#### **Deep Learning Methods For NLP**

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**MICS - CentraleSupelec** 

**Introduction To (Deep) Natural Language Processing** 



# **Final Project**

#### **Lectures Outline**

- 1. The Basics of Natural Language Processing (February 1st)
- 2. Representing Text with Vectors (February 1st)
- 3. Deep Learning Methods for NLP (February 8th)
- 4. Language Modeling (February 8th)
- 5. Sequence Labelling (Sequence Classification) (February 15th)
- 6. Sequence Generation Tasks (February 15th)

## **Today Lecture Outline**

- Deep Learning Framework
- The Multi-Layer Perceptron
- Recurrent Neural Network
- Attention Mechanism
- Self-Attention Mechanism and the Transformer Architecture

#### **Motivations**

So far, we have seen, techniques to represent tokens with vectors

Given a certain representations of tokens:

→ How can we model a sequence of tokens to perform a specific task?

In the past 10 years, a "new" class of machine learning techniques has become very popular and successful in NLP: **Deep Learning** 

In this session, we introduce Deep Learning with a focus on the methods used in NLP

#### **Framework**

We want to model  $(X_1, \dots, X_T)$  i.e. find the correct label Y

$$dnn: \mathbb{R}^{d,T} \rightarrow \mathbb{R}^p \quad or [0, |K|]^p$$

$$(X_1, \dots, X_T) \rightarrow \hat{Y}$$

- ullet Output space is  $\mathbb{R}^p$  for **Regression** tasks
- Output space is  $[0, |K|]^p$  for Classification tasks

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**Questions: when we do Deep Learning...** 

- ullet How do we define  $f_{ heta}$
- How do we train.  $f_{\theta}$  with data?

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Most Deep Learning Models (all the ones we will use in this course):

- are **parametric** (i.e.  $\theta \in \Theta = \mathbb{R}^D$ )
- defined as a composition of "simple" functions (linear & non-linear)
- are trained in an end-to-end fashion with backpropagation

NB: In Deep Learning, the parametrization of  $f_{\theta}$  is called the Architecture

## **Different Types of Architecture**

How can we define our predictive function dnn

- → Multi-Layer Perceptron
- → Recurrent Layers
- → Attention Layers
- → Self-Attention Layers (in a Transformer Architecture)

#### **Different Types of Architecture**

How can we define our predictive function

- → Multi-Layer Perceptron
- → Recurrent Layers
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How do we **train our model**? (i.e. estimate the parameters of the model)

→ Stochastic Gradient Descent also called backpropagation in this context

aka "the Most simple Deep Learning Architecture"

The **MLP** works **on unidimensional data** (e.g. dimension d)

We present the MLP in the regression case (e.g. output space is.  $\mathbb{R}^2$ ))

$$dnn: \mathbb{R}^d \longrightarrow \mathbb{R}^2$$

$$X \longrightarrow \hat{Y}$$

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 $W_1, b_1, W_2$  and  $b_2$  are trainable parameters.  $W_1 \in \mathbb{R}^{\delta \times d}, b_1 \in \mathbb{R}^{\delta}, W_2 \in \mathbb{R}^{2 \times \delta}$  and  $b_2 \in \mathbb{R}$   $\varphi_1$  is a fixed non-linear function,  $\varphi_1 : \mathbb{R}^d \to \mathbb{R}^\delta$ 

→ This model is a *2-layer* MLP model

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- → This model is a **2-layer MLP** model
- → With 1 *hidden layer* of dimension
- $\rightarrow$  Taking as input a vector of dimension d to output a vector of dimension 2
- → Such a model is also referred to as a *Feed-Forward* Neural Network (FNN)

# The MultiLayer Perceptron: Diagram View

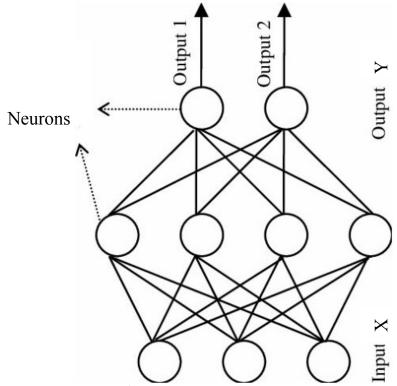
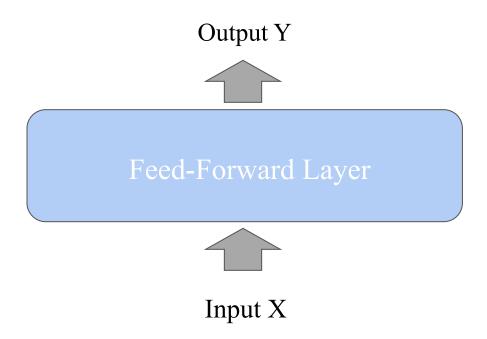


Figure from (R. Rezvani et. al. 2012)

In Deep Learning, it is usual to represent equations with diagrams

# The MultiLayer Perceptron: Diagram View



In Deep Learning, it is usual to represent equations with diagrams

#### The MultiLayer Perceptron:

We have defined a 2-layers MLP model
We can define in the same way a 3-layers, 4-layers, L-layers MLP

$$dnn_{(W_i b_i, i \in [|1, L|])}(X) = W_L \varphi_{L-1}(...\varphi_2 \circ W_2 \varphi_1(W_1 X + b_1) + b_2)...) + b_L$$

 $W_l$  and  $b_l$  are trainable parameters.  $W_l \in \mathbb{R}^{\delta_{l-1} \times \delta_l}$ ,  $b_l \in \mathbb{R}^{\delta_l}$ , with  $\delta_l \in \mathbb{N}^*$ ,  $\forall l \in [|1, L|]$   $\varphi_l$  fixed non-linear functions,  $\varphi_l : \mathbb{R}^{\delta_{l-1}} \to \mathbb{R}^{\delta_l}$ ,  $\forall l \in [|1, L-1|]$ 

## The MultiLayer Perceptron

The same equation with a loop...

$$h_{i+1} = \varphi_i(W_i h_i + b_i), \forall i \in [|1, L - 1|]$$
 with  $h_1 = X$  and  $\hat{Y} = dnn(X) = h_L$ 

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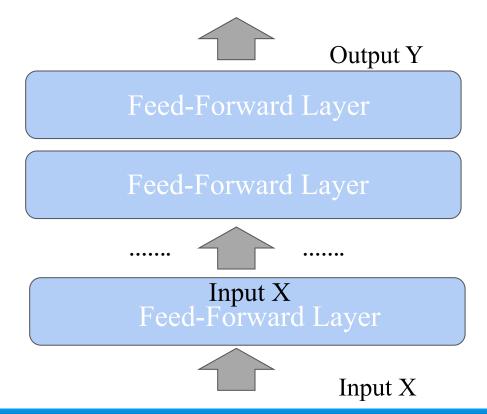
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 $h_i$  are called hidden states ( $h_i \in \mathbb{R}^{\delta_i}$ ).

# The MultiLayer Perceptron: Diagram View



## **Output Activation Function for Classification**

When we do a classification task the goal is to learn a distribution of probability on the output label space

To do so, we usually use the softmax function as the last activation function

$$softmax(s) = \left(\frac{e^{s_i}}{\sum_k e^{s_k}}\right)_{i \in [|1,K|]}, \text{ for } s \in \mathbb{R}^K$$

#### **Loss Functions**

Based on the task we aim at modeling, we can use:

#### For Regression: Mean-Square Error

$$l(y,\hat{y}) = \|y - \hat{y}\|_2^2 = \sum_i (y_i - \hat{y}_i)^2$$
 assuming  $y_i, \ \hat{y}_i \in \mathbb{R}$ 

#### For Classification: Cross-Entropy Loss

$$l(y, \hat{y}) = CE(y, \hat{y}) = \sum_{i} y_i \log(\hat{y}_i)$$
 assuming  $y_i, \hat{y}_i \in [0, 1]$ 

Most NLP tasks will be based on the Cross-Entropy loss

- Number of hidden layers
- Hidden layers dimensions
- Initialization of the trainable parameters/weights

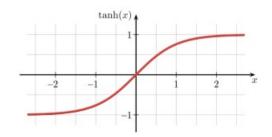
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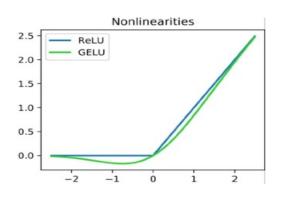
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#### How to define them?

- → Look for **best practices** to choose which are the best
- → In most DL libraries, the "good" hyperparameters are usually the default
- → If no best practices/default: you have to find the best ones empirically

## **Training Deep Learning Models**

Nearly all Deep Learning models are trained with (some version of)
 Stochastic Gradient Descent (SGD)

#### **Stochastic Gradient Descent**

- The goal is find the set of parameters/weights that minimizes the loss function
- To do so, SGD estimates the true gradient of a function with **one** sample at time
- Repeat this process multiple times

**NB:** in deep learning, we usually train all the parameters together "end-to-end"

#### **Stochastic Gradient Descent**

```
Algorithm 2 Stochastic Gradient Descend
Given observations ((x_i), (y_i)) of two variables (X, Y)
Given a loss function l. An architecture dnn_{\theta}
The goal is to find the best \theta s.t. E(l(Y, dnn_{\theta}(X))) is small. Given a learning rate \alpha
for step < max do
    Sample (x, y)
    # Forward pass:
    \hat{y} = dnn_{\theta}(x) and l(y, \hat{y})
    # Backward pass:
    \nabla_{\theta} l(y, \hat{y}) # compute loss
    \theta := \theta - \alpha \nabla_{\theta} \, l(y, \hat{y}) # parameter update
end
```

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Given observations ((x_i), (y_i)) of two variables (X, Y)
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Given a loss function l. An architecture  $dnn_{\theta}$ 

The goal is to find the best  $\theta$  s.t.  $E(l(Y, dnn_{\theta}(X)))$  is small. Given a learning rate  $\alpha$ 

**for** step < max **do** 

```
Sample (x, y)
```

# Forward pass:

$$\hat{y} = dnn_{\theta}(x)$$
 and  $l(y, \hat{y})$ 

# Backward pass:

$$\nabla_{\theta} l(y, \hat{y})$$
 # compute loss

$$\theta := \theta - \alpha \nabla_{\theta} l(y, \hat{y})$$
 # parameter update

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for step < max do
    Sample (x, y)
    # Forward pass:
    \hat{u} = dnn_{\theta}(x) and l(u, \hat{u})
    # Backward pass:
    \nabla_{\theta} l(y, \hat{y}) # compute gradients
    \theta := \theta - \alpha \nabla_{\theta} l(y, \hat{y}) # parameter update
end
```

### **Optimization Hyperparameters**

### **Learning Rate**

• Can be refined with variable learning rate

E.g. increasing during the first steps (warmup) then decreasing

#### **Number of steps**

• Usually defined with the validation loss

When it stops decreasing we can stop training (= early stopping)

Optimizing large Deep Learning Models is challenging

- Unstable training
- Overfitting
- Take a lot of steps/epochs

To make training better, many refinement of the SGD have been proposed

• In practice, we (nowadays) use the ADAM optimizer (cf. Kingma et. al 2015)

Let  $(X, Y) \in \mathbb{R}^d \times \mathbb{R}$ , the MSE loss  $l(y, \hat{y}) = (y - \hat{y})^2$ .

We define a 1-hidden-layer MLP with a Relu activation function of dimension  $\delta$ .

$$\hat{y} = dnn_{W_1, W_2}(x) = W_2 \max(W_1 x, 0)$$
 and  $W_1 \in \mathbb{R}^{d \times \delta}$  and  $W_2 \in \mathbb{R}^{1 \times \delta}$ 

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→ Goal: Apply SGD to dnn

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1. Forward pass: Compute

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- 1. Forward pass
- 2. Compute Gradients

$$\nabla_{W_1} l(y, \hat{y}) \quad \nabla_{W_2} l(y, \hat{y})$$

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- 1. Forward pass
- 2. Compute Gradients
- 3. Backward pass (parameter update)

Let  $(X, Y) \in \mathbb{R}^d \times \mathbb{R}$ , the MSE loss  $l(y, \hat{y}) = (y - \hat{y})^2$ .

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Idea: we use **the chain rule** to decompose **the gradient** starting **from the top layers** 

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$$\hat{y} = dnn_{W_1, W_2}(x) = W_2 \underbrace{\max(W_1 x, 0)}_{h_1} \text{ and } W_1 \in \mathbb{R}^{d \times \delta} \text{ and } W_2 \in \mathbb{R}^{1 \times \delta}$$

#### **Compute Gradient**

$$\nabla_{W_2} l(y, \hat{y}) = \frac{\partial l}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial W_2}$$

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$$\nabla_{W_2} l(y, \hat{y}) = \frac{\partial l}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial W_2} = 2(y - \hat{y}) h_1$$

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## **Backpropagation and Deep Learning in practice**

In practice, we use Deep Learning Libraries

- Define the Architecture with tensor operators
- Backpropagation is done seamlessly using automatic differentiation

# Deep Learning & Backpropagation in practice

In practice, we use Deep Learning Libraries (e.g. pytorch, tensorflow, jax)

- Define the Architecture with tensor operators
- Backpropagation is done seamlessly using automatic differentiation

 Standard layers are pre-implemented (Feed-Forward Layers, LSTM, Attention, Self-Attention...)

See code example with pytorch

## **Recurrent Neural Network**

### Vanilla Recurrent Neural Network

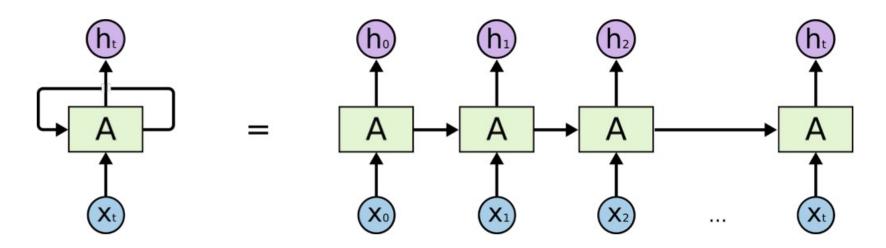
 $(X_1,..,X_T)$  in  $\mathbb{R}^{d,T}$ We would like to model sequences (e.g. words)

We can introduce a recurrence relation into our MLP to model it:

$$h_{i+1,t+1} = \varphi_i(W_i h_{i,t} + U_i h_{i+1,t} + b_i), \forall i \in [|1, L-1|]$$
 with  $h_{1,t} = X_t$  and  $\hat{Y}_t = dnn(X_t) = h_{L,t} \, \forall \, t \in [|1, T-1|]$ 

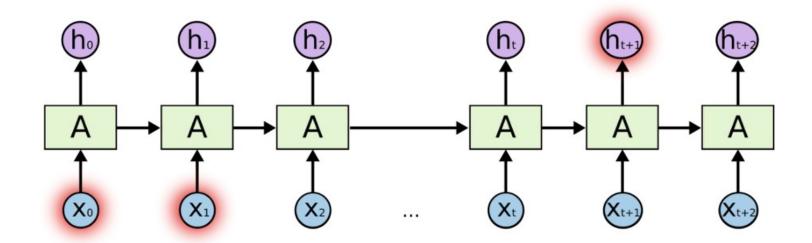
### **Recurrent Neural Network**

### Illustration of a 1-layer Recurrent Neural Network



### **Recurrent Neural Network**

### Illustration of a 1-layer Recurrent Neural Network



## **Training Recurrent Neural Network**

Recurrent Neural Network are trained with an extension of the Backpropagation algorithm

→ Backpropagation Through Time (BPTT)

BPTT follows exactly the same ideas as backpropagation

- SGD
- Chain Rule starting from the last layer and the last hidden state
- With extra derivative dependencies between state *t* and *t*+1

### **Limits of Recurrent Neural Networks**

Vanilla Recurrent Neural Network have trouble to capture long-term dependencies

#### Idea:

- Encode explicitly in a vector a "memory" in the recurrent architecture
- Control what is memorized and forgotten
- Train all those parameters end-to-end

Introduce a memory vector  $C_t$ 

 $C_t$  is designed to capture long term dependencies

The output state  $h_t$  of each LSTM cell is based on i  $C_t$  and an output gate  $o_t$ 

$$o_t = \sigma (W_o [h_{t-1}, x_t] + b_o)$$
$$h_t = o_t * \tanh (C_t)$$

## Introduce a memory vector $C_t$

 $C_t$  is designed to capture long term dependencies

 $C_t$  is define recurrently based on the previous step and the input and the forget gate. Those gates control what is memorized and forgotten.

$$C_t = f_t * C_{t-1} + i_t * \tilde{C}_t$$

$$i_t = \sigma \left( W_i \cdot [h_{t-1}, x_t] + b_i \right)$$
  
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

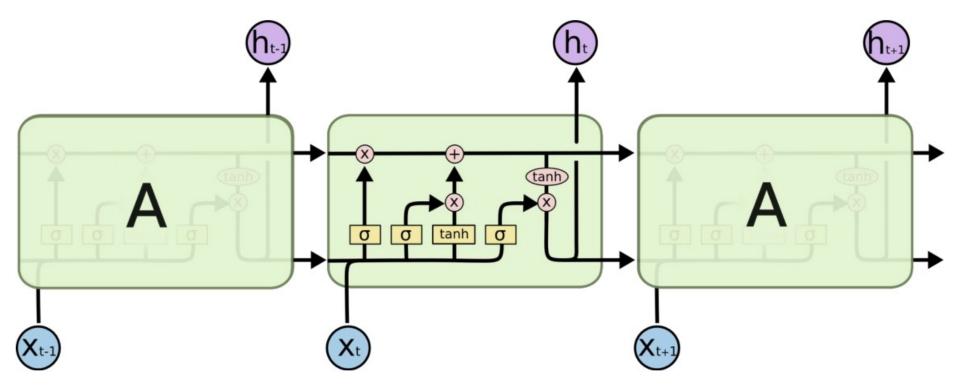


Figure from colah

- We train LSTM with Backpropagation (through time)
- LSTM cells are usually combined with Feed-Forward Layers

NB: Until recently (2018), LSTM-based models were delivering State-of-the-art performance for most sequence modelling tasks

### **Attention Mechanism**

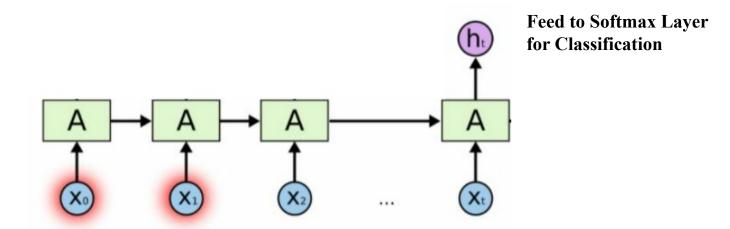
#### **Motivation for Attention Mechanisms**

- The Deep Learning Architecture that we have seen so far are hard to interpret (black-box)
- Recurrent Network provide a fixed vector encoding of a sequence at each step

→ Attention Mechanisms

We want to classify (X0, Xt) sequences (e.g. sentiment analysis)

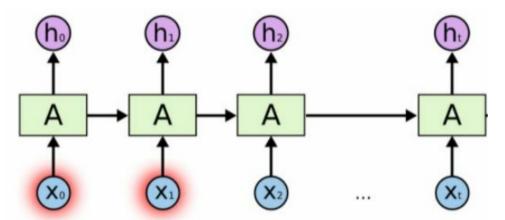
**Solution 1:** Use a LSTM model → Problem (not interpretable)



We want to classify (X0, Xt) sequences (e.g. sentiment)

**Solution 2:** Integrate an Attention Mechanism to interpret what input impacts the prediction

→ <u>Learn</u> a ponderation/weighting of the hidden states ht



We want to classify (X0, Xt) sequences (e.g. sentiment)

### How to learn this weighting?

- 1. Define a specific type of layer to learn the ponderation
- 2. Train this layer end-to-end with all the other parameters of the model

We want to classify (X0, Xt) sequences (e.g. sentiment)

#### How to learn this weighting?

Given  $(h_1, ..., h_T)$  hidden representations of  $(x_1, ..., x_T)$  (e.g. output of a LSTM Layer).

$$q_i = tanh(W_a h_i + b_a), \text{ with } W_a \in \mathbb{R}^{\delta \times \delta_a}$$

$$s_t = \frac{e^{q_t q_T}}{\sum_j e^{q_j q_T}}, \text{ i.e. } \sum_{t \in [|1,T|]} s_i = 1$$

$$\tilde{h_T} = \sum_{t \in [1,T]} s_t . h_t$$

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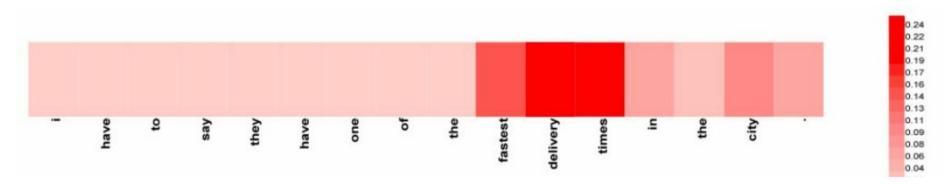
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We want to classify (X0, Xt) sequences (e.g. sentiment classification)

After we trained the model, **Attention scores** can be used **to interpret the model** behavior and **what input vector impacted the decision** 





Many variant of Attention Mechanisms (in combination with LSTM layers) have been designed

### **Design Choices**

- How to define the *query vectors*?
- How to define the *scoring function*?

Many variants exists but the principles are the same.

## The Transformer Architecture

#### Attention might be all we need

Do we really need recurrent layers?

RNN models (such as vanilla RNN, LSTM...) were designed to model sequential data

Still, for most tasks, we need both left and right context (e.g. sequence classification, sequence labelling..)

Why not modelling sequences in a bi-directional way directly

→ Using Self-Attention Mechanism

Given a sequence of input vectors  $(x_1,..,x_T) \in \mathbb{R}^{\delta}$  (noted  $(h_{0,1},..,h_{0,T})$ ).

#### **Objective:**

• Build a representation of the input vectors based on the **surrounding vectors** (both right-and left-context)

#### Idea:

- No need of recurrent cells
- → Self-Attention

Given a sequence of input vectors  $X = (x_1, ..., x_T) \in \mathbb{R}^{\delta}$  (noted  $H = (h_{0,1}, ..., h_{0,T})$ ).

We build 3 new vectorial representation of our sequence  $H = (h_1, ..., h_T)$ .

- For a given vector  $h_t$  and its query vector  $q_t$  we want to build the new representation vector  $\tilde{h}_t$
- Using the best ponderation of the information encoded in  $(v_1,..,v_T)$
- This ponderation being computed by finding the key vectors in  $(k_1, ..., k_T)$  that are more similar to the query vector  $q_t$  (that encodes relevant information from  $h_t$ ).

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$$q_t = W_Q h_t$$
 ,  $\forall \, t \in [|1,T|] \text{ with } W_Q \in \mathbf{R}^{\delta_q imes \delta}$ 

$$k_t = W_K h_t$$
,  $\forall t \in [|1, T|]$  with  $W_K \in \mathbb{R}^{\delta_k \times \delta}$ 

$$v_t = W_V h_t$$
,  $\forall t \in [|1,T|]$  with  $W_V \in \mathbb{R}^{\delta_v \times \delta}$ 

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$$\tilde{H} = softmax(\frac{QK^T}{\sqrt{\delta_K}})V$$

i.e. 
$$\tilde{h_t} = softmax(\frac{q_t K^T}{\sqrt{\delta_K}}).V = \sum_{t'} s_{t'} v_{t'} \text{ with } s_{t'} = \frac{e^{q_{t'}k_t}}{\sum_t e^{q_{t'}k_t}}$$

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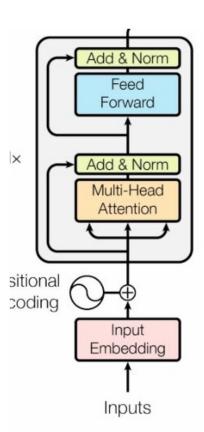
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#### The Transformer Architecture

#### The Transformer Architecture is

- Stack of [Self-Attention + FF Layer]
- With Skip-Layer and Normalization
   Layers in between
- Encoding the position with positional vector



### **Positional Embedding Vector**

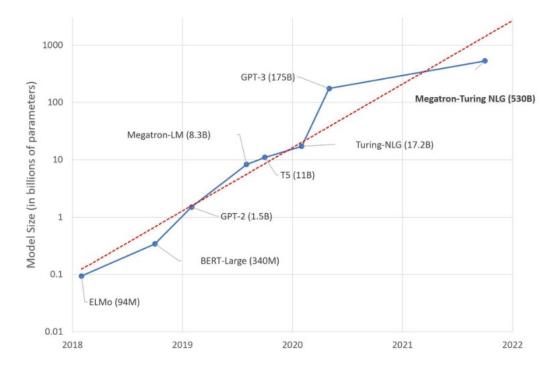
- Limitation: self attention does not take position into account!
- Indeed, shuffling the input gives the same results
- · Solution: add position encodings.
- Replace the matrix **W** by **W** + **E**, where  $\mathbf{E} \in \mathbb{R}^{d \times T}$
- E can be learned, or defined using sin and cos:

$$e_{2i,j}=\sin\left(rac{j}{10000^{2i/d}}
ight)$$
  $e_{2i+1,j}=\cos\left(rac{j}{10000^{2i/d}}
ight)$ 

### **Scaling Laws Intuition**

- The larger the dimension of the weight matrices
- The larger the number of parameters in the model
- The more "expressive" is the model
- The better it will generalizes

# **Typical Architecture Sizes**



#### **Lecture Summary**

#### Deep Learning is a powerful and general modelling approach

- Designing Architectures, i.e. composition of linear transformation and non-linear transformation (possibly including recurrences)
- All those transformations **should be differentiable**
- All the parameters of the model are trained with backpropagation
- Toward a specific task s.t. regression or classification
- All the hyperparameters are chosen based on **best-practices** or empirical research