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Astro Notes

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0 Class overview

Office hours tues and thurs 11-12 astro 237

ta office hours

wed 3:30-5:30 astro 2367

hw due wed

hw posted week before

- solar system
- stellar evo
- compact objects
- galaxy quasi darkmatter
- cosmic web
- big bang

course goals

- apply pys to universe
- understand foundations of modern astro, astrophys, and cosmology
- conceptual understanding of the uni based on physical principles

1 Early Astronomy

1.0.1 Greek

- Aristotle
 - earth is spherical
 - partial lunar eclipses
 - some stars visible from southern locations but not northern and vice versa

- had ideas regarding perfect geo influenced by Pythagoras and Plato
- Aristarchus (310-230 BC):
 - unprecedented heliocentric framework
 - trig distances earth-moon-sun system
 - angular diameters $\theta_{sun} \approx \theta_{moon} \frac{A}{C} = \frac{D_{moon}}{D_{moon}}$
 - diameters from lunar eclipses $D_{moon} < D_{earth}$
- Eratosthenes (176-195 BC):
 - Determined radius of spherical earth R_E
 - Sun at zenith at noon on summer solstice at Aswan
 - But further north in Alexandria, Egypt, the sun is south of the zenith by angle α
- Hipparchus (190-120 BC):
 - Discover precession of the equinoxes from examination of star catalogs over centuries
 - established the magnitude system
- Copernicus (1473-1543):
 - heliocentric
 - earth rotates
 - still assumed uniform circular celestial motion
 - inferior planets: orbit smaller than earths
 - superior planets: orbits larger than earths

1.1 Emergence of modern Astro

Inferior planets

- $B/C = \sin \theta_E$
- $B = C \sin \theta_E$
- C is AU
- Early astronomers didnt know C, so they could only infer ratios of B/C.
Ie. Orbital radii measured in AU

Superior Planets

- Measure time between opposition and eastern quadrature
- want angle θ between opp and east quad

- $\theta = (\omega_E - \omega_p)$ and $C/B = \cos\theta$
- measure τ and synodic period, calculate sidereal period and ω_p ; know ω_E and infer C/B

Galilean Revolution

- Galileo Galilei (1564 -1642)
 - improved and used a basic refracting telescoping
- def publication of early results 1610 "*starry messenger*"
 - Moon is cratered; not a perfect Sphere
 - milkyway is made out of stars
 - Jupiter has moons (or as he thought, stars)
 - measured phases of Venus

Phases of Venus

- direct confrontation with Ptolemaic geocentric models
- in Ptolemaic models you only see crescent phases

Tycho Brahe (1546-1601)

- Denmark, later Prague
- Given island by king Fredrick (and staff)
- made a accurate and vast database of celestial motion
- had a lead nose?
- Threw giant ragers
- supernova named after him

Johannes Kepler (1571–1630, Prague)

- 'Inherited' (maybe stole) Brahe's data
- also has a SN
- Kepler fit a new empirical model of heliocentric orbits, abandoning perfect circles
 - "*It was as if I awoke from sleep and saw a new light*" (Kepler, New astronomy)

Kepler's Laws

First law

- The planets travel on elliptical orbits with the sun at one focus
- Semimajor axis, half the major axis
- eccentricity: how elliptical (stretched) an orbit is - distance between foci divided by major axis.

second law

- A line drawn from the sun to a planet sweeps out equal areas in equal time intervals'
- perihelion: orbital point closet to the sun
- aphelion: furthest orbital point from the sun

third law

Def: *The square of the sidereal orbital periods of the planets are prop to the cubes of the Semimajor axis of their orbits*

$$p^2 = Ka^3$$

P = planets sidereal period
a= length of semimajor axis
K = constant

Consequences of heliocentric model

- retrograde motion of outer planets
- positions of outer and inner planets wrt sun
- annual parallax
- aberration of starlight
- Coriolis effect

Parallax

- annual parallax: change in the apparent position when seen from two diff locations due to earth revolving around the sun. First measured by Bessel in 1838

Aberration of starlight

- deflection of apparent stellar positions in the direction of the observers motion
- analog: running throw rain and getting wet in the front and not in the back
- detected (Picard, 1680); explained (Bradley, 1729)

- telescope is moving along orbital vector around the sun; translation along orbit cannot exceed transit time of light through telescope

Coriolis effect: evidence of earth rotation

- coriolis acceleration is perp to the direction of motion
-

$$a_{cor}^{\vec{}} = s\vec{v} \times \vec{\omega}$$

- can be deduced from a pendulum
- and in hurricanes!

2 Orbital Mechanics I

2.1 Newtonian mechanics

Parametric vectors

Displacement $\vec{r}(t) = x(t)\hat{i} + y(t)\hat{j} + z(t)\hat{k}$

distance: $r(t) = |\vec{r}(t)| = \sqrt{\vec{r} \cdot \vec{r}}$

2.2 Newtons laws

First law

- Isaac newton(1642-1727)
- an objects' velocity remains constant unless a net outside force acts upon it
- $\vec{v}(t) = \vec{v}_0 = const$

second law

- $\vec{F} = m\vec{a}(t)$
- $\vec{F} = \frac{d\vec{p}(t)}{dt}$
- $d\vec{v}/dt = \vec{f}/m$
- force changes velocity
- used a lot in computational math

third law

- forces come in pairs, equal in magnitude, and opposite in direction

Newtonian gravity

- a force, grav, exists between any two objects having mass m and M, prop to the product of their masses mM and inversely proportional to the square of the separation distance r of their centers
- for coordinates centered on M:
- $\vec{F} = -G \frac{Mm}{|\vec{r}|^2} \hat{r}$

2.3 Displacement vector and polar coordinates

- cartesian coordinates are often written as (x,y,z) in a coordinate system centered on mass M
- Axis orientations are chosen so that the planet orbits in the x-y plane
- Displacement $\vec{r}(t) = x(t)\hat{i} + y(t)\hat{j}$

velocity vector and polar coordinates

- unit vectors in polar coordinates vary with $\theta(t)$
-

$$\frac{d\hat{r}(t)}{dt} = \frac{d\hat{r}(t)}{d\theta} \frac{d\theta(t)}{dt} = \frac{d\theta(t)}{dt} \hat{\theta}(t)$$

- .
- .
- .
-

$$\vec{v}(t) = v_r \hat{r} + v_t \hat{\theta}$$

- two velocity components in polar coords

2.4 Kepler laws: angular momentum

- .

2.5 keplers 2nd law = consv, angular momentum

-

$$d\vec{L}/dt = 0$$

-

$$\vec{L} = \vec{R} \times \vec{p} = \vec{r} \times m\vec{v} = \text{const}$$

-

$$|\vec{v}| = L = mrv_1$$

2.6 Keplers Laws

2.6.1 Keplers First Law

- $\frac{d\vec{v}}{dt} = -\frac{GM}{r^2}\hat{r}$

-

$$\frac{L}{GMm} \frac{d\vec{v}}{dt} = \frac{d\hat{\theta}}{dt}$$

-

$$\frac{L}{GMm} \vec{v} = \hat{\theta} + e\hat{j}$$

- take dot product of both sides with unit vector $\hat{\theta}$, using

- $\hat{j} \cdot \hat{\theta} = \cos \theta$

-

$$\vec{v} \cdot \hat{\theta} = v_t = \frac{L}{mr}$$

2.7 Kepler III

- we know that $\frac{dA}{dt} = \frac{l}{2m} = \text{const}$

- area of a ellipse $A = \pi ab$ of orb period p.

-

$$\frac{A}{P} = \frac{\pi ab}{P} = \frac{L}{2m}$$

- eclipse geo : $b^2 = a^2(1 - e^2)$

- also, $\frac{L^2}{m^2} GMa(1 - e^2)$

-

$$P^2 = \frac{4\pi^2}{GM} a^3$$

3 Orbital energetics

- total energy e is conserved

- sum of K and U

-

$$E = K + U$$

$$= \frac{1}{2}mv^2 - \frac{GMm}{r}$$

- total E is conserved
-

$$E = \left(\frac{GMm}{L}\right)^2 \frac{m}{2}(e^2 - 1)$$

- Hyperbolic orbit: $e > 1, E > 0, K > |U|$
 - open orbit, unbound; single perihelion passage at $\theta = 0$
- Parabolic orbit: $e = 1, E = 0, K = |U|$
 - marginally unbound; velocity approach zero at infinite time
- elliptical orbit: $e < 1, E < 0, K = |U|$
- objects originating outside our solar system are easily identified by their total energy
 - measure total energy (how far away it is, how fast is it moving)

3.1 Checking energy in circular orbits

- governing equation for circular orbits in scalar form
-

$$f = ma$$

-

$$\frac{GM}{r^2} = \frac{v^2}{r} = \omega^2 r$$

-

$$v = \sqrt{\frac{GM}{r}}$$

3.2 Negative total energy orbits

- bound orbits have $E < 0$
- must add energy to break “unbind” the orbits

3.3 Parabolic orbits: escape speeds

- Escape speed is the speed that will bring your total pot energy to 0
- velocity becomes zero at infinite distance
-

$$\frac{1}{2}mv^2 = \frac{GMm}{r}$$

-

$$v_{esc} = \sqrt{\frac{2GM}{r}}$$

3.4 Hohmann transfer orbit

- Elliptical transfer orbit from earth to superior planet
 - earths orbit becomes the transfer orbits perihelion passage
 - inserted into superior planet orbit at aphelion. This constrains launch windows
 - theoretically requires only two burns: at launch and aphelion insertion point
- semimajor axis of transfer orbit
-

$$a_{to} = \frac{a + a_{sup}}{2}; Earth$$

4 Earth-Moon System

4.1 Motion of the moon

- 27.3 sidereal orbit
- 29.5 synodic orbit
- rises in east and sets in west diurnally, but moves eastwards by about 12 deg per day rel to stars
- rises hour later per night

4.2 Precession

- earth is an oblate spheroid with equatorial bulge of .3% cause by separation
- sun, moon, and planets exert a torque τ on earth
-

$$\vec{\tau} = \vec{r} \times \vec{F}$$

- results in precession of spin axis of earth around ecliptic pole
- NCP moves. Polaris will not always be at NCP
- moves through stars with $P \approx 28500yr$
- opening angle
-

$$47^\circ (= 2 \times 23.5^\circ)$$

4.3 Tidal Forces

- Moon exerts diff tidal forces on matter on earth
- esp noticeable on earths ocean surface as tides
- when sun and moon align (sun-earth-moon at 0° and 180°) high-amp tides result, called spring tides
- when sun and moon are at 90° they sum destructively, producing neap tides

4.3.1 Diff gravitational tidal forces

- arise from the r^{-2} dependence of grav force
- Taylor expansion about center of earth r_0
-

$$\delta F = \frac{2GM_{moon}m}{r^3}(r - r_0)$$

- Sun exerts about half as strong as moon tidal forces

4.3.2 Rotation of tides

- tidal bulges produced on earths by the moon rotate at the same angular rate as the moons orbit around earth
- but the earth is rotating faster at once per sidereal day by 4 minutes. Drags the tides forward from where they would otherwise be by about 10° by friction
 - therefore high tides occur shortly after upper transit of moon
 - the misalignment drives angular momentum transfer between earth and Moon
 - moon pulls strongly on nearer tidal bulge than farther tidal bulge
 - net torque to slow earth rotation
 - but conversely the tidal bulge pulls more strongly on the moon, pulling it forward, increasing its angular momentum

4.4 Earth Shape

- moon stretches earth in a prolate deformation
- spin of the earth causes an oblate deformation
- oblate is much greater the prolate def

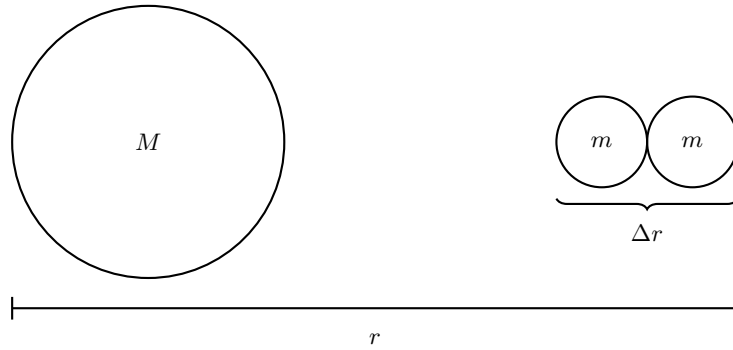
4.5 Roche Limit

- object get too close, forces on one side much greater then other, rip object apart
- approx a planet as two spheres 2m
-

$$\Delta F = \frac{dF}{dr} \Delta r = \frac{2GMm}{r^3} \Delta r$$

- Is there a force holding 2m together? yes, self grav
-

$$F = -\frac{Gmm}{(\Delta r)^2}$$



4.6 Hill radius

- Tidal forces of sun on earth-moon systems means that there is a maximum orbital distance for the moon, if it is to remain bound to the earth

4.7 Plane of lunar orbit

- Inclined by 5.1°
- the moon is near the cele equator so the moon is above the horizon about 50% of the time for most observers on earth
- moves north and south in the sky in addition to its motion around the earth. greatest dec is $23.5 + 5.1 = 28.6$ and min is $-23.5 - 5.1 = -28.6$
- causes eclipses to be retrograde

4.8 Tidal forces: earth vs moon

- earth exerts greater tidal forces on moon than the moon does on the earth.
-

$$\Delta g_{moon \rightarrow earth} = \frac{\Delta F}{m} \propto \frac{M_{Moon} R_{Earth}}{r^3}$$

-

$$\Delta g_{earth \rightarrow moon} = \propto \frac{M_{Earth} R_{Moon}}{r^3}$$

-

$$\frac{\Delta g_{moon \rightarrow earth}}{\Delta g_{earth \rightarrow moon}} \frac{M_{moon} R_{earth}}{M_{earth} r_{moon}} \approx \frac{1}{20}$$

4.9 lunar librations

- E-w and n-s nodding motions of the moon seen from earth, caused by parallax
- tidal locking is not perfect, so the libration happens in longitude
- because the rotation axis is inclined there is libration in lat

5 Waves

5.1 Spectra (How do we know what the universe is made out of?)

Multi-messenger astronomy

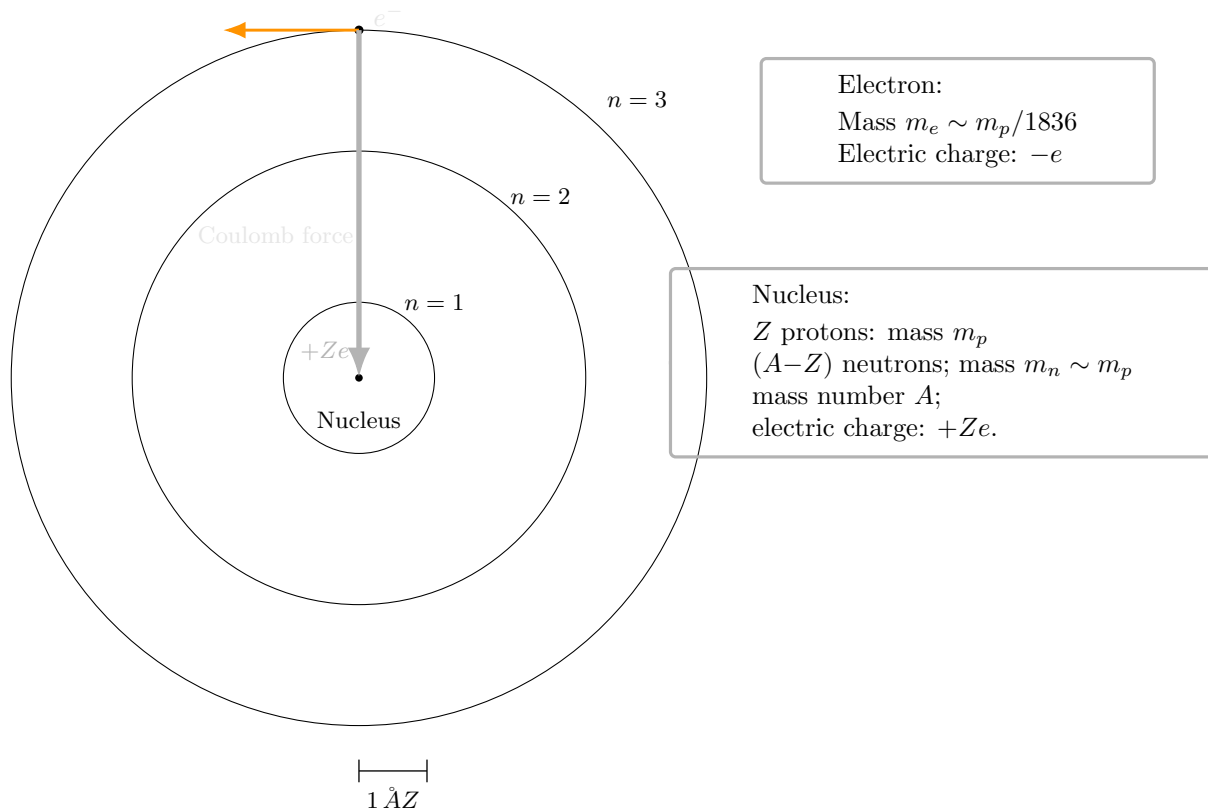
- Electromagnetic radiation
- cosmic rays
- meteorites
- neutrinos
- gravitational waves

5.2 Atoms and spectra

Hydrogen gas exhibits emission lines at discrete visible wavelengths, fit by empirical relation by Balmer in 1885

$$\frac{1}{\lambda} = R(1/4 - 1/n^2)$$
$$n = \text{integer} > 2$$

5.3 Bohrs model



Because orbital angular momentum is quantized, so is r_n and $E_n \rightarrow$ discrete orbital levels

5.4 Atomic transition processes

- Transitions to free unbounded states behave similarly, however, they have diff names
- ionization and recombination
- photoionization (electron is knocked free). photon knocks electron free
- collisional ionization (electron becomes free). any other particle knocks electron free
- a positively charged ion may combine with a free electron, and atom emits radiation (photons) as the electrons drop to lower levels. called **recombination**

5.5 Kirchoff's Laws

- blackbody
- emission lines
- absorption lines

5.6 Temperature affects internal states of atoms and molecules

- temp of gas determines the kinetic energies of the colliding particles
- and the incoming photons
- we observe outgoing photons

5.7 Temperature vs velocity

- Thermal motions: emitted or absorbed photons inherit their energy from the Doppler velocities of the thermal motions of particles/atoms
- equilibrium distribution of particle speeds in an ideal gas is given by the Maxwell-Boltzmann distribution

5.8 mean free path and opt depth

- mean free path x_m . Distance which intensity decreases by a factor of $1/e$
- optical depth $\tau = x/x_m$. Thickness of slab in units of mean free path x_m
- column density, $N(x)$: total number of absorbing particles in a column with cross-section area 1 m^2 and length x

6 Telescopes

6.1 photoelectric effect

- Photoemission - emission of an electron from a material in response to an incident photon
 - photoemissive material (underlying material)
 - work function (min energy required to produce light)
 - photoelectric effect (photoemission from atoms in certain materials)
 - photoelectron (released electron)
- particle energy of EM radiation

7 Glossary

Synodic period

- time elapsed between success conjunctions or oppositions
- this is the period we observe from earth, which is moving

Sidereal Period

- elapsed time of full orbit relative to the fixed stars (inertial ref frame)
- This is the one we will want to put in Keplers laws