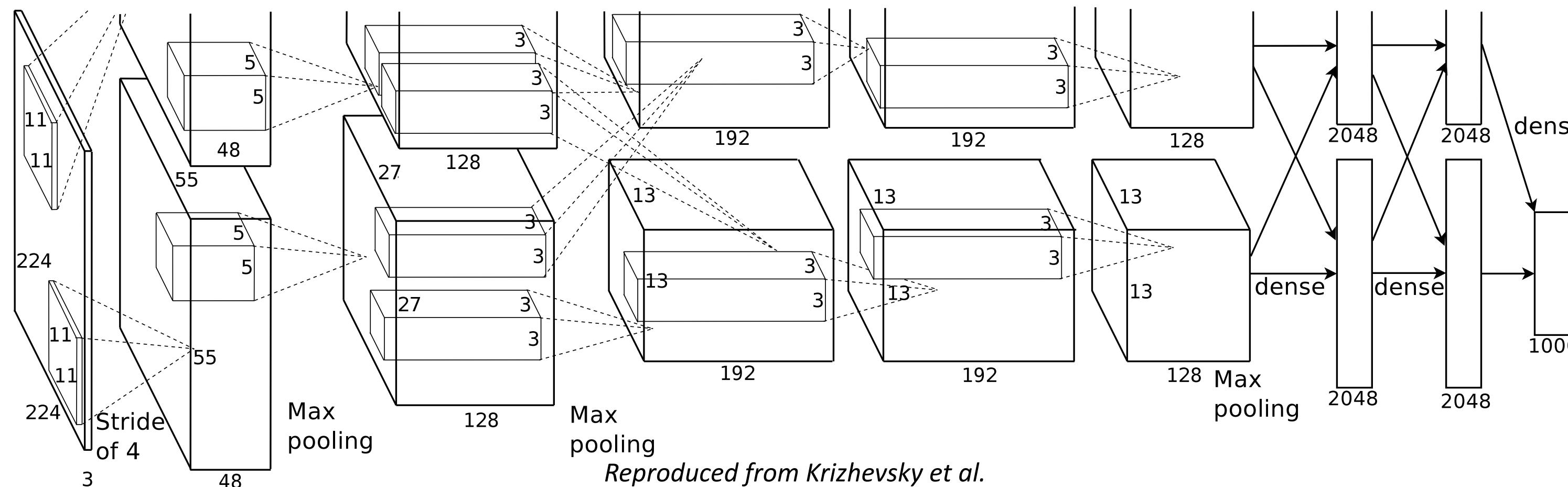


Artificial Intelligence & Data Analysis

Lecture 1: Convolutional Neural Networks



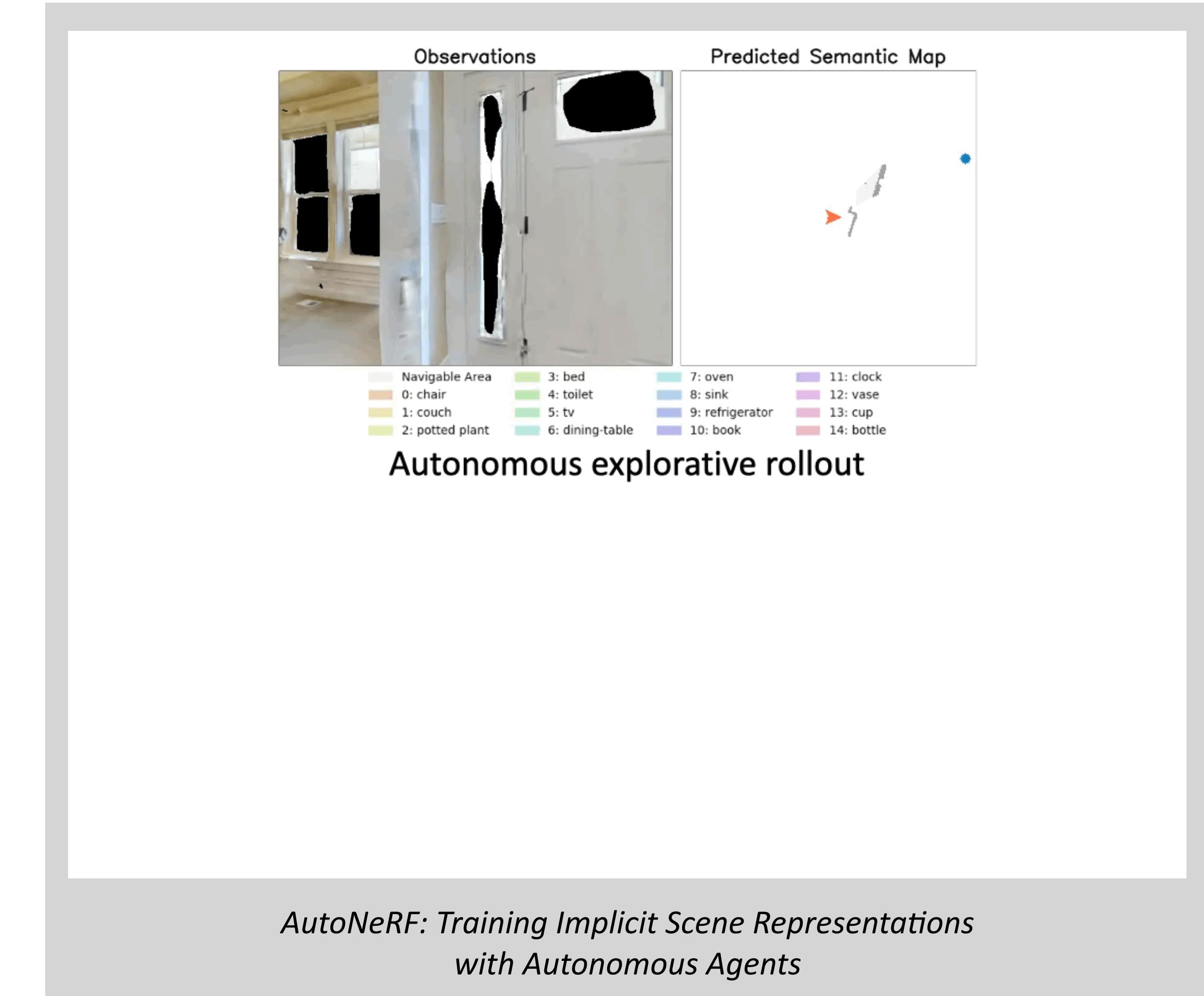
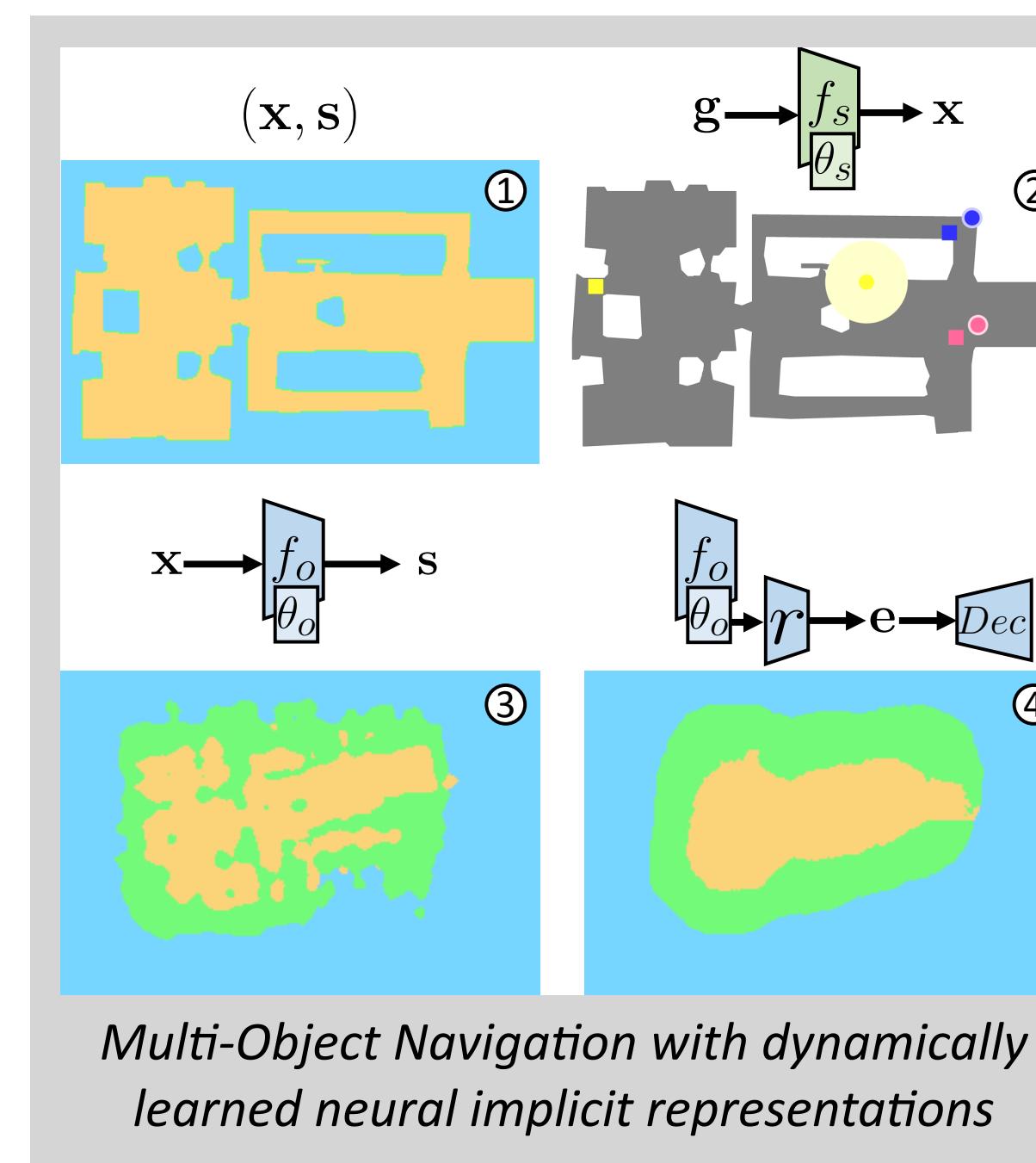
Lyon 1

Pierre Marza

About me

Pierre Marza: PhD student at INSA Lyon

Embodied AI, Visual Navigation, Deep Learning, Computer Vision, Reinforcement Learning



Course Overview

1. Convolutional Neural Networks (Lecture + practical)
2. Recurrent Neural Networks (Lecture + *optional* practical)
3. Reinforcement Learning 1 (Johan Peralez)
4. Reinforcement Learning 2 (Johan Peralez)
5. Project (15h)

Evaluation

1. Project oral/written presentation
2. Final exam (Multiple-choice questions)

Useful resources

Ian Goodfellow, Yoshua Bengio, Aaron Courville, **Deep Learning**, 2017, MIT Press (<https://www.deeplearningbook.org/>)

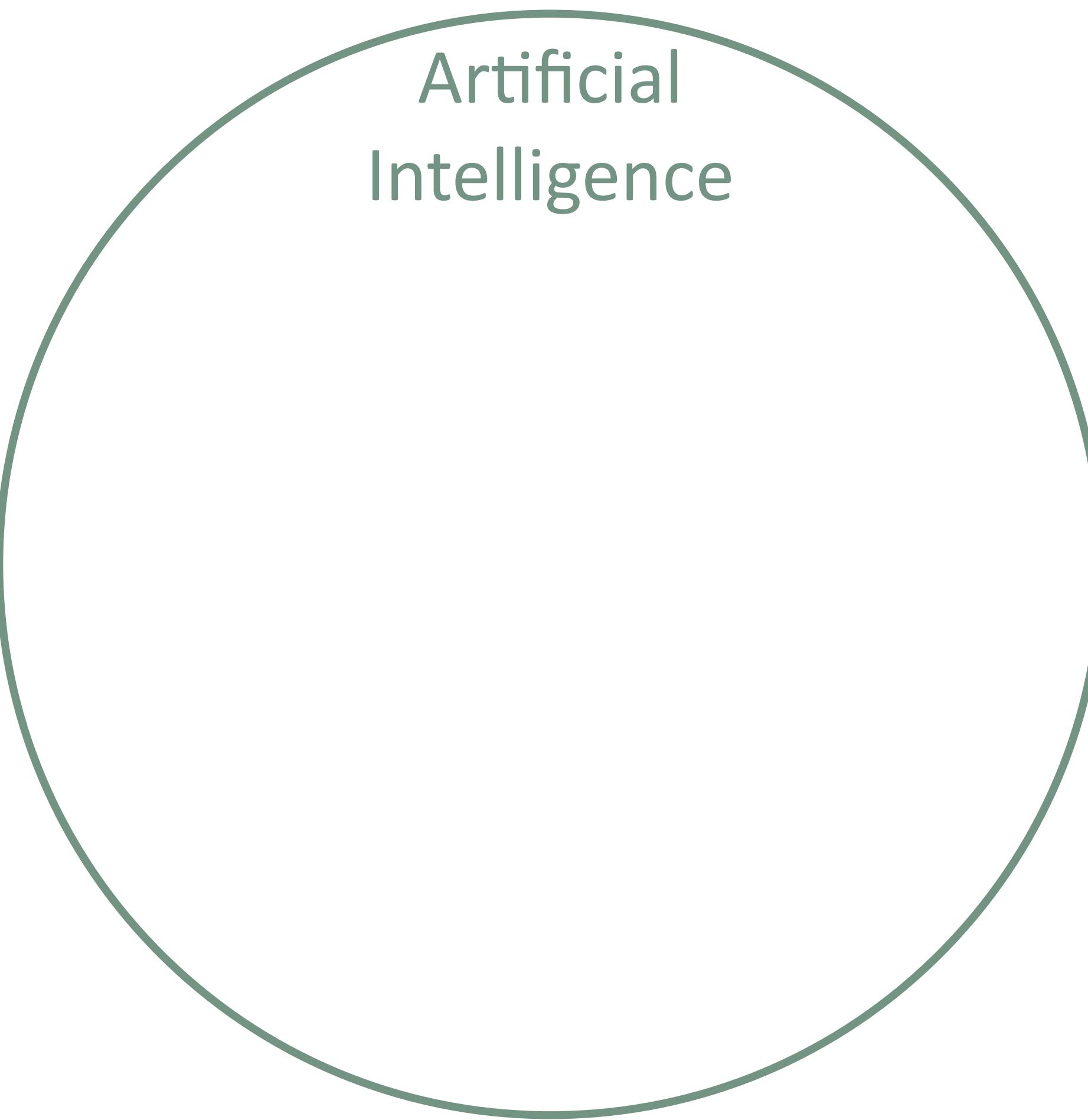
Pytorch Tutorials: <https://pytorch.org/tutorials/>

Christopher M. Bishop, **Pattern recognition and machine learning**, 2006, Springer (Machine Learning resource, not only Deep Learning)

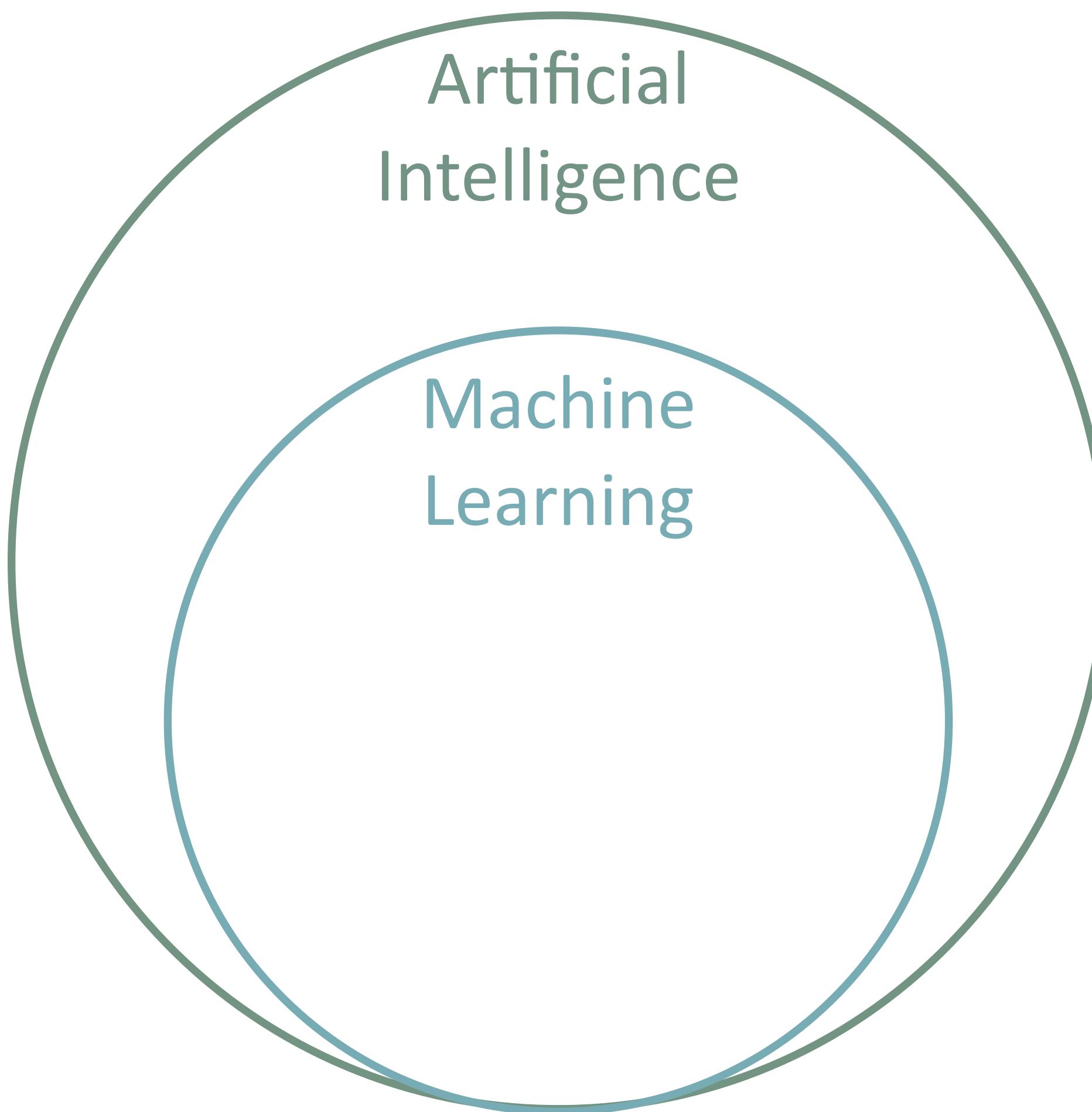
Interesting read: Rich Sutton, **The Bitter Lesson**, 2019 (<http://www.incompleteideas.net/Incldeas/BitterLesson.html>)

Some of the material of this course is inspired by the lectures given by Christian Wolf (my PhD advisor) at INSA Lyon. You can find his full course here: <https://chriswolfvision.github.io/www/teaching/index.html>

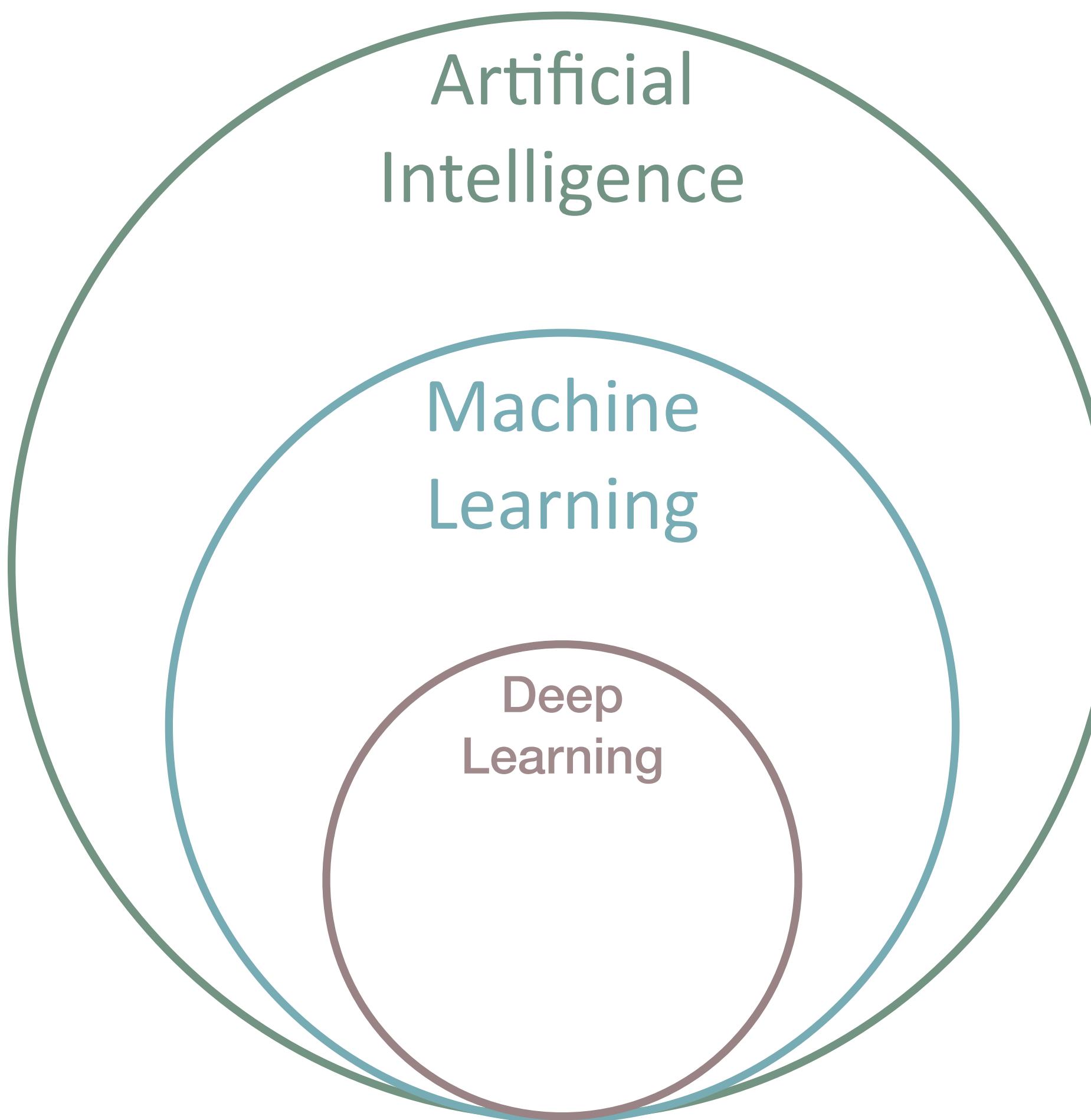
Artificial Intelligence



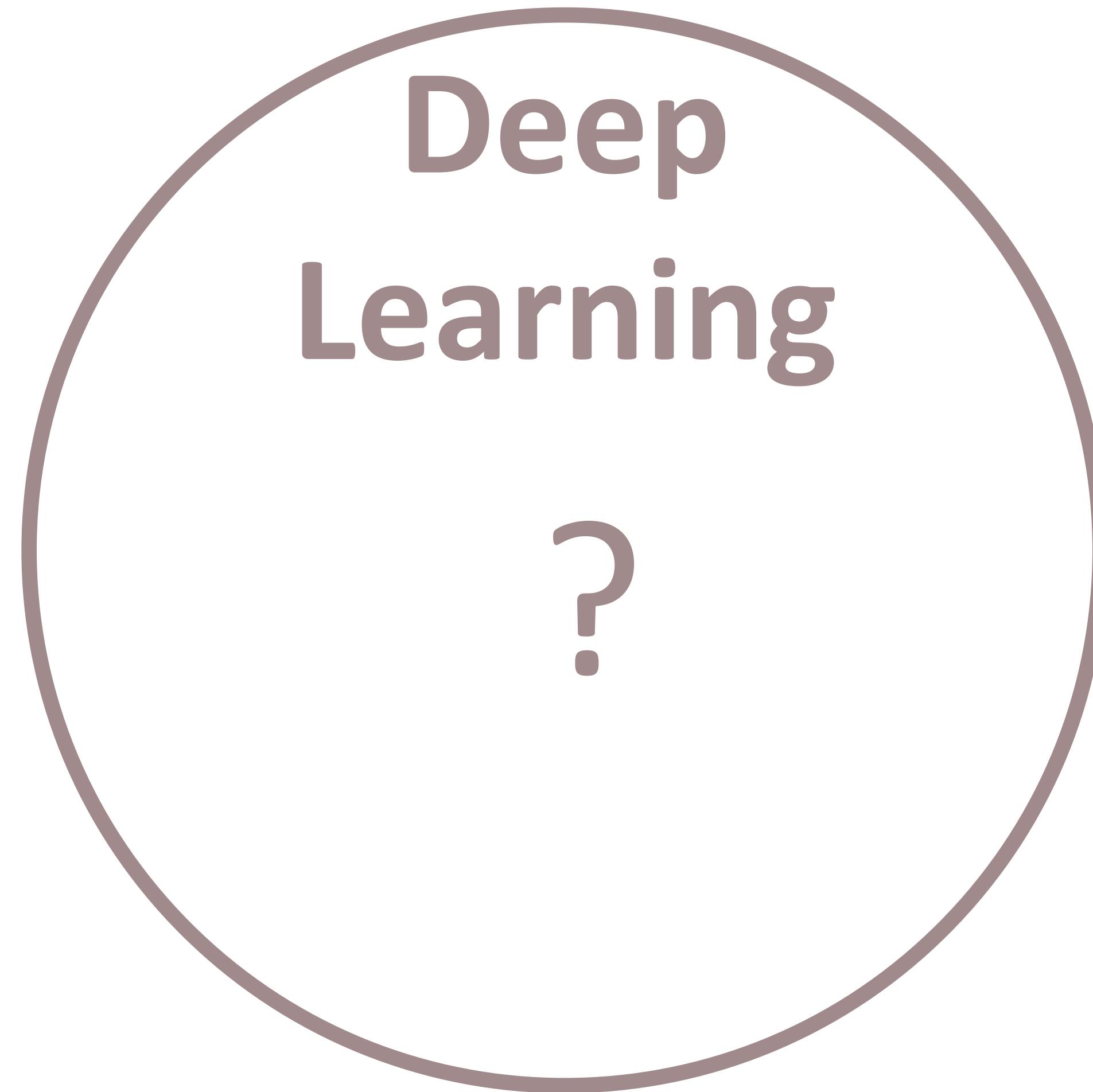
Artificial Intelligence



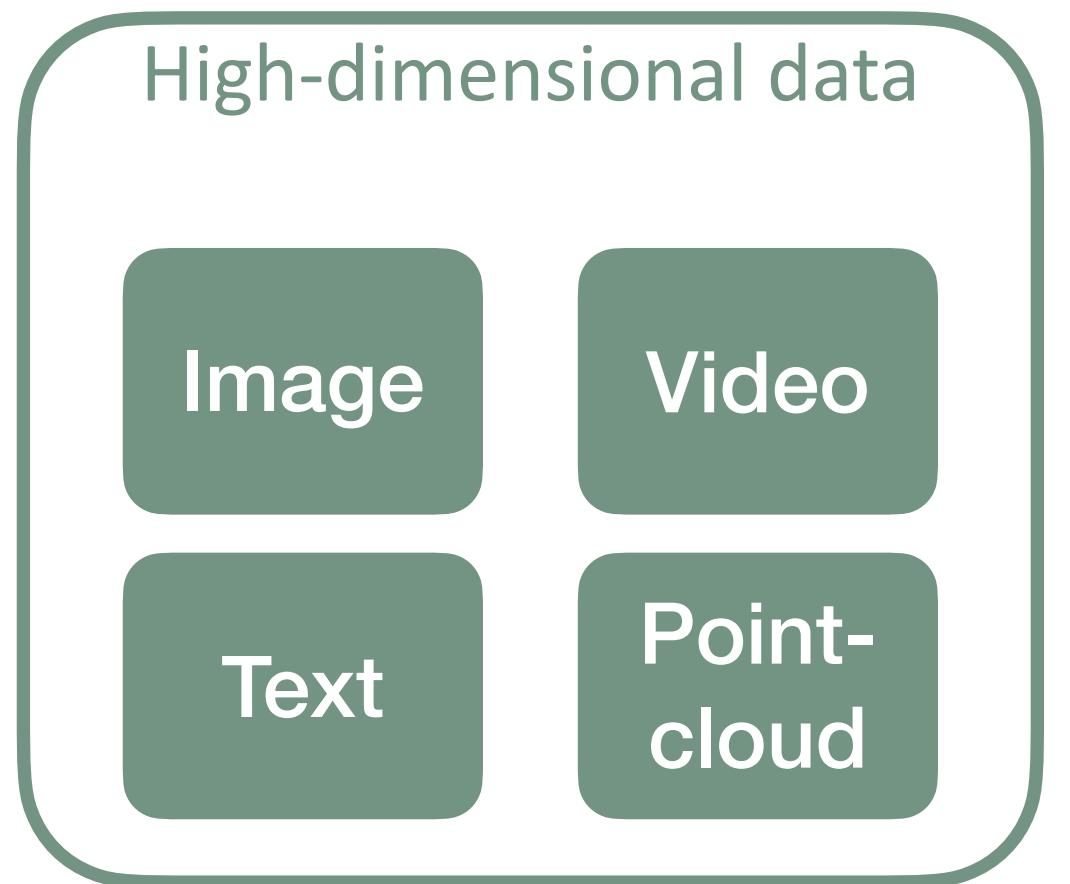
Artificial Intelligence



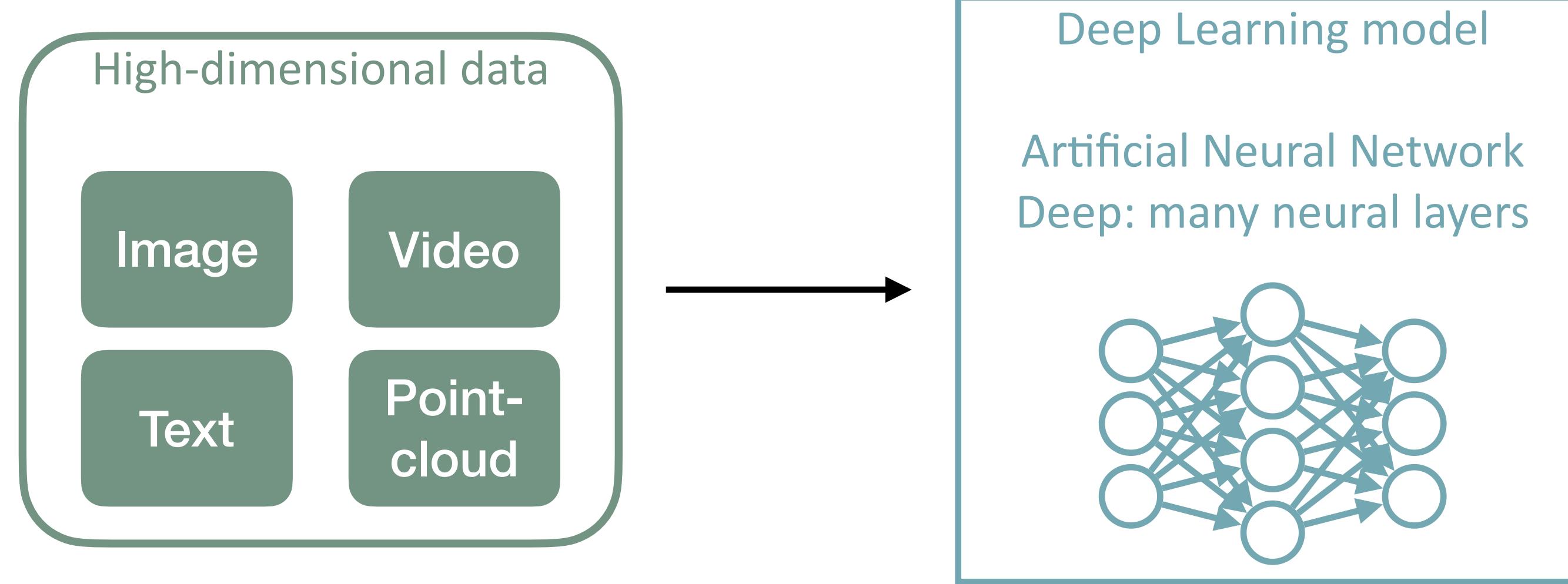
Artificial Intelligence



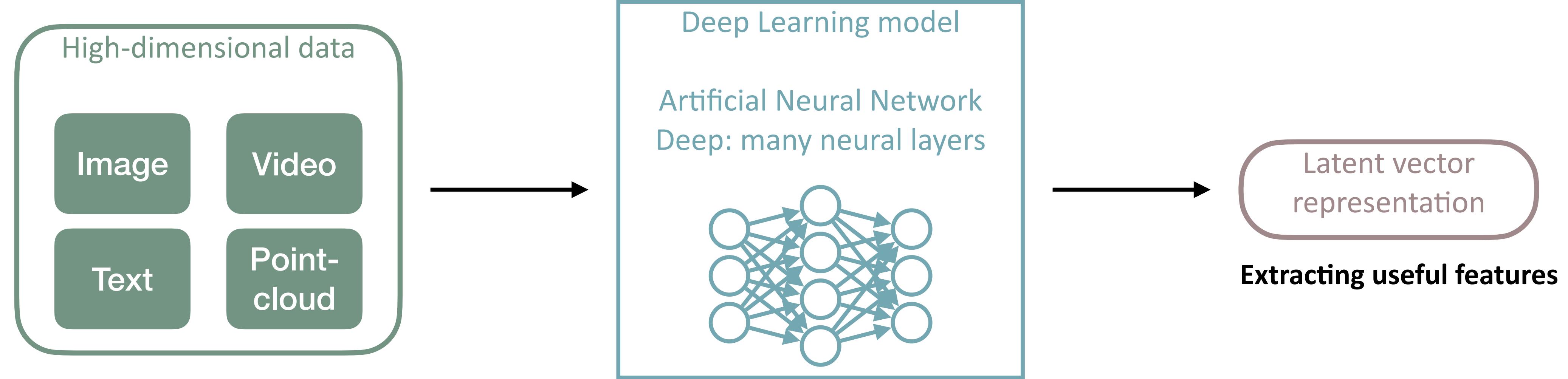
What is Deep Learning?



What is Deep Learning?



What is Deep Learning?



What is Deep Learning?

Image Generation



*An astronaut riding a horse
in photorealistic style.*

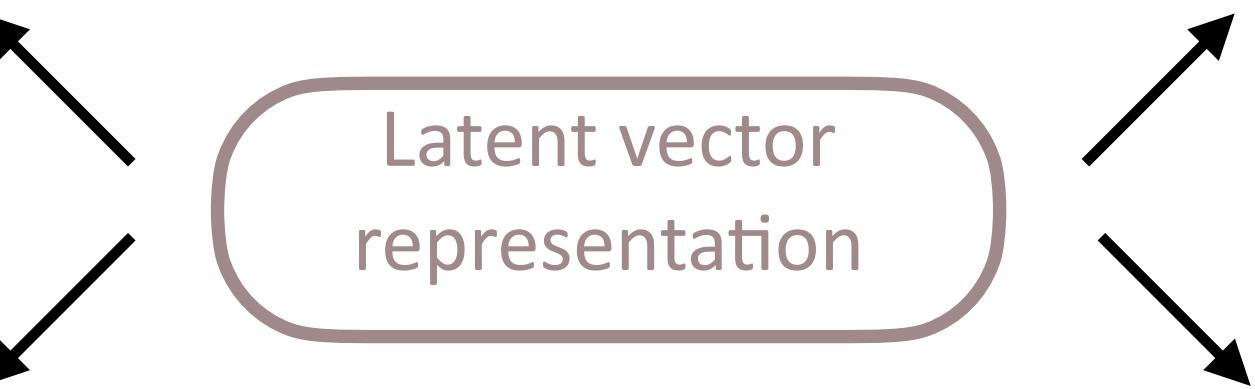
(Reproduced from DALLE 2 website)

User what is the fermat's little theorem

ChatGPT Fermat's Little Theorem states that if p is a prime number and a is an integer not divisible by p , then $a^p \equiv a$ (mod p). In other words, if we divide a^p by p , the remainder is always a .
For example, if $p = 5$ and $a = 2$, then $2^5 = 32$, and 32 divided by 5 has a remainder of 2. Therefore, $2^5 \equiv 2$ (mod 5), and Fermat's Little Theorem holds for this case.
Fermat's Little Theorem is often used in cryptography and other applications where it is necessary to perform modular arithmetic operations quickly and efficiently. It is also a useful tool for proving other theorems in number theory

(Reproduced from ChatGPT website)

Text Generation



Classification



Cat



Dog



Cat (96%)

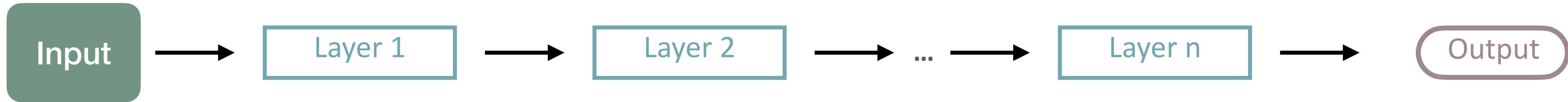


Dog (99%)

Detection

What is Deep Learning?

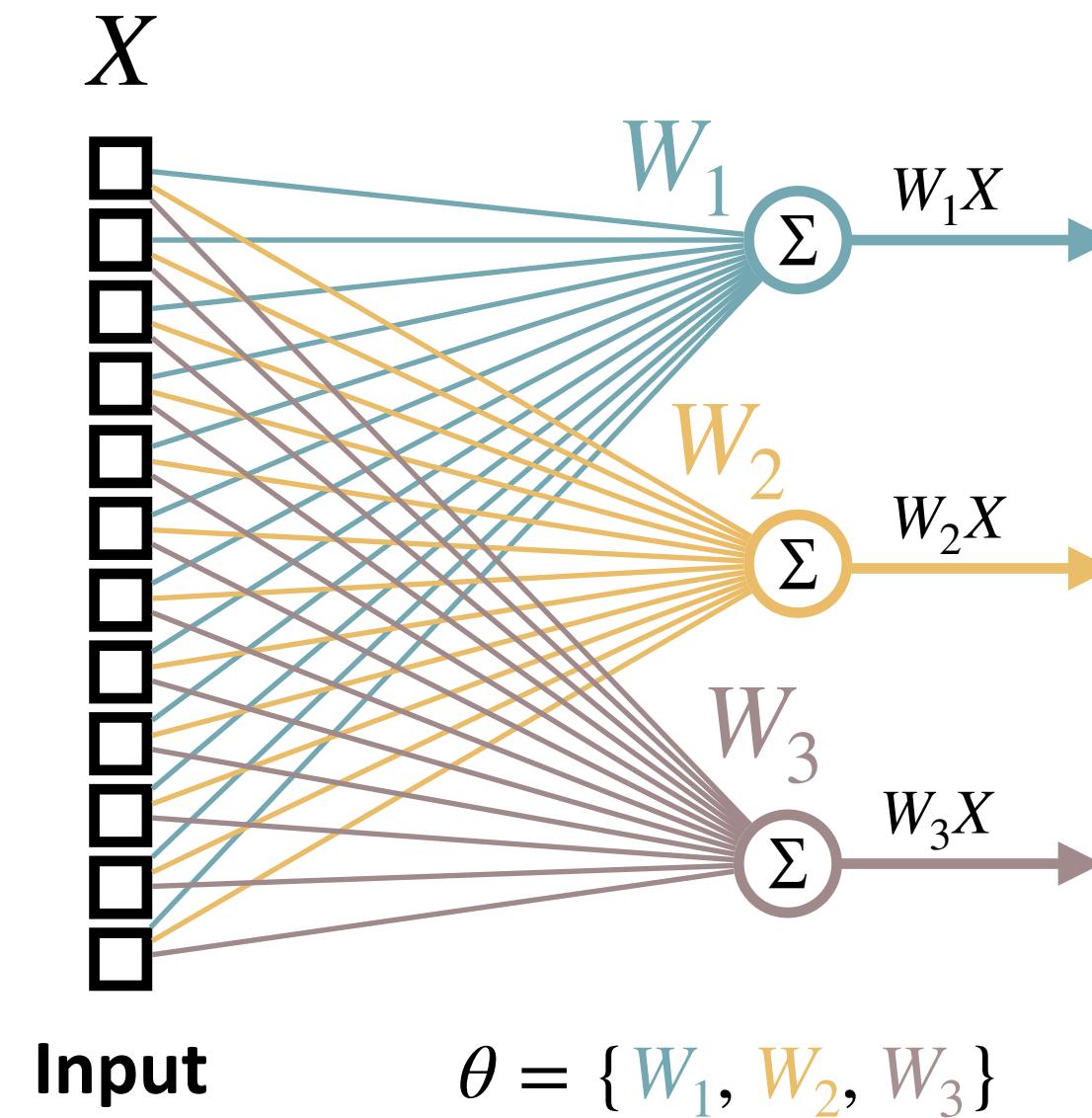
What is an Artificial Neural Network?



- **Parameters/Weights:** each layer is composed of **neurons** that are **parametrized by weights** that we want to **optimize**. This is the **learning** part.
- **Hyperparameters:**
 - Type and number of layers
 - Number of neurons per layer
 - Activation functions, etc.

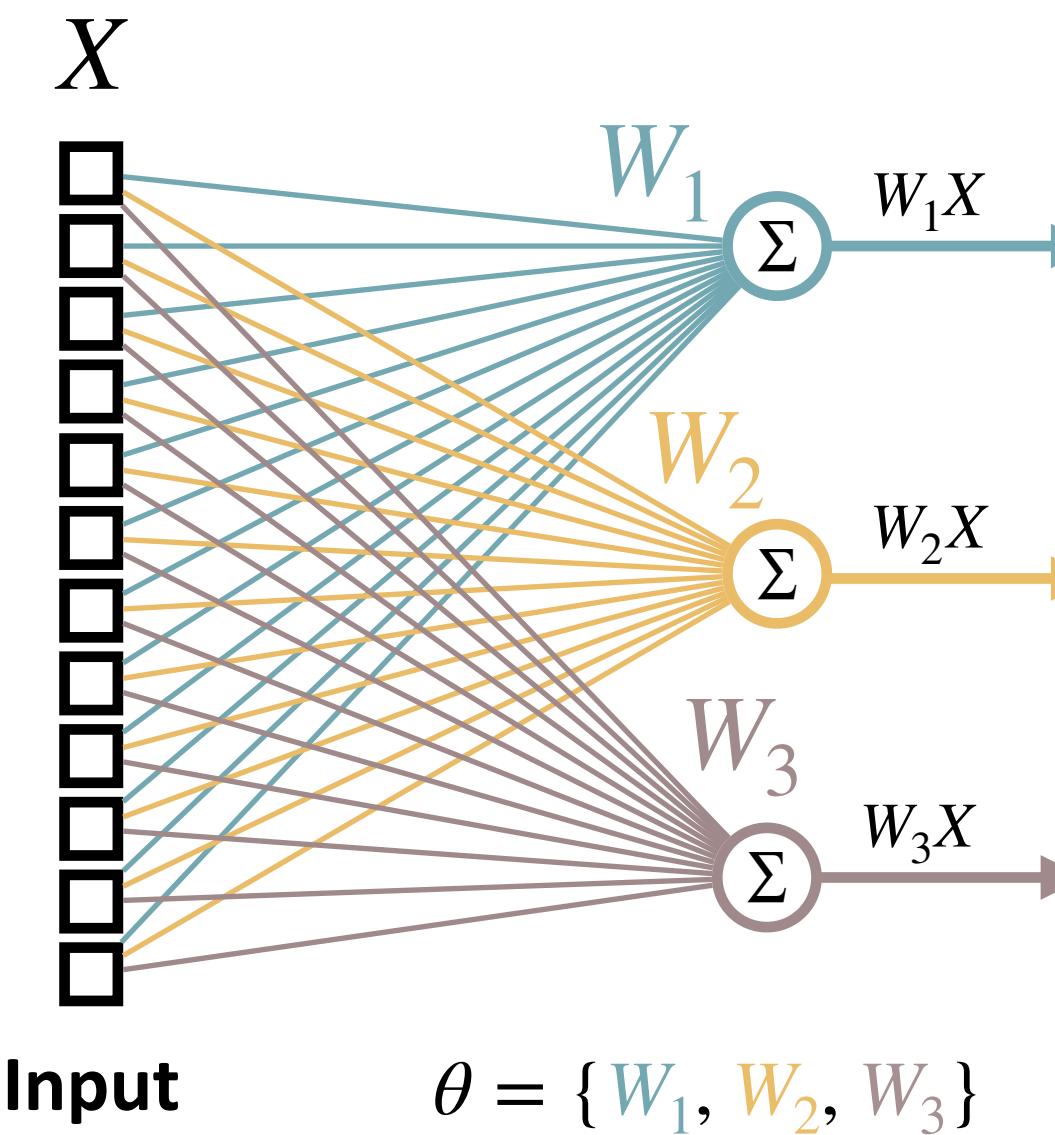
What is Deep Learning?

Recap (?): The Linear Layer



What is Deep Learning?

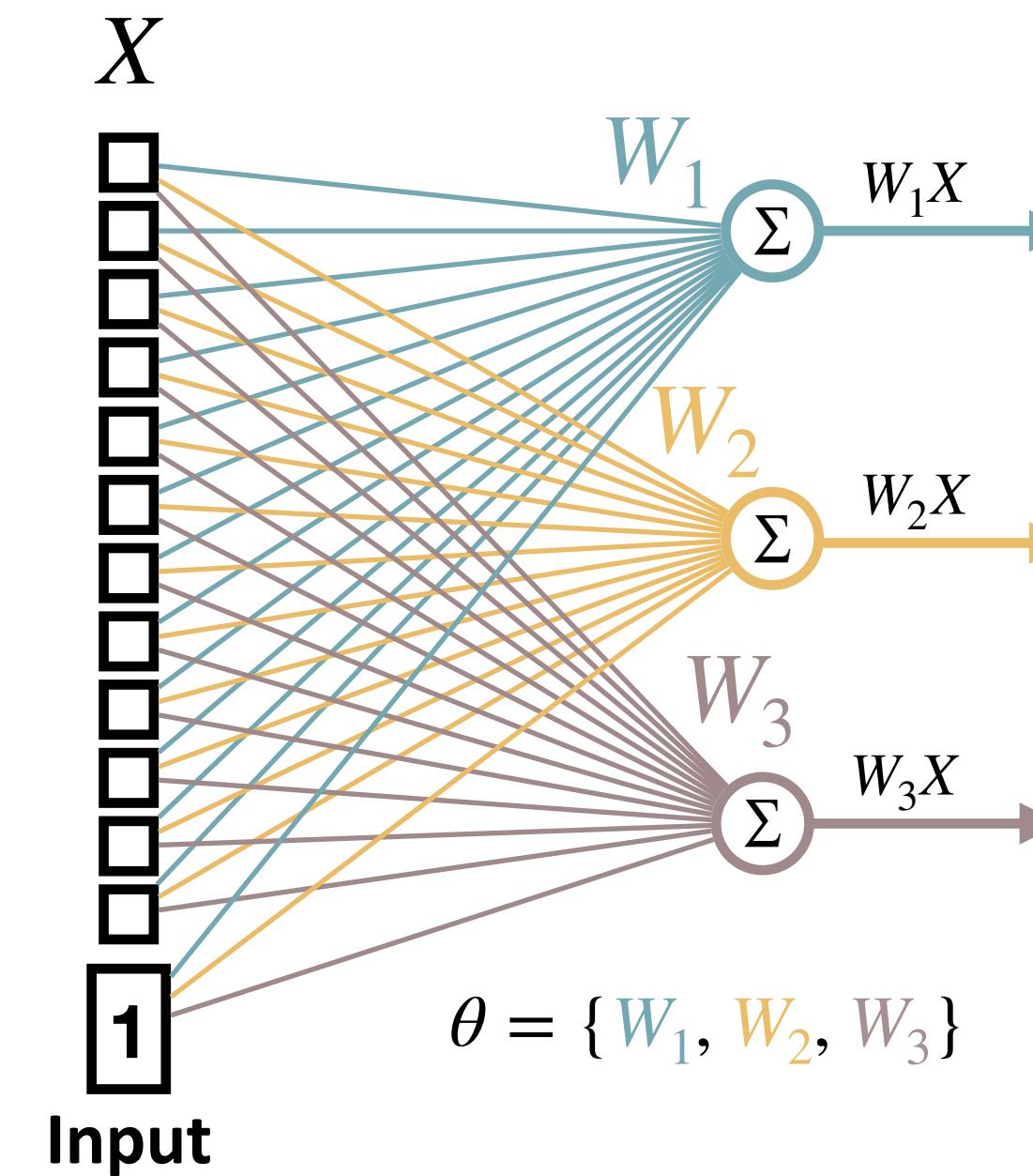
Recap (?): The Linear Layer



But, here we can just learn a **linear** function ($y = ax$) and not an **affine** function ($y = ax + b$) —> We need to **add a bias term**.

What is Deep Learning?

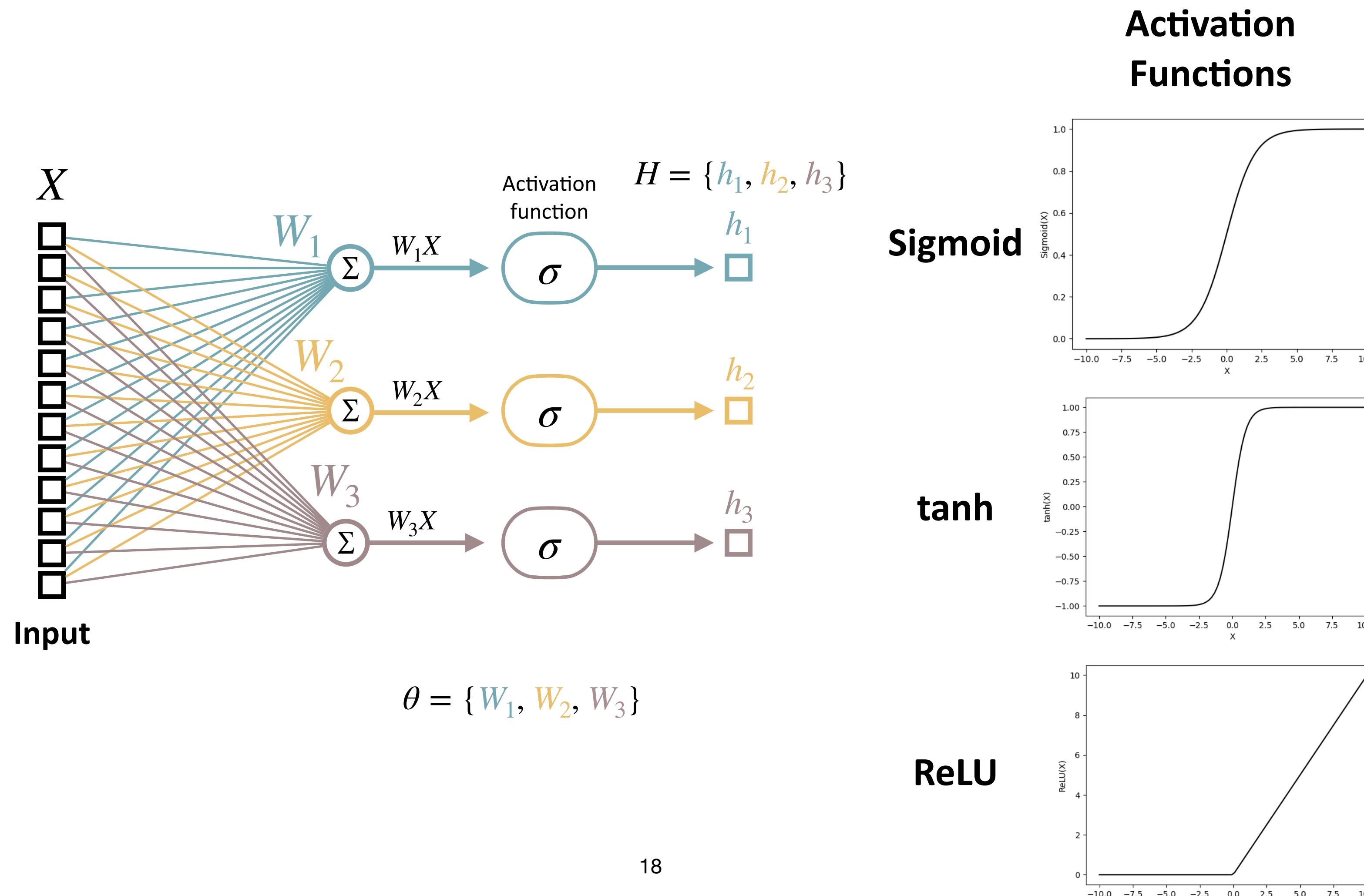
Recap (?): The Linear Layer



What we often do is that we **add a '1' at the end of the input.**

What is Deep Learning?

Recap (?): Activation Functions



What is Deep Learning?

Recap (?): Loss Functions

To train your neural network, you need to **compare its output with the ground-truth labels**. This is where you need to use a **loss function**.

Example 1: Let's consider you have n training samples and are solving a **regression problem**. For a given (input, ground-truth) pair (I_i, T_i) , the output of your neural network is \hat{t}_i . Then, you can use the **Mean Squared Error** as your loss function:

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (T_i - \hat{t}_i)^2$$

What is Deep Learning?

Recap (?): Loss Functions

To train your neural network, you need to **compare its output with the ground-truth labels**. This is where you need to use a **loss function**.

Example 2: Let's consider you have n training samples and are solving a **classification problem** that involves M classes. For a given (input, ground-truth) pair (I_i, T_i) , the output of your neural network is \hat{t}_i . More specifically, for a given class c , $T_{i,c}$ is a binary indicator of whether class c is the correct one for sample i , and $\hat{t}_{i,c}$ if the predicted probability for sample i to belong to class c .

Then, you can use the **Cross-Entropy Loss** as your loss function:

$$\text{CE} = -\frac{1}{n} \sum_{i=1}^N \sum_{c=1}^M T_{i,c} \log (\hat{t}_{i,c})$$

What is Deep Learning?

Recap (?): Loss Functions

To train your neural network, you need to **compare its output with the ground-truth labels**. This is where you need to use a **loss function**.

Example 2: Let's consider you have n training samples and are solving a **classification problem** that involves M classes. For a given (input, ground-truth) pair (I_i, T_i) , the output of your neural network is \hat{t}_i . More specifically, for a given class c , $T_{i,c}$ is a binary indicator of whether class c is the correct one for sample i , and $\hat{t}_{i,c}$ if the predicted probability for sample i to belong to class c .



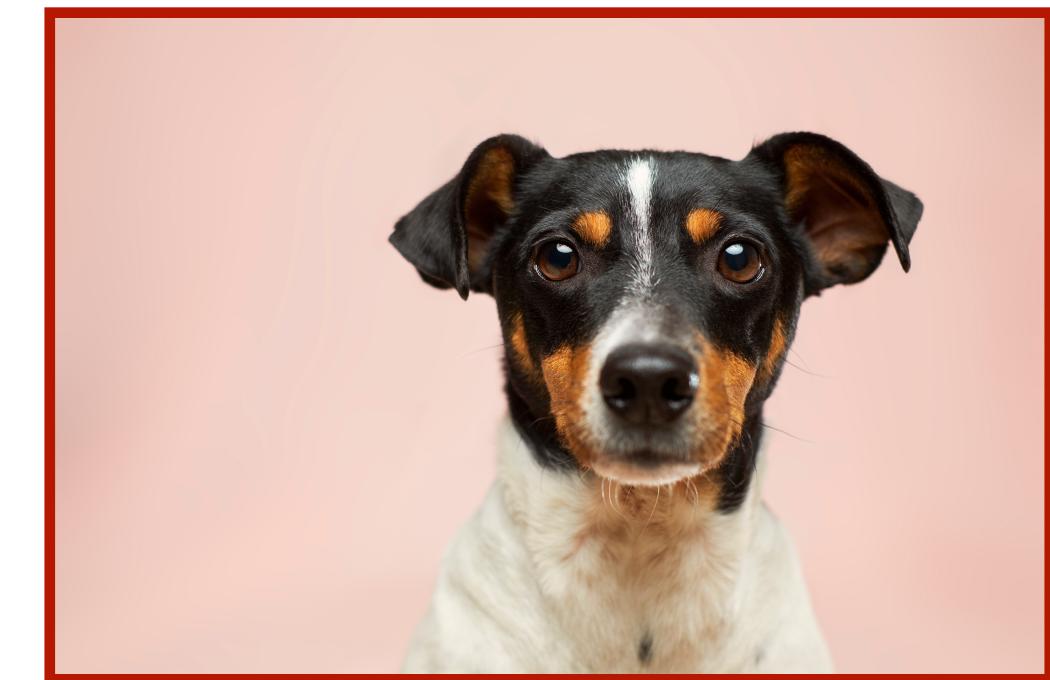
When solving a classification problem, the output of the neural network will generally be a probability distribution over possible classes.

Standard Deep Learning Pipeline

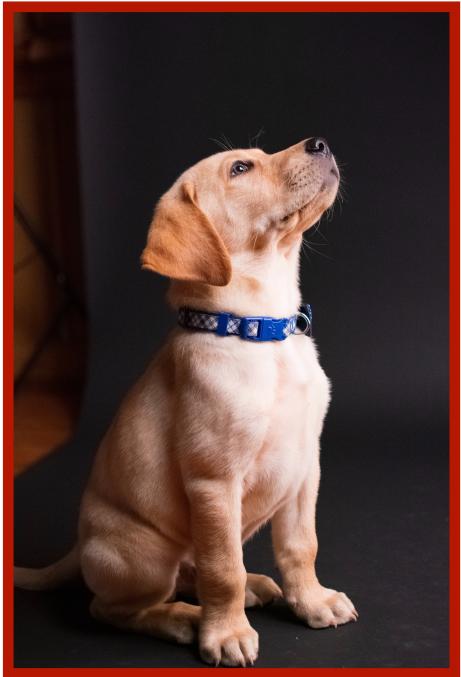
1. Find a dataset, i.e. pairs of (input, output)



Cat



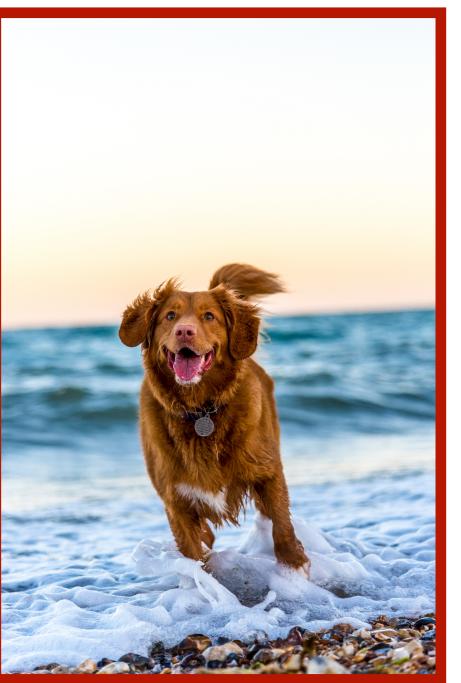
Dog



Dog



Cat



Dog



Cat



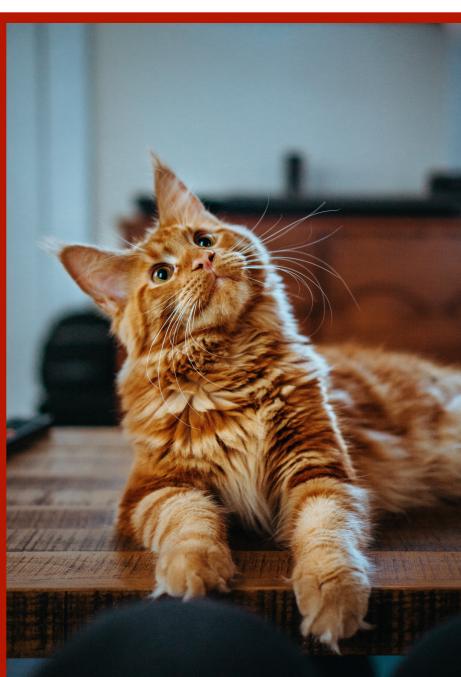
Dog



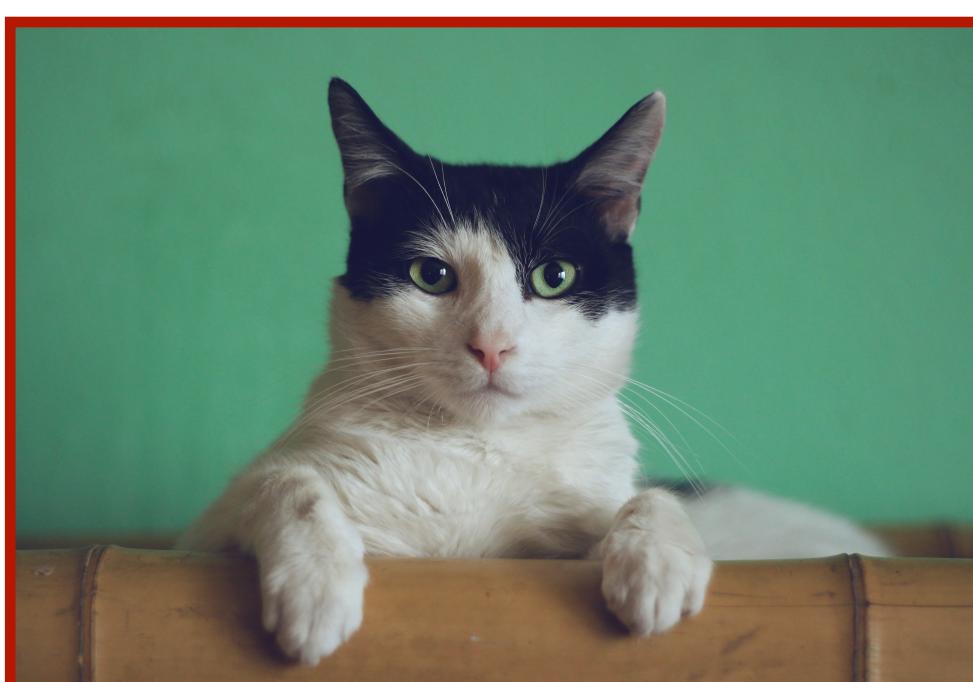
Cat



Dog



Cat



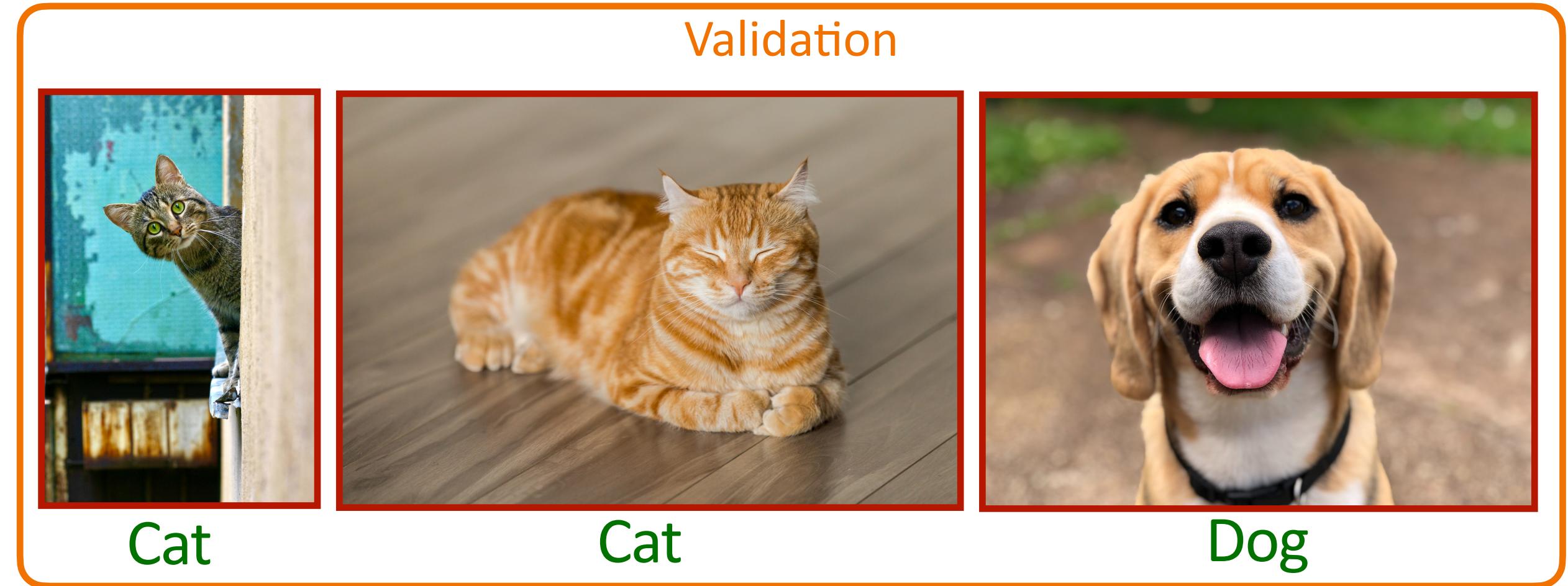
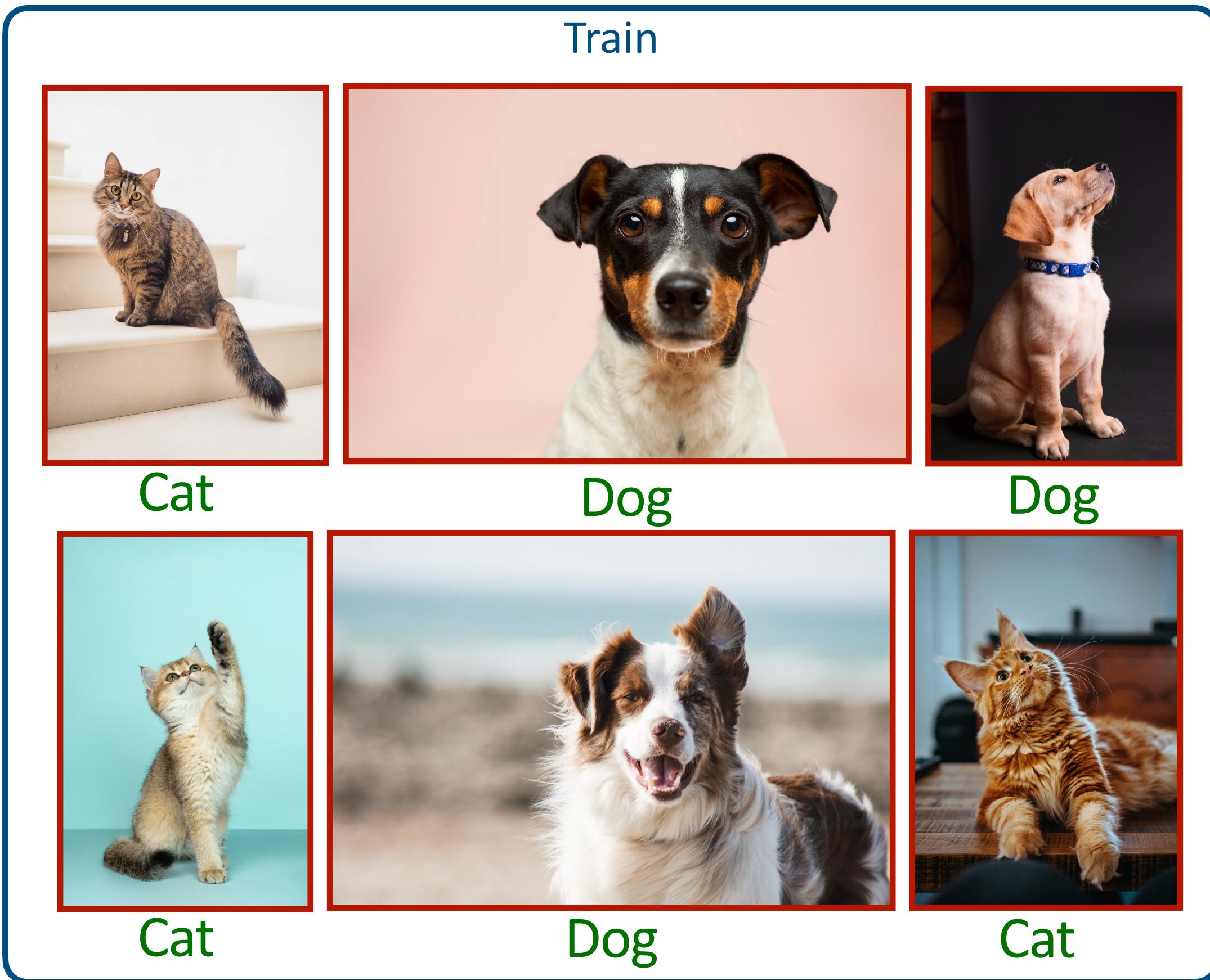
Cat



Dog

Standard Deep Learning Pipeline

1. Find a dataset, i.e. pairs of (**input**, **output**)
2. **Split your data** into 3 sets: **train**, **validation**, **test**



Standard Deep Learning Pipeline

1. Find a dataset, i.e. pairs of (**input**, **output**)
2. **Split your data** into 3 sets: **train**, **validation**, **test**

Train

To **train your neural network**, i.e. optimise its weights/parameters based on the difference between its predictions and **ground-truth outputs**.

Validation

To evaluate the choice of hyper parameters, e.g. number of layers, neurons, type of activations, loss functions...

This set is very important: allows to evaluate the performance on data not used during **training** but different from the final **test set** (to avoid choosing hyper params that only work on this specific test set).

Test

To evaluate the final performance of you neural network (after hyper params have been chosen and weight values optimised)

Standard Deep Learning Pipeline

1. Find a dataset, i.e. pairs of (**input**, **output**)
2. Split your data into 3 sets: **train**, **validation**, **test**
3. **Build your neural network** (this process is often iterative based on **validation performance**).
 1. Types of layers (linear, convolutional, recurrent, etc.)
 2. Activation functions
 3. Number of layers, neurons, etc.

Standard Deep Learning Pipeline

1. Find a dataset, i.e. pairs of (**input**, **output**)
2. Split your data into 3 sets: **train**, **validation**, **test**
3. Build your neural network (this process is often iterative based on **validation performance**).
4. **Train your neural network**

Stochastic Gradient Descent (SGD)

Epoch: a full iteration over your **train set**.

Training batch: a set of samples from the **train set**.

f_θ : neural network parametrised by weights θ .

\mathcal{L} : chosen loss function (e.g. Cross-Entropy for classification problems).

Iterate over n epochs

 Iterate over m training batches

Sampling training batch $\mathcal{B}_i = \{\mathbf{I}_i, \mathbf{T}_i\}$ from **train set**, where \mathbf{I}_i and \mathbf{T}_i are **inputs** and **ground-truth outputs** respectively.

Forward pass: $\hat{t}_i = f_\theta(\mathbf{I}_i; \theta)$, where \hat{t}_i is the prediction from the neural network.

Error computation: $e_i = \mathcal{L}(\hat{t}_i, \mathbf{T}_i)$ where e_i is the error between the predictions and the **ground truth**.

Backward pass: Computing gradient of e_i with respect to network weights θ , and updating θ .

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Course Overview

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Useful resources about CNNs

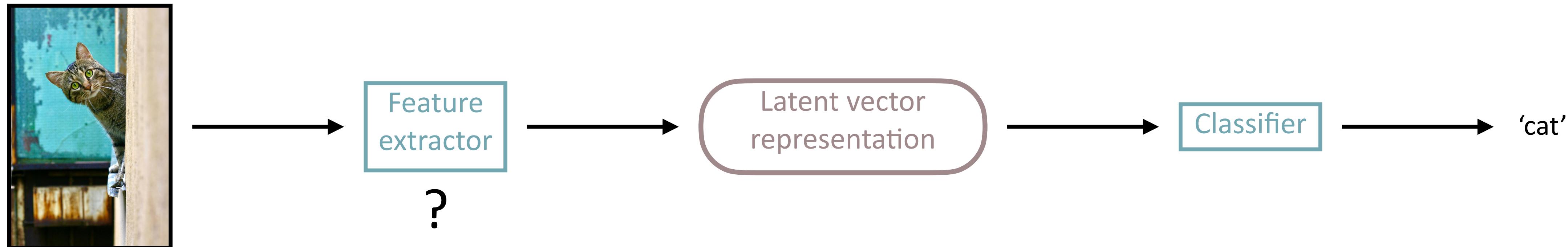
- AlexNet paper (winner of the Imagenet competition): Krizhevsky et al. ImageNet Classification with Deep Convolutional Neural Networks, NeurIPS 2012
- ResNet paper (a method that is still used a lot in Computer Vision): He et al., Deep Residual Learning for Image Recognition, CVPR 2016
- A nice blog post from my PhD advisor (Christian Wolf) about shift equivariance: <https://chriswolfvision.medium.com/what-is-translation-equivariance-and-why-do-we-use-convolutions-to-get-it-6f18139d4c59>

Convolutional Neural Networks — Motivation

How to extract a feature representation of an image?

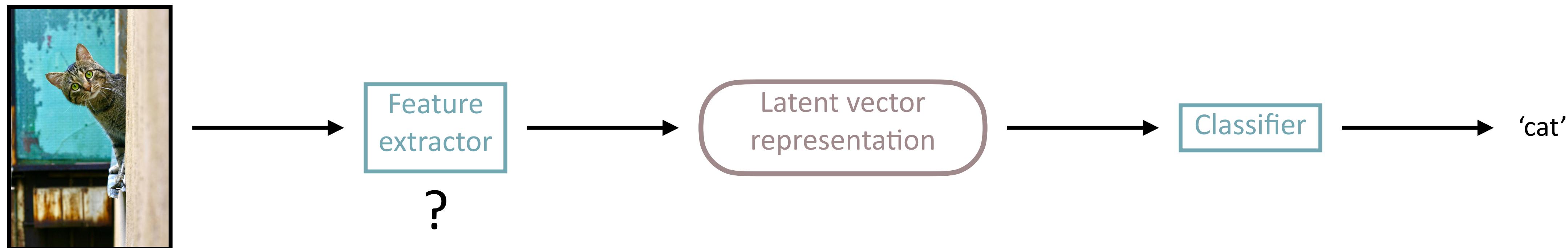
Convolutional Neural Networks — Motivation

How to extract a feature representation of an image?



Convolutional Neural Networks — Motivation

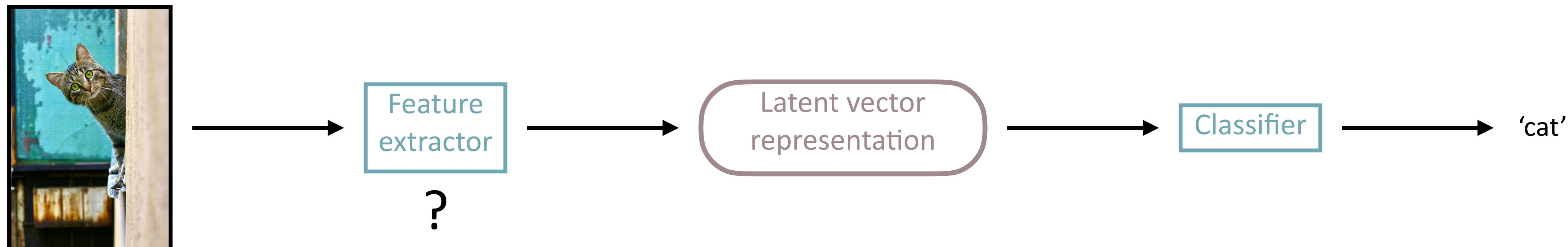
How to extract a feature representation of an image?



Before Deep Learning: SIFT, HoG features, etc.

Convolutional Neural Networks — Motivation

How to extract a feature representation of an image?



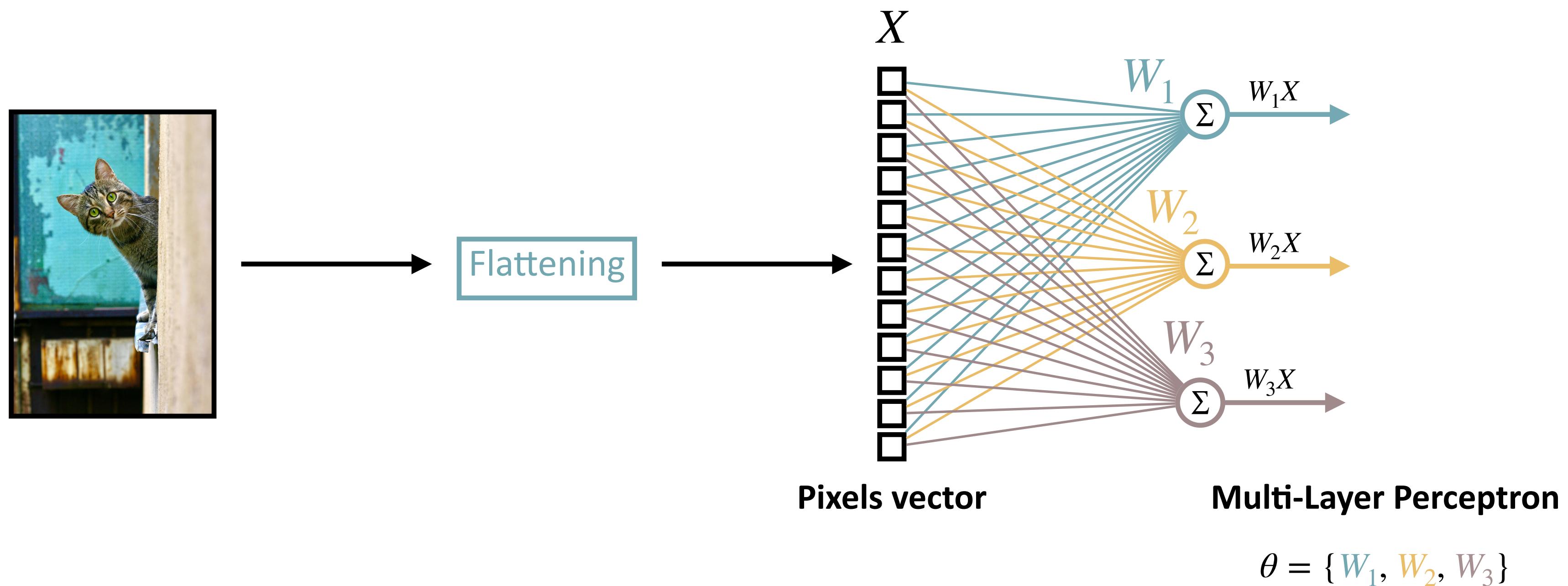
Before Deep Learning: SIFT, HoG features, etc.

Artificial Neural Network: Couldn't we use a simple Multi-Layer Perceptron?

Convolutional Neural Networks — Motivation

Artificial Neural Network: Couldn't we use a simple Multi-Layer Perceptron?

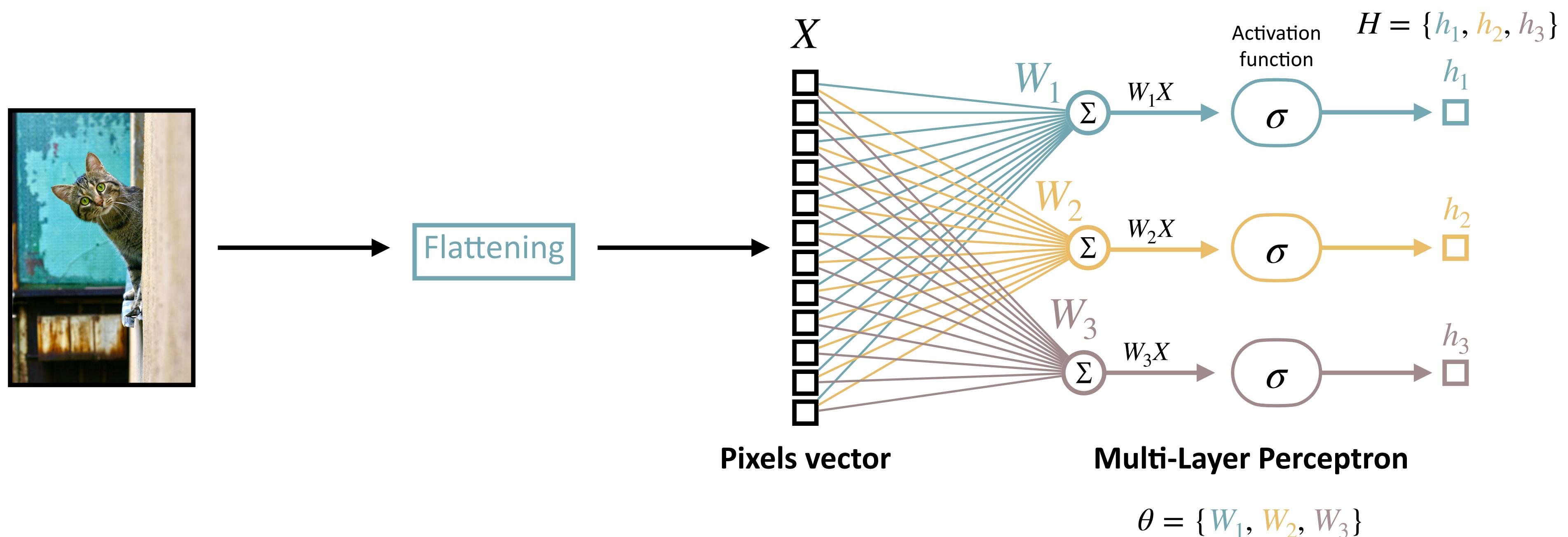
Answer: Maybe, but it can be hard to train... even sometimes impossible...



Convolutional Neural Networks — Motivation

Artificial Neural Network: Couldn't we use a simple Multi-Layer Perceptron?

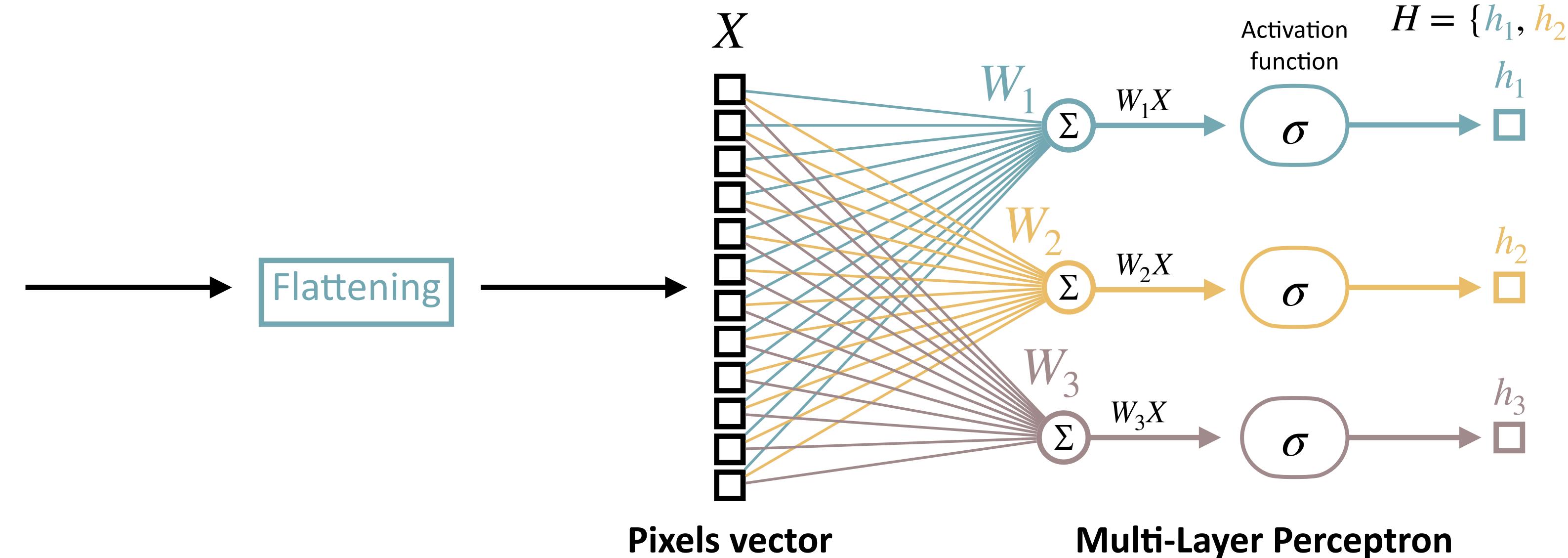
Answer: Maybe, but it can be hard to train... even sometimes impossible...



Convolutional Neural Networks — Motivation

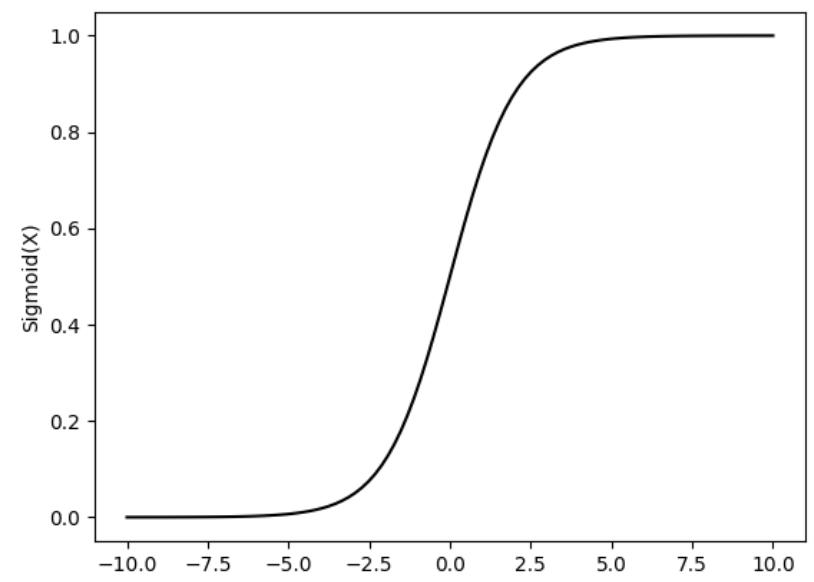
Artificial Neural Network: Couldn't we use a simple Multi-Layer Perceptron?

Answer: Maybe, but it can be hard to train... even sometimes impossible...

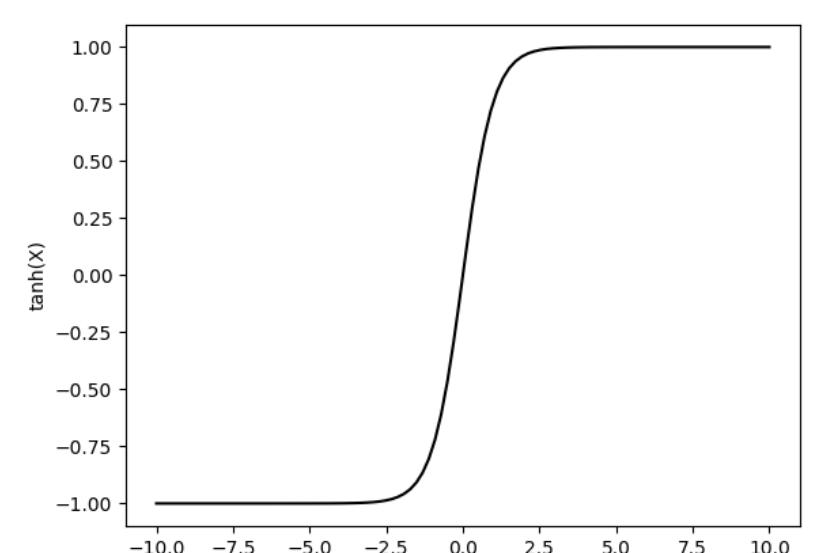


Activation Functions

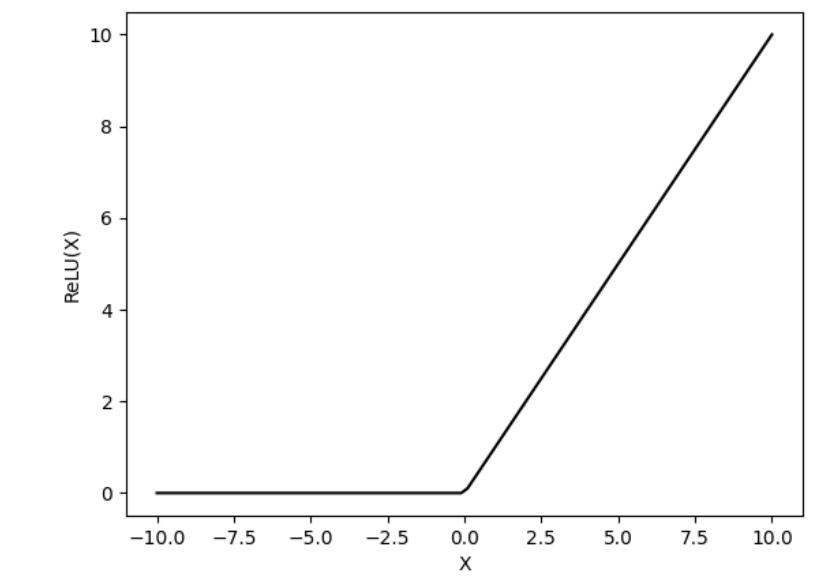
Sigmoid



tanh



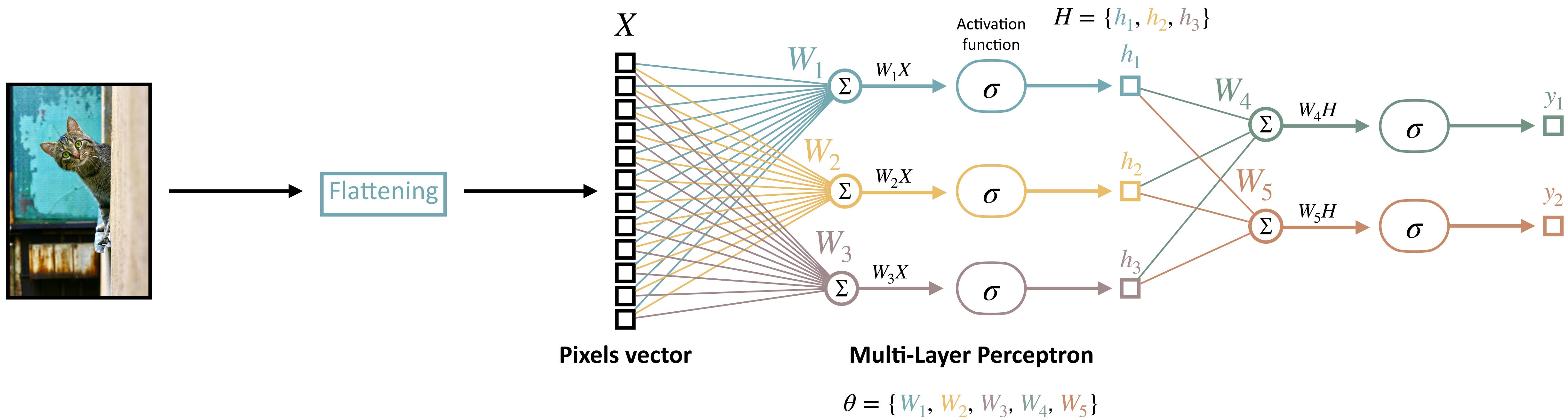
ReLU



Convolutional Neural Networks — Motivation

Artificial Neural Network: Couldn't we use a simple Multi-Layer Perceptron?

Answer: Maybe, but it can be hard to train... even sometimes impossible...



Convolutional Neural Networks — Motivation

Issues with MLP

- Spatial information is lost when flattening the image. We loose information about whether a given input pixel was close to others in the original image.

Convolutional Neural Networks — Motivation

Issues with MLP

- Spatial information is lost when flattening the image. We loose information about whether a given input pixel was close to others in the original image.
- The number of parameters to learn quickly grows with the size of the input image.

If we have a **224*224*3** input image \rightarrow **150528 input values**

Now let's say we want a **single linear layer** with **256 neurons**
 $\rightarrow 256 * (150528 + 1) = 38535424 \sim 38M$ parameters for a single layer!

Bias term



Convolutional Neural Networks — Motivation

Issues with MLP

- Spatial information is lost when flattening the image. We loose information about whether a given input pixel was close to others in the original image.
- The number of parameters to learn quickly grows with the size of the input image.
- It is not translation invariant (outputs a different representation for a given input image and its shifted version)

Convolutional Neural Networks — Motivation

Inductive biases:

- The set of assumptions about the target function to approximate.
- A way to constrain the search space for suitable functions.
- Incorporates prior knowledge about the task to solve.

Convolutional Neural Networks — Motivation

Inductive biases:

- The set of assumptions about the target function to approximate.
- A way to constrain the search space for suitable functions.
- Incorporates prior knowledge about the task to solve.

There are 2 important inductive biases when dealing with images:

- Locality: pixels spatially close share information
- Translation equivariance

Convolutional Neural Networks — Motivation

An operation ϕ is known to be **shift/translation equivariant** if, given an input X and a translation operator T , we have the following:

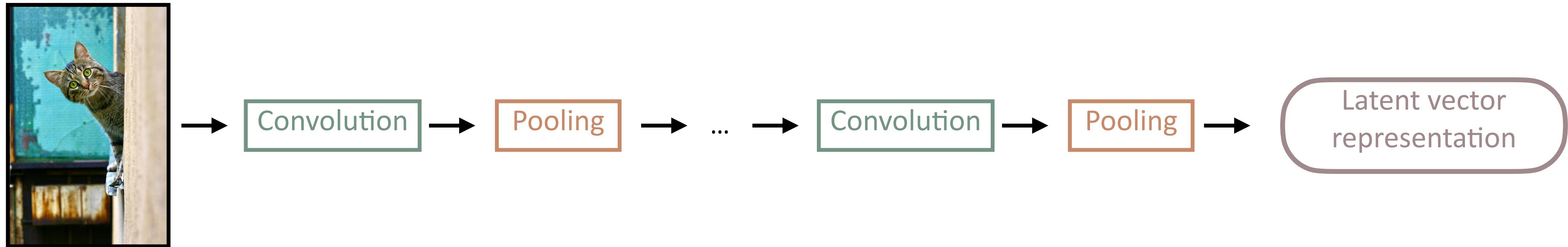
$$\phi(T(X)) = T(\phi(X))$$

Why is it interesting? If we consider shifting an image slightly, we might want the final pixel-wise representation of this image to be the same, just translated by the applied shift.

Convolutional Neural Networks — Standard Architecture

Two important operations:

1. Convolution
2. Pooling



Convolutional Neural Networks – Convolution

Let's consider an **input tensor** with size $H \times W \times C$,

- H is the height ($H = 5$ in the example below)
- W is the width ($W = 5$ in the example below)
- C is the number of channels ($C = 3$ in the example below as is the case for an RGB image)

Input tensor
($H = 5, W = 5, C = 3$)

4	112	34	20	5
55	40	1	8	27
70	87	2	190	25
240	101	67	42	12
44	109	4	1	87

Channel 0 (e.g. R in RGB)

25	37	115	60	88
177	24	37	92	145
15	50	108	124	44
5	71	133	74	58
27	39	82	118	243

Channel 1 (e.g. G in RGB)

12	250	194	145	117
37	26	129	107	99
87	75	60	191	230
20	11	48	61	72
87	33	71	48	100

Channel 2 (e.g. B in RGB)

Convolutional Neural Networks – Convolution

Let's consider a **convolution kernel** with size $H \times W \times C$,

- H is the height ($H = 3$ in the example below)
- W is the width ($W = 3$ in the example below)
- C is the number of channels ($C = 3$ in the example below to match input channels)

Input tensor
($H = 5, W = 5, C = 3$)

4	112	34	20	5
55	40	1	8	27
70	87	2	190	25
240	101	67	42	12
44	109	4	1	87

Channel 0 (e.g. R in RGB)

Convolution kernel
($H = 3, W = 3, C = 3$)

3	2	4
0	1	8
2	7	6

Channel 1 (e.g. G in RGB)

25	37	115	60	88
177	24	37	92	145
15	50	108	124	44
5	71	133	74	58
27	39	82	118	243

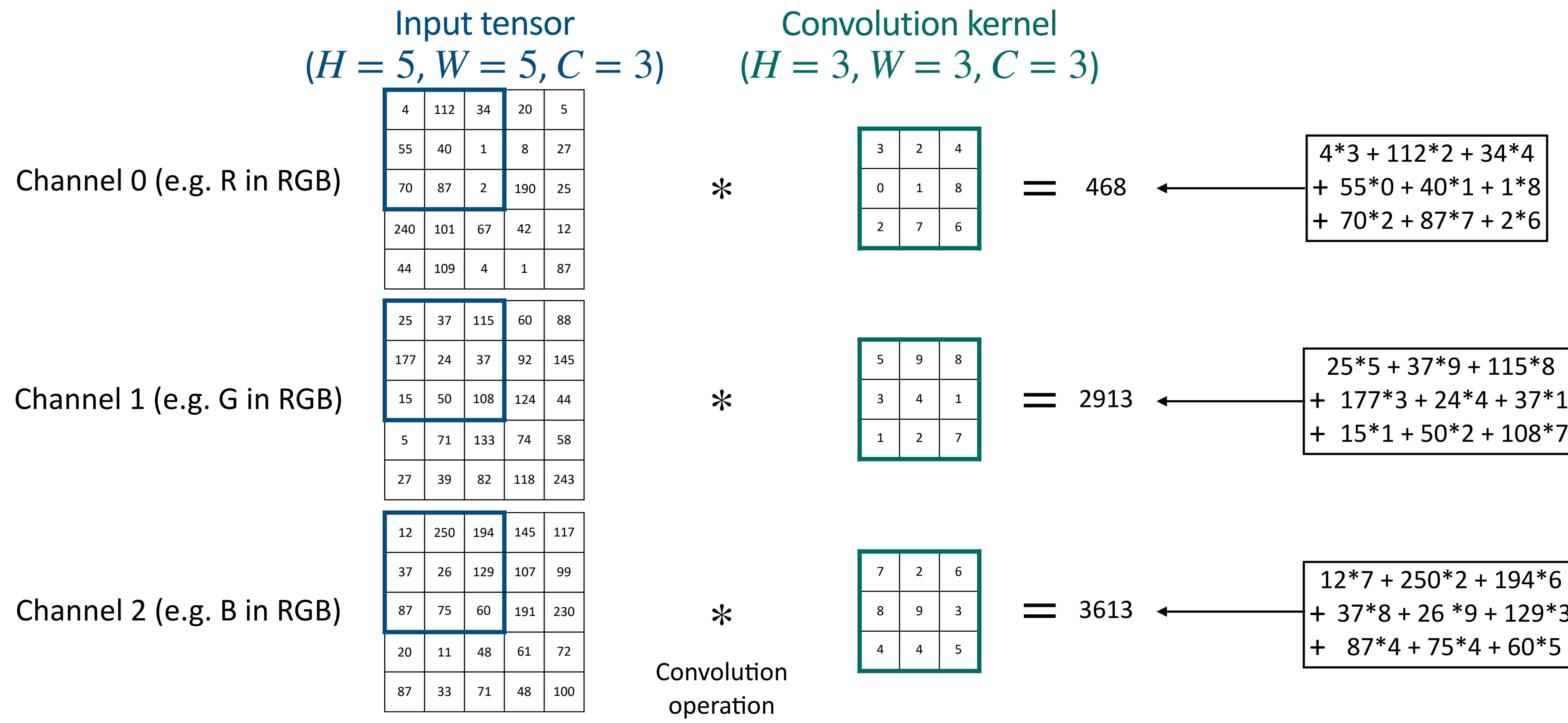
Channel 2 (e.g. B in RGB)

5	9	8
3	4	1
1	2	7

12	250	194	145	117
37	26	129	107	99
87	75	60	191	230
20	11	48	61	72
87	33	71	48	100

7	2	6
8	9	3
4	4	5

Convolutional Neural Networks – Convolution



Convolutional Neural Networks – Convolution

Channel 0 (e.g. R in RGB)

Input tensor
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Channel 1 (e.g. G in RGB)

Convolution kernel $(H = 3, W = 3, C = 3)$

3	2	4
0	1	8
2	7	6

46

1

Channel 2 (e.g. B in RGB)

Convolution operation

Output tensor
 $(H = 3, W = 3, C = 1)$

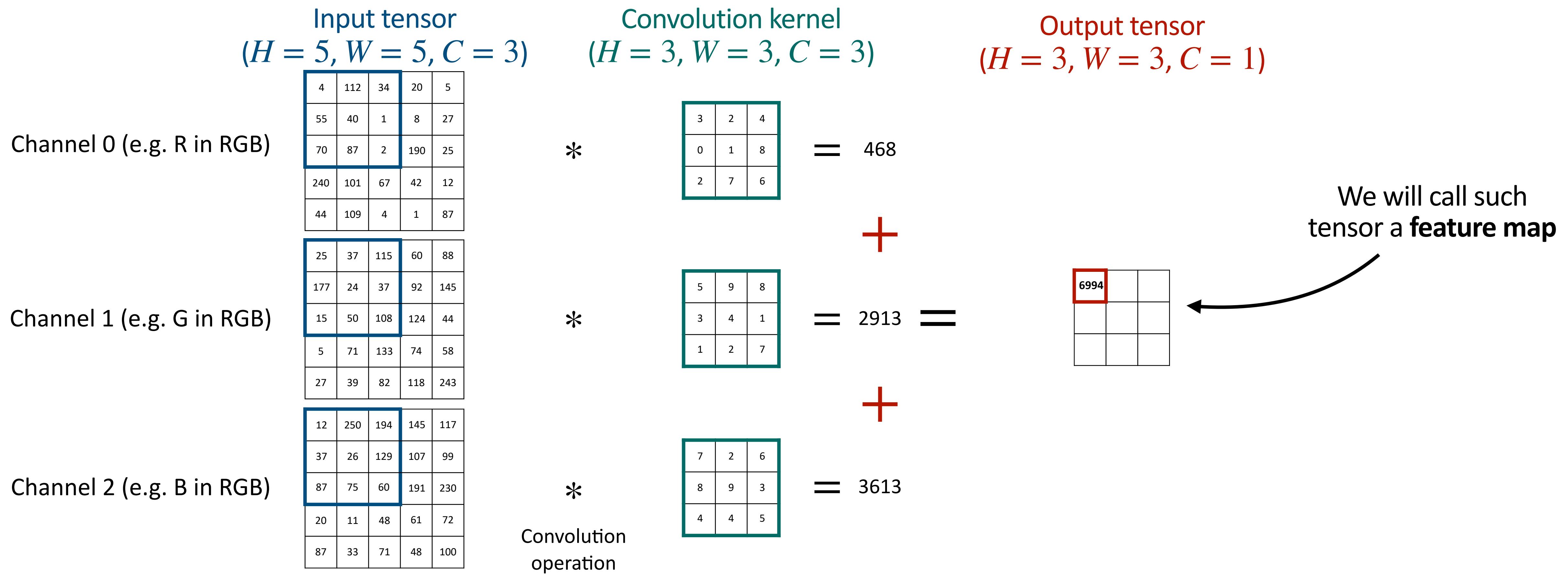
6994

2913

1

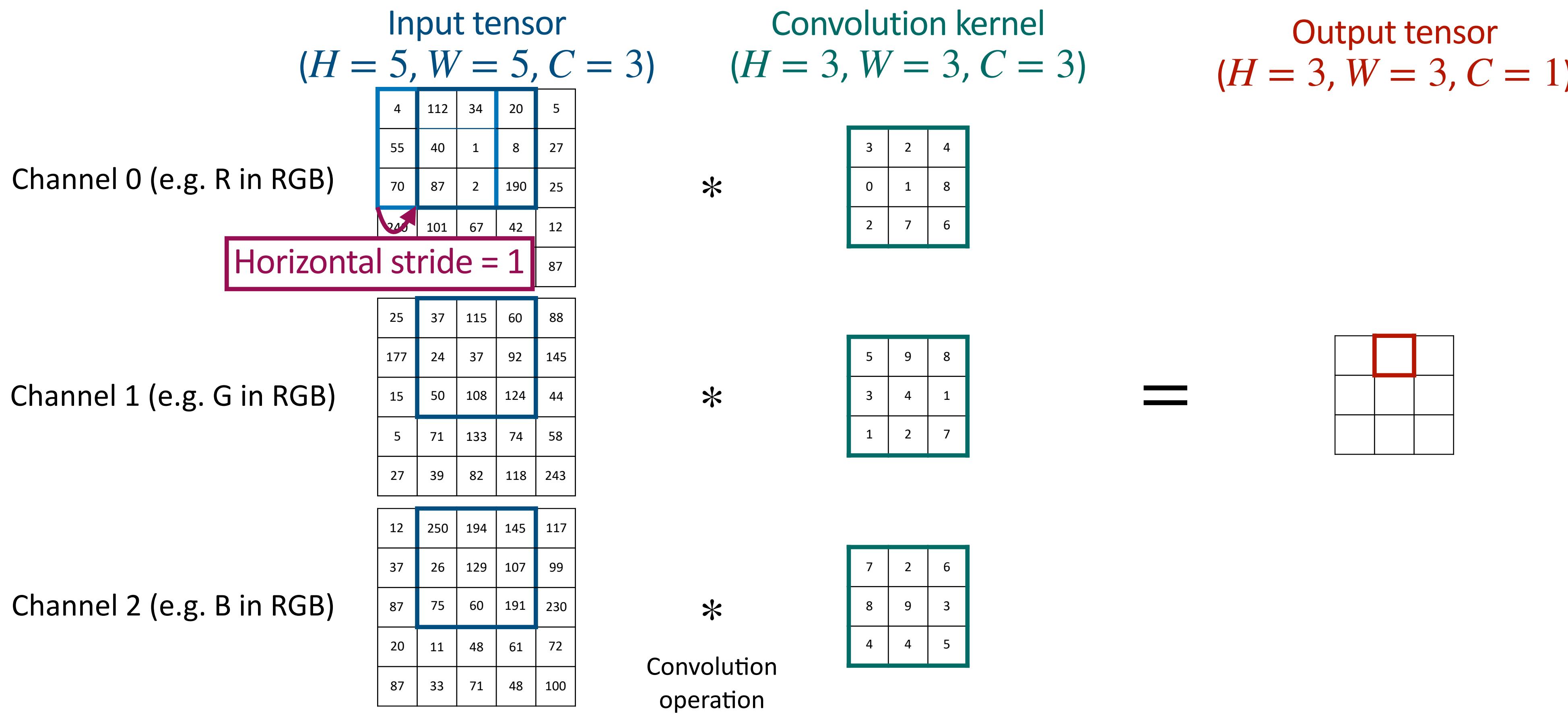
— 361

Convolutional Neural Networks – Convolution



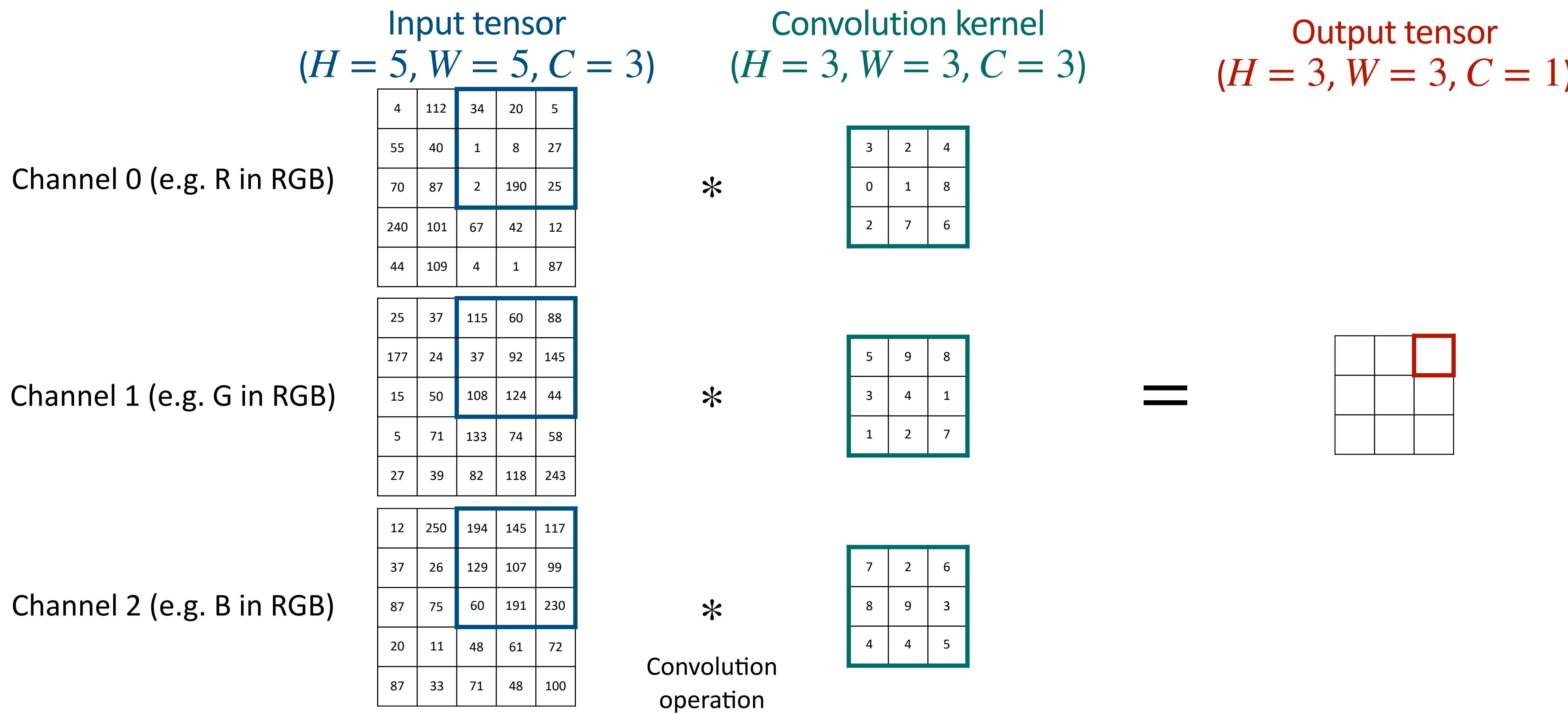
Convolutional Neural Networks – Convolution

Additional to the kernel size ($H \times W \times C$), there is another important hyperparameter of the convolution kernel: **the stride**, i.e. **by how much to slide the kernel**. In the example below, horizontal and vertical strides are set to 1.



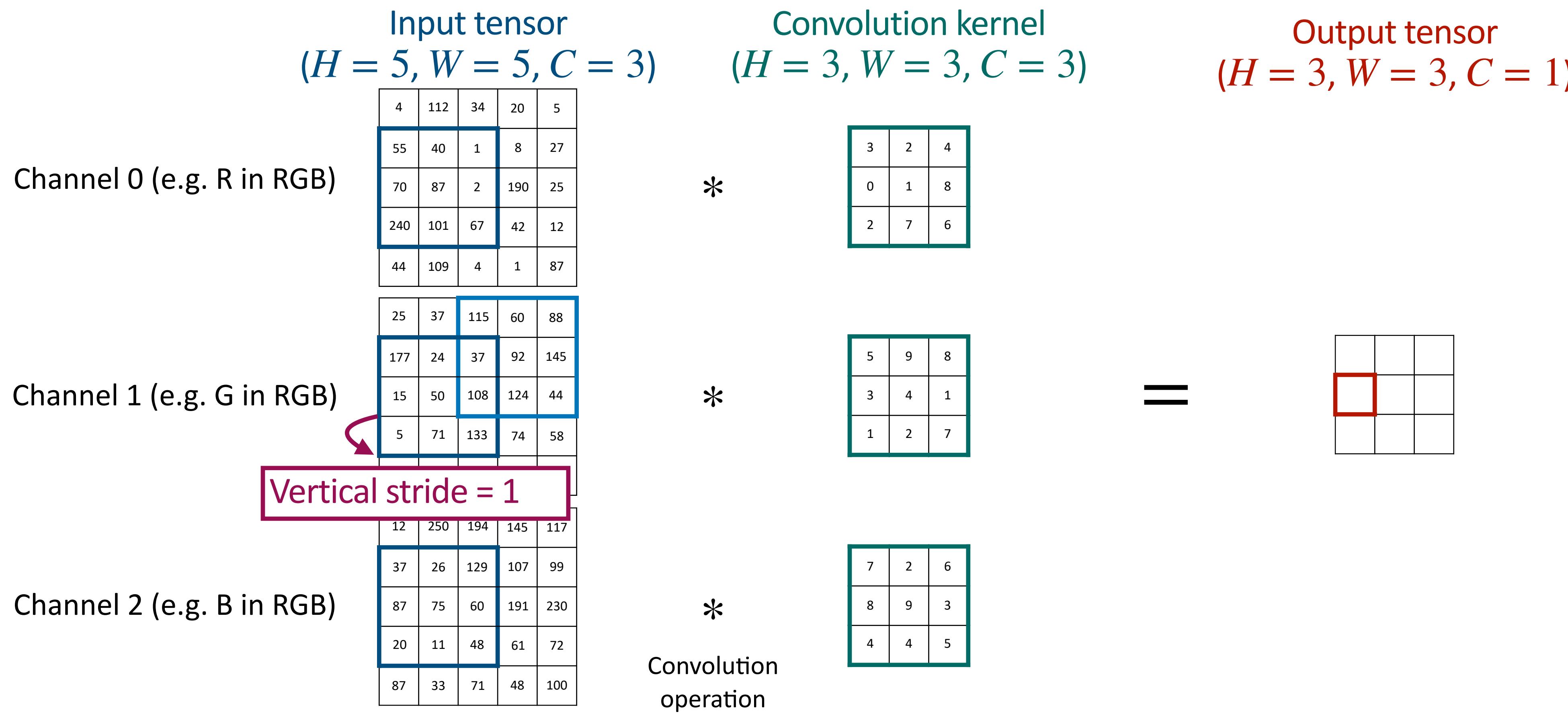
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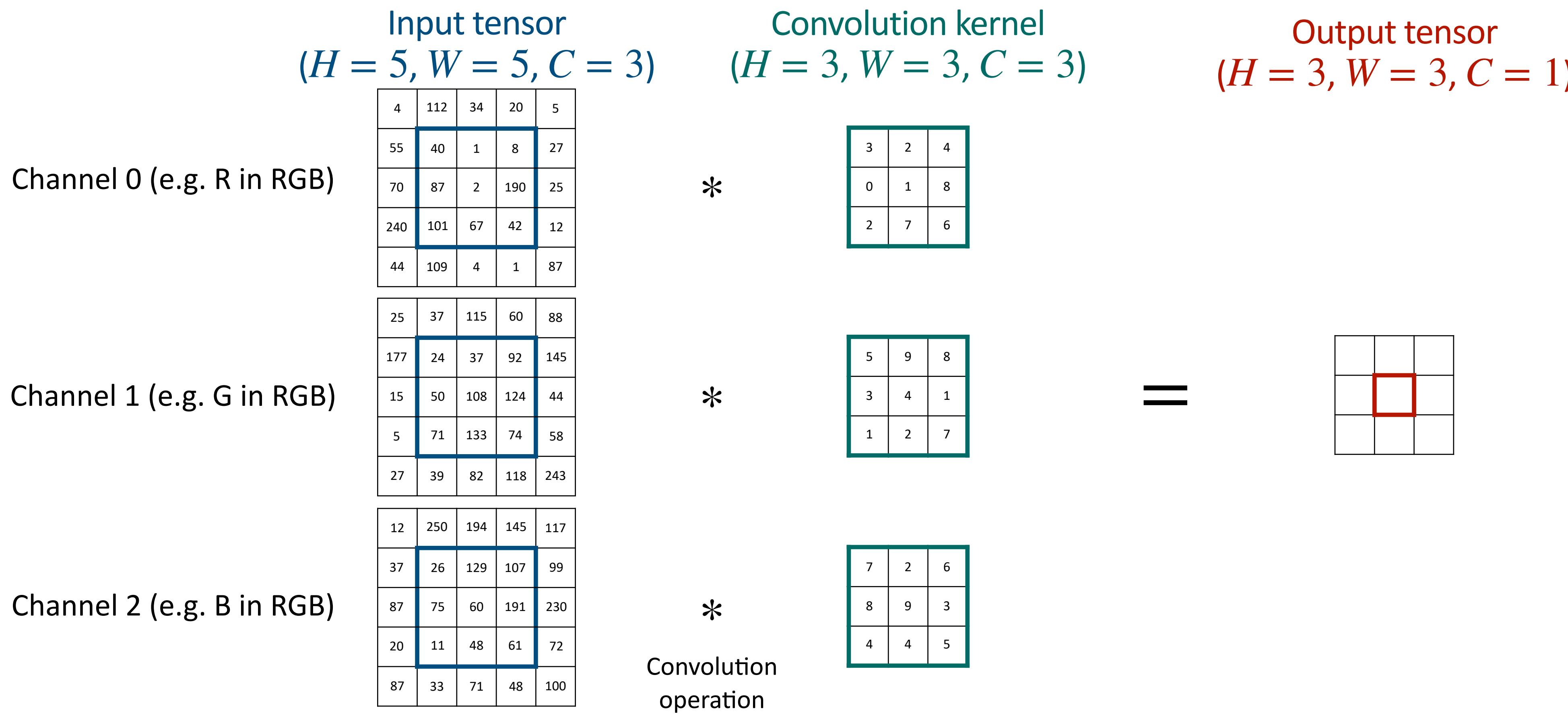
Convolutional Neural Networks – Convolution

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Convolutional Neural Networks – Convolution

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Convolutional Neural Networks – Convolution

Another hyper parameter of the convolution layer is **padding**. Sometimes you might want to **pad the input tensor with a border of zeros**, e.g. to avoid border values in the input to be less important in the final result. The width of this border is called the **padding size**.

Input tensor
 $(H = 5, W = 5, C = 3)$

Channel 0 (e.g. R in RGB)

4	112	34	20	5
55	40	1	8	27
70	87	2	190	25
240	101	67	42	12
44	109	4	1	87

Channel 1 (e.g. G in RGB)

25	37	115	60	88
177	24	37	92	145
15	50	108	124	44
5	71	133	74	58
27	39	82	118	243

Channel 2 (e.g. B in RGB)

12	250	194	145	117
37	26	129	107	99
87	75	60	191	230
20	11	48	61	72
87	33	71	48	100

Padding (padding size = 1)

0	0	0	0	0	0	0	0
0	4	112	34	20	5	0	0
0	55	40	1	8	27	0	0
0	70	87	2	190	25	0	0
0	240	101	67	42	12	0	0
0	44	109	4	1	87	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	25	37	115	60	88	0	0
0	177	24	37	92	145	0	0
0	15	50	108	124	44	0	0
0	5	71	133	74	58	0	0
0	27	39	82	118	243	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	12	250	194	145	117	0	0
0	37	26	129	107	99	0	0
0	87	75	60	191	230	0	0
0	20	11	48	61	72	0	0
0	87	33	71	48	100	0	0
0	0	0	0	0	0	0	0

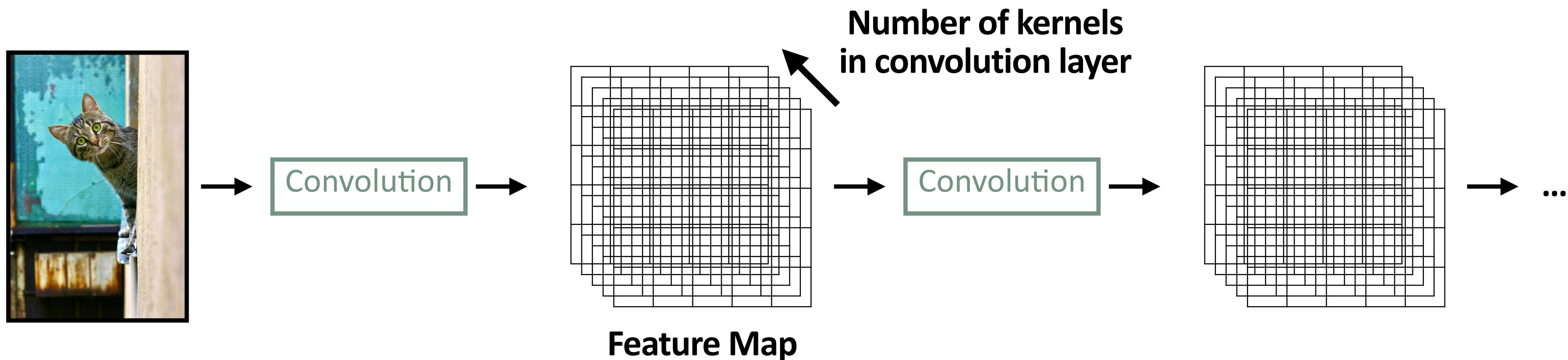
Convolutional Neural Networks – Convolution

- All weights in a convolutional kernel are learnt.
- CNN is **parameter efficient**: weights are **shared across the whole input** (only sliding the kernel with fixed weights). **Much better than our MLP!**

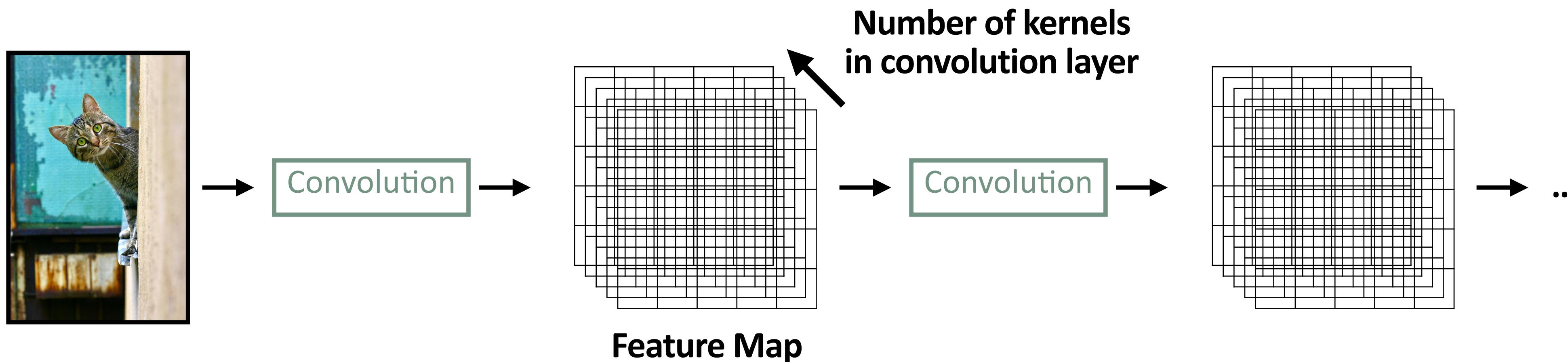
Convolutional Neural Networks – Convolution

- All weights in a convolutional kernel are learnt.
- CNN is **parameter efficient**: weights are **shared across the whole input** (only sliding the kernel with fixed weights). **Much better than our MLP!**
- One kernel provides one scalar for each position in the output tensor.
- To increase the capacity of a convolutional layer, **we learn several kernels** (output channel dimension is equal to the number of kernels).

Convolutional Neural Networks – Convolution



Convolutional Neural Networks – Convolution

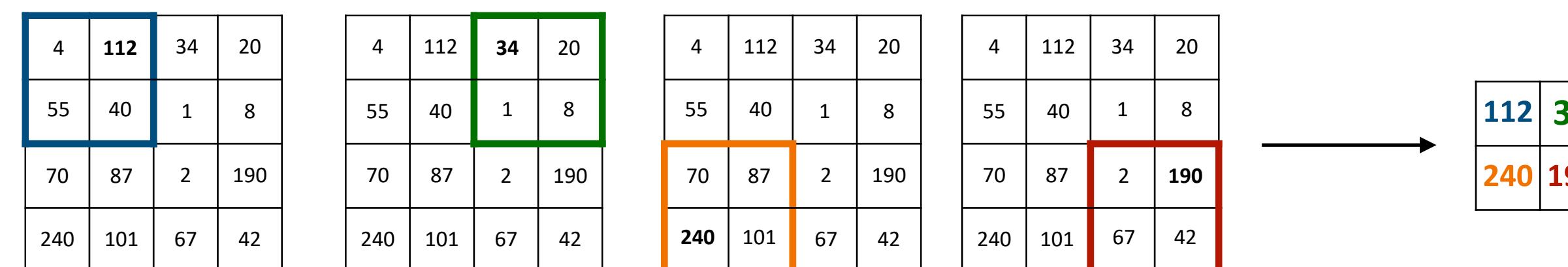


But, CNNs are not only a sequence of convolution layers! There is another operation involved: **pooling**.

Convolutional Neural Networks — Pooling

- The pooling operation allows to **reduce the spatial resolution of a tensor**.
- This is a **non-learned operation**, i.e. not parametrized by any learnable weight.
- Sliding a kernel as for the convolution operation, but instead of computing the weighted sum of inputs, it takes:
 - The max value (Max Pooling)
 - The min value (Min Pooling)
 - The average value (Mean Pooling)

Example of Max Pooling Operation with **kernel size 2×2** and **stride 2** (both horizontal and vertical strides):



Convolutional Neural Networks — Pooling

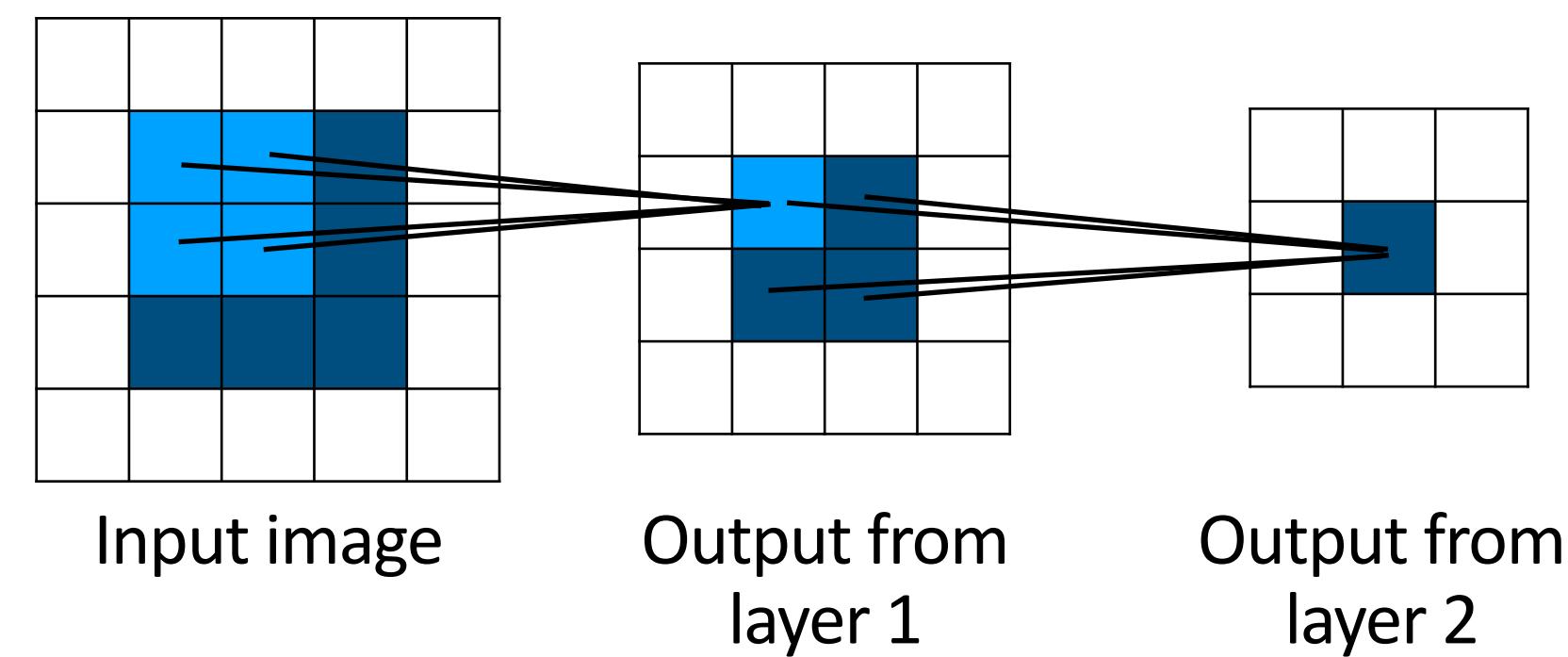
Why do we need pooling?

1. **Makes the network less sensitive to small shifts** in the input by discarding some non-important details. Pooling provides a form of **local shift invariance**.
2. With lower resolution maps, **convolution computations are faster**.
3. **Increases the size of the receptive field** of each neuron.

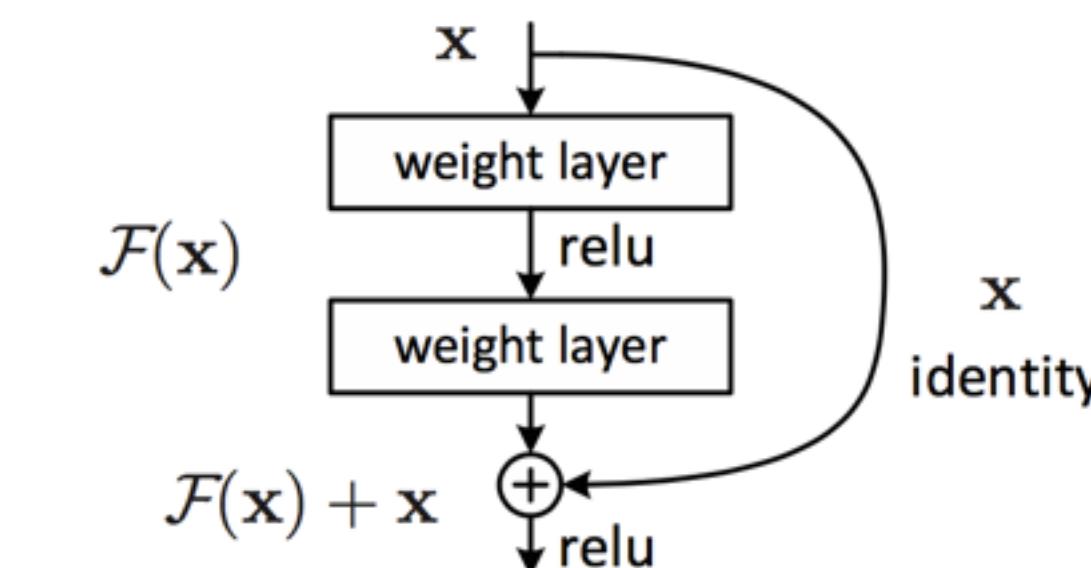
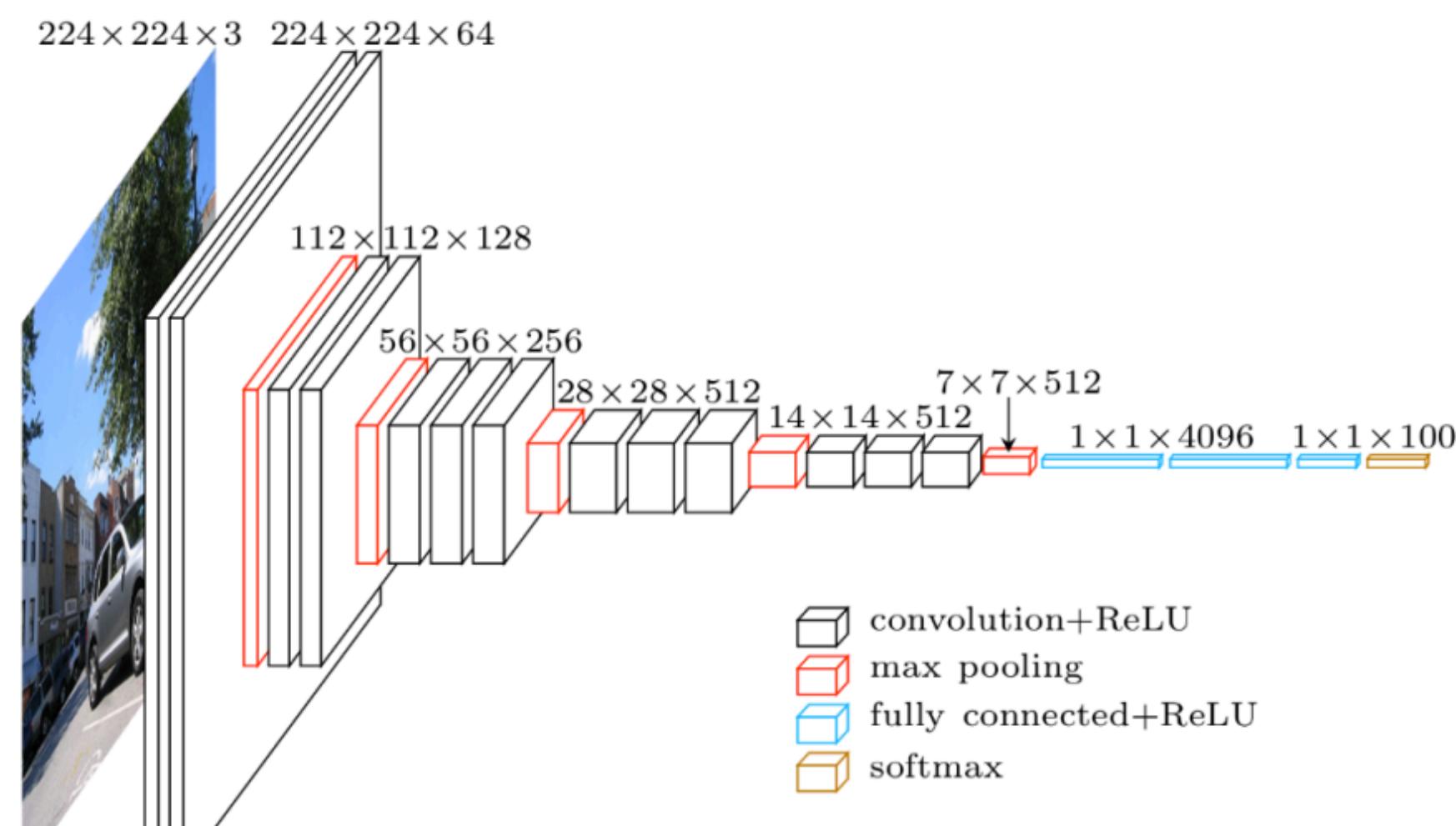
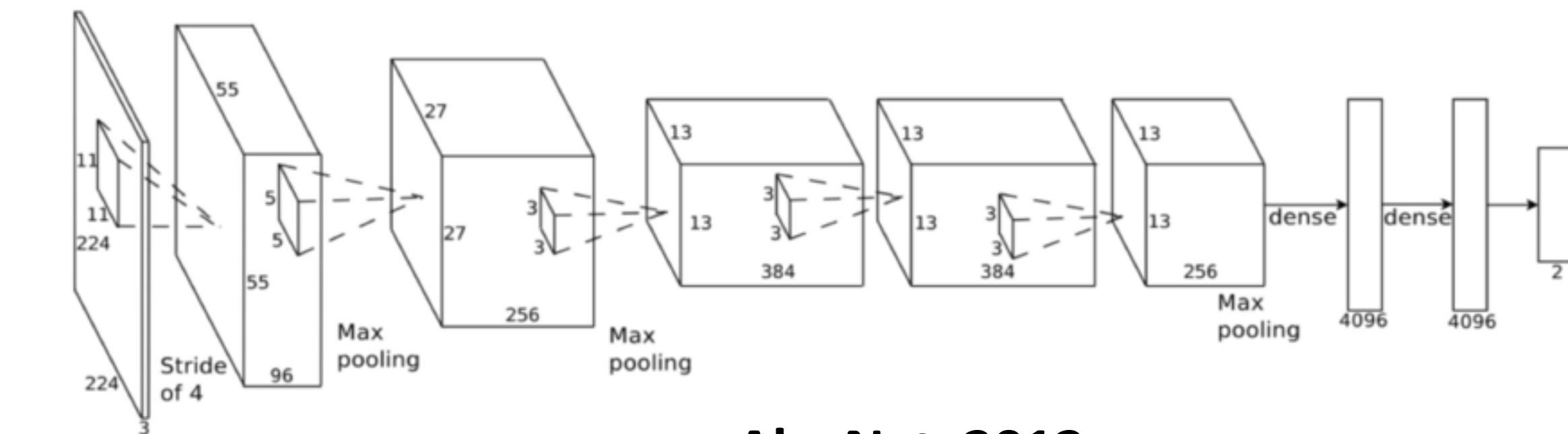
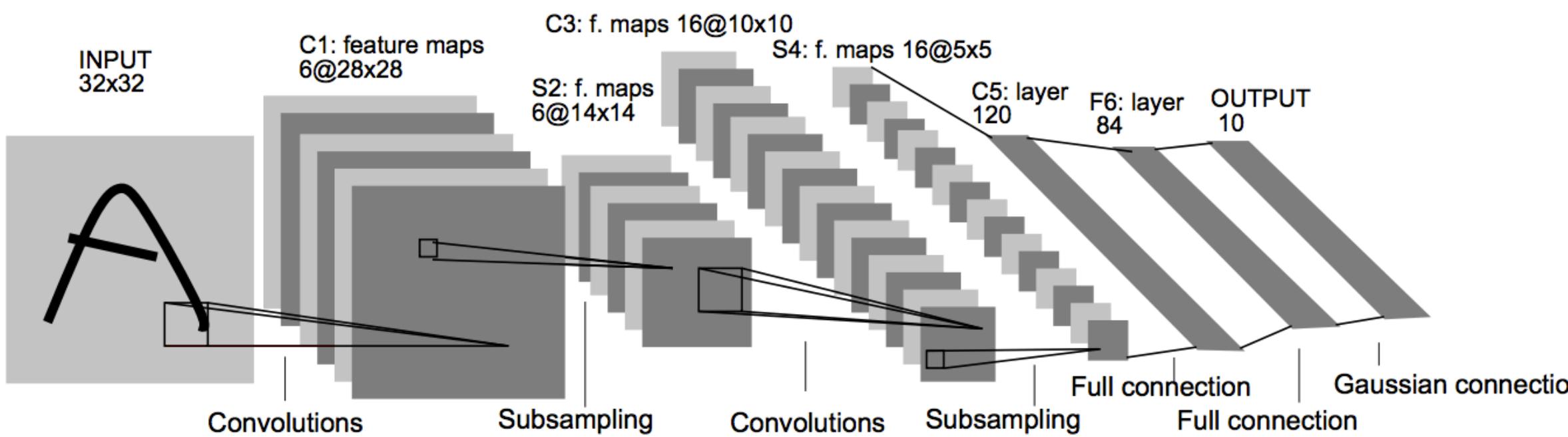
Convolutional Neural Networks — Pooling

The **receptive field** of a neuron is the part of the input image that brings information to the given neuron.

By applying a pooling operation, i.e. downsampling a feature map, we increase the receptive field of next neurons.



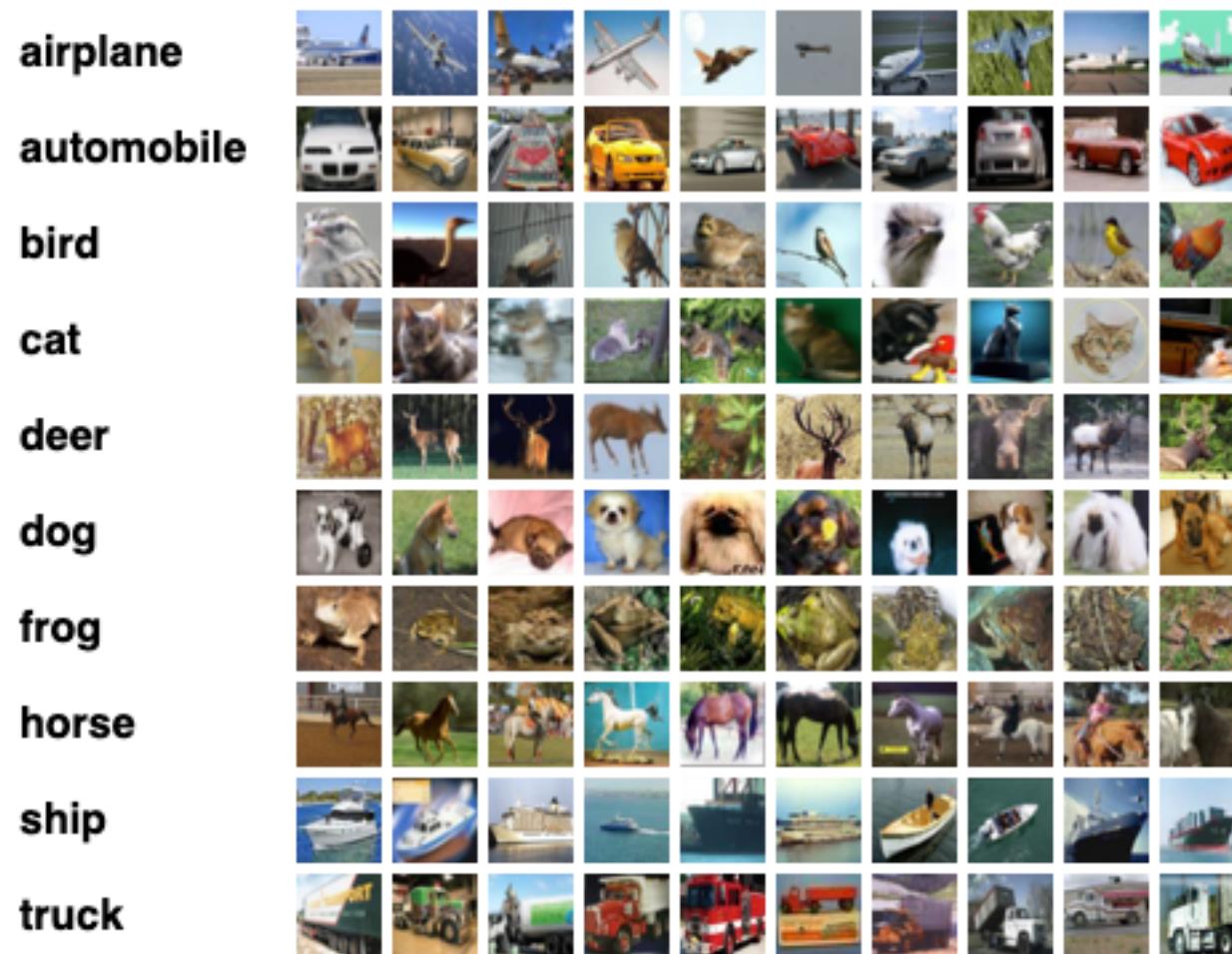
Convolutional Neural Networks — Standard Architectures



Convolutional Neural Networks — Practical

Goals:

1. Implementing a Convolutional Neural Network
2. Understanding the involved computations
3. Building a full Deep Learning pipeline in PyTorch to train a model on a given dataset



CIFAR-10

