

# Third SPICE Exercise

Fundamentals Of Electronics - a.a. 2018-2019 - University of Padua (Italy)

Pietro Prandini (mat. 1097752)

June 8, 2019



# Contents

<b>1</b>	<b>Differential amplifier with MOS current source</b>	<b>5</b>
1.1	MOSFET current mirror source - Analytic solution . . . . .	6
1.1.1	$I_{D_4}$ . . . . .	6
1.2	SPICE Operating Point analysis . . . . .	6



# Chapter 1

## Differential amplifier with MOS current source

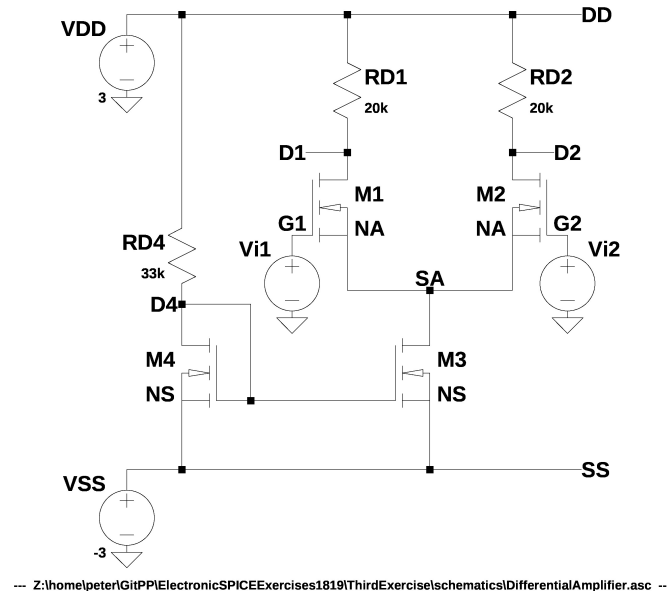


Figure 1.1: Differential amplifier with MOS current source

Data:

$$V_t = 0.5V \quad (1.1)$$

$$K'_n = \mu_n C_{ox} = 200 \frac{\mu A}{V^2} \quad (1.2)$$

$$\lambda = 0 \quad (1.3)$$

$$\left(\frac{W}{L}\right)_1 = \left(\frac{W}{L}\right)_2 = 20 \quad (1.4)$$

$$\left(\frac{W}{L}\right)_3 = \left(\frac{W}{L}\right)_4 = 5 \quad (1.5)$$

$$R_{D1} = R_{D2} = 20k\Omega \quad (1.6)$$

$$R_{D4} = \frac{30}{1000} \cdot 1097752\Omega = 32.93k\Omega \simeq 33k\Omega \quad (1.7)$$

$$V_{DD} = 3V \quad (1.8)$$

$$V_{SS} = -3V \quad (1.9)$$

## 1.1 MOSFET current mirror source - Analytic solution

### 1.1.1 $I_{D_4}$

The transistor  $M_4$  has a short circuit between its drain and its gate, so the transistor works in saturation mode. The current  $I_{D_4}$  could be calculated as:

$$I_{D_4} = \frac{1}{2} K'_n \left( \frac{W}{L} \right)_4 (V_{D_4SS} - V_t)^2 \quad (1.10)$$

Other expression of the current  $I_{D_4}$  could be calculated using the LKT:

$$V_{DD} - R_{D_4} I_{D_4} - V_{D_4SS} - V_{SS} = 0 \implies I_{D_4} = \frac{V_{DD} - V_{D_4SS} - V_{SS}}{R_{D_4}} \quad (1.11)$$

Using the equations 1.10 and 1.11 it's possible calculating  $V_{D_4SS}$ :

$$\frac{1}{2} K'_n \left( \frac{W}{L} \right)_4 (V_{D_4SS} - V_t)^2 = \frac{V_{DD} - V_{D_4SS} - V_{SS}}{R_{D_4}} \quad (1.12)$$

$$\frac{1}{2} \cdot 200 \frac{\mu A}{V^2} \cdot 5 \frac{\mu m}{\mu m} (V_{D_4SS} - 0.5V)^2 = \frac{3V - V_{D_4SS} - (-3V)}{33k\Omega} \quad (1.13)$$

$$500 \frac{\mu A}{V^2} (V_{D_4SS} - 0.5V)^2 = \frac{6}{33} mA - \frac{1}{33k\Omega} V_{D_4SS} \quad (1.14)$$

$$500 \frac{\mu A}{V^2} (V_{D_4SS}^2 - V_{D_4SS} \cdot V + 0.25V^2) = \frac{6}{33} mA - \frac{1}{33k\Omega} V_{D_4SS} \quad (1.15)$$

$$500 \frac{\mu A}{V^2} \cdot V_{D_4SS}^2 + \left( -500 \frac{\mu A}{V^2} V + \frac{1}{33k\Omega} \right) V_{D_4SS} + 500 \frac{\mu A}{V^2} \cdot 0.25V^2 - \frac{6}{33} mA = 0 \quad (1.16)$$

$$0.5 \frac{mA}{V^2} \cdot V_{D_4SS}^2 + \left( -0.5 \frac{mA}{V^2} V + \frac{1}{33k\Omega} \right) V_{D_4SS} + 0.5 \frac{mA}{V^2} \cdot 0.25V^2 - \frac{6}{33} mA = 0 \quad (1.17)$$

$$\left( 0.5 \frac{mA}{V^2} \right) V_{D_4SS}^2 + \left( -\frac{31}{66} \frac{mA}{V} \right) V_{D_4SS} + (-0.05682mA) = 0 \quad (1.18)$$

$$V_{D_4SS_{1,2}} = \frac{-\left(-\frac{31}{66} \frac{mA}{V}\right) \pm \sqrt{\left(-\frac{31}{66} \frac{mA}{V}\right)^2 - 4 \cdot \left(0.5 \frac{mA}{V^2}\right) \cdot (-0.05682mA)}}{2 \cdot 0.5 \frac{mA}{V^2}} = \begin{cases} 1.04784V \\ -0.10845V \end{cases} \quad (1.19)$$

## 1.2 SPICE Operating Point analysis

```
* Differential Amplifier
*****
* 3st Exercise – Fundamentals Of Electronics – a.a. 2018–2019 – UniPD – Italy *
*                               Pietro Prandini – mat. 1097752                               *
*                                                                                               *
* This work is licensed under the Creative Commons Attribution–ShareAlike 4.0 *
* International License. To view a copy of this license, visit                               *
* http://creativecommons.org/licenses/by-sa/4.0/ or send a letter to Creative *
* Commons, PO Box 1866, Mountain View, CA 94042, USA.                                     *
*****

* Parameters
.param RD = 20k
.param VG1 = 0
.param VG2 = 0

* NMOS models
.model NA NMOS VT0=0.5 KP=200u LAMBDA=0 W=4.00u L=0.20u
```

```

.model NS NMOS VT0=0.5 KP=200u LAMBDA=0 W=1.25u L=0.25u

* Resistances
RD1 DD D1 {RD}
RD2 DD D2 {RD}
RD4 DD D4 33k

* Transistors
M1 D1 G1 SA SA NA
M2 D2 G2 SA SA NA
M3 SA D4 SS SS NS
M4 D4 D4 SS SS NS

* Voltage sources
VDD DD 0 3
VSS SS 0 -3
Vi1 G1 0 {VG1}
Vi2 G2 0 {VG2}

* Analysis
.op

.END

```

—— Operating Point ——

V(dd):	3	voltage
V(d1):	1.49935	voltage
V(d2):	1.49935	voltage
V(d4):	-1.95216	voltage
V(g1):	0	voltage
V(sa):	-0.693691	voltage
V(g2):	0	voltage
V(ss):	-3	voltage
Id(M4):	0.000150065	device_current
Ig(M4):	0	device_current
Ib(M4):	-1.05784e-012	device_current
Is(M4):	-0.000150065	device_current
Id(M3):	0.000150065	device_current
Ig(M3):	0	device_current
Ib(M3):	-2.31631e-012	device_current
Is(M3):	-0.000150065	device_current
Id(M2):	7.50327e-005	device_current
Ig(M2):	0	device_current
Ib(M2):	-2.20304e-012	device_current
Is(M2):	-7.50327e-005	device_current
Id(M1):	7.50327e-005	device_current
Ig(M1):	0	device_current
Ib(M1):	-2.20304e-012	device_current
Is(M1):	-7.50327e-005	device_current
I(Rd4):	0.000150065	device_current
I(Rd2):	7.50327e-005	device_current
I(Rd1):	7.50327e-005	device_current
I(Vi2):	0	device_current
I(Vi1):	0	device_current
I(Vss):	0.000300131	device_current
I(Vdd):	-0.000300131	device_current