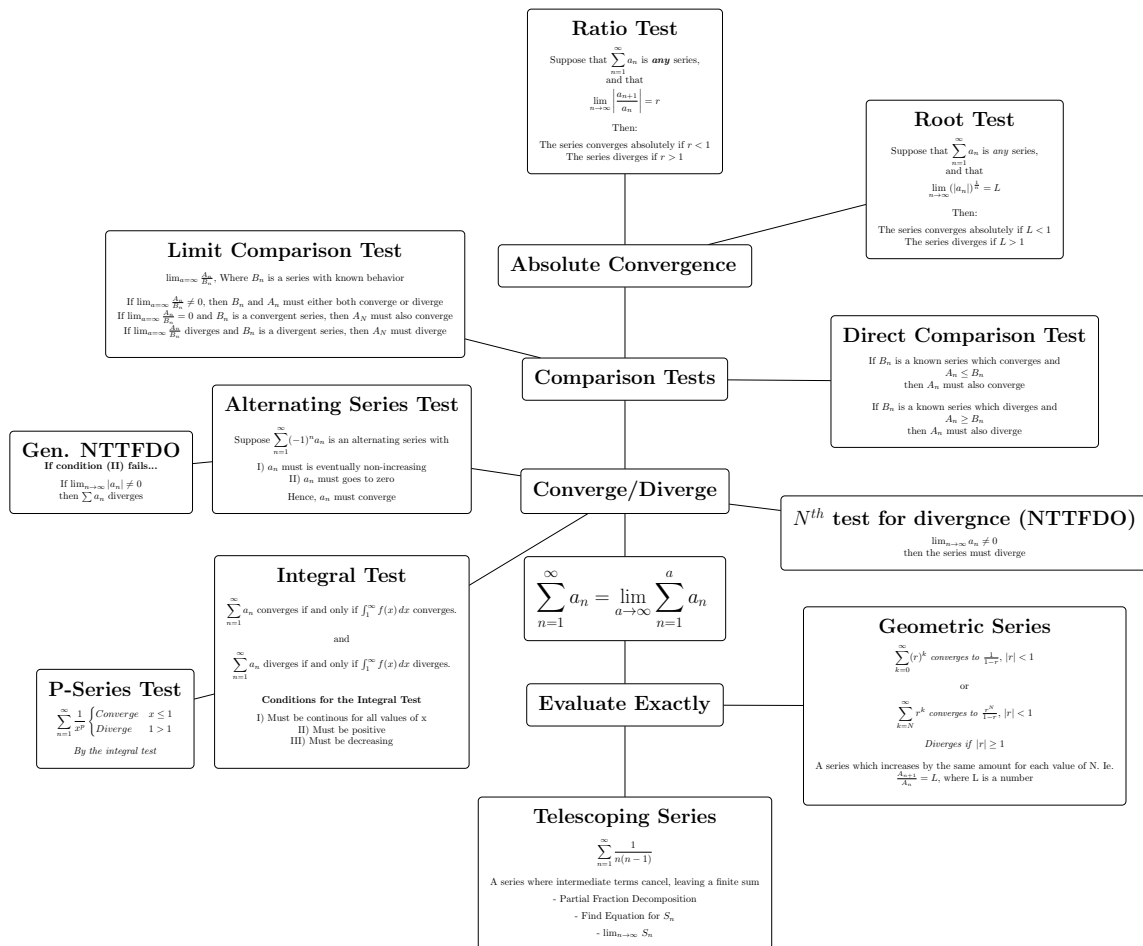


Calc II Notes  
Pierson L



# 1 Absolute Convergence

## 10.5

### 1.1 Good Practice Problems

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### 1.2 Ratio Test

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The Ratio Test<sup>1</sup> states that

Suppose that  $\sum_{n=1}^{\infty} a_n$  is **any** series,  
and that

$$\lim_{n \rightarrow \infty} \left| \frac{a_{n+1}}{a_n} \right| = r$$

Then:

The series converges absolutely if  $r < 1$

The series diverges if  $r > 1$

#### 1.2.1 Examples

ex. 1

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Simplify  $\frac{(n+2)!}{(n-1)!}$

*Ratio of factorials*

$$= \frac{(n+2)!}{(n-1)!}$$

$$= \frac{(n+1)(n+1)(n)(n-1) \cdots (1)}{(n-1)(n-2)(n-3) \cdots (1)}$$

$$= \frac{(n+1)(n+1)(n)(n-1)}{(n-1)}$$

$$= (n+1)(n+1)(n)$$

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<sup>1</sup>Very important regarding factorials

## 1.3 Misc

### 1.3.1 Factorials

ex.1

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$$4! = 4 \times 3! = 4 \times 3 \times 2! = 4 \times 3 \times 2 \times 1! = 4 \times 3 \times 2 \times 1 \times 0!$$

$\rightarrow$

$$0! = 1$$

$\rightarrow$

$$4! = 24$$

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ex. 2

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Simplify  $\frac{(n+2)!}{(n-1)!}$

*Ratio of factorials*

$$= \frac{(n+2)!}{(n-1)!}$$

$$= \frac{(n+1)(n+1)(n)(n-1) \cdots (1)}{(n-1)(n-2)(n-3) \cdots (1)}$$

$$= \frac{(n+1)(n+1)(n)(n-1)}{(n-1)}$$

$$= (n+1)(n+1)(n)$$