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# Antennas and Radio Wave Propagation

EP2950



**KTH Technology  
and Health**

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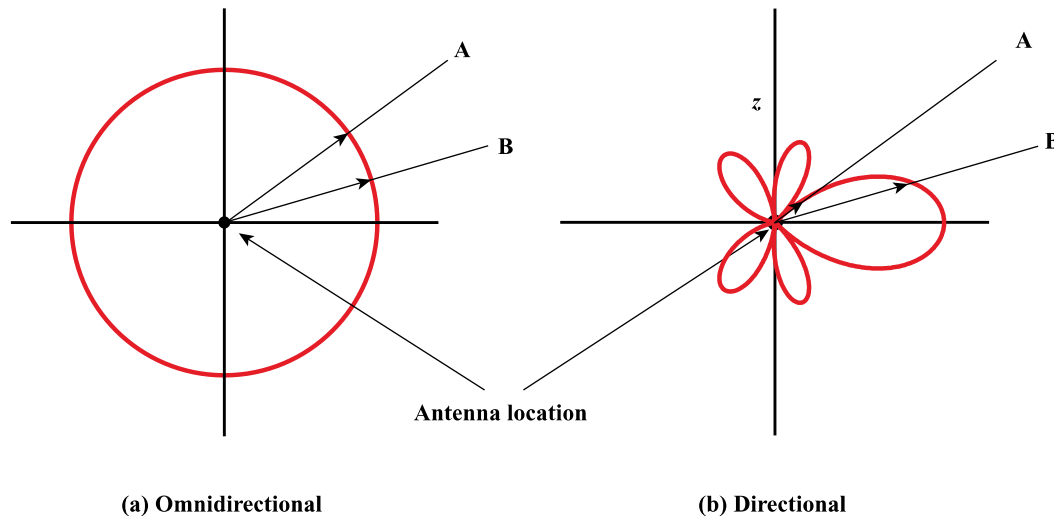
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# Outline

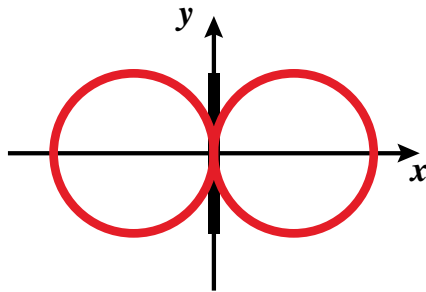
- Antennas and radiation
- Wireless transmission impairment
- Multipath fading

# Antennas and radiation patterns

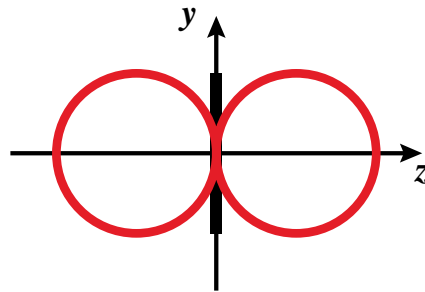
- Transmits and receives electromagnetic energy
- Idealized radiation patterns (isotropic)
- Omnidirectional and directional
- Main lobe, side lobes and nulls
- Beam width (half-power) – a measure of directivity



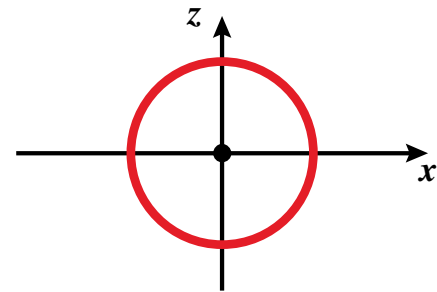
# Radiation patterns



Side view ( $xy$ -plane)

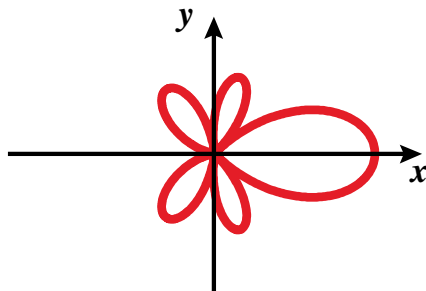


Side view ( $zy$ -plane)

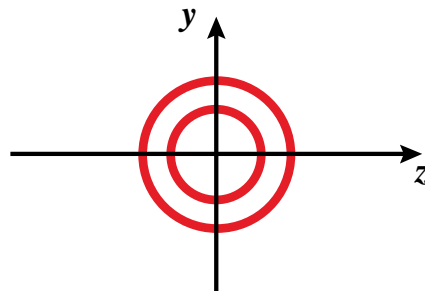


Top view ( $xz$ -plane)

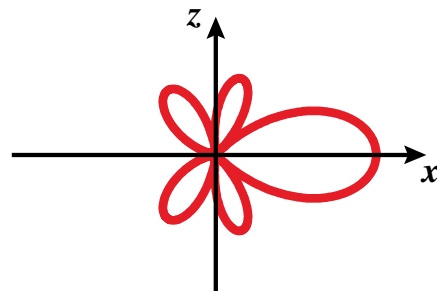
(a) Simple dipole



Side view ( $xy$ -plane)



Side view ( $zy$ -plane)



Top view ( $xz$ -plane)

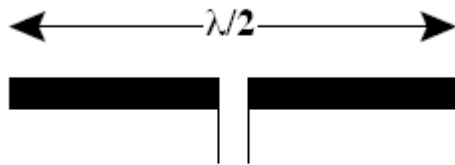
(b) Directed antenna

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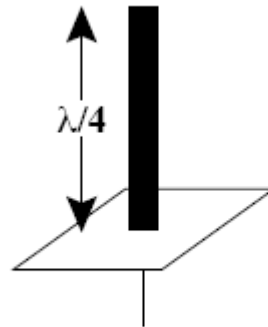
# Types of antennas

- Isotropic antenna (idealized)
  - ✓ Radiates power equally in all directions
- Dipole
  - ✓ Half-wave dipole antenna (or Hertz antenna)
  - ✓ Quarter-wave vertical antenna (or Marconi antenna)
- Parabolic reflective antenna

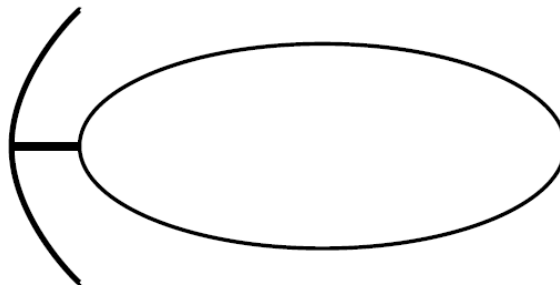
# Antenna types



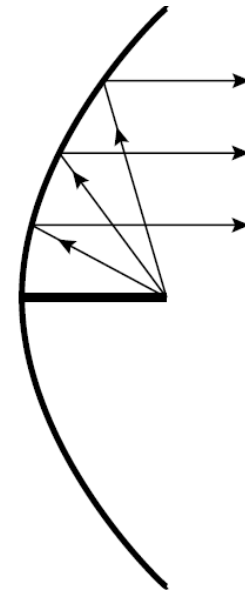
(a) Half-wave dipole



(b) Quarter-wave antenna

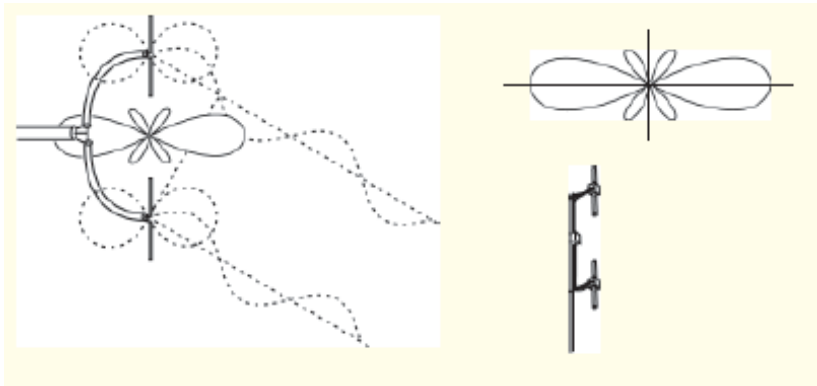


(c) Cross-section of parabolic antenna  
showing radiation pattern



(b) Cross-section of parabolic antenna  
showing reflective property

- Combining several antenna elements



4 elements increase the directivity

This section illustrates a four-element antenna array. On the left, a physical schematic shows four vertical antenna elements mounted on a single vertical support structure. To the right, a radiation pattern is shown with four main lobes pointing horizontally, indicating increased directivity compared to the two-element array. Below the radiation pattern is a solid orange rectangular box.

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# Antenna gain

- Antenna gain
  - ✓ Measure of directionality
  - ✓ Power output, in a particular direction, compared to that produced in any direction by a perfect omnidirectional antenna (isotropic antenna)
- Effective area -  $A_e$ 
  - ✓ Related to physical size and shape



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- Antenna gain and effective area

$G$  = antenna gain

$A_e$  = effective area

$f$  = carrier frequency

$c$  = speed of light ( $\approx 3 \times 10^8$  m/s)

$\lambda$  = carrier wavelength

$$G = \frac{4\pi A_e}{\lambda^2} = \frac{4\pi f^2 A_e}{c^2}$$

- Antenna gain and directivity,  $G = \eta \cdot D$

$G$  = antenna gain

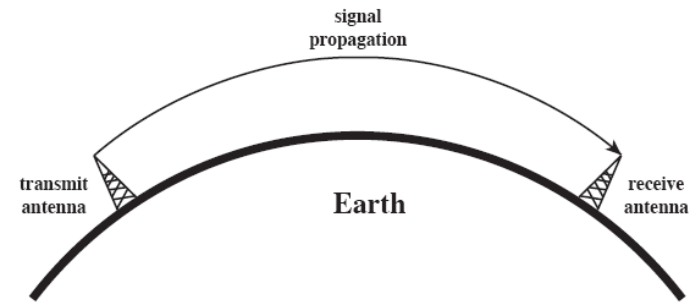
$\eta$  = efficiency of the antenna

$D$  = directivity

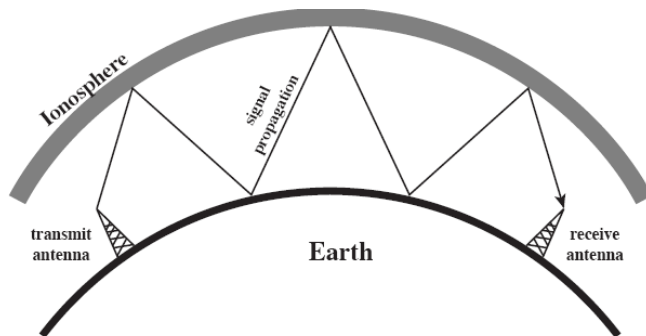
$\eta$  is often close to 1.0

# Propagation modes

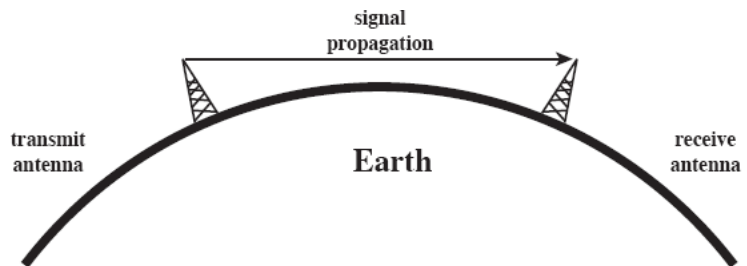
- Ground-wave propagation
- Sky-wave propagation
- Line-of-sight propagation



(a) Ground-wave propagation (below 2 MHz)



(b) Sky-wave propagation (2 to 30 MHz)



(c) Line-of-sight (LOS) propagation (above 30 MHz)

**Table 5.3 Frequency Bands**

| Band                           | Frequency Range    | Free-Space Wavelength Range | Propagation Characteristics   | Typical Use  |
|--------------------------------|--------------------|-----------------------------|---|--|
| ELF (extremely low frequency)  | 30 to 300 Hz       | 10,000 to 1,000 km          | GW  | Power line frequencies; used by some home control systems.   |
| VF (voice frequency)           | 300 to 3000 Hz     | 1,000 to 100 km             | GW  | Used by the telephone system for analog subscriber lines.  |
| VLF (very low frequency)       | 3 to 30 kHz        | 100 to 10 km                | GW; low attenuation day and night; high atmospheric noise level                               | Long-range navigation; submarine communication   |
| LF (low frequency)             | 30 to 300 kHz      | 10 to 1 km                  | GW; slightly less reliable than VLF; absorption in daytime                                    | Long-range navigation; marine communication radio beacons  |
| MF (medium frequency)          | 300 to 3000 kHz    | 1,000 to 100 m              | GW and night SW; attenuation low at night, high in day; atmospheric noise                     | Maritime radio; direction finding; AM broadcasting.  |
| HF (high frequency)            | 3 to 30 MHz        | 100 to 10 m                 | SW; quality varies with time of day, season, and frequency.                                   | Amateur radio; international broadcasting, military communication; long-distance aircraft and ship communication |
| VHF (very high frequency)      | 30 to 300 MHz      | 10 to 1 m                   | LOS; scattering because of temperature inversion; cosmic noise                                | VHF television; FM broadcast and two-way radio, AM aircraft communication; aircraft navigational aids            |
| UHF (ultra high frequency)     | 300 to 3000 MHz    | 100 to 10 cm                | LOS; cosmic noise   | UHF television; cellular telephone; radar; microwave links; personal communications systems                      |
| SHF (super high frequency)     | 3 to 30 GHz        | 10 to 1 cm                  | LOS; rainfall attenuation above 10 GHz; atmospheric attenuation due to oxygen and water vapor | Satellite communication; radar; terrestrial microwave links; wireless local loop                                 |
| EHF (extremely high frequency) | 30 to 300 GHz      | 10 to 1 mm                  | LOS; atmospheric attenuation due to oxygen and water vapor                                    | Experimental; wireless local loop  |
| Infrared                       | 300 GHz to 400 THz | 1 mm to 770 nm              | LOS   | Infrared LANs; consumer electronic applications  |
| Visible light                  | 400 THz to 900 THz | 770 nm to 330 nm            | LOS   | Optical communication  |

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- Radio line-of-sight (LOS) equations

- ✓ Maximum distance between two antennas

- ✓ K due to refraction

$$d=3.57(\sqrt{Kh_1}+ \sqrt{Kh_2})$$

- ✓ K=4/3 (rule of thumb)

$$d=4.1(\sqrt{h_1}+ \sqrt{h_2})$$

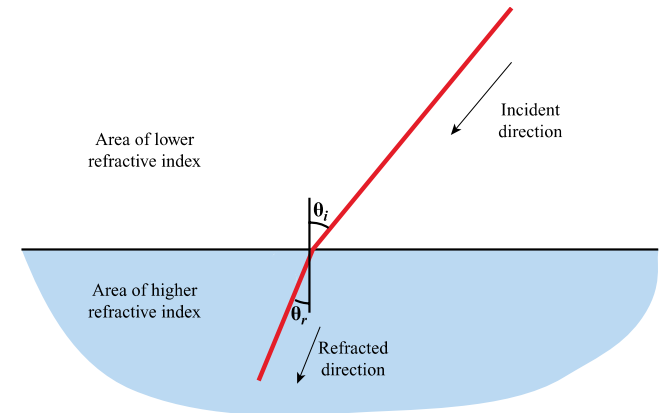
d = distance (km)

$h_1$  = height of antenna one (m)

$h_2$  = height of antenna two (m)

## ■ Five basic propagation mechanisms

- ✓ Free-space propagation
- ✓ Transmission through a medium  
Refractions
- ✓ Reflections
- ✓ Diffractions  
“Bending” round corners
- ✓ Scattering



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# Wireless transmission impairment

- Free space loss
- Noise
- Atmospheric absorption
- Multipath
- Refraction

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- Free space loss

- ✓ Ideal isotropic antenna

$$\frac{P_t}{P_r} = \frac{(4\pi d)^2}{\lambda^2} = \frac{(4\pi f d)^2}{c^2}$$

$P_t$  = signal power at transmitting antenna

$P_r$  = signal power at receiving antenna

$\lambda$  = carrier wavelength

$d$  = propagation distance between antennas

$c$  = speed of light ( $\approx 3 \times 10^8$  m/s)

where  $d$  and  $\lambda$  are in the same units (e.g., meters)

- 
- Expressed in dB

$$\begin{aligned} L_{dB} &= 10 \lg \frac{P_t}{P_r} = 20 \lg \left( \frac{4\pi d}{\lambda} \right) \\ &= -20 \lg(\lambda) + 20 \lg(d) + 21.98 \text{ dB} \\ &= 20 \lg \left( \frac{4\pi f d}{c} \right) = 20 \lg(f) + 20 \lg(d) - 147.56 \text{ dB} \end{aligned}$$

- If expressed as path loss exponent

$$20 \lg(f) + 10n \lg(d) - 147.56 \text{ dB}$$



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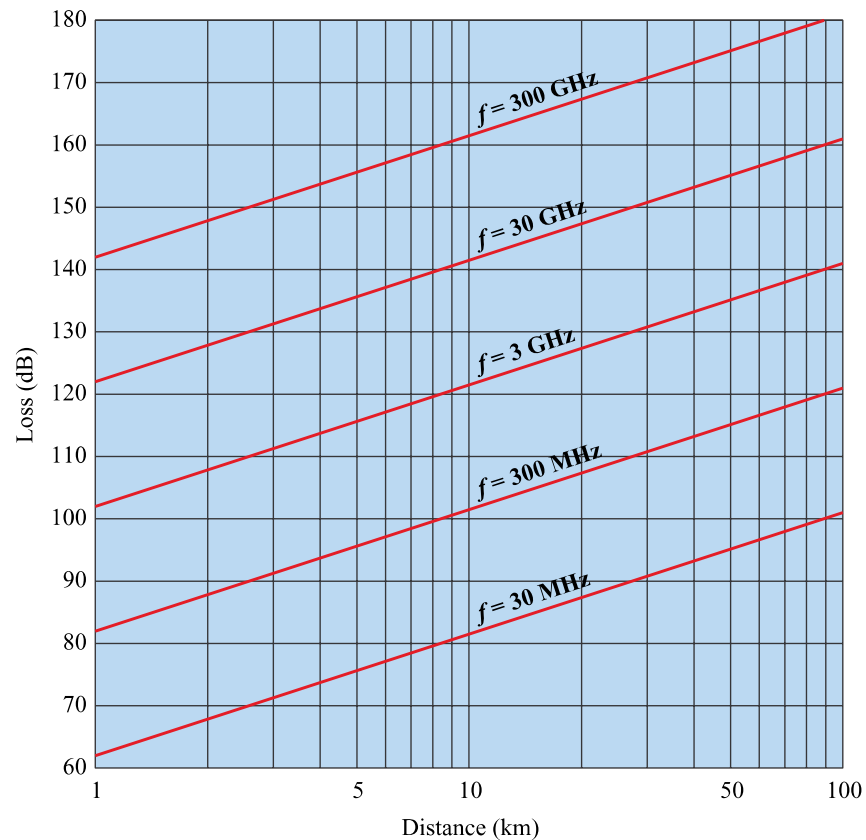
- Path loss exponents

**Table 6.5 Path Loss Exponents for Different Environments [RAPP02]**

| Environment               | Path Loss Exponent, $n$ |
|---------------------------|-------------------------|
| Free space                | 2                       |
| Urban area cellular radio | 2.7 to 3.5              |
| Shadowed cellular radio   | 3 to 5                  |
| In building line-of-sight | 1.6 to 1.8              |
| Obstructed in building    | 4 to 6                  |
| Obstructed in factories   | 2 to 3                  |

- Example:  $f=300$  MHz,  $d=1$  km

$$L_{dB} = -147.56 + 20 \cdot \lg(1000) + 20 \cdot \lg(300 \cdot 10^6) = \\ -147.56 + 60 + 169.54 = 82 \text{ dB}$$



- 
- Taking antenna gain into account

$$\frac{P_t}{P_r} = \frac{(4\pi d)^2}{G_r G_t \lambda^2} = \frac{(\lambda d)^2}{A_r A_t} = \frac{(cd)^2}{f^2 A_r A_t}$$

$G_t$  = gain of transmitting antenna     $G = (4\pi A_e) / \lambda^2$

$G_r$  = gain of receiving antenna

$A_t$  = effective area of transmitting antenna

$A_r$  = effective area of receiving antenna

$$\begin{aligned} L_{dB} &= 20 \lg(\lambda) + 20 \lg(d) - 10 \lg(A_t A_r) \\ &= -20 \lg(f) + 20 \lg(d) - 10 \lg(A_t A_r) + 169.54 \text{dB} \end{aligned}$$

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# Thermal noise

- Amount of thermal noise to be found in a bandwidth of 1Hz in any device or conductor is

$$N_0 = kT \text{ (W/Hz)}$$

$N_0$  = noise power density in watts per 1 Hz of bandwidth

$k$  = Boltzmann's constant =  $1.3803 \times 10^{-23}$  J/K

$T$  = temperature, in Kelvin (absolute temperature)

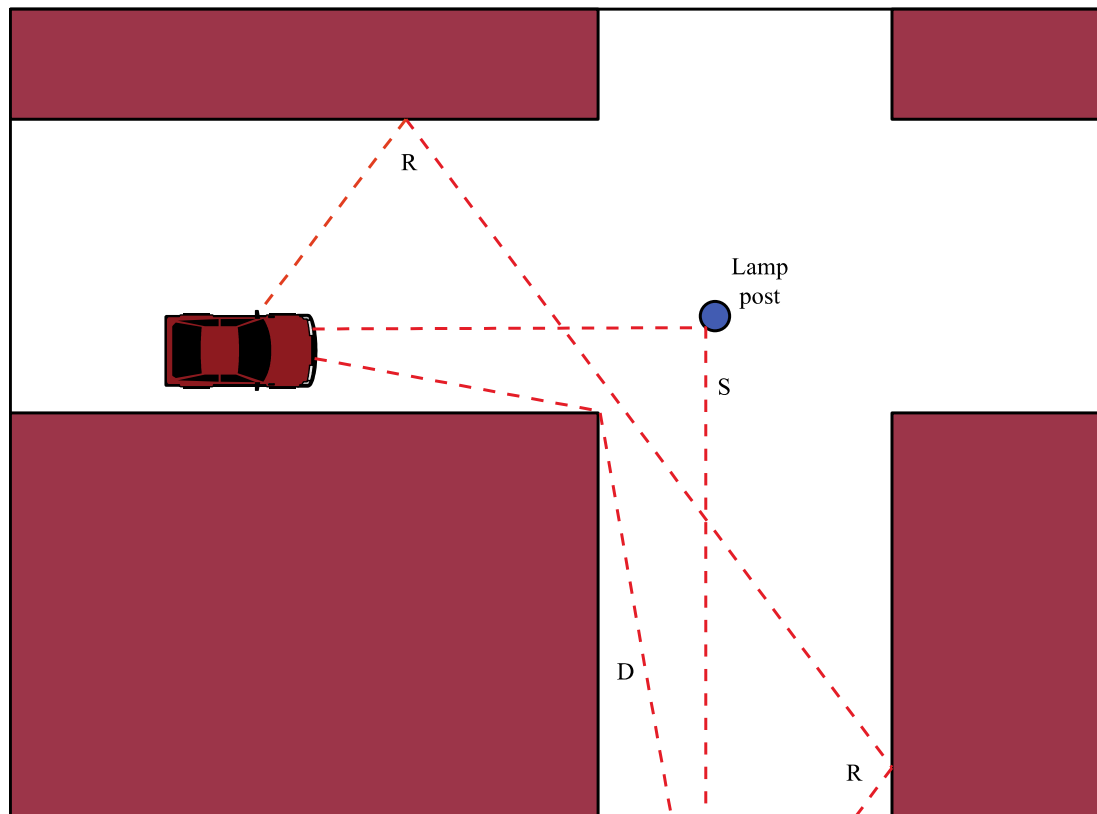
$$N = kTB$$

$$N = 10 \lg k + 10 \lg T + 10 \lg B$$

$$= -228.6 \text{ dBW} + 10 \lg T + 10 \lg B$$

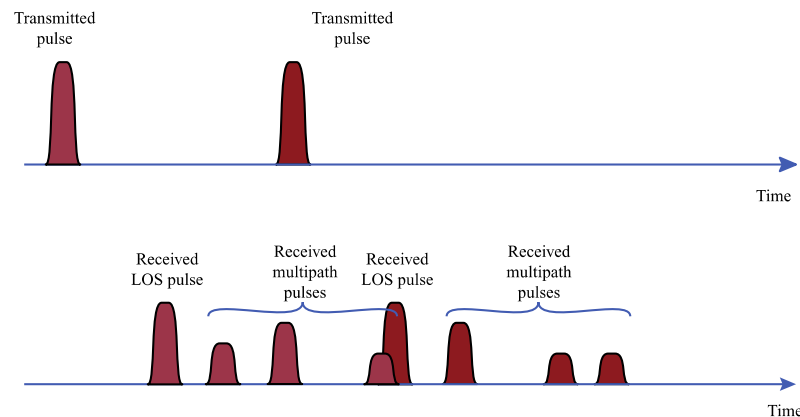
# Multipath propagation and fading

- Reflection (R), scattering (S) and diffraction (D)



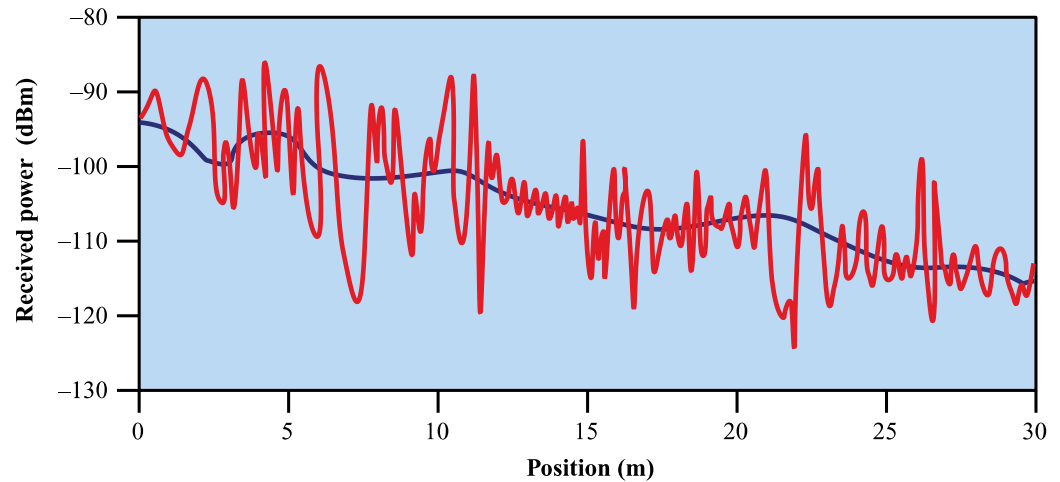
# Effect of multipath propagation

- Multiple copies of a signal may arrive at different phases
  - ✓ If phases add destructively, the signal level relative to noise declines, making detection more difficult
- Inter-symbol interference - ISI
  - ✓ One or more delayed copies of a pulse may arrive at the same time as the primary pulse for a subsequent bit

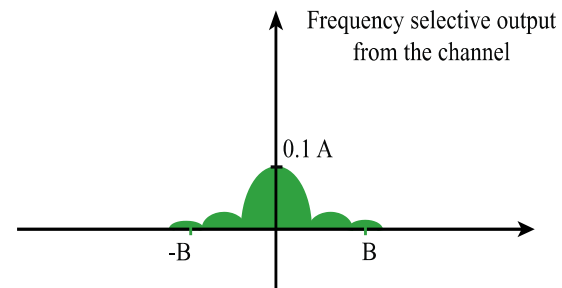
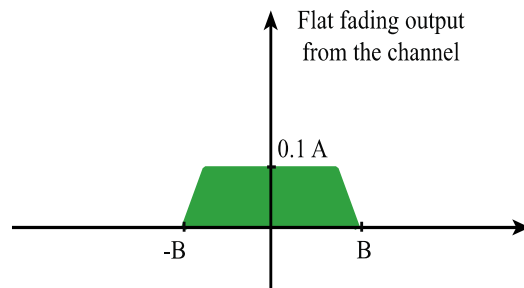
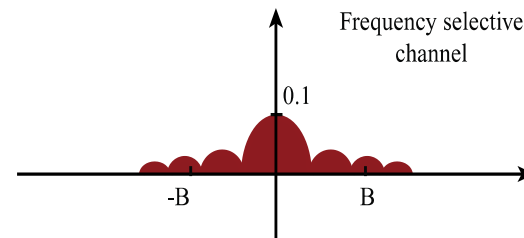
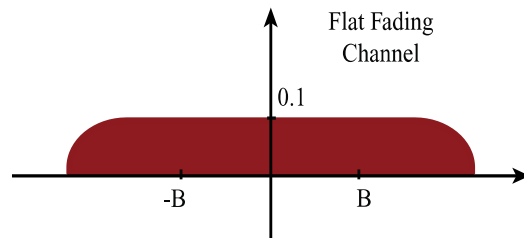
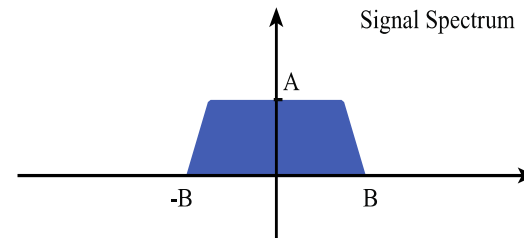
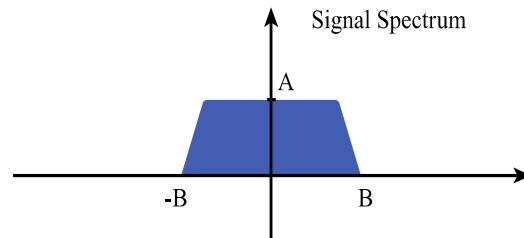


# Types of fading

- Fast fading
- Slow fading
- Flat fading
- Selective fading
- Rayleigh fading
- Rician fading



# Flat and frequency selective fading





- 
- Fast or short-term fading
    - ✓ Rapid variation in signal strength, e.g. MS moves in urban area
    - ✓ Short reflections – delay  $< 20\%$  of symbol time  $\approx 3.7\ \mu\text{s}$  (220 m)
    - ✓ Rayleigh/Rice fading
  - Slow or long-term fading
    - ✓ Shadowing e.g. large buildings, mountains etc.
    - ✓ Time dispersion (delay spread), inter-symbol interference (ISI)
  - Okumura-Hata path loss model
    - ✓  $L_{\text{dB}}(\text{urban})$ ,  $L_{\text{dB}}(\text{suburban})$  and  $L_{\text{dB}}(\text{open})$
    - ✓ Stallings p. 175-176

- 
- Coherence bandwidth and time
    - ✓  $B_C$  is the range of frequencies where the channel is “flat”
    - ✓ Coherence time  $T_C = 1/B_C$ , the time when the channel is stable
  - Signal bandwidth and time
    - ✓  $T_B$  bit time,  $T_B = 1/r_B$  where  $r_B$  is the bit rate.
    - ✓ Symbol time  $T_S = T_B$  (if one bit per symbol)
    - ✓  $B_S$  is the signal bandwidth ( $B_S \approx r_B$ )
  - If  $T_C \gg T_S$ , coherence time  $\gg$  symbol time
    - ✓ Slow fading, otherwise fast fading
  - If  $B_C \gg B_S$ , channel bandwidth  $\gg$  signal bandwidth
    - ✓ Flat fading, otherwise frequency-selective
  - Delay disperse ( $T_D$ ) and symbol time ( $T_S$ )
  - Inter-symbol interference (ISI)
    - ✓  $T_D$  larger than  $T_S$
-

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# Example slow fading

- Doppler spread
    - Frequency fluctuations caused by movement
    - Coherence time  $T_c$  characterizes Doppler shift
      - How long a channel remains the same
    - Coherence time  $T_c \gg T_b$  bit time  $\rightarrow$  *slow fading*
      - The channel does not change during the bit time
    - Otherwise *fast fading*
  - Example 6.11
    - $T_c = 70$  ms, bit rate  $r_b = 100$  kbps
    - Bit time  $T_b = 1/100 \times 10^3 = 10$   $\mu$ s
    - Is  $T_c \gg T_b$ ?  $70$  ms  $\gg 100$   $\mu$ s
    - True, slow fading
-

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## Example frequency selective fading

### ■ Multipath fading

- Multiple signals arrive at the receiver
- Coherence bandwidth  $B_c$  characterizes multipath
  - Bandwidth over which the channel response remains relatively constant
  - Related to delay spread, the spread in time of the arrivals of multipath signals
- Signal bandwidth  $B_s$  is proportional to the bit rate
- If  $B_c \gg B_s$ , then *flat fading*
  - The signal bandwidth fits well within the channel bandwidth
- Otherwise, *frequency selective fading*

### ■ Example 6.11

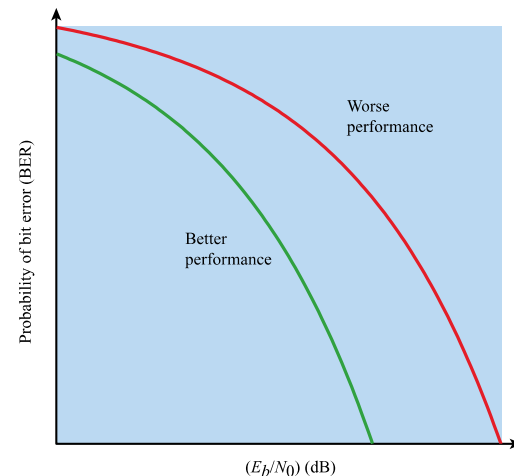
- $B_c = 150$  kHz, bit rate  $r_b = 100$  kbps
  - Assume signal bandwidth  $B_s \approx r_b$ ,  $B_s = 100$  kHz
  - Is  $B_c \gg B_s$ ?  $150$  kHz  $\gg$   $100$  kHz?
  - False, so frequency selective fading
-

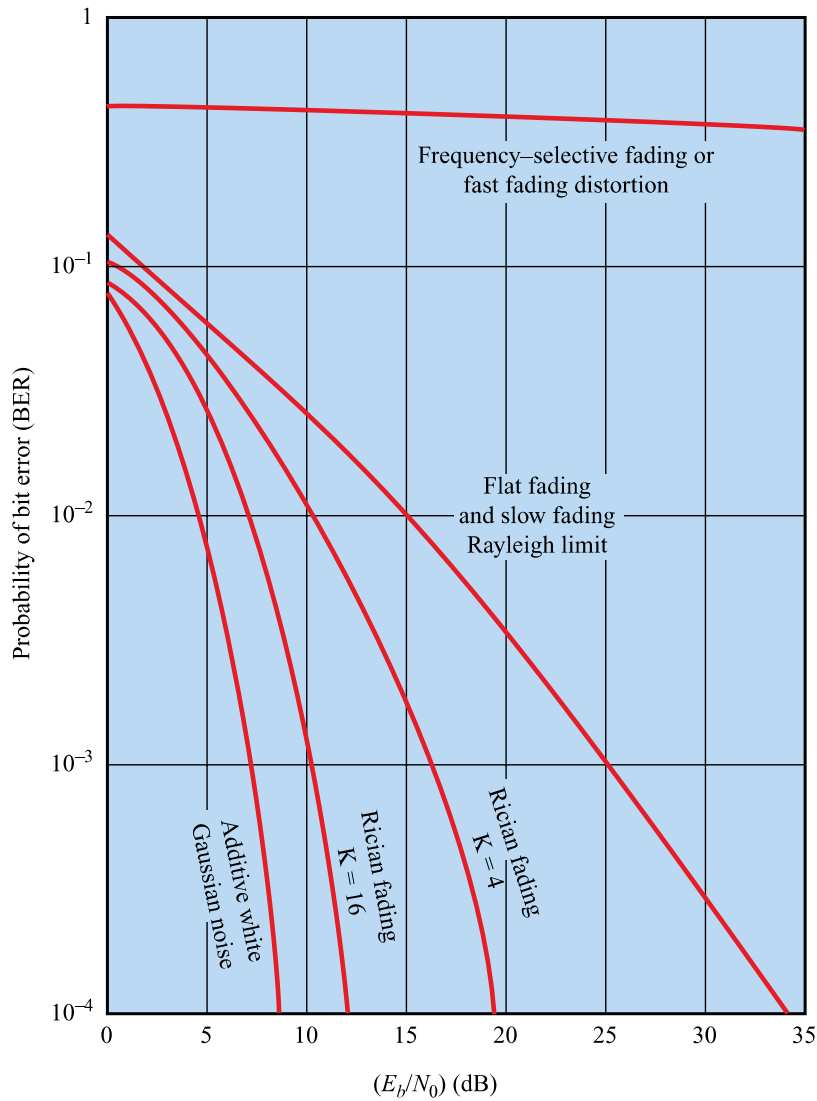
# The expression $E_b/N_0$

- Ratio of signal energy per bit to noise power density per Hertz

$$\frac{E_b}{N_0} = \frac{S / R}{N_0} = \frac{S}{kTR} \quad \text{if } R=B \quad \frac{E_b}{N_0} = \frac{S}{kTB} = \frac{S}{N}$$

- The bit error rate for digital data is a function of  $E_b/N_0$ 
  - ✓ Given a value for  $E_b/N_0$  to achieve a desired error rate, parameters of this formula can be selected
  - ✓ As bit rate  $R$  increases, transmitted signal power must increase to maintain required  $E_b/N_0$





$$K = \frac{\text{Power in dominant path}}{\text{Power in the scattered paths}}$$

$K=0 \Rightarrow$  Rayleigh fading

$K > 0 \Rightarrow$  Rician fading

$K = \text{infinite} \Rightarrow$  AWGN

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# Channel correction mechanisms

- Forward error correction
  - Adaptive equalization
  - Adaptive modulation and coding
  - Diversity techniques and MIMO
  - OFDM
  - Spread spectrum
  - Bandwidth expansion
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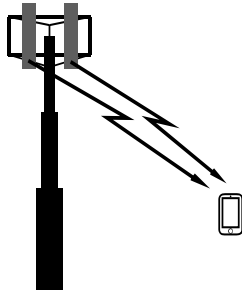
# Multiple input multiple output (MIMO)

- Use antenna arrays for
    - ✓ Same stream - several antennas
    - ✓ Multiple streams – increase capacity
    - ✓ Beamforming – directional antennas
    - ✓ Multi-user MIMO – directional beams to multiple simultaneous users
  - Modern systems
    - ✓  $4 \times 4$  (4 transmitter and 4 receiver antennas)
    - ✓  $8 \times 8$
    - ✓ Future: massive MIMO with many more antennas
-

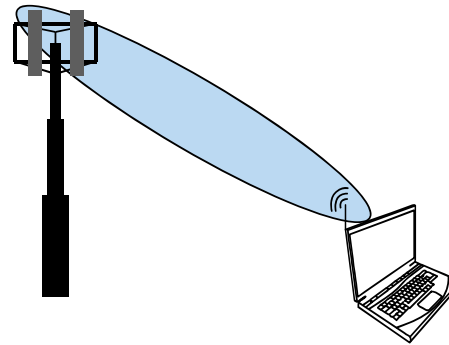


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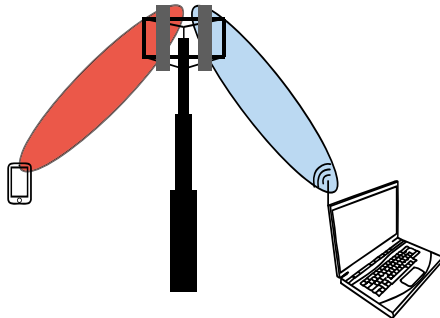
# Four cases of MIMO



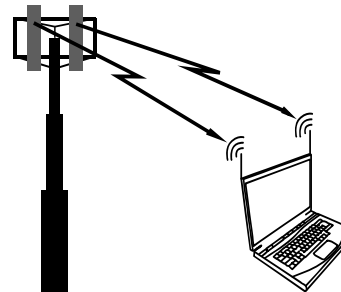
Diversity for improved  
system performance



Beam-forming for improved coverage  
(less cells to cover a given area)



Spatial division multiple access  
("MU-MIMO") for improved capacity  
(more user per cell)



Multi layer transmission  
("SU-MIMO") for higher data rates  
in a given bandwidth

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# Link budget calculations

|     |  |   |       |       |
|-----|--|---|-------|-------|
| 1.  | Transmitter power, $P_t$ .....         | + | ..... | [dBW] |
| 2.  | Attenuation in cable .....             | - | ..... | [dB]  |
| 3   | Transmitting antenna Gain, $G_t$ ..... | + | ..... | [dBi] |
| 4.  | Free space loss, $L_s$ .....           | - | ..... | [dB]  |
| 5.  | Atmospheric absorption .....           | - | ..... | [dB]  |
| 6.  | Effect of rain .....                   | - | ..... | [dB]  |
| 7.  | Effects of vegetation .....            | - | ..... | [dB]  |
| 8.  | Fading .....                           | - | ..... | [dB]  |
| 9.  | Receiving antenna gain .....           | + | ..... | [dBi] |
| 10. | Attenuation in cable .....             | - | ..... | [dB]  |
|     | Power to receiver: .....               | = | ..... | [dBW] |

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# Decibel (dB)

- See Appendix 2A
- $G_{\text{dB}} = 10 \cdot \lg(P_{\text{out}}/P_{\text{in}})$  – a dimensionless ratio
  - 1B=10dB

|                 |        |
|-----------------|--------|
| $1000=10^3$     | 30 dB  |
| $100=10^2$      | 20 dB  |
| $10=10^1$       | 10 dB  |
| $1=10^0$        | 0 dB   |
| $0.1=10^{-1}$   | -10 dB |
| $0.01=10^{-2}$  | -20 dB |
| $0.001=10^{-3}$ | -30 dB |

|     |                        |       |
|-----|------------------------|-------|
| 2   | $10\lg 2 \approx 3$    | 3 dB  |
| 4   | $10\lg 4 \approx 6$    | 6 dB  |
| 8   | $10\lg 8 \approx 9$    | 9 dB  |
| 1/2 | $10\lg 1/2 \approx -3$ | -3 dB |
| 1/4 | $10\lg 1/4 \approx -6$ | -6 dB |
| 1/8 | $10\lg 1/8 \approx -9$ | -9 dB |

- 
- Logarithms
    - $\lg(a \cdot b) = \lg(a) + \lg(b)$ ;  $\lg(a/b) = \lg(a) - \lg(b)$
  - $G_{\text{dB}} = 10 \times \lg(P_{\text{ut}}/P_{\text{in}})$ 
    - $G$  positive  $\rightarrow$  amplification
    - $G$  negative  $\rightarrow$  attenuation
  - Reference levels
    - dBW means that 0 dBW = 1 W
    - dBm means that 0 dBm = 1 mW
    - 0 dBW = 30 dBm
    - 0 dBm = -30 dBW
    - 100 mW = 20 dBm = -10 dBW
    - 2 W  $\approx$  3 dBW = 33 dBm

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## – Exercise

- Which amplification corresponds to 16 dB?
- $16 \text{ dB} = (10+3+3) \text{ dB}$  means  $10 \times 2 \times 2 = 40$  times ( $10^{1.6} \approx 40$ )
- “An electromagnetic wave is transmitted through an optical fibre that has attenuation 0.25 dB/km. Compute the distance from the starting point at which the power has decreased with 75 % of the original level.”
- Method 1: Power in:  $P_{\text{in}}$ . Power after  $L$  km:  $P_L$ .  
 $P_L = \frac{1}{4} \times P_{\text{in}}$   
 $10 \times \lg(P_L/P_{\text{in}}) = -0.25L$   
 $-0.25L = 10 \times \lg(1/4) \rightarrow L = 24 \text{ km}$
- Method 2:  
 $\frac{1}{4} = -6 \text{ dB}$  (attenuation 4 times).  
 $6 \text{ dB} = 0.25 \text{ dB} \times L \rightarrow L = 24 \text{ km}.$