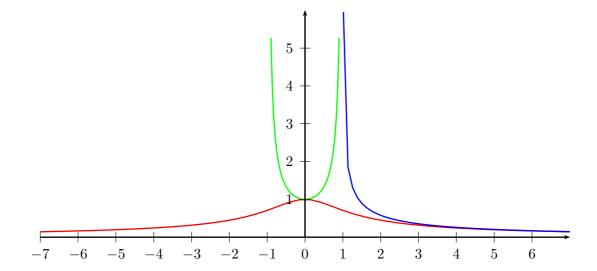


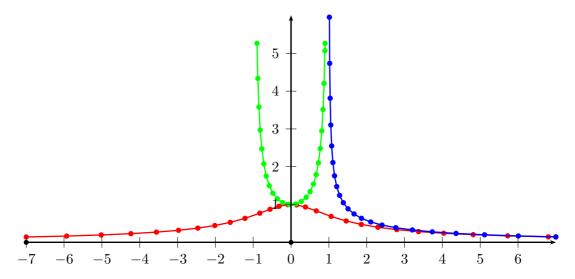
```
\begin{array}{c} \begin{array}{c} \mathbf{begin} \{ pspicture \} (-3, -4) (3, 4) \end{array} \end{array}
   \psset{algebraic=true,linewidth=1pt}
    \psplot[linecolor=red,linewidth=1pt]{-2}{2}{Derive(1,sh(x))}
    \psplot[linecolor=blue,linewidth=1pt]{-2}{2}{Derive(1,ch(x))}
    \psplot[linecolor=green,linewidth=1pt]{-3}{3}{Derive(1,th(x))}
    psaxes{->}(0,0)(-3,-4)(3,4)
  \end{pspicture}
  \hspace{1em}
  \begin{array}{c} \begin{array}{c} \mathbf{begin} \{ pspicture \} (-3, -4) (3, 4) \end{array} \end{array}
  \psset{algebraic=true, VarStep=true, VarStepEpsilon=.001, showpoints=true}
    \psplot[linecolor=red,linewidth=1pt]{-2}{2}{Derive(1,sh(x))}
    \psplot[linecolor=blue,linewidth=1pt]{-2}{2}{Derive(1,ch(x))}
12
    \psplot[linecolor=green,linewidth=1pt]{-3}{3}{Derive(1,th(x))}
    psaxes{->}(0,0)(-3,-4)(3,4)
15 \end{pspicture}
```





```
\begin{array}{c} \begin{array}{c} \\ \\ \end{array} \begin{array}{c} \\ \end{array} \end{array} \begin{array}{c} \\ \end{array} \end{array} \begin{array}{c} \\ \end{array} \end{array} \begin{array}{c} \\ \end{array} \end{array} \begin{array}{c} \\ \end{array} \end{array} \begin{array}{c} \\ \end{array} \begin{array}{c} \\ \end{array} \begin{array}{c} \\ \end{array} \begin{array}{c} \\ \end{array} \end{array} \begin{array}{c} \\ \end{array} \end{array} \begin{array}{c} \\ \end{array} \end{array} \begin{array}{c} \\ \end{array} \begin{array}{c} 
                                 \psset{algebraic=true}
                                             \psplot[linecolor=red,linewidth=1pt]{-7}{7}{Argsh(x)}
                                               \psplot[linecolor=blue,linewidth=1pt]{1}{7}{Argch(x)}
                                                 \psplot[linecolor=green,linewidth=1pt]{-.99}{.99}{Argth(x)}
                                                 psaxes{--}(0,0)(-7,-3)(7,3)
                                 \end{pspicture}\\[\baselineskip]
                               \begin{array}{c} \begin{array}{c} \mathbf{begin} \{ pspicture \} (-7, -3) (7, 3) \end{array} \end{array}
                                                 \psset{algebraic=true, VarStep, VarStepEpsilon=.001, showpoints=true}
                                               \psplot[linecolor=red,linewidth=1pt]{-7}{7}{Argsh(x)}
10
                                             \psplot[linecolor=blue,linewidth=1pt]{1.001}{7}{Argch(x)}
11
                                             \psplot[linecolor=green,linewidth=1pt]{-.99}{.99}{Argth(x)}
                                             psaxes{->}(0,0)(-7,-3)(7,3)
13
                               \end{pspicture}
```





```
\begin{pspicture}(-7,-0.5)(7,6)
  \psset{algebraic=true}
    \psplot[linecolor=red,linewidth=1pt]{-7}{7}{Derive(1,Argsh(x))}
    \psplot[linecolor=blue,linewidth=1pt]{1.014}{7}{Derive(1,Argch(x))}
    \psplot[linecolor=green,linewidth=1pt]{-.9}{.9}{Derive(1,Argth(x))}
    psaxes{->}(0,0)(-7,0)(7,6)
  \end{pspicture}\\[\baselineskip]
  \begin{array}{l} \begin{array}{l} \textbf{begin} \{ pspicture \} (-7, -0.5) (7,6) \end{array} \end{array}
  \psset{algebraic=true}
    \psset{algebraic=true, VarStep=true, VarStepEpsilon=.001, showpoints=true}
10
    \psplot[linecolor=red,linewidth=1pt]{-7}{7}{Derive(1,Argsh(x))}
11
12
    \psplot[linecolor=blue,linewidth=1pt]{1.014}{7}{Derive(1,Argch(x))}
    \psplot[linecolor=green,linewidth=1pt]{-.9}{.9}{Derive(1,Argth(x))}
13
    psaxes{->}(0,0)(-7,0)(7,6)
14
  \end{pspicture}
```

# 25. \psplotDiffEqn - solving diffential equations

A differential equation of first order is like

$$y' = f(x, y, y') \tag{1}$$

where y is a function of x. We define some vectors  $Y = [y, y', \dots, y^{(n-1)}]$  and  $Y' = [y', y'', \dots, y^n]$ , depending on the order n. The syntax of the macro is

$$\verb|\psplotDiffEqn| [Options] $\{x0\}\{x1\}\{y0\}\{f(x,y,y',...)\}$$$

- options: the \psplotDiffEqn specific options and all other of PSTricks, which make sense;
- $x_0$ : the start value;
- $x_1$ : the end value of the definition interval;
- $y_0$ : the initial values for  $y(x_0)$   $y'(x_0)$  ...;
- f(x, y, y', ...): the differential equation, depending to the number of initial values, e.g.: {0 1} for  $y_0$  are two initial values, so that we have a differential equation of second order f(x, y, y') and the macro leaves y y' on the stack.

#### The new options are:

- method: integration method (euler for order 1 euler method, rk4 for 4<sup>th</sup> order Runge-Kutta method);
- whichabs: select the abscissa for plotting the graph, by default it is x, but you can specify a number which represent a position in the vector y;
- whichord: same as precedent for the ordinate, by default y(0);
- plotfuncx: describe a ps function for the abscissa, parameter whichabs becomes useless:
- plotfuncy: idem for the ordinate;
- buildvector: boolean parameter for specifying the input-output of the f description:

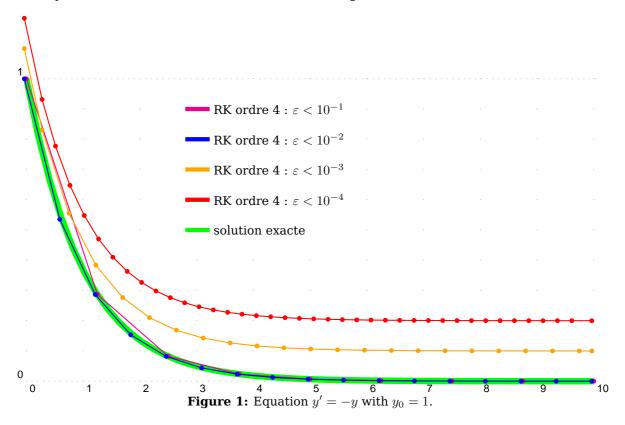
true (default): y is put on the stack element by element, y' must be given in the same way;

false: y is put on the stack as a vector, y' must be returned in the same way;

• algebraic=true: algebraic=true description for f, buildvector parameter is useless when activating this option.

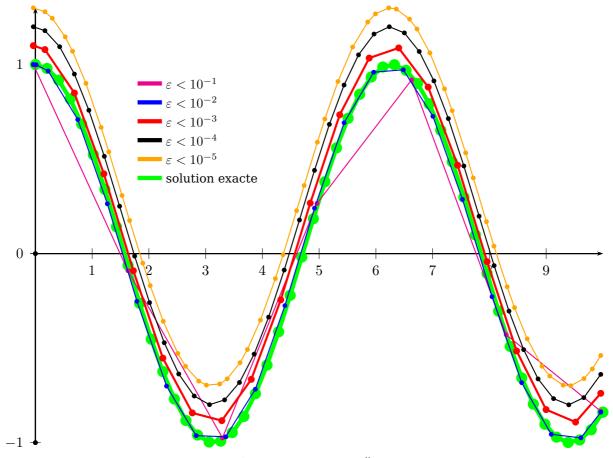
#### 25.1. Variable step for differential equations

A new algorithm has been added for adjusting the step according to the variations of the curve. The parameter method has a new possible value: varrkiv to activate the Runge-Kutta method with variable step, then the parameter varsteptol (real value; .01 by default) can control the tolerance of the algorithm.



```
\def\Funct{neg}\def\FunctAlg{-y[0]}
  \psset{xunit=1.5, yunit=8, showpoints=true}
  \begin{pspicture}[showgrid=true](0,0)(10,1.2)
   \psplot[linewidth=6\pslinewidth, linecolor=green, showpoints=false]{0}{10}{
     Euler x neg exp}
   \psplotDiffEqn[linecolor=magenta, method=varrkiv, varsteptol=.1, plotpoints
     =2]{0}{10}{1}{\mathsf{Funct}}
   \rput(0,.0){\psplotDiffEqn[linecolor=blue, method=varrkiv, varsteptol=.01,
     plotpoints=2]{0}{10}{1}{\Funct}}
   \rput(0,.1){\psplotDiffEqn[linecolor=Orange, method=varrkiv, varsteptol
     =.001, plotpoints=2]{0}{10}{1}{\Funct}}
   \rput(0,.2){\psplotDiffEqn[linecolor=red, method=varrkiv, varsteptol=.0001,
     plotpoints=2]{0}{10}{1}{\Funct}}
   \psset{linewidth=4\pslinewidth,showpoints=false}
   \rput*(3.3,.9){\psline[linecolor=magenta](-.75cm,0)}
10
   \rut*[1](3.3,.9){\small RK ordre 4 : $\varepsilon<10^{-1}$}
11
   \rule (3.3, .8) {\psline[linecolor=blue](-.75cm, 0)}
12
   \rut*[1](3.3,.8){\small RK ordre 4 : $\varepsilon<10^{-2}$}
13
   \rput*(3.3,.7){\psline[linecolor=Orange](-.75cm,0)}
```

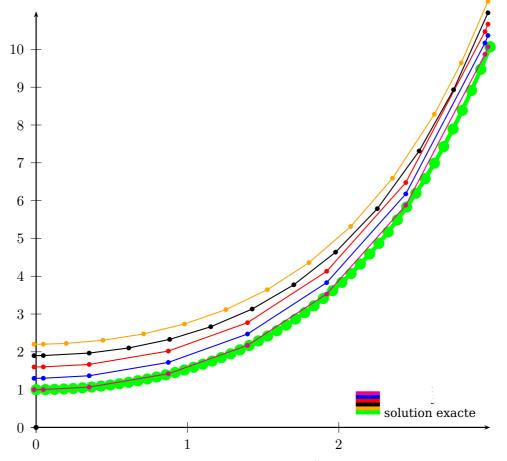
```
15  \rput*[l](3.3,.7){\small RK ordre 4 : $\varepsilon<10^{-3}$}
16  \rput*(3.3,.6){\psline[linecolor=red](-.75cm,0)}
17  \rput*[l](3.3,.6){\small RK ordre 4 : $\varepsilon<10^{-4}$}
18  \rput*(3.3,.5){\psline[linecolor=green](-.75cm,0)}
19  \rput*[l](3.3,.5){\small solution exacte}
20  \end{pspicture}</pre>
```



**Figure 2:** Equation y'' = -y

```
\def\Funct{exch neg}
  \psset{xunit=1.5, yunit=5, method=varrkiv, showpoints=true}%
  \def\quatrepi{12.5663706144}
  \begin{array}{l} \begin{array}{l} \begin{array}{l} \textbf{begin} \{ pspicture \} (0,-1) (10,1.3) \end{array} \end{array}
   psaxes{->}(0,0)(0,-1)(10,1.3)
   \psplot[linewidth=4\pslinewidth, linecolor=green, algebraic=true]{0}{10}{cos
     (x)}
   \rput(0,.0){\psplotDiffEqn[linecolor=magenta, plotpoints=7, varsteptol
     =.1]{0}{10}{1 0}{\mathsf{Funct}}
   \rput(0,.0){\psplotDiffEqn[linecolor=blue, plotpoints=201, varsteptol
     =.01{0}{10}{1 0}{\Funct}}
   \rput(0,.1){\psplotDiffEqn[linewidth=2\pslinewidth, linecolor=red,
     varsteptol=.001]{0}{10}{1 0}{\Funct}}
   10
     Funct}}
```

```
\rput(0,.3){\psplotDiffEqn[linecolor=Orange, varsteptol=.00001]{0}{10}{1
     0}{\Funct}}
   \psset{linewidth=4\pslinewidth,showpoints=false}
12
   \rput*(2.3,.9){\psline[linecolor=magenta](-.75cm,0)}
13
   \rule {1}(2.3,.9){\small $\varepsilon<10^{-1}$}
14
   \rput*(2.3,.8){\psline[linecolor=blue](-.75cm,0)}
15
   \rput*[l](2.3,.8){\small $\varepsilon<10^{-2}$}
16
   \rput*(2.3,.7){\psline[linecolor=red](-.75cm,0)}
17
   \rule *[1](2.3,.7){\small $\varepsilon<10^{-3}$}
18
   \rput*(2.3,.6){\psline[linecolor=black](-.75cm,0)}
19
   \rule *[1](2.3,.6){\small $\operatorname{varepsilon}_{-4}}
20
   \rput*(2.3,.5){\psline[linecolor=Orange](-.75cm,0)}
21
   \rput*[l](2.3,.5){\small $\varepsilon<10^{-5}$}
   \rput*(2.3,.4){\psline[linecolor=green](-.75cm,0)}
23
   \rput*[l](2.3,.4){\small solution exacte}
  \end{pspicture}
```



**Figure 3:** Equation y'' = y

```
1 \def\Funct{exch}
2 \psset{xunit=4, yunit=1, method=varrkiv, showpoints=true}%
3 \def\quatrepi{12.5663706144}
4 \begin{pspicture}(0,-0.5)(3,11)
```

```
psaxes{->}(0,0)(3,11)
          \psplot[linewidth=4\pslinewidth, linecolor=green, algebraic=true]{0}{3}{ch(x
               )}
          \rule (0,.0) \prop \pr
               Funct}}
          \rput(0,.3){\psplotDiffEqn[linecolor=blue, varsteptol=.01]{0}{3}{1 0}{\Funct
          \rput(0,.6){\psplotDiffEqn[linecolor=red, varsteptol=.001]{0}{3}{1 0}{\Funct
          \rput(0,.9){\psplotDiffEqn[linecolor=black, varsteptol=.0001]{0}{3}{1 0}{\
10
               Funct}}
          \rput(0,1.2){\psplotDiffEqn[linecolor=Orange, varsteptol=.00001]{0}{3}{1}
11
               0}{\Funct}}
          \psset{linewidth=4\pslinewidth,showpoints=false}
12
          \rput*(2.3,.9){\psline[linecolor=magenta](-.75cm,0)}
13
          \rule *[1](2.3,.9){\small $\operatorname{varepsilon}<10^{-1}$}
14
          \rput*(2.3,.8){\psline[linecolor=blue](-.75cm,0)}
15
          \rule *[1](2.3,.8){\small $\varepsilon<10^{-2}$}
16
          \rule *(2.3,.7) {\psline[linecolor=red](-.75cm,0)}
17
          \rput*[l](2.3,.7){\small $\varepsilon<10^{-3}$}
18
          \rput*(2.3,.6){\psline[linecolor=black](-.75cm,0)}
19
          \rput*[l](2.3,.6){\small $\varepsilon<10^{-4}$}
20
          \rput*(2.3,.5){\psline[linecolor=Orange](-.75cm,0)}
21
          \rput*[l](2.3,.5){\small $\varepsilon<10^{-5}$}
          \rput*(2.3,.4){\psline[linecolor=green](-.75cm,0)}
23
          \rput*[l](2.3,.4){\small solution exacte}
24
25 \end{pspicture}
```

### 25.2. Equation of second order

Here is the traditional simulation of two stars attracting each other according to the classical gravitation law in  $\frac{1}{r^2}$ . In 2-Dimensions, the system to be solved is composed of four second order differential equations. In order to be described, each of them gives two first order equations, then we obtain a 8 sized vectorial equation. In the following example the masses of the stars are 1 and 20.

$$\begin{cases} x_1'' = \frac{M_2}{r^2} \cos(\theta) \\ y_1'' = \frac{M_2}{r^2} \sin(\theta) \\ x_2'' = \frac{M_1}{r^2} \cos(\theta) \\ y_2'' = \frac{M_1}{r^2} \sin(\theta) \end{cases} \text{ avec } \begin{cases} r^2 = (x_1 - x_2)^2 + (y_1 - y_2)^2 \\ \cos(\theta) = \frac{(x_1 - x_2)}{r} \\ \sin(\theta) = \frac{(y_1 - y_2)}{r} \end{cases}$$

```
% x1 y1 x'1 y'1 x2 y2 x'2 y'2

/yp2 exch def /xp2 exch def /ay2 exch def /ax2 exch def % mise en variables

/yp1 exch def /xp1 exch def /ay1 exch def /ax1 exch def % mise en variables

/ro2 ax2 ax1 sub dup mul ay2 ay1 sub dup mul add def % calcul de r*r

xp1 yp1

ax2 ax1 sub ro2 sqrt div ro2 div

ay2 ay1 sub ro2 sqrt div ro2 div

xp2 yp2

3 index -20 mul

% calcul de x"2=-20x"1

% calcul de y"2=-20y"1
```

**Table 1:** PostScriptsource code for the gravitational interaction

**Table 2:** Algebraic description for the gravitational interaction

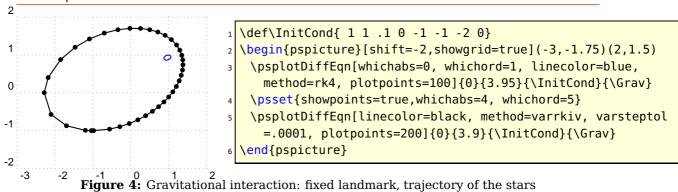
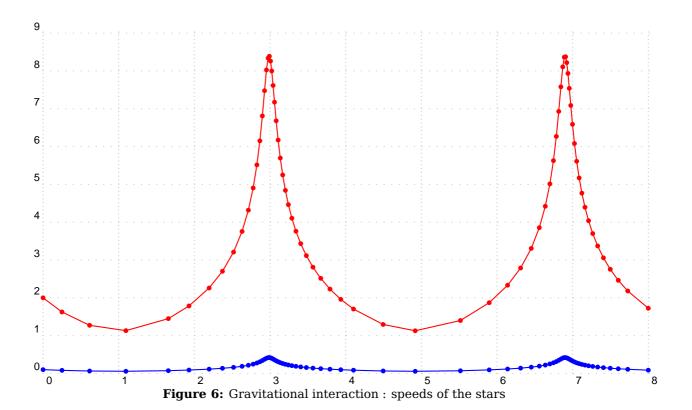


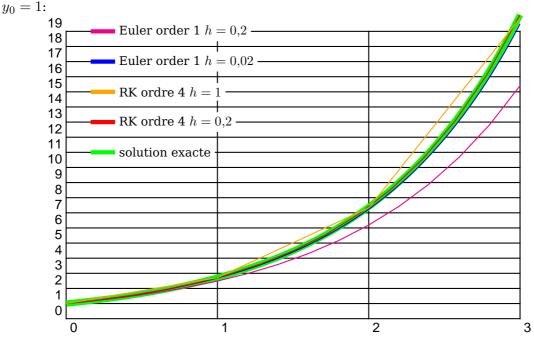
Figure 5: Gravitational interaction: landmark defined by one star



```
1 \psset{xunit=2}
2 \begin{pspicture}[showgrid=true](0,0)(8,9)
3 \psset{showpoints=true}
```

#### Simple equation of first order y' = y

For the initial value y(0)=1 we have the solution  $y(x)=e^x$ . y is always on the stack, so we have to do nothing. Using the algebraic=true option, we write it as y[0]. The following example shows different solutions depending to the number of plotpoints with



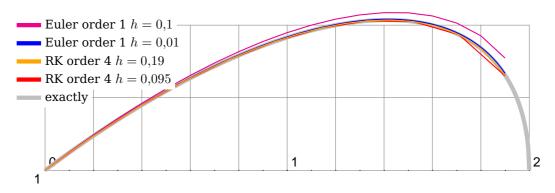
```
\psset{xunit=4, yunit=.4}
  \begin{pspicture}(3,19)\psgrid[subgriddiv=1]
   \psplot[linewidth=6\pslinewidth, linecolor=green]{0}{3}{Euler x exp}
   \psplotDiffEqn[linecolor=magenta,plotpoints=16,algebraic=true]{0}{3}{1}{y
     [0]}
   \psplotDiffEqn[linecolor=blue,plotpoints=151]{0}{3}{1}{}
   \psplotDiffEqn[linecolor=red,method=rk4,plotpoints=15]{0}{3}{1}{}
    \psplotDiffEqn[linecolor=Orange,method=rk4,plotpoints=4]{0}{3}{1}{}
   \psset{linewidth=4\pslinewidth}
   \rule *(0.35,19) {\psline[linecolor=magenta](-.75cm,0)}
   \rput*[l](0.35,19){\small Euler order 1 $h=0{,}2$}
10
   \rput*(0.35,17){\psline[linecolor=blue](-.75cm,0)}
11
   \rule *[l](0.35,17){\small Euler order 1 $h=0{,}02$}
12
   \rput*(0.35,15){\psline[linecolor=0range](-.75cm,0)}
13
   \rput*[l](0.35,15){\small RK ordre 4 $h=1$}
14
   \rput*(0.35,13){\psline[linecolor=red](-.75cm,0)}
15
   \rule *[1](0.35,13){\small RK ordre 4 $h=0{,}2$}
16
   \rule *(0.35,11) {\psline[linecolor=green](-.75cm,0)}
17
   \rput*[l](0.35,11){\small solution exacte}
19 \end{pspicture}
```

$$y' = \frac{2 - ty}{4 - t^2}$$

For the initial value y(0) = 1 the exact solution is  $y(x) = \frac{t + \sqrt{4 - t^2}}{2}$ . The function f described in PostScript code is like (y is still on the stack):

```
x %% y x
mul %% x*y
2 exch sub %% 2-x*y
4 x dup mul %% 2-x*y 4 x^2
sub %% 2-x*y 4-x^2
div %% (2-x*y)/(4-x^2)
```

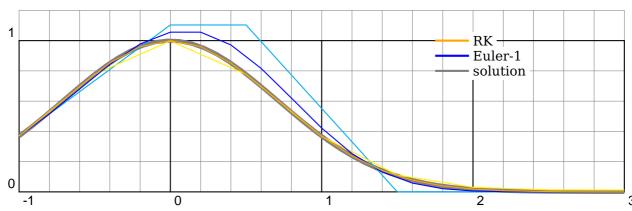
The following example uses  $y_0 = 1$ .



```
1 \psset{xunit=6.4, yunit=9.6, showpoints=false}
 \begin{pspicture}(0,1)(2,1.7) \psgrid[subgriddiv=5]
  { \psset{linewidth=4\pslinewidth,linecolor=lightgray}
  \proonup \{0\}\{1.8\}\{x \ dup \ dup \ mul \ 4 \ exch \ sub \ sqrt \ add \ 2 \ div\}
   \proonup \{1.8\}{2}{x dup dup mul 4 exch sub sqrt add 2 div} 
   \def\InitCond{1}
6
   \def\Func{x mul 2 exch sub 4 x dup mul sub div}
   \psplotDiffEqn[linecolor=magenta, plotpoints=20]{0}{1.9}{\InitCond}{\Func}
   \psplotDiffEqn[linecolor=blue, plotpoints=191]{0}{1.9}{\InitCond}{\Func}
   \psplotDiffEqn[linecolor=red, method=rk4, plotpoints=11,%
10
     algebraic=true]\{0\}\{1.9\}\{\setminus InitCond\}\{(2-x*y[0])/(4-x^2)\}
11
   \psplotDiffEqn[linecolor=Orange, method=rk4, plotpoints=21,%
12
     algebraic=true]\{0\}\{1.9\}\{\setminus InitCond\}\{(2-x*y[0])/(4-x^2)\}
13
   \psset{linewidth=4\pslinewidth}
14
   \t (0.3,1.6) \
15
     order 1 h=0\{,\}1\}
   \t (0.3,1.55) {\psline[linecolor=blue](-.75cm,0)}\rput*[l](0.3,1.55) {\small Euler order}
16
      1 $h=0{,}01$}
   \t (0.3,1.5) 
17
     $h=0{,}19$}
```

```
y' = -2xy
```

```
For y(-1) = \frac{1}{e} we get y(x) = e^{-x^2}.
```



```
\psset{unit=4}
                     \begin{pspicture}(-1,0)(3,1.1)\psgrid
                                \psplot[linewidth=4\pslinewidth,linecolor=gray]{-1}{3}{Euler x dup mul neg
                                                   exp}
                                \psset{plotpoints=9}
                                  \protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\pro
                                  \protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\pro
                                                 mul}
                                \psset{plotpoints=21}
                                  \proonup {1}{psplotDiffEqn[linecolor=blue]{-1}{3}{1 Euler div}{x -2 mul mul}}
                                  \protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\pro
                               \psset{linewidth=2\pslinewidth}
                               \rput*(2,1){\psline[linecolor=0range](-0.25,0)}
11
                                \rput*[l](2,1){RK}
12
                               \rput*(2,.9){\psline[linecolor=blue](-0.25,0)}
13
                               \rput*[l](2,.9){\textsc{Euler}-1}
14
                               \rput*(2,.8){\psline[linecolor=gray](-0.25,0)}
15
                              \rput*[l](2,.8){solution}
                     \end{pspicture}
```

# **Spiral of Cornu**

The integrals of Fresnel:

$$x = \int_0^t \cos \frac{\pi t^2}{2} dt \tag{2}$$

$$x = \int_0^t \cos \frac{\pi t^2}{2} dt$$

$$y = \int_0^t \sin \frac{\pi t^2}{2} dt$$
(2)

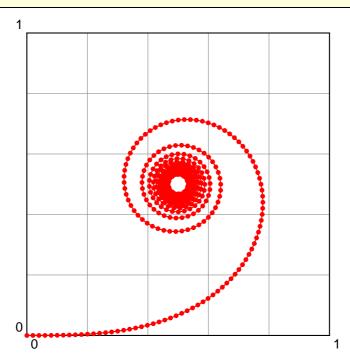
with

$$\dot{x} = \cos \frac{\pi t^2}{2}$$

$$\dot{y} = \sin \frac{\pi t^2}{2}$$
(5)

$$\dot{y} = \sin\frac{\pi t^2}{2} \tag{5}$$

```
\psset{unit=8}
\begin{pspicture}(1,1)\psgrid[subgriddiv=5]
 \psplotDiffEqn[whichabs=0,whichord=1,linecolor=red,method=rk4,algebraic=true
   plotpoints = 500, showpoints = true] \{0\} \{10\} \{0\ 0\} \{cos(Pi*x^2/2) \mid sin(Pi*x^2/2)\} \}
\end{pspicture}
```



#### Lotka-Volterra

The Lotka-Volterra model describes interactions between two species in an ecosystem, a predator and a prey. This represents our first multi-species model. Since we are considering two species, the model will involve two equations, one which describes how the prey population changes and the second which describes how the predator population changes.

For concreteness let us assume that the prey in our model are rabbits, and that the predators are foxes. If we let R(t) and F(t) represent the number of rabbits and foxes, respectively, that are alive at time t, then the Lotka-Volterra model is:

$$\dot{R} = a \cdot R - b \cdot R \cdot F \tag{6}$$

$$\dot{F} = e \cdot b \cdot R \cdot F - c \cdot F \tag{7}$$

where the parameters are defined by:

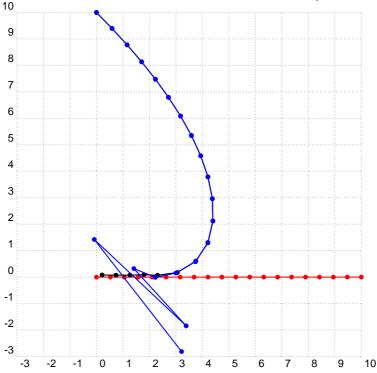
a is the natural growth rate of rabbits in the absence of predation,

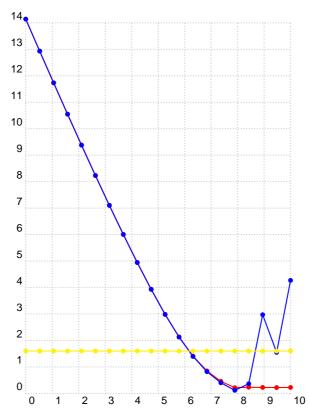
c is the natural death rate of foxes in the absence of food (rabbits),

b is the death rate per encounter of rabbits due to predation,

e is the efficiency of turning predated rabbits into foxes.

The Stella model representing the Lotka-Volterra model will be slightly more complex than the single species models we've dealt with before. The main difference is that our model will have two stocks (reservoirs), one for each species. Each species will have its own birth and death rates. In addition, the Lotka-Volterra model involves four parameters rather than two. All told, the Stella representation of the Lotka-Volterra model will use two stocks, four flows, four converters and many connectors.





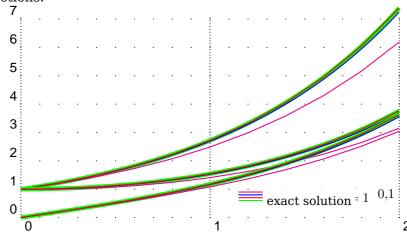
```
mul add sqrt,linecolor=blue]{0}{10}{\InitCond}{\Faiglelapin}

psplotDiffEqn[plotfuncy=pop Func aload pop pop dup mul exch dup mul add sqrt,
linecolor=yellow]{0}{10}{\InitCond}{\Faiglelapin}

lend{pspicture}
```

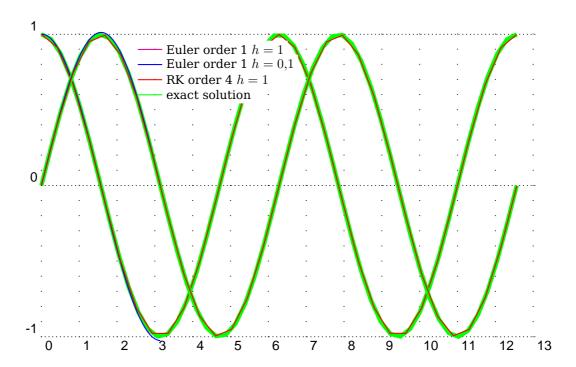
### y'' = y

Beginning with the initial equation  $y(x) = Ae^x + Be^{-x}$  we get the hyperbolic trigonometrical functions.



```
\def\Funct{exch} \psset{xunit=5cm, yunit=0.75cm}
         \begin{pspicture}(0,-0.25)(2,7)\psgrid[subgriddiv=1,griddots=10]
          \proonup \
          \psplotDiffEqn[linecolor=magenta, plotpoints=11]{0}{2}{1 1}{\Funct}
          \psplotDiffEqn[linecolor=blue, plotpoints=101]{0}{2}{1 1}{\Funct}
           \psplotDiffEqn[linecolor=red, method=rk4, plotpoints=11]{0}{2}{1 1}{\Funct}
           \psplot[linewidth=4\pslinewidth, linecolor=green]{0}{2}{Euler dup x exp %ch(x)
                   exch x neg exp add 2 div}
          \psplotDiffEqn[linecolor=magenta, plotpoints=11]{0}{2}{1 0}{\Funct}
           \psplotDiffEqn[linecolor=blue, plotpoints=101]{0}{2}{1 0}{\Funct}
          \psplotDiffEqn[linecolor=red, method=rk4, plotpoints=11]{0}{2}{1 0}{\Funct}
11
         \psplot[linewidth=4\pslinewidth, linecolor=green]{0}{2}{Euler dup x exp
12
                      exch x neg exp sub 2 div\} %sh(x)
13
       \psplotDiffEqn[linecolor=magenta, plotpoints=11]{0}{2}{0 1}{\Funct}
15
          \psplotDiffEqn[linecolor=blue, plotpoints=101]{0}{2}{0 1}{\Funct}
         \psplotDiffEqn[linecolor=red, method=rk4, plotpoints=11]{0}{2}{0 1}{\Funct}
         \t (1.3,.9) \psline[linecolor=magenta](-.75cm,0) \put*[l](1.3,.9) \small\textsc{
                  Euler} order 1 $h=1$}
          \rule (1.3,.8) \psline[linecolor=blue](-.75cm,0) \rule *[l](1.3,.8) \small\textsc{Euler}
18
                  } order 1 $h=0{,}1$}
         \t (1.3,.7) \psline[linecolor=red](-.75cm,0) \rput*[l](1.3,.7) \small RK order 4 $h
         \runtering \runterin
                  solution}
21 \end{pspicture}
```

```
y'' = -y
```



```
\def\Funct{exch neg}
      \psset{xunit=1, yunit=4}
      \def\quatrepi{12.5663706144}%4pi=12.5663706144
      \begin{pspicture}(0,-1.25)(\quatrepi,1.25)\psgrid[subgriddiv=1,griddots=10]
        \psplot[linewidth=4\pslinewidth,linecolor=green]{0}{\quatrepi}{x RadtoDeg cos
              }%cos(x)
        \psplotDiffEqn[linecolor=blue, plotpoints=201]{0}{3.1415926}{1 0}{\Funct}
        \protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\pro
             Funct}
        \psplot[linewidth=4\pslinewidth,linecolor=green]{0}{\quatrepi}{x RadtoDeg sin
             } %%sin(x)
       \psplotDiffEqn[linecolor=blue,plotpoints=201]{0}{3.1415926}{0 1}{\Funct}
       \psplotDiffEqn[linecolor=red,method=rk4, plotpoints=31]{0}{\quatrepi}{0 1}{\
              Funct}
11 \rput*(3.3,.9){\psline[linecolor=magenta](-.75cm,0)}\rput*[l](3.3,.9){\small
             Euler order 1 $h=1$}
12 \rput*(3.3,.8) \\psline[linecolor=blue](-.75cm,0) \\rput*[l](3.3,.8) \\small
             Euler order 1 h=0\{,\}1\}
13 \rput*(3.3,.7) \\psline[linecolor=red](-.75cm,0) \\rput*[l](3.3,.7) \\small RK
             order 4 $h=1$}
14 \rput*(3.3,.6){\psline[linecolor=green](-.75cm,0)}\rput*[l](3.3,.6){\small
             exact solution}
      \end{pspicture}
```

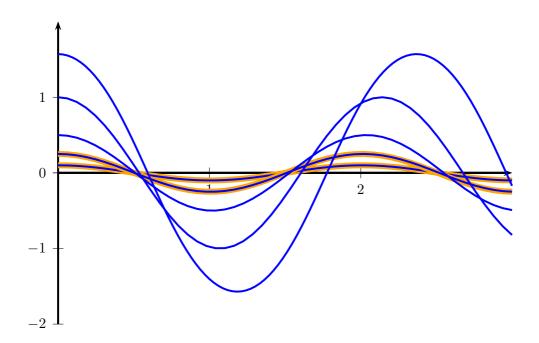
# The mechanical pendulum: $y'' = -\frac{g}{l}\sin(y)$

For small oscillations  $\sin(y) \simeq y$ :

$$y(x) = y_0 \cos\left(\sqrt{\frac{g}{l}}x\right)$$

The function f is written in PostScript code:

```
exch RadtoDeg sin -9.8 mul % y' -gsin(y)
```

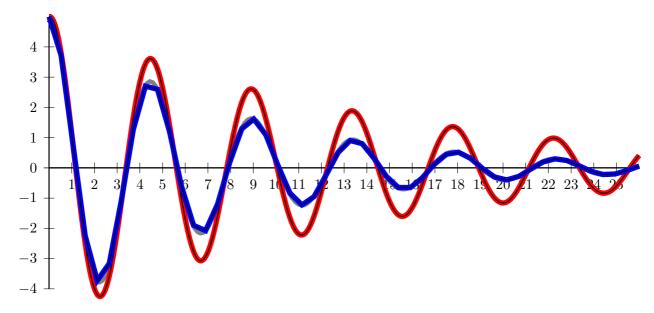


```
1 \def\Func{y[1]|-9.8*sin(y[0])}
2 \psset{yunit=2, xunit=4, algebraic=true, linewidth=1.5pt}
3 \begin{pspicture}(0, -2.25)(3, 2.25)
4 \psaxes{->}(0,0)(0,-2)(3,2)
5 \psplot[linewidth=3\pslinewidth, linecolor=0range]{0}{3}{.1*cos(sqrt(9.8)*x)}
6 \psset{method=rk4, plotpoints=50, linecolor=blue}
7 \psplotDiffEqn{0}{3}{.1 0}{\Func}
8 \psplot[linewidth=3\pslinewidth, linecolor=0range]{0}{3}{.25*cos(sqrt(9.8)*x)}
9 \psplotDiffEqn{0}{3}{.25 0}{\Func}
\psplotDiffEqn{0}{3}{.5 0}{\Func}
\psplotDiffEqn{0}{3}{.1 0}{\Func}
\psplotDiffEqn{0}{3}{.1 0}{\Func}
\psplotDiffEqn{0}{3}{.1 0}{\Func}
\psplotDiffEqn{0}{3}{.1 0}{\Func}
\psplotDiffEqn[plotpoints=100]{0}{.1 0}{.1 0}{\Func}
\psplotDiffEqn[plotpoints=100]{0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0}{.1 0
```

$$y'' = -\frac{y'}{4} - 2y$$

For  $y_0 = 5$  and  $y'_0 = 0$  the solution is:

$$5e^{-\frac{x}{8}}\left(\cos\left(\omega x\right) + \frac{\sin(\omega x)}{8\omega}\right) \text{ avec } \omega = \frac{\sqrt{127}}{8}$$

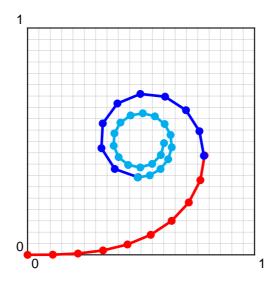


```
\psset{xunit=.6,yunit=0.8,plotpoints=500}
         \begin{pspicture}(0,-4.25)(26,5.25)
              psaxes{->}(0,0)(0,-4)(26,5)
              \protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\pro
                      Euler x -8 div exp x 127 sqrt 8 div mul RadtoDeg dup cos 5 mul exch sin
                             127 sqrt div 5 mul add mul}
              \psplotDiffEqn[linecolor=red,linewidth=5\pslinewidth]{0}{26}{5 0}
                      {dup 3 1 roll -4 div exch 2 mul sub}
              [0]}
              \psset{method=rk4, plotpoints=50}
              \label{linear} $$ \pslinewidth=5\pslinewidth]{0}{26}{5} 0}{\$} $$
10
                         dup 3 1 roll -4 div exch 2 mul sub}
11
              \psplotDiffEqn[linecolor=black,algebraic=true]{0}{26}{5 0}{y[1]|-y[1]/4-2*y
12
                     [0]}
         \end{pspicture}
```

## 25.3. Save final state of a equation

With the macros \BeginSaveFinalState and \EndSaveFinalState the end values of a differential equation can be saved and then used with the optional argument GetFinalState as starting values for another equation.

```
\psset{unit=10cm,linewidth=2pt}
  \begin{pspicture}(1,1)\psgrid[subgridcolor=black!20,subgriddiv=20]
  \BeginSaveFinalState
   \psplotDiffEqn[
    whichabs=0, whichord=1, linecolor=red, method=rk4,
    plotpoints=10, showpoints=true]{0}{1}{0 0}{
    x dup mul 2 div 180 mul cos %% dx/dt
    x dup mul 2 div 180 mul sin % dy/dt
10
  \psplotDiffEqn[GetFinalState,
11
    whichabs=0, whichord=1, linecolor=blue, method=rk4, %SaveFinalState,
12
    plotpoints=10, showpoints=true]{1}{2}{0 0}{
13
14
    x dup mul 2 div 180 mul cos %% dx/dt
15
    x dup mul 2 div 180 mul sin % dy/dt
16
17
  \psplotDiffEqn[GetFinalState,
18
    whichabs=0, whichord=1, linecolor=cyan, method=rk4, %SaveFinalState,
19
    plotpoints=19, showpoints=true]{2}{3}{0 0 }{
    pop pop
21
    x dup mul 2 div 180 mul cos %% dx/dt
    x dup mul 2 div 180 mul sin %% dy/dt
23
24
  \EndSaveFinalState
25
  \end{pspicture}
```



# 26. \psMatrixPlot

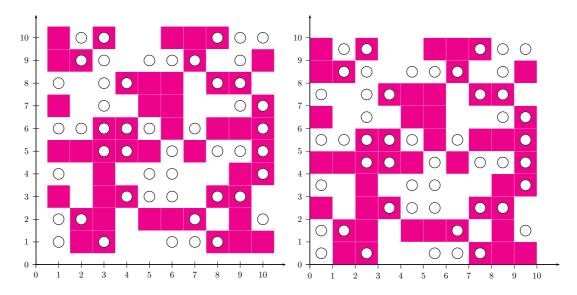
This macro allows you to visualize a matrix. The datafile must be defined as a PostScript matrix named dotmatrix:

```
/dotmatrix [ % <----- important line
0 1 1 0 0 0 0 1 1 1
      0 1 1 1 0 1 0
1 0 1 1 0 0 0 1 1 0
 0 1 0 0 0 0 0 1 1
1 1 1 1 1 0 1 0 0 1
   1
      1
       0 1 0 1
                1 1
1 0 0 0 1 1 0 0 0 1
0 0 0 1 1 1 0 1 1 0
1 1 0 0 0 0 1 0 0 1
1 0 1 0 0 1 1 1 0 0
 def
        % <----- important line
```

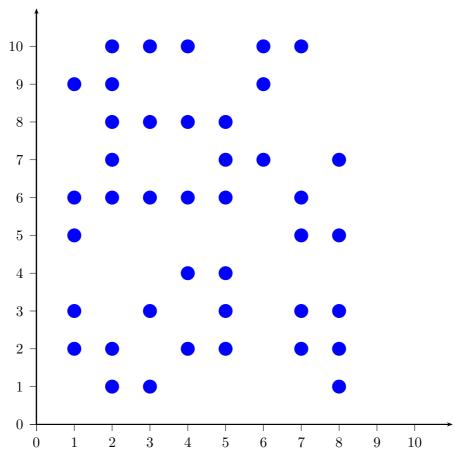
Only the value 0 is important, in which case nothing happens, and for all other cases a dot is printed. The syntax of the macro is:

```
\verb|\psMatrixPlot[Options]| \{rows\} \{columns\} \{data\ file\}|
```

The matrix is scanned line by line from the the first one to the last. In general it appears as a bottom-to-top version of the above listed matrix, the first row 0110000111 is the first plotted line (y=1). With the option ChangeOrder=true it looks exactly like the above view.



```
psscalebox{0.6}{%
begin{pspicture}(-0.5,-0.75)(11,11)
  \psaxes[ticksize=-5pt 0]{->}(11,11)
  \psMatrixPlot[dotsize=1.1cm,dotstyle=square*,linecolor=magenta]%
  {10}{10}{matrix.data}
  \psMatrixPlot[dotsize=.5cm,dotstyle=o,ChangeOrder]{10}{10}{matrix.data}
```



```
begin{pspicture}(-0.5,-0.75)(11,11)

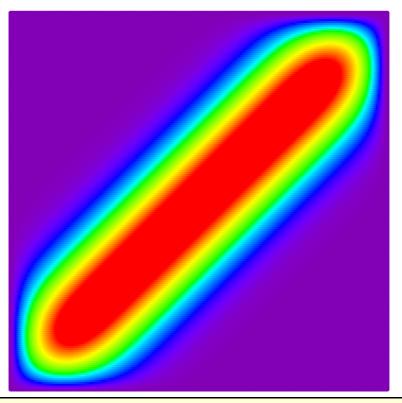
psaxes[ticksize=-5pt 0]{->}(11,11)

psMatrixPlot[dotscale=3,dotstyle=*,linecolor=blue]{10}{8}{matrix.data}

end{pspicture}
```

With the colorType=1 the data is printed as continuous color in the range of the wavelength. The smallest value of the data array is set to red and the biggest value is set to violett. All other values are substituted by the corresponding color of the wavlength. colorType=2 ist the same, but vice versa with the color, from violet to red. colorType=3 is the grayscale image and colorType=4 the same invers.

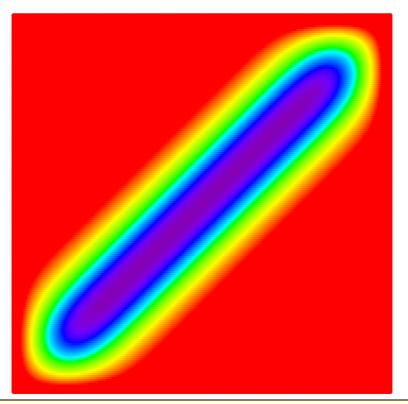
The following examples use a  $200\times200$  matrix data, which is saved as /dotmatrix [...] in the file pstricks-add-doc.dat.



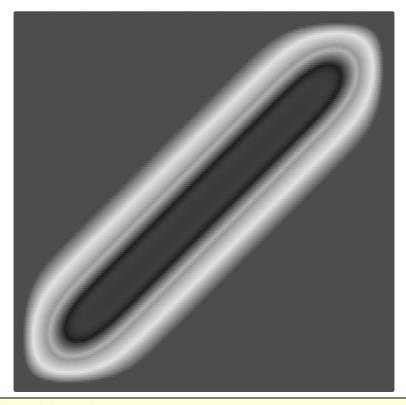
<sup>1 \</sup>begin{pspicture}(10,10)

psMatrixPlot[colorType=1,xStep=0.05,yStep=0.05]{200}{200}{dotmatrix.data}

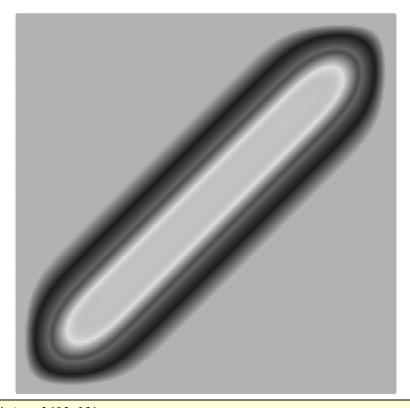
<sup>3 \</sup>end{pspicture}



\begin{pspicture}(10,10)
\psMatrixPlot[colorType=2,xStep=0.05,yStep=0.05]{200}{200}{dotmatrix.data}
\end{pspicture}

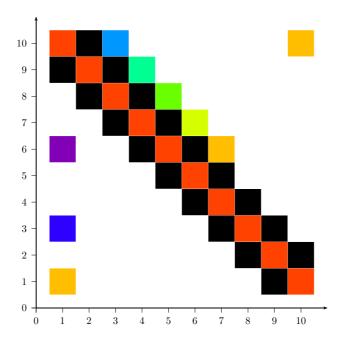


1 \begin{pspicture}(10,10)
2 \psMatrixPlot[colorType=3,xStep=0.05,yStep=0.05]{200}{200}{dotmatrix.data}
3 \end{pspicture}



1 \begin{pspicture}(10,10)
2 \psMatrixPlot[colorType=4,xStep=0.05,yStep=0.05]{200}{200}{dotmatrix.data}
3 \end{pspicture}

With the colorType=5 the color setting can be user defined by the optional argument colorTypeDef. On the stack is the current value which can be used for the setting but must be left on the stack when everything is finished. The following example prints the 0 as color white, the value 1 as black and all other values depending to the corresponding gray value.



```
\begin{filecontents}{matrix1.data}
  /dotmatrix [ % <----- important line
 3 0 0 0 0 0 0 0 1 2
  0 0 0 0 0 0 0 1 2 1
  8 0 0 0 0 0 1 2 1 0
  0 0 0 0 0 1 2 1 0 0
  0 0 0 0 1 2 1 0 0 0
   0 0 1 2 1 3 0 0 0
  0 0 1 2 1 4 0 0 0 0
  0 1 2 1 5 0 0 0 0 0
  1 2 1 6 0 0 0 0 0 0
12 2 1 7 0 0 0 0 0 0 3
13 ] def % <----- important line</pre>
  \end{filecontents}
15 \psscalebox{0.7}{%
16 \begin{pspicture}(-0.5, -0.75)(11,11)
17 \psaxes[ticksize=-5pt 0]{->}(11,11)
  \psMatrixPlot[
18
   colorType=5,
19
   colorTypeDef={
20
     dup /value exch def % save value and leave one on the stack
21
     value Min sub dMaxMin div neg 1 add 300 mul 400 add \pswavelengthToGRAY
22
     value 0 eq \pslbrace 1 \psrbrace if %
23
     value 1 eq \pslbrace 0 \psrbrace if
24
     setgray
```

```
26     },
27     dotsize=1.1cm,xStep=1,yStep=1,dotstyle=square*]{10}{10}{matrix1.data}
28     \end{pspicture}}
```

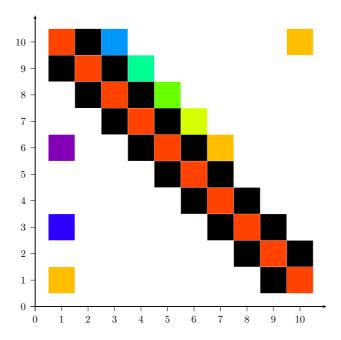
if statements in the color definition must be enclosed with \pslbrace and \psrbrace when they are parentheses used in PostScript. In the above example the color definition should be modified when the matrix is a real big one, in such a case a nested ifelse makes more sense:

```
colorTypeDef={
  dup /value exch def
  value 0 eq
    \pslbrace 1 setgray \psrbrace
    \pslbrace value 1 eq
    \pslbrace 0 setgray \psrbrace
    \pslbrace Min sub dMaxMin div neg 1 add 300 mul 400 add
    \pswavelengthToGRAY setgray \psrbrace ifelse
    \psrbrace ifelse
},
```

Replace the \pslbrace and \psrbrace with { and } if it maybe confusing to read:

```
dup /value exch def
value 0 eq
{ 1 setgray }
{ value 1 eq
      { 0 setgray }
      { Min sub dMaxMin div neg 1 add 300 mul 400 add
      \pswavelengthToGRAY setgray } ifelse
} ifelse
```

Another possibility is to define the color procedure onside the data file, where it *must* be named colorTypeDef. If such a definition exists, the one from the optional argument colorTypeDef will be ignored. There can be no TEX-specific code inside this definition because it is read on PostScript level, the reason why \pswavelengthToGRAY cannot be used.



```
\begin{filecontents}{matrix1.data}
  /colorTypeDef {
   dup /value exch def
   value 0 eq
     { 1 setgray }
     { value 1 eq
       { 0 setgray }
       { Min sub dMaxMin div neg 1 add 300 mul 400 add
         \pswavelengthToRGB not possible
         tx@addDict begin wavelengthToRGB Red Green Blue end
10
        setrqbcolor
11
      } ifelse
12
     } ifelse
13
14 } def
/dotmatrix [ % <----- important line
16 3 0 0 0 0 0 0 0 1 2
17 0 0 0 0 0 0 0 1 2 1
18 8 0 0 0 0 0 1 2 1 0
  0 0 0 0 0 1 2 1 0 0
20 0 0 0 0 1 2 1 0 0 0
21 9 0 0 1 2 1 3 0 0 0
22 0 0 1 2 1 4 0 0 0 0
23 0 1 2 1 5 0 0 0 0 0
24 1 2 1 6 0 0 0 0 0 0
25 2 1 7 0 0 0 0 0 0 3
26 ] def % <----- important line
27 \end{filecontents}
28 \psscalebox{0.7}{%
29 \begin{pspicture}(-0.5,-0.75)(11,11)
30 \psaxes[ticksize=-5pt 0]{->}(11,11)
31 \psMatrixPlot[colorType=5,dotsize=1.1cm,xStep=1,yStep=1,
dotstyle=square*]{10}{10}{matrix1.data}
```

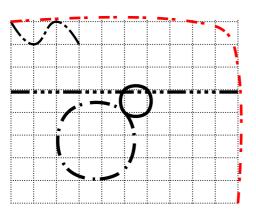
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```
33 \end{pspicture}}
```

# 27. Dashed Lines

Tobias Nähring has implemented an enhanced feature for dashed lines. The number of arguments is no longer limited.

```
dash=value1 unit value2 unit ...
```



```
1 \psset{linewidth=2.5pt,unit=0.6}
  \begin{array}{c} \mathbf{begin} \{ pspicture \} (-5, -4) (5, 4) \end{array}
   \psgrid[subgriddiv=0,griddots=10,gridlabels
     =0pt]
    \psset{linestyle=dashed}
    \pscurve[dash=5mm 1mm 1mm,linewidth
      =0.1](-5,4)(-4,3)(-3,4)(-2,3)
    \psline[dash=5mm 1mm 1mm 1mm 1mm 1mm 1
     mm 1mm 1mm](-5,0.9)(5,0.9)
    \protect\operatorname{psccurve}[linestyle=solid](0,0)(1,0)(1,1)
    \psccurve[linestyle=dashed,dash=5mm 2mm
      0.1 0.2, linetype=0](0,0)(-2.5,0)
      (-2.5, -2.5)(0, -2.5)
    \pscurve[dash=3mm 3mm 1mm,linecolor=
      red, linewidth=2pt](5,-4)(5,2)(4.5,3.5)
      (3,4)(-5,4)
10 \end{pspicture}
```

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# 28. Arrows

#### 28.1. Definition

pstricks-add defines the following "'arrows"':

Value	Example	Name
-		None
<->	<b>←</b>	Arrowheads.
>-<	<b></b>	Reverse arrowheads.
<<->>	<del>****</del>	Double arrowheads.
>>-<<	<b>»</b> ——«	Double reverse arrowheads.
-	<del></del>	T-bars, flush to endpoints.
*- *	<del></del>	T-bars, centered on endpoints.
[-]	<del></del>	Square brackets.
] - [	1———[	Reversed square brackets.
( - )	<del>(                                    </del>	Rounded brackets.
) - (	)———(	Reversed rounded brackets.
0-0	00	Circles, centered on endpoints.
*-*	•	Disks, centered on endpoints.
00-00	oo	Circles, flush to endpoints.
**-**	•	Disks, flush to endpoints.
<->	<b>├</b>	T-bars and arrows.
>-<	<b>——</b>	T-bars and reverse arrows.
h-h		left/right hook arrows.
H-H	>	left/right hook arrows.
v - v	<b>←</b> >	left/right inside vee arrows.
V - V	>	left/right outside vee arrows.
f - f		left/right inside filled arrows.
F-F		left/right outside filled arrows.
t-t		left/right inside slash arrows.
T-T		left/right outside slash arrows.

You can also mix and match, e.g.,  $\rightarrow$ , \*-) and [-> are all valid values of the arrows parameter. The parameter can be set with

or for some macros with a special option, like

\psline[<general options>]{<arrow type>}(A)(B)
\psline[linecolor=red,linewidth=2pt]{|->}(0,0)(0,2)

# 28.2. Multiple arrows

There are two new options which are only valid for the arrow type << or >>. nArrow sets both, the nArrowA and the nArrowB parameter. The meaning is declared in the following

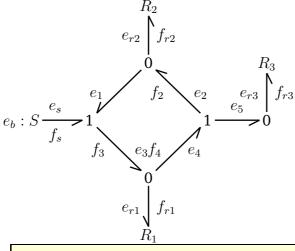
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tables. Without setting one of these parameters the behaviour is like the one described in the old PSTricks manual.

Value	Meaning	
->>	-A	
<<->>	A-A	
<<-	A-	
>>-	B-	
-<<	-B	
>>-<<	B-B	
>>->>	B-A	
<<<	A-B	

Value	Example
\psline{->>}(0,1ex)(2.3,1ex)	<b></b>
\psline[nArrowsA=3]{->>}(0,1ex)(2.3,1ex)	<b></b>
\psline[nArrowsA=5]{->>}(0,1ex)(2.3,1ex)	<b></b>
\psline{<<-}(0,1ex)(2.3,1ex)	<b>**</b>
\psline[nArrowsA=3]{<<-}(0,1ex)(2.3,1ex)	
\psline[nArrowsA=5]{<<-}(0,1ex)(2.3,1ex)	
\psline{<<->>}(0,1ex)(2.3,1ex)	<b>──</b>
\psline[nArrowsA=3]{<<->>}(0,1ex)(2.3,1ex)	<b>****</b>
\psline[nArrowsA=5]{<<->>}(0,1ex)(2.3,1ex)	<b>*********</b>
\psline{<<- }(0,1ex)(2.3,1ex)	<b>**</b>
\psline[nArrowsA=3]{<<-<<}(0,1ex)(2.3,1ex)	₩ ₩
\psline[nArrowsA=5]{<<-0}(0,1ex)(2.3,1ex)	<del>~~~~</del> 0
\psline[nArrowsA=3,nArrowsB=4]{<<-<}(0,1ex)(2.3,1ex)	
\psline[nArrowsA=3,nArrowsB=4]{>>->>}(0,1ex)(2.3,1ex)	<b>&gt;&gt;&gt;&gt;</b>
\psline[nArrowsA=1,nArrowsB=4]{>>->>}(0,1ex)(2.3,1ex)	<b>&gt;&gt;&gt;&gt;</b>

# 28.3. hookarrow



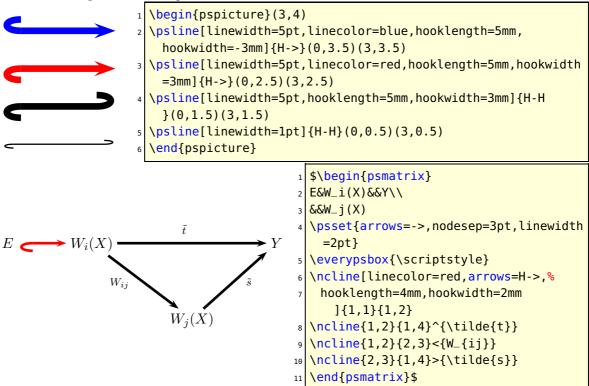
\psset{arrowsize=8pt,arrowlength=1,linewidth=1pt,nodesep=2pt,shortput=tablr}

```
2 \large
  \begin{psmatrix}[colsep=12mm,rowsep=10mm]
      & & $R_2$
                     //
      & & 0 & & $R_3$\\
  $e_b:S$ & 1 & & 1 & 0 \\
      & & 0
                     11
      & & $R_1$
                     11
 \end{psmatrix}
  \ncline{h-}{1,3}{2,3}<{$e_{r2}$}>{$f_{r2}$}\ncline{-h}{2,3}{3,2}<{$e_1$}
11 \ncline{-h}{3,1}{3,2}^{$e_s$}_{$f_{s}$} \ncline{-h}{3,2}{4,3}>{$e_3$}<{$f_3$}
13 \ncline{-h}{3,4}{3,5}^{$e_5$}
14 \ncline{-h}{3,5}{2,5}<{$e_{r3}$}>{$f_{r3}$}
15 \ncline{-h}{4,3}{5,3}<{$e_{r1}$}>{$f_{r1}$}
```

### 28.4. hookrightarrow and hookleftarrow

This is another type of arrow and is abbreviated with H. The length and width of the hook is set by the new options hooklength and hookwidth, which are by default set to  $\protect{hooklength=3mm,hookwidth=1mm}$ 

If the line begins with a right hook then the line ends with a left hook and vice versa:



### 28.5. ArrowInside Option

It is now possible to have arrows inside lines and not only at the beginning or the end. The new defined options

Name	Example	Output
ArrowInside	\psline[ArrowInside=->](0,0)(2,0)	<del></del>
ArrowInsidePos	\psline[ArrowInside=->,%	<del></del>
	ArrowInsidePos=0.25](0,0)(2,0)	
ArrowInsidePos	\psline[ArrowInside=->,%	<del></del>
	ArrowInsidePos=10](0,0)(2,0)	
ArrowInsideNo	\psline[ArrowInside=->,%	$\rightarrow$
	ArrowInsideNo=2](0,0)(2,0)	
ArrowInsideOffset	\psline[ArrowInside=->,%	$\longrightarrow$
	ArrowInsideNo=2,%	
	ArrowInsideOffset=0.1](0,0)(2,0)	
ArrowInside	\psline[ArrowInside=->]{->}(0,0)(2,0)	$\longrightarrow$
ArrowInsidePos	\psline[ArrowInside=->,%	$\rightarrow$
	ArrowInsidePos=0.25]{->}(0,0)(2,0)	
ArrowInsidePos	\psline[ArrowInside=->,%	<b>→</b>
	ArrowInsidePos=10]{->}(0,0)(2,0)	
ArrowInsideNo	\psline[ArrowInside=->,%	$\rightarrow \rightarrow \rightarrow$
	ArrowInsideNo=2]{->}(0,0)(2,0)	
ArrowInsideOffset	\psline[ArrowInside=->,%	$\longrightarrow \longrightarrow$
	ArrowInsideNo=2,%	
	ArrowInsideOffset=0.1]{->}(0,0)(2,0)	
ArrowFill	\psline[ArrowFill=false,%	<b>─</b>
	arrowinset=0]{->}(0,0)(2,0)	
ArrowFill	\psline[ArrowFill=false,%	
	arrowinset=0]{«-»}(0,0)(2,0)	
ArrowFill	\psline[ArrowInside=->,%	$\longrightarrow \longrightarrow \longrightarrow$
	arrowinset=0,%	
	ArrowFill=false,%	
	ArrowInsideNo=2,%	
	ArrowInsideOffset=0.1]{->}(0,0)(2,0)	

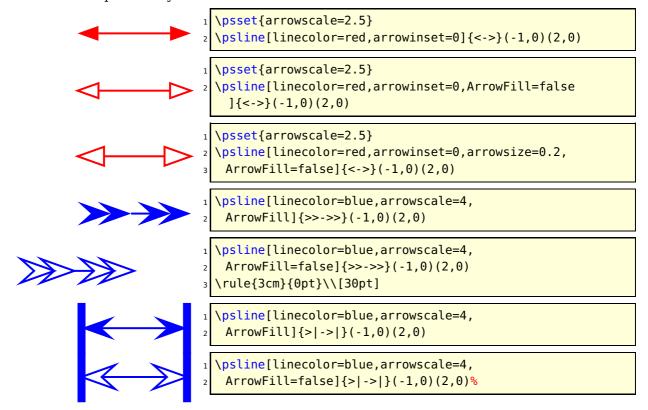
Without the default arrow definition there is only the one inside the line, defined by the type and the position. The position is relative to the length of the whole line. 0.25 means at 25% of the line length. The peak of the arrow gets the coordinates which are calculated by the macro. If you want arrows with an absolute position difference, then choose a value greater than 1, e.g. 10 which places an arrow every 10 pt. The default unit pt cannot be changed.

The ArrowInside takes only arrow definitions like -> into account. Arrows from right to left (<-) are not possible and ignored. If you need such arrows, change the order of the pairs of coordinates for the line or curve macro.

### 28.6. ArrowFill Option

By default all arrows are filled polygons. With the option ArrowFill=false there are "white" arrows. Only for the beginning/end arrows are they empty, the inside arrows

are overpainted by the line.



## 28.7. Examples

All examples are printed with \psset{arrowscale=2,linecolor=red}.

#### **\psline**

```
begin{pspicture}(2,2)
psset{arrowscale=2,ArrowFill=true}
psline[ArrowInside=->]{|<->|}(2,1)

dend{pspicture}

begin{pspicture}(2,2)
psset{arrowscale=2,ArrowFill=true}
psline[ArrowInside=-|]{|-|}(2,1)
dend{pspicture}

begin{pspicture}(2,2)
psset{arrowscale=2,ArrowFill=true}
psline[ArrowInside=->,ArrowInsideNo=2]{->}(2,1)
dend{pspicture}
```

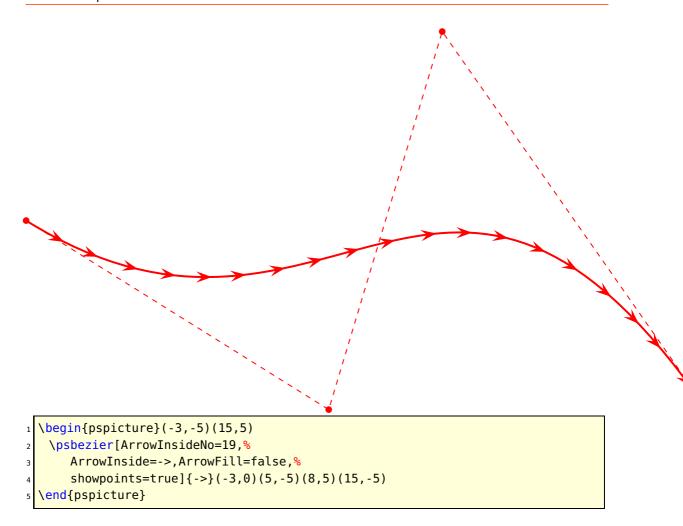
```
\begin{pspicture}(2,2)
\psset{arrowscale=2,ArrowFill=true}
\psline[ArrowInside=->,ArrowInsideNo=2,ArrowInsideOffset
\end{pspicture}
                      \begin{pspicture}(6,2)
                      \psset{arrowscale=2,ArrowFill=true}
                      \psline[ArrowInside=-*]\{->\}(0,0)(2,1)(3,0)
                         (4,0)(6,2)
                       \end{pspicture}
                       \begin{pspicture}(6,2)
                      \psset{arrowscale=2,ArrowFill=true}
                       \psline[ArrowInside=-*,ArrowInsidePos
                        =0.25 \{->\} \{0,0\} \{2,1\} \{3,0\} \{4,0\} \{6,2\}
                       \end{pspicture}
                       \begin{pspicture}(6,2)
                       \psset{arrowscale=2,ArrowFill=true}
                       \psline[ArrowInside=-*,ArrowInsidePos
                        =0.25, ArrowInsideNo=2] { ->}%
                         (0,0)(2,1)(3,0)(4,0)(6,2)
                       \end{pspicture}
                      \begin{pspicture}(6,2)
                       \psset{arrowscale=2,ArrowFill=true}
                      \psline[ArrowInside=->, ArrowInsidePos
                        =0.25 \{->\}%
                             (0,0)(2,1)(3,0)(4,0)(6,2)
                       \end{pspicture}
                       \begin{pspicture}(6,2)
                      \psset{arrowscale=2,ArrowFill=true}
                      \psline[linestyle=none,ArrowInside=->,
                        ArrowInsidePos=0.25]{->}%
                             (0,0)(2,1)(3,0)(4,0)(6,2)
                      \end{pspicture}
                       \begin{pspicture}(6,2)
                       \psset{arrowscale=2,ArrowFill=true}
                       \psline[ArrowInside=-<, ArrowInsidePos</pre>
                        =0.75]{->}%
                          (0,0)(2,1)(3,0)(4,0)(6,2)
                      \end{pspicture}
                       \begin{pspicture}(6,2)
                      \psset{arrowscale=2,ArrowFill=true,
                        ArrowInside=-*}
                       \protect{psline}(0,0)(2,1)(3,0)(4,0)(6,2)
                      \psset{linestyle=none}
                      \protect\operatorname{Posline}[ArrowInsidePos=0](0,0)(2,1)(3,0)
                         (4,0)(6,2)
                      \protect\operatorname{Posline}[ArrowInsidePos=1](0,0)(2,1)(3,0)
                         (4,0)(6,2)
                       \end{pspicture}
```

```
\begin{pspicture}(6,5)
                                       \psset{arrowscale=2,ArrowFill=true}
                                       \psline[ArrowInside=->,ArrowInsidePos
                                         =20](0,0)(3,0)%
                                             (3,3)(1,3)(1,5)(5,5)(5,0)(7,0)(6,3)
                                       \end{pspicture}
                                       \begin{pspicture}(6,2)
                                       \psset{arrowscale=2,ArrowFill=true}
                                       \psline[ArrowInside=-|]{<->}(0,2)(2,0)
                                         (3,2)(4,0)(6,2)
                                       \end{pspicture}
\pspolygon
                                       \begin{pspicture}(6,3)
                                       \psset{arrowscale=2}
                                       \pspolygon[ArrowInside=-|](0,0)(3,3)(6,3)
                                         (6,1)
                                       \end{pspicture}
                                       \begin{pspicture}(6,3)
                                       \psset{arrowscale=2}
                                       \pspolygon[ArrowInside=->,ArrowInsidePos
                                           (0,0)(3,3)(6,3)(6,1)
                                        \end{pspicture}
                                       \begin{pspicture}(6,3)
                                       \psset{arrowscale=2}
                                       \pspolygon[ArrowInside=->,ArrowInsideNo=4]
                                             (0,0)(3,3)(6,3)(6,1)
                                       \end{pspicture}
                                       \begin{pspicture}(6,3)
                                       \psset{arrowscale=2}
                                       \pspolygon[ArrowInside=->,ArrowInsideNo=4,
                                         ArrowInsideOffset=0.1](0,0)(3,3)(6,3)
                                           (6,1)
                                        \end{pspicture}
```

```
\begin{pspicture}(6,3)
                                           \psset{arrowscale=2}
                                           \protect\operatorname{\mathsf{Npspolygon}}[\operatorname{ArrowInside=-}](0,0)(3,3)(6,3)
                                           \psset{linestyle=none,ArrowInside=-*}
                                           \pspolygon[ArrowInsidePos=0](0,0)(3,3)
                                             (6,3)(6,1)
                                           \pspolygon[ArrowInsidePos=1](0,0)(3,3)
                                             (6,3)(6,1)
                                           \psset{ArrowInside=-o}
                                           \pspolygon[ArrowInsidePos=0.25](0,0)(3,3)
                                             (6,3)(6,1)
                                           \pspolygon[ArrowInsidePos=0.75](0,0)(3,3)
                                             (6,3)(6,1)
                                           \end{pspicture}
                                           \begin{pspicture}(6,5)
                                           \psset{arrowscale=2}
                                            \pspolygon[ArrowInside=->,ArrowInsidePos
                                              (0,0)(3,0)(3,3)(1,3)(1,5)(5,5)(5,0)
                                                (7,0)(6,3)
                                           \end{pspicture}
\psbezier
                         \begin{pspicture}(3,3)
                         \psset{arrowscale=2}
                           \protect{
| psbezier[ArrowInside=-|](0,1)(1,0)(2,1)(3,3)}

                           \psset{linestyle=none,ArrowInside=-o}
                           \protection [ArrowInsidePos=0.25](0,1)(1,0)(2,1)(3,3)
                           \protect{psbezier[ArrowInsidePos=0.75](0,1)(1,0)(2,1)(3,3)}
                           \psset{linestyle=none,ArrowInside=-*}
                           \protect{psbezier[ArrowInsidePos=0](0,1)(1,0)(2,1)(3,3)}
                           \protection [ArrowInsidePos=1](0,1)(1,0)(2,1)(3,3)
                         \end{pspicture}
                               \begin{pspicture}(4,3)
                               \psset{arrowscale=2}
                               \psbezier[ArrowInside=->,showpoints]%
                                \{*-*\}(0,0)(2,3)(3,0)(4,2)
                               \end{pspicture}
```

```
\begin{pspicture}(4,3)
\psset{arrowscale=2}
 \psbezier[ArrowInside=->,showpoints=true,
    ArrowInsideNo=2](0,0)(2,3)(3,0)(4,2)
\end{pspicture}
\begin{pspicture}(4,3)
\psset{arrowscale=2}
 \psbezier[ArrowInside=->,showpoints=true,
   ArrowInsideNo=2, ArrowInsideOffset=-0.2]%
    \{->\}(0,0)(2,3)(3,0)(4,2)
\end{pspicture}
     \begin{pspicture}(5,3)
     \psset{arrowscale=2}
      \psbezier[ArrowInsideNo=9,ArrowInside=-|,%
        showpoints=true]\{*-*\}(0,0)(1,3)(3,0)(5,3)
     \end{pspicture}
\begin{pspicture}(4,3)
\psset{arrowscale=2}
 \psset{ArrowInside=-|}
 \psbezier[ArrowInsidePos=0.25,showpoints=true
   ]*-*(2,3)(3,0)(4,2)
 \psset{linestyle=none}
 \protect{psbezier}[ArrowInsidePos=0.75](0,0)(2,3)(3,0)(4,2)
end{pspicture}
     \begin{pspicture}(5,6)
     \psset{arrowscale=2}
      \poode(3,4){A}\poode(5,6){B}\poode(5,0){C}
      \psbezier[ArrowInside=->,%
         showpoints=true](A)(B)(C)
      \psset{linestyle=none,ArrowInside=-<}</pre>
      \psbezier[ArrowInsideNo=4](0,0)(A)(B)(C)
      \psset{ArrowInside=-0}
       \psbezier[ArrowInsidePos=0.1](0,0)(A)(B)(C)
      \psbezier[ArrowInsidePos=0.9](0,0)(A)(B)(C)
      \psset{ArrowInside=-*}
      \psbezier[ArrowInsidePos=0.3](0,0)(A)(B)(C)
  12
      \psbezier[ArrowInsidePos=0.7](0,0)(A)(B)(C)
     \end{pspicture}
```



### **\pcline**

These examples need the package pst-node.

#### \pccurve

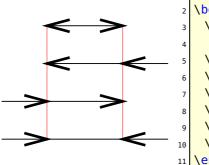
These examples also need the package pst-node.

```
\begin{pspicture}(2,2)
 \psset{arrowscale=2}
 \pccurve[ArrowInside=->,ArrowInsidePos=0.65,showpoints=true
  ]*-*(0,0)(2,2)
 \naput[labelsep=0.3]{\large$h$}
 \end{pspicture}
\begin{pspicture}(2,2)
 \psset{arrowscale=2}
 \pccurve[ArrowInside=->,ArrowInsideNo=3,showpoints=true
  ]\{|->\}(0,0)(2,2)
 \naput[labelsep=0.3]{\large$i$}
 \end{pspicture}
           \begin{pspicture}(4,4)
           \psset{arrowscale=2}
k
           \pccurve[ArrowInside=->,ArrowInsidePos=20]{|-|}(0,0)
           \naput[labelsep=0.3]{\large$k$}
            \end{pspicture}
```

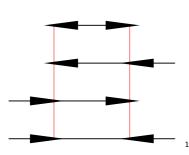
#### 28.8. Special arrows v-V,t-T, and f-F

Possible optional arguments are

name	meaning	
veearrowlength	default is 3mm	
veearrowangle	default is 30	
veearrowlinewidth	default is 0.35mm	
filledveearrowlength	default is 3mm	
filledveearrowangle	default is 15	
filledveearrowlinewidth	default is 0.35mm	
tickarrowlength	default is 1.5mm	
tickarrowlinewidth	default is 0.35mm	
arrowlinestyle	default is solid	



```
1 \psset{unit=5mm}
2 \begin{pspicture}(4,6)
3 \psset{dimen=middle,arrows=c-c,
4 arrowscale=2,linewidth=.25mm}
5 \psline[linecolor=red,linewidth=.05mm](0,0)(0,6)
6 \psline[linecolor=red,linewidth=.05mm](4,0)(4,6)
7 \psline{v-v}(0,6)(4,6)
8 \psline{v-v}(0,6)(4,4)
9 \psline{v-V}(0,4)(4,4)
9 \psline{V-V}(0,2)(4,2)
\psline{V-V}(0,0)(4,0)
11 \end{pspicture}
```



```
psset{unit=5mm}
begin{pspicture}(4,6)

psset{dimen=middle,arrows=c-c,
    arrowscale=2,linewidth=.25mm}

psline[linecolor=red,linewidth=.05mm](0,0)(0,6)

psline[linecolor=red,linewidth=.05mm](4,0)(4,6)

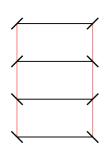
psline{f-f}(0,6)(4,6)

psline{f-F}(0,4)(4,4)

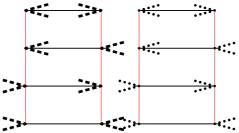
psline{F-F}(0,2)(4,2)

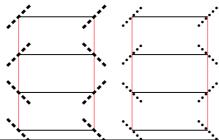
psline{F-F}(0,0)(4,0)

end{pspicture}
```



```
psset{unit=5mm}
begin{pspicture}(4,6)
    \psset{dimen=middle,arrows=c-c,linewidth=.25mm}
    \psline[linecolor=red,linewidth=.05mm](0,0)(0,6)
    \psline[linecolor=red,linewidth=.05mm](4,0)(4,6)
    \psline{t-t}(0,6)(4,6)
    \psline{t-T}(0,4)(4,4)
    \psline{T-T}(0,2)(4,2)
    \psline{T-T}(0,0)(4,0)
    \end{pspicture}
```

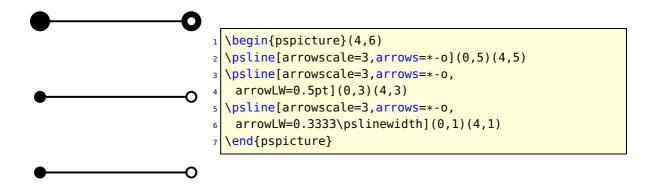




### 28.9. Special arrow option arrowLW

Only for the arrowtype o and \* it is possible to set the arrowlinewidth with the optional keyword arrowLW. When scaling an arrow by the keyword arrowscale the width of the

borderline is also scaled. With the optional argument arrowLW the line width can be set separately and is not taken into account by the scaling value.



# 29. Ticks and other marks along a curve

#### 29.1. Quick overview

The macros described below allow you to place tick and other marks along an arbitrary parametric curve with placement rules similar to those used by  $\protect\protec$ 

In addition, a new command \Put is proposed, expanding as appropriate to \rput or \uput. Its syntax is

```
\P = \{ options \}  { < ref > } ( < position > ) { < stuff > }
```

where the optional \* blanks the background, the optional <code>[Options]</code> may be used to specify a rotation using any form acceptable to \SpecialCoor (eg, rot=45 or rot={(1,1)} or rot=(P), and ref takes one of two forms: (a) a refpt such as Bl, in which case \rput is called; (b) a polar form of offset (eg, 7pt;30, or; (P) — in the latter case, \pslabelsep is substituted for the missing radius), in which case a modified form of \uput is called. The idea of \Put is to allow position, ref and rot to be specified in any of the forms acceptable to \SpecialCoor and to do so with the same output no matter what form is used. The cost of this consistency is that \Put can lead to results that differ from \uput in some special cases.

#### 29.2. Details

Suppose you have drawn a parametric curve using \psparametricplot, and you wish to indicate some points on the curve using tick-marks like those on the axes. This is a two-step process, the first of which serves to define at the PostScript level a number

29.2. Details **106** 

of data arrays containing information about the curve. Those arrays are used in the second step to compute tick positions and draw the ticks. The first step is to run the macro \pscurvepoints. For example,

\pscurvepoints[plotpoints=20]{0}{6}{t t t mul 12 div}{Pt}%

makes a virtual (ie, data only—nothing is rendered) polyline with 20 vertices approximating the curve  $x(t)=t,y(t)=t^2/12,\ 0\le t\le 6$ . The last argument Pt is the root name given to the data arrays. PostScript arrays will be created with the following names: Pt.X, Pt.Y for the coordinates of the vertices, PtDelta.X, PtDelta.Y for the increments between the vertices (using, eg, PtDelta.X[2]=Pt.X[2]-Pt.X[1]) and PtNormal.X, PtNormal.Y for a vector normal to PtDelta.X, PtDelta.Y in the visual, not mathematical, sense. (Both senses are the same if the scales on the axes are identical.) The Normal is always constructed so as to point "upward" (ie, to your left) as you traverse the curve in the positive direction. The PostScript variable unitratio provides the ratio of the unit on the y axis to that on x axis, and unitratiosq is its square. All of these PostScript objects are stored in the main pstricks dictionary tx@Dict which should be automatically made available when using many pstricks macros. If gs returns you an error message like

Error: /undefined in Pt.X

then you may need to enclose the offending PostScript code within a block of the form

tx@Dict begin ... end

so that the dictionary is made available.

With this preparation, the main tick-making macro may be run. For example,

\pspolylineticks{Pt}{ dx dy add 3 div }{1}{2}%

looks for data arrays made using \pscurvepoints with the root name Pt. The next argument, dx dy add 3 div, specifies the (PostScript) function of increments that should be used to construct the metric. If the keyword metricInitValue is defined, eg, with \psset{metricInitValue=2.5}, it is used as the initial value of the metric, otherwise it is defined to be 0. In the previous example, the increment function is always positive, and care should be taken to guarantee this is so or the results will not be meaningful. (If we wanted to use arc-length, the function would have been ds, assuming equal scales on the axes.) The last two arguments determine the index of the first tick and the number of ticks. Tick numbering begins with index 0, so the example says to drop the first tick and draw the next 2 ticks. In this example, where all keywords take their default values, ticks are potentially located at values on the curve where the metric takes a positive integer value. In the arc-length example, the tick with index 0 is at the beginning of the curve, and subsequent ticks are at unit distance, measured along the curve. At each index where a tick is drawn, a \pnode is created: In this example, you create nodes PtTick1, PtTick2 on the curve where the ticks are located. This is handy for placing labels using, eg, \Put. In addition, PostScript data arrays (in this example, PtTickN.X,

PtTickN.Y of the normals at these nodes are stored in the dictionary TDict. More importantly, the tangent and normal vectors at PtTickO etc are constructed as nodes with names PtTangentO, PtNormalO etc. See the last example below for typical usage.

The shape of the ticks is governed by the keywords ticksize (default value -4pt 4pt) and tickwidth (default value .5\linewidth.) With the default settings, ticks are drawn perpendicular the the curve extending 4pt to each side. The line

```
\pspolylineticks[ticksize=-6pt 6pt]{Pt}{ dx dy add 3 div }{1}{2}%
```

would draw longer ticks than the default.

Placement of the ticks is governed by the keywords Ds and Os, whose meaning for the curve is similar to (but not the same as) the meanings of Dx and Ox with respect to the x axis. That is, if Ds=2 and Os=0, ticks will be drawn where the metric takes values 0, 2, 4 and so on. More generally, ticks are placed where the metric takes value Os, Os+Ds, Os+2\*Ds,..., as long as those positions are on the curve. If Os has an empty value as a result, say, of \psset{0s=}, then Os is set internally to the initial metric value. If Ds has an empty value, it is set internally to the final metric value less the initial metric value, divided by 10.

To draw major and minor ticks requires two passes—one to draw the minor ticks and then one to draw the major ticks.

Note that a ticks may be placed at arbitrary metric values on the curve by running the macro once for each point, like:

```
\pspolylineticks[ticksize=-6pt 6pt,0s=1.3]{Pt}{ dx dy add 3 div }\{0\}\{1\}% \pspolylineticks[ticksize=-6pt 6pt,0s=2.4]{Pt}{ dx dy add 3 div }\{0\}\{1\}%
```

You may also dispense entirely with the tick and use the macro to generate a node sequence that can be used to place other graphic objects. For example:

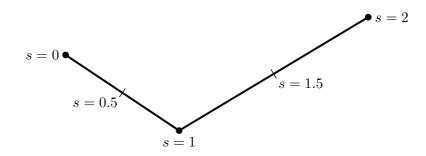
There is another way to define a metric function without using increments. If the keywork metricFunction is set to true, then the function you present as an argument to pspolylineticks must be a function of x and y only, and must be designed to increase along the curve. It is useful only in those cases where, in essence, the increment function can be explicitly integrated. For example, in the elliptical motion of planets and comets around the sun, it is not hard to integrate the area function explicitly, and this provides a convenient metric, being proportional to time elapsed.

There is some useful information left in the log by these macros. They report the starting and ending values of the metric function, the the range of indices for the Tick related arrays.

## 29.3. Examples

The examples in this section make use of very recent (as of May, 2010) versions of pstricks and related packages.

The first couple of examples are constructed entirely by hand, and have no interest other than to illustrate what is going on under the surface in the simplest case.



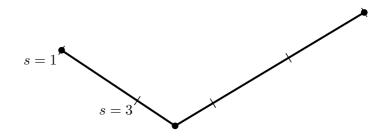
```
\begin{pspicture}(-1,-1)(10,4)
  psline[showpoints=true](1,2)(4,0)(9,3)%
  \uput[180](1,2){$s=0$}%
  \uput[-90](4,0){$s=1$}%
  \uput[0](9,3){$s=2$}%
  \makeatletter% need to use macro names containing @
  \pstVerb{tx@Dict begin %the pstricks dictionary
  % declare arrays of length 3 (indices 0,1,2) to hold points,
9 % differences and normals
/P.X [ 1 4 9 ] def %array of x coords
12 /P.Y [ 2 0 3 ] def %array of y coords
13 /PDelta.X [ 0 3 5 ] def % 3=4-1, 5=9-4, 0 never used
14 /PDelta.Y [ 0 -2 3 ] def % -2=0-2, 3=3-0, 0 never used
15 % normal to (3,-2) is (2,3), normal to (5,3) is (-3,5)
16 / PNormal.X [ 2 2 -3 ] def % index 0 = index 1
17 / PNormal.Y [ 3 3 5 ] def % index 0 = index 1
18 end }
19 \def\Ppointcount{2}
20 \makeatother
21 % make ticks using metric function with values 0,1,2
22 \pspolylineticks[0s=.5,Ds=1]{P}{1}{0}{2}
% ticks at s=0.5,1.5 (increment function =1)
24 \uput[-135](PTick0){$s=0.5$}%
25 \uput[-45](PTick1){$s=1.5$}%
26 \end{pspicture}
```

Now the same data, but with arc-length as metric. We change the last few lines:



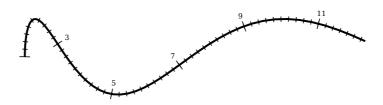
```
\begin{pspicture}(-1,-1)(10,4)
  \psline[showpoints=true](1,2)(4,0)(9,3)%
  %\uput[180](1,2){$s=0$}%
  %\uput[-90](4,0){$s=1$}%
  %\uput[0](9,3){$s=2$}%
  \makeatletter% need to use macro names containing @
  \pstVerb{tx@Dict begin %the pstricks dictionary
  % declare arrays of length 3 (indices 0,1,2) to hold points,
9 % differences and normals
11 /P.X [ 1 4 9 ] def %array of x coords
12 /P.Y [ 2 0 3 ] def %array of y coords
13 /PDelta.X [ 0 3 5 ] def % 3=4-1, 5=9-4, 0 never used
14 /PDelta.Y [ 0 -2 3 ] def % -2=0-2, 3=3-0, 0 never used
15 % normal to (3,-2) is (2,3), normal to (5,3) is (-3,5)
16 / PNormal.X [ 2 2 -3 ] def % index 0 = index 1
17 / PNormal.Y [ 3 3 5 ] def % index 0 = index 1
18 end }
19 \def\Ppointcount{2}
20 \makeatother
21 % make ticks using metric function arc-length
22 \pspolylineticks[0s=1,Ds=1]{P}{ ds }{0}{9}
23 % ticks at s=1,2... (increment function = distance)
24 \uput[-135](PTick0){$s=1$}%
25 \uput[-135](PTick1){$s=2$}%
26 \end{pspicture}
```

Once again the same data, but with metric equal to the x coordinate. Change the last few lines to:



```
\begin{pspicture}(-1,-1)(10,4)
  \psline[showpoints=true](1,2)(4,0)(9,3)%
  %\uput[180](1,2){$s=0$}%
  %\uput[-90](4,0){$s=1$}%
  %\uput[0](9,3){$s=2$}%
 \makeatletter% need to use macro names containing @
7 \pstVerb{tx@Dict begin %the pstricks dictionary
  % declare arrays of length 3 (indices 0,1,2) to hold points,
  % differences and normals
/unitratiosq 1 def % yunit=xunit
11 /P.X [ 1 4 9 ] def %array of x coords
12 /P.Y [ 2 0 3 ] def %array of y coords
13 /PDelta.X [ 0 3 5 ] def % 3=4-1, 5=9-4, 0 never used
14 /PDelta.Y [ 0 -2 3 ] def % -2=0-2, 3=3-0, 0 never used
^{15} % normal to (3,-2) is (2,3), normal to (5,3) is (-3,5)
16 / PNormal.X [ 2 2 -3 ] def % index 0 = index 1
17 / PNormal.Y [ 3 3 5 ] def % index 0 = index 1
18 end }
19 \def\Ppointcount{2}
20 \makeatother
 % make ticks using metric function arc-length
22 \pspolylineticks[metricFunction,0s=1,Ds=2]{P}{ x }{0}{5}
^{23} % ticks at x=1,3,... , start at tick index 0, draw 5 ticks
% the tick at s=1 has index 0
25 % ticks at s=1,2... (increment function = distance)
26 \uput[-135](PTick0){$s=1$}%
27 \uput[-135](PTick1){$s=3$}%
28 \end{pspicture}
```

The next example is a smooth path where subticks are drawn first, followed by major ticks. The metric is arc-length with initial value s=1.



```
begin{pspicture}(-1,-1)(10,4)
%\parametricplot[algebraic]{0}{9}{(t^2)/9 | 4*Ex(-t)*(1+t+(t^{2})/2+(t^{3})/6)}
}

psparametricplot[algebraic]{0}{9}{t^2/9 | sin(t)+1}%

pscurvepoints{0}{9}{(t^2)/9 | sin(t)+1}{P}%

make ticks using arc-length metric

pspolylineticks[metricInitValue=1,ticksize=-2pt 2pt,0s=1,Ds=.2]{P}{ ds }{1}{56}%

pspolylineticks[metricInitValue=1,0s=1,Ds=2]{P}{ ds }{0}{6}%

multido{\iA=1+1,\iB=3+2}{5}{\Put{6pt;(PNormal\iA)}(PTick\iA){\tiny \iB}}%

multido{\iA=1+1,\iB=3+2}{5}{\uput{6pt}[(PNormal\iA))](PTick\iA){\iB}}%

multido{\iA=1+1,\iB=3+2}{5}{\uput{6pt}[(PNormal\iA))](PTick\iA){\iB}}%

multido{\iA=1+1,\iB=3+2}{5}{\uput{6pt}[(PNormal\iA))](PTick\iA){\iB}}%

ticks at x=1,3,..., start at tick index 0, draw 5 ticks

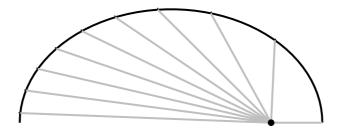
ticks at s=1,2... (increment function = distance)

end{pspicture}
```

Suppose for the next example that we have an ellipse  $x^2/a^2+y^2/b^2=1$  (a>b) with eccentricity  $\epsilon=(1-b^2/a^2)^{1/2}$ . With planetary motion in mind, a natural metric for the ellipse is the area swept out by the radial line from the focus  $(\epsilon a,0)$  starting from (a,0) around to an arbitrary location (x,y), where y>0, as this quantity is proportional to the time elapsed since perihelion. A routine calculation gives the following formula:

$$A = \frac{ab}{2}\arccos\left(\frac{x}{a}\right) - \frac{\epsilon ay}{2}.$$

Remembering that PostScript's acos gives its result in degrees, not radians, we have the following, drawn for the case a=4, b=3.



```
begin{pspicture}(-4.5,-.5)(4.5,3.5)

pstVerb{ /smajor 4 def /sminor 3 def % define semimajor, semiminor

/ecc 1 sminor smajor div dup mul sub sqrt def % compute eccentricity

/ab smajor sminor mul 2 div def %first coeff

/ea smajor ecc mul 2 div def }% second coeff

psparametricplot[algebraic]{0}{3.142}{smajor*cos(t) | sminor*sin(t)}%

pscurvepoints{0}{3.142}{smajor*cos(t) | sminor*sin(t)}{P}%

pspolylineticks[metricFunction,Ds=2,ticksize=-1.5pt 0]{P}{ ab x smajor div acos %

180 div PI mul mul ea y mul sub }{1}{9}%

pnode(! ecc smajor mul 0){S}% focus

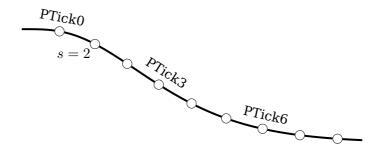
psline[linecolor=lightgray](S)(!smajor 0)%

multido{\i=1+1}{9}{\psline[linecolor=lightgray](S)(PTick\i)}

psdot(S)

end{pspicture}
```

The next examples works without visible ticks, using the macros to construct nodes at which other objects will be placed.



```
begin{pspicture}(-1,-1)(10,4)
psparametricplot[algebraic]{0}{9}{t| 3*Ex(-t)*(1+t+t^2/2+t^3/6)}

pscurvepoints{0}{9}{t| 3*Ex(-t)*(1+t+t^2/2+t^3/6)}{P}%

pspolylineticks[0s=1,Ds=1,ticksize=0 0]{P}{ ds }{0}{9}%

multido{\i=0+1}{9}{\psdot[dotscale=1.5,dotstyle=0](PTick\i)}%

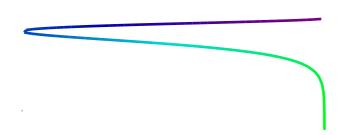
ticks at s=1,2,..., start at tick index 0, set 9 ticks

the tick at s=1 has index 0

ticks at s=1,2... (increment function = distance)
multido{\i=0+3}{3}{\Put[rot=(PTangent\i)]{7pt;(PNormal\i)}(PTick\i){PTick\i}}%

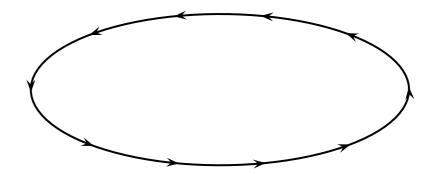
uput[-135](PTickl){$s=2$}%
lend{pspicture}
```

This variant also has no visible ticks, but makes a color gradient along the curve based on arc-length from the start.



30. Troubleshooting

Here is a another variant of this technique which allows arrows to be placed at locations on the curve where the metric takes particular values.



```
begin{pspicture}(-1,-1)(10,4.5)

psparametricplot[plotpoints=100]{0}{360}{t cos 1 add 5 mul t sin 1 add 2 mul}

pscurvepoints[plotpoints=100]{0}{360}{t cos 1 add 5 mul t sin 1 add 2 mul}{P}

pspolylineticks[0s=0,Ds=2.3,ticksize=0 0]{P}%

ds }{0}{10}% distance

multido{\i=0+1}{10}{\psrline[arrows=->,arrowscale=1.5](PTick\i)(2pt;{(PTangent\i)})}%

end{pspicture}
```

## 30. Troubleshooting

If you get PostScript errors when you process your file, the most likely culprit is the function you specified to define the metric. There are some things to look out for:

- If metricFunction, the function you specify in PostScript code must involve only x and y, and must leave exactly one real value on the stack as a result of substituting specific values for x and y. The function must be strictly increasing on the curve.
- If metricFunction=false(the default), the function you specify in PostScript code must involve only the variables x, y, dx, dy, ds (where ds is defined to be the arclength element dx dup mul dy dup mul add sqrt, and must leave exactly one strictly positive real value on the stack when specific values are substituted for those variables. The constant function 1 gives equal weight to each segment in the curve, so in effect it gives you the original parametrization, up to a constant factor.
- If the function you specify in \parametricplot and \pscurvepoints is algebraic, make sure you follow precisely the syntax it understands. In complex cases, PostScript may be the safer solution.
- It is unwise to use a different resolution for \psparametricplot and \pscurvepoints. The default value of plotpoints=50 is marginal except for modest curve segments, and 200 should suffice for most smooth curves.

#### 31. Transparent colors

Transparency is now part of the main pstricks package. But pay attention, the names and syntax have changed and you need to run ps2pdf with the option -dCompatibilityLevel=1.4.

### 32. "Manipulating transparent colors"

pstricks-add supports real transparency and a simulated one with hatch lines:

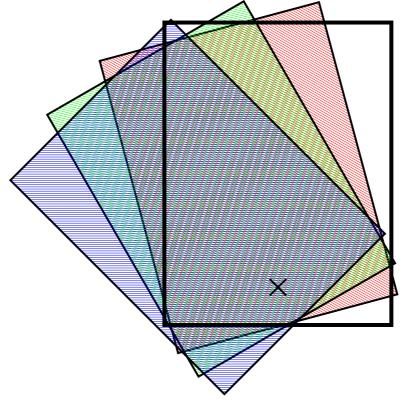
```
\def\defineTColor{\@ifnextchar[{\defineTColor@i}{\defineTColor@i[]}}

\def\defineTColor@i[#1]#2#3{% transparency "Colors"
  \newpsstyle{#2}{%
    fillstyle=vlines,hatchwidth=0.1\pslinewidth,
    hatchsep=1\pslinewidth,hatchcolor=#3,#1%
    }%
}

\defineTColor{TRed}{red}
\defineTColor{TGreen}{green}
\defineTColor{TBlue}{blue}
```

There are three predefined "'transparent"' colors TRed, TGreen, TBlue. They are used as PSTricks styles and not as colors:

33. Calculated colors



```
begin{pspicture}(-3,-5)(5,5)

psframe(-1,-3)(5,5) % objet de base

psrotate(2,-2){15}{%

psframe[style=TRed](-1,-3)(5,5)}

psrotate(2,-2){30}{%

psframe[style=TGreen](-1,-3)(5,5)}

psrotate(2,-2){45}{%

psframe[style=TBlue](-1,-3)(5,5)}

psframe[linewidth=3pt](-1,-3)(5,5)

psdots[dotstyle=+,dotangle=45,dotscale=3](2,-2) % centre de la rotation
lend{pspicture}
```

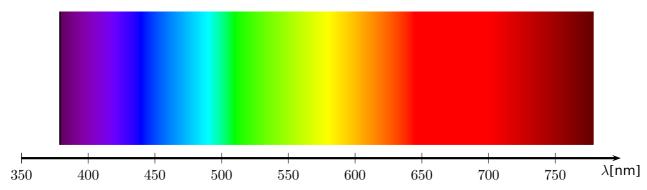
#### 33. Calculated colors

The xcolor package (version 2.6) has a new feature for defining colors:

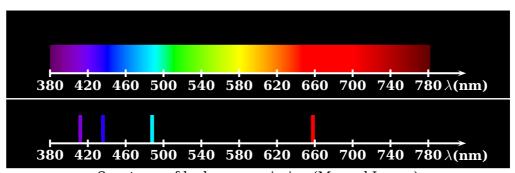
```
\definecolor[ps]{<name>}{<model>}{< PS code >}
```

model can be one of the color models, which PostScriptwill understand, e.g. rgb. With this definition the color is calculated on the PostScriptside.

33. Calculated colors



```
1 \definecolor[ps]{bl}{rgb}{tx@addDict begin Red Green Blue end}%
2 \psset{unit=1bp}
3 \begin{pspicture}(0, -30)(400,100)
4 \multido{\iLAMBDA=0+1}{400}{%}
5 \pstVerb{
6 \iLAMBDA\space 379 add dup /lambda exch def
7 tx@addDict begin wavelengthToRGB end
8 }%
9 \psline[linecolor=bl](\iLAMBDA,0)(\iLAMBDA,100)%
10 }
11 \psaxes[yAxis=false,0x=350,dx=50bp,Dx=50]{->}(-29,-10)(420,100)
12 \uput[-90](420,-10){$\lambda$[\textsf{nm}]}
13 \end{pspicture}
```



Spectrum of hydrogen emission (Manuel Luque)

```
\newcommand\Touch{%
  \psframe[linestyle=none,fillstyle=solid,fillcolor=bl,dimen=middle](0.1,0.75)}
  \definecolor[ps]{bl}{rgb}{tx@addDict begin Red Green Blue end}%
  % Echelle 1cm <-> 40 nm
          1 nm <-> 0.025 cm
  \psframebox[fillstyle=solid,fillcolor=black]{%
  \begin{pspicture}(-1,-0.5)(12,1.5)
  \multido{\iLAMBDA=380+2}{200}{%
   \pstVerb{
10
     /lambda \iLAMBDA\space def
11
     tx@addDict begin wavelengthToRGB end
12
13
   \rput(! lambda 0.025 mul 9.5 sub 0){\Touch}
14
15 }
```

34. Gouraud shading

```
16 \multido{\n=0+1,\iDiv=380+40}{11}{%
               \psline[linecolor=white](\n,0.1)(\n,-0.1)
               \uput[270](\n,0){\texttextbf}{\textwhite}\}
18
                \psline[linecolor=white]{->}(11,0)
19
                \uput[270](11,0){\textbf{\white$\lambda$(nm)}}
21 \end{pspicture}}
23 \psframebox[fillstyle=solid,fillcolor=black]{%
      \begin{array}{l} \begin{array}{l} \text{begin} \{pspicture\}(-1,-0.5)(12,1) \end{array} \end{array}
          \pstVerb{
25
                /lambda 656 def
26
               lambda
27
               tx@addDict begin wavelengthToRGB end
28
29
30 \rput(! 656 0.025 mul 9.5 sub 0){\Touch}
31
          \pstVerb{
                /lambda 486 def
32
                lambda
33
34
               tx@addDict begin wavelengthToRGB end
          }%
35
36 \rput(! 486 0.025 mul 9.5 sub 0){\Touch}
37
             \pstVerb{
               /lambda 434 def
38
               lambda
39
               tx@addDict begin wavelengthToRGB end
40
41
42 \rput(! 434 0.025 mul 9.5 sub 0){\Touch}
          \pstVerb{
43
               /lambda 410 def
44
               lambda
               tx@addDict begin wavelengthToRGB end
46
47
48 \rput(! 410 0.025 mul 9.5 sub 0){\Touch}
      \multido{\n=0+1,\iDiv=380+40}{11}{%
               \prootember \pro
50
               \uput[270](\n,0){\texttextbf}{\textwhite}\}
51
               \psline[linecolor=white]{->}(11,0)
52
                \uput[270](11,0){\textbf{\white$\lambda$(nm)}}
54 \end{pspicture}}
55
56 Spectrum of hydrogen emission (Manuel Luque)
```

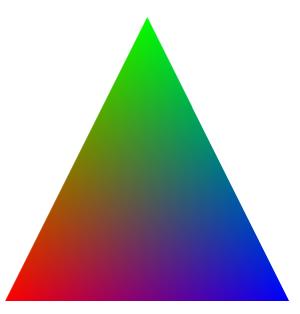
## 34. Gouraud shading

Gouraud shading is a method used in computer graphics to simulate the differing effects of light and colour across the surface of an object. In practice, Gouraud shading is used to achieve smooth lighting on low-polygon surfaces without the heavy computational requirements of calculating lighting for each pixel. The technique was first presented by Henri Gouraud in 1971.

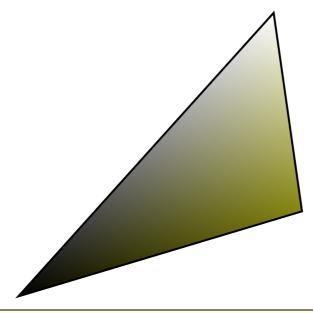
#### http://www.wikipedia.org

PostScript level 3 supports this kind of shading and it can only be seen with Acroread 7 or later. The syntax is easy:

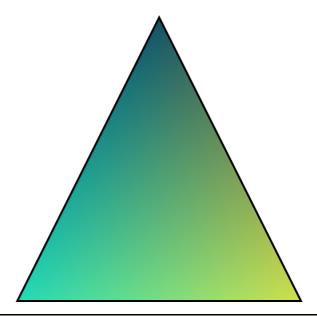
 $\psGTriangle(x1,y1)(x2,y2)(x3,y3)\{color1\}\{color2\}\{color3\}$ 



```
1 \begin{pspicture}(0,-.25)(10,10)
2 \psGTriangle(0,0)(5,10)(10,0){red}{green}{blue}
3 \end{pspicture}
```



```
1 \begin{pspicture}(0,-.25)(10,10)
2 \psGTriangle*(0,0)(9,10)(10,3){black}{white!50}{red!50!green!95}
3 \end{pspicture}
```



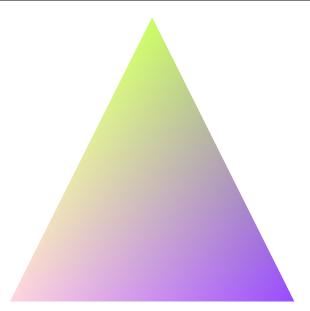
```
begin{pspicture}(0,-.25)(10,10)

psGTriangle*(0,0)(5,10)(10,0){-red!100!green!84!blue!86}

{-red!80!green!100!blue!40}

{-red!60!green!30!blue!100}

end{pspicture}
```



```
1 \definecolor{rose}{rgb}{1.00, 0.84, 0.88}
2 \definecolor{vertpommepasmure}{rgb}{0.80, 1.0, 0.40}
3 \definecolor{fushia}{rgb}{0.60, 0.30, 1.0}
4 \begin{pspicture}(0, -.25)(10,10)
5 \psGTriangle(0,0)(5,10)(10,0){rose}{vertpommepasmure}{fushia}
6 \end{pspicture}
```

#### 35. Internal color macros

The internal macros \pswavelengthToRGB and \pswavelengthToRGB can be used for own purposed. They are defines as follows:

```
1 \def\pswavelengthToGRAY{ tx@addDict begin wavelengthToGRAY end }
2 \def\pswavelengthToRGB{ tx@addDict begin wavelengthToRGB Red Green Blue end }
```

both macros leave the value(s) on the stack which then can be used for further manipulating or setting the color with setgray or setrgbcolor. For an example see Section 26.

A. \resetOptions

## A. \resetOptions

Sometimes it is difficult to know what options, which are changed inside a long document, are different to the default ones. With this macro all options belonging to pst-plot can be reset. This refers to all options of the packages pstricks, pst-plot and pst-node.

## **B. PostScript**

PostScript uses the stack system and the LIFO system, "'Last In, First Out"'.

Table 4: Some primitive PostScript macros

Eunstian	Meaning	
Function	on stack before $ ightarrow$ after	
add	$x  y \rightarrow x + y$	
sub	$x  y \rightarrow x - y$	
mul	$x \ y \rightarrow x \times y$	
div	$x \ y \rightarrow x \div y$	
sqrt	$x \to \sqrt{x}$	
abs	$x \rightarrow  x $	
neg	$x \rightarrow -x$	
cos	$x   o  \cos(x)$ ( $x$ in degrees)	
sin	$x  o \sin(x)$ ( $x$ in degrees)	
tan	x  ightarrow  an(x) ( $x$ in degrees)	
atan	$y$ $x$ $ o$ $\angle(ec{Ox}; ec{OM})$ (in degrees of $M(x,y)$ )	
ln	$x \to \ln(x)$	
log	$x \to \log(x)$	
array	$n \rightarrow v$ (of dimension $n$ )	
aload	$v \rightarrow x_1  x_2  \cdots  x_n  v$	
astore	$\begin{bmatrix} x_1 & x_2 & \cdots & x_n & v \rightarrow [v] \end{bmatrix}$	
pop	$x \rightarrow -$	
dup	$x \rightarrow x  x$	

# C. List of all optional arguments for pstricks-add

Key	Type	Default
CMYK	boolean	true
intSeparator	ordinary	[none]
braceWidth	ordinary	[none]
bracePos	ordinary	[none]
braceWidthInner	ordinary	[none]
braceWidthOuter	ordinary	[none]
parallelogramsep	ordinary	3mm
veearrowlength	ordinary	3mm
veearrowangle	ordinary	30
veearrowlinewidth	ordinary	0.35mm
filledveearrowlength	ordinary	3mm
filledveearrowangle	ordinary	15
filledveearrowlinewidth	ordinary	0.35mm
arrowlinestyle	ordinary	solid
tickarrowlength	ordinary	1.5mm
tickarrowlinewidth	ordinary	0.35mm
hooklength	ordinary	3mm
hookwidth	ordinary	1mm
ArrowFill	boolean	true
nArrowsA	ordinary	2
nArrowsB	ordinary	2
nArrows	ordinary	2
ArrowInside	ordinary	[none]
ArrowInsidePos	ordinary	0.5
ArrowInsideNo	ordinary	1
ArrowInsideOffset	ordinary	0
0s	ordinary	0
Ds	ordinary	1
metricInitValue	ordinary	0
metricFunction	boolean	true
randomPoints	ordinary	1000
color	boolean	true
blName	command	
bcName	command	
brName	command	
clName	command	
ccName	command	
crName	command	
tlName	command	
tcName	command	
trName	command	

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Key	Type	Default
whichabs	ordinary	[none]
whichord	ordinary	[none]
plotfuncx	ordinary	[none]
plotfuncy	ordinary	[none]
expression	ordinary	[none]
buildvector	boolean	true
varsteptol	ordinary	[none]
adamsorder	ordinary	[none]
StepType	ordinary	[none]
Derive	ordinary	[none]
Tnormal	boolean	true
GetFinalState	boolean	true
filename	ordinary	[none]
saveData	boolean	true
Xoffset	ordinary	0pt
Yoffset	ordinary	0pt
XYoffset	ordinary	0pt
colorType	ordinary	0
colorTypeDef	ordinary	
chartStyle	ordinary	[none]
chartColor	ordinary	[none]
chartSep	ordinary	[none]
chartStack	ordinary	[none]
chartStackDepth	ordinary	[none]
chartStackWidth	ordinary	[none]
chartHeight	ordinary	[none]
userColor	ordinary	[none]
chartNodeI	ordinary	[none]
chartNodeO	ordinary	[none]
cancelType	ordinary	[none]
markAngle	boolean	true
basename	ordinary	[none]
rotate	ordinary	[none]

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